

# SF2943 Time Series Analysis

## TS 6

KTH Royal Institute of Technology

*titing@kth.se*

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# Overview

- 1 Introduction to the Data
- 2 Preprocessing
- 3 Model Analysis and Evaluation
- 4 Forecast
- 5 Conclusion

# Original Data

The dataset contains the measurements for  $CO_2$ -concentration in the atmosphere of Mauna Loa, Hawaii from 1965 to 1980.

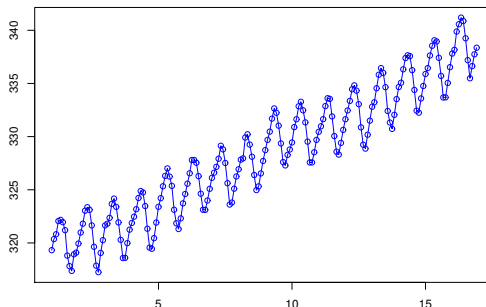


Figure:  $CO_2$  (ppm) mauna loa, 1965-1980

# Model Assumption

We assume the ts follows the classical additive model:

$$Y_t = T_t + S_t + X_t$$

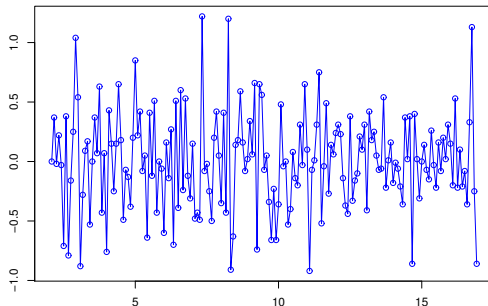
where  $T_t$  is the trend ,  $S_t$  is the seasonality , and  $X_t$  is the stationary component.

By applying a differencing operator with lag  $d = 12$ , because  $S_t$  has a period  $d = 12$ , we can obtain:

$$Y_t - Y_{t-d} = (1 - B^d)Y_t = T_t - T_{t-d} + X_t - X_{t-d}$$

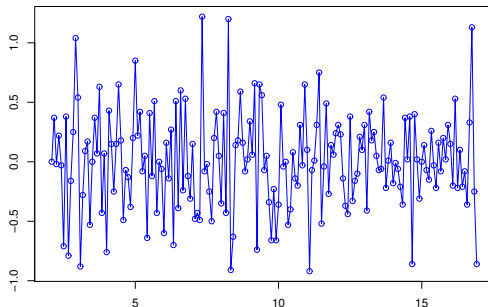
Now the polynomial trend term  $T_t - T_{t-d}$  can be eliminated by applying a power of the differencing operator.

# Preprocessed Time Series



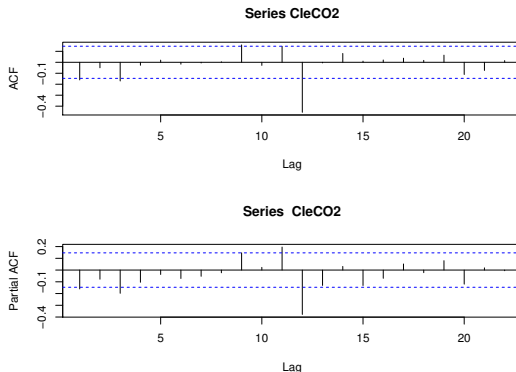
After the differencing, we get the preprocessed time series  $\hat{x}_t$ . Then we use the Augmented Dickey-Fuller test to check the stationarity of the series.

# Preprocessed Time Series (function *adf.test*)



The result of the ADF test can sufficiently reject the null hypothesis of a unit root at level 0.05.

# Model Analysis



The ACF value is significant when  $\text{lag} = 12$ , which implies a seasonal ARMA model may be suitable.

# Final Model

Function `auto.arima()`:  $(1, 0, 1) \times (0, 0, 1)_{12}$  (Smallest AICC Value)

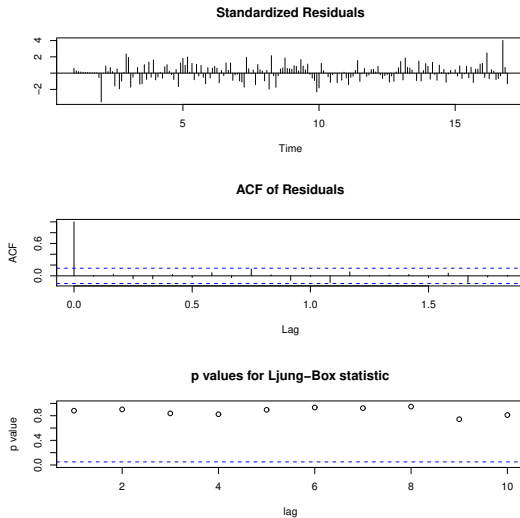
Combining the pre-differencing procedure  $(1 - B)(1 - B^{12})Y_t$ , our final model is SARIMA model with parameters  $(1, 1, 1) \times (0, 1, 1)_{12}$ .

With maximum likelihood method, the coefficients for the final model are estimated as:

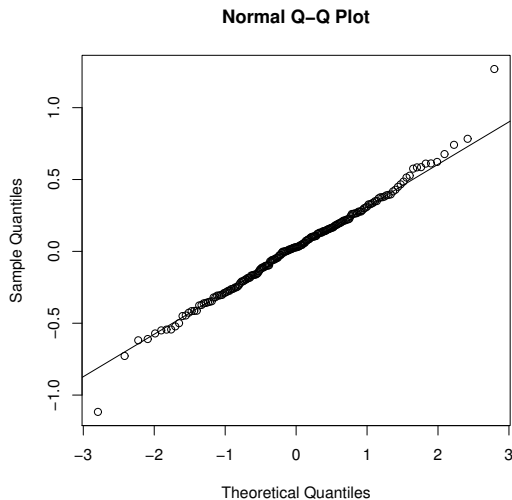
Coefficients	Estimate	Standard error
$ar_1$	0.3714	0.1746
$ma_1$	-0.6709	0.1378
$sma_1$	-0.8293	0.0871



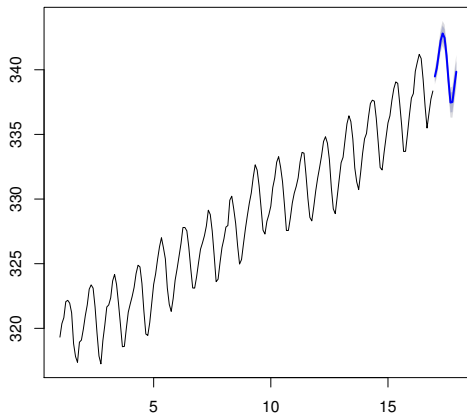
# Model Evaluation (function *tsdiag*)



# Model Evaluation



**Forecasts from ARIMA(1,1,1)(0,1,1)[12]**



# Conclusion

From the graph of the original  $CO_2$  data, we can see that the additive model seems applicable.

We eliminate the trend and seasonality of the original data with differencing method.

We use a SARIMA model to characterize the stationary component with the help of *auto.arima()* .

The tests (*tsdiag*) of the residuals show that our model has achieved preferable results.