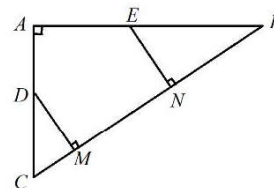


Hybleland L9-Triangle Area and Area Method II-Assignment

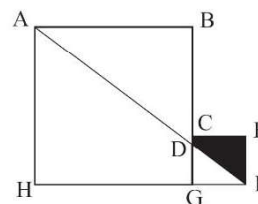
**Problem 1.** In the figure shown,  $\angle A = 90^\circ$ .  $D$  and  $E$  are the points on  $AB$  and  $AC$ , respectively.  $DM = EN = 2$ . Find the area of triangle  $ABC$  if the area of triangle  $CMD$  is  $1/5$  of the area of triangle  $ABC$ , and the area of triangle  $BNE$  is  $1/4$  of the area of triangle  $ABC$ .

- (A)  $4\sqrt{5}$  (B)  $2\sqrt{5}$  (C)  $8\sqrt{5}$  (D) 9 (E) 10



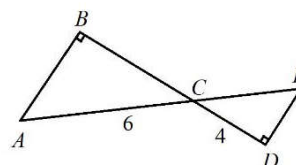
**Problem 2.** In the figure below, a 5-inch by 5-inch square adjoins a 16-inch by 16-inch square. What is the area of the shaded region?

- (A)  $\frac{200}{21}$  (B)  $\frac{325}{21}$  (C)  $\frac{245}{16}$  (D)  $\frac{25}{2}$  (E) 12



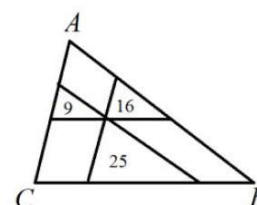
**Problem 3.** In the figure,  $AC = 6$  cm,  $CD = 4$  cm, and  $DE = 3$  cm. Find the number of square centimeters in the area of the triangle  $ABC$ .

- (A)  $\frac{36}{25}$  (B) 9 (C)  $\frac{17}{2}$  (D)  $\frac{216}{25}$  (E)  $\frac{25}{36}$



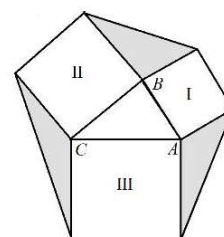
**Problem 4.** In  $\triangle ABC$ , line segments are drawn parallel to each of the sides dividing the triangle into six regions. The areas of three regions are shown in the figure. What is the total area of  $\triangle ABC$ ?

- (A) 144 (B) 72 (C) 64 (D) 81 (E) 70



**Problem 5.** In  $\triangle ABC$  we have  $AB = 2$ , and  $AC = 3$ . I, II, and III are the squares of sides  $AB$ ,  $BC$ , and  $CA$ , respectively. What is the greatest possible value of the sum of the shaded regions?

- (A) 6 (B) 9 (C) 18 (D) 12 (E) 10



**Problem 6.** Point  $D$  lies on side  $AC$  of equilateral triangle  $ABC$  such that the measure of angle  $DBC$  is 45 degrees. What is the ratio of the area of triangle  $ADB$  to the area of triangle  $CDB$ ? Express your answer as a common fraction in simplest radical form.

**Problem 7.** A triangle has sides of length 12, 17 and 25 units. What is the radius of its circumscribed circle? Express your answer as a common fraction.

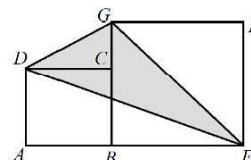
(A)  $85/6$  (B)  $79/6$  (C)  $69/7$  (D)  $89/9$  (E)  $15$

**Problem 8.** The three side lengths of a particular triangle are 2, 5 and  $x$  units, and the area of the triangle is  $x$  square units. What is the value of  $x$ ? Express your answer in simplest radical form.

**Problem 9.** Two squares are put together as shown.  $FE = 20$  and  $AB = 15$ .

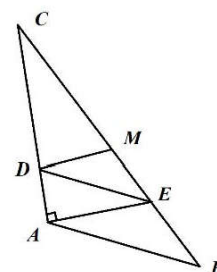
Connect  $EG$ ,  $ED$ , and  $DG$ . Find the shaded area.

(A) 212 (B) 262 (C) 228 (D) 200 (E) 256



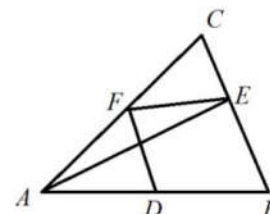
**Problem 10.** As shown in the figure,  $\triangle ABC$  is an obtuse triangle.  $M$  is the midpoint of  $BC$ .  $AE \perp AC$ .  $MD \parallel AE$ . What is the area of  $\triangle CDE$  if the area of  $\triangle ABC$  is 2016?

(A) 1008 (B) 502 (C) 252 (D) 200 (E) 256



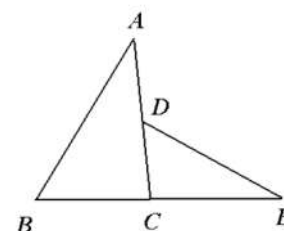
**Problem 11.** As shown in the figure, the area of triangle  $ABC$  is 18. Points  $D$ ,  $E$ , and  $F$  are on sides  $AB$ ,  $BC$  and  $AC$  respectively, and  $AD = 4$ ,  $DB = 5$ . Find the area of triangle  $ABE$  if triangles  $ABE$  and quadrilateral  $DBEF$  have the same areas.

(A) 10 (B) 5 (C)  $9/5$  (D) 2 (E) 6



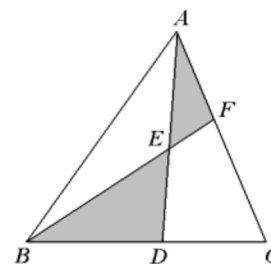
**Problem 12.** As shown in the figure,  $BC = CE$ ,  $AD = CD$ . Find the area triangle  $CDE$  if the area of triangle  $ABC$  is 200.

(A) 100 (B) 102 (C) 152 (D) 120 (E) 125



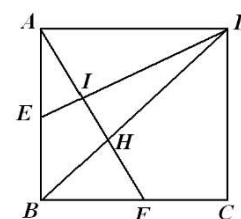
**Problem 13.** As shown in the figure,  $S_{\triangle ABC} = 120$ ,  $AE = ED$ , and  $AF = \frac{1}{2}FC$ . Find the shaded area.

(A) 20 (B) 24 (C) 30 (D) 36 (E) 40



**Problem 14.** (AMC) If  $ABCD$  is a  $2 \times 2$  square,  $E$  is the midpoint of  $\overline{AB}$ ,  $F$  is the midpoint of  $\overline{BC}$ ,  $\overline{AF}$  and  $\overline{DE}$  intersect at  $I$ , and  $\overline{BD}$  and  $\overline{AF}$  intersect at  $H$ , then the area of quadrilateral  $BEIH$  is

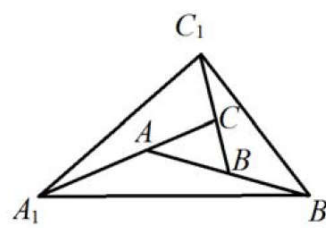
- (A)  $\frac{1}{3}$  (B)  $\frac{2}{5}$  (C)  $\frac{7}{15}$  (D)  $\frac{8}{15}$  (E)  $\frac{3}{5}$



**Problem 15.** Triangle  $ABC$  in the figure has area 1. Points  $A_1$ ,  $B_1$ , and  $C_1$ , all distinct from  $A$ ,  $B$ , and  $C$ , are on the extensions of sides  $CA$ ,  $AB$ , and  $BC$ ,

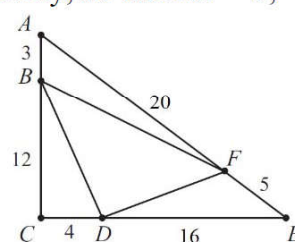
respectively, and  $AA_1 = 2CA$ ,  $BB_1 = 2AB$ ,  $CC_1 = 2BC$ . Find the area of  $\triangle A_1B_1C_1$ .

- (A) 16 (B) 17 (C) 15 (D) 12 (E) 19



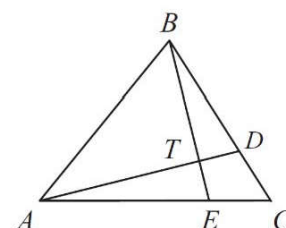
**Problem 16.** In right triangle  $\triangle ACE$ , we have  $AC = 15$ ,  $CE = 20$ , and  $EA = 25$ . Points  $B$ ,  $D$ , and  $F$  are located on  $AC$ ,  $CE$ , and  $EA$ , respectively, so that  $AB = 3$ ,  $CD = 4$ , and  $EF = 5$ . What is the ratio of the area of  $\triangle BDF$  to that of  $\triangle ACE$ ?

- (A)  $\frac{13}{25}$  (B)  $\frac{12}{29}$  (C)  $\frac{13}{30}$  (D)  $\frac{39}{76}$  (E)  $\frac{1}{2}$



**Problem 17.** In  $\triangle ABC$  points  $D$  and  $E$  lie on  $BC$  and  $AC$ , respectively. Suppose that  $AD$  and  $BE$  intersect at  $T$  so that  $AT/DT = 3$  and  $BT/ET = 4$ . What is the value of  $AE/EC$ ?

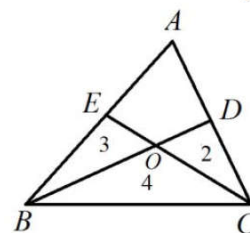
- (A)  $\frac{11}{5}$  (B)  $\frac{12}{5}$  (C)  $\frac{13}{5}$  (D)  $\frac{4}{3}$  (E)  $\frac{5}{2}$





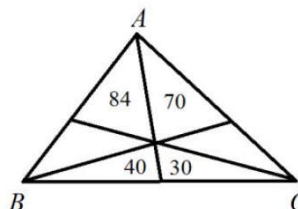
**Problem 18.** As shown in the figure,  $\triangle ABC$  is divided into three smaller triangles and one quadrilateral. The areas of three triangles are as indicated. Find the area of quadrilateral  $ADOE$ .

- (A)  $\frac{39}{5}$  (B)  $\frac{21}{5}$  (C)  $\frac{18}{5}$  (D) 8 (E)  $\frac{63}{10}$



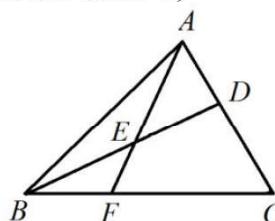
**Problem 19.** As shown in the figure,  $\triangle ABC$  is divided into six smaller triangles by lines drawn from the vertices through a common interior point. The areas of four of these triangles are as indicated. Find the area  $\triangle ABC$ .

- (A) 316 (B) 317 (C) 315 (D) 312 (E) 319



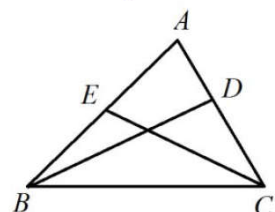
**Problem 20.** As shown in the figure,  $D$  and  $F$  are points on  $AC$  and  $BC$ , respectively of  $\triangle ABC$ .  $AF$  and  $BD$  meet at  $E$ .  $AD : DC = 1 : 2$ .  $BE = ED$ . Find the value of  $BF : FC$ .

- (A)  $\frac{3}{5}$  (B)  $\frac{2}{5}$  (C)  $\frac{1}{5}$  (D)  $\frac{1}{3}$  (E)  $\frac{3}{10}$



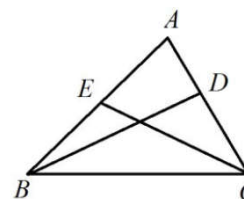
**Problem 21.** As shown in the figure,  $E$  and  $D$  are points on  $AB$  and  $AC$ , respectively.  $\triangle ABC$  is divided into three smaller triangles and one quadrilateral.  $AE : BE = 2$ .  $AD : DC = 1 : 2$ . Find the area of the quadrilateral  $AEFD$  if the area of  $\triangle ABC$  is 42.

- (A) 16 (B) 14 (C) 13 (D) 12 (E) 19



**Problem 22.** As shown in the figure,  $E$  and  $D$  are points on  $AB$  and  $AC$ , respectively.  $\triangle ABC$  is divided into three smaller triangles and one quadrilateral.  $AE = EB$ .  $AD : DC = 1 : 2$ . Find the area of the quadrilateral  $AEFD$  if the area of  $\triangle ABC$  is 90.

- (A) 21 (B) 24 (C) 23 (D) 22 (E) 19



**Problem 23.** In the figure shown,  $ABCD$  is a parallelogram.  $O$  is the intersection of  $AC$  and  $BD$ .  $E$  is a point on the extension of  $AB$ . Connect  $OE$  to meet  $BC$  at  $F$ .  $AB = 5$ ,  $AD = 4$ , and  $BE = 3$ . What is the length of  $BF$ ?

- (A)  $17/11$  (B)  $14/11$  (C)  $15/11$  (D)  $13/11$  (E)  $12/11$

