

Hybleland L9-Lesson 04 Combination 2-Assignment

Practice 1. Five distinct circles are drawn in a plane. What is the maximum number of points where at least two of the circles intersect?

- (A)18 (B)19 (C)20 (D)22 (E)26

Practice 2. Ten distinct circles are drawn in a plane. What is the maximum number of points where at least two of the circles intersect?

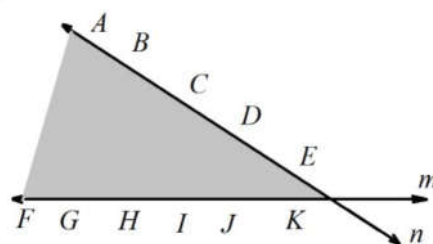
- (A)90 (B)45 (C)80 (D)82 (E)86

Practice 3. Three distinct circles and four straight lines are drawn in a plane. What is the maximum number of points of intersection?

- (A)12 (B)24 (C)30 (D)36 (E)48

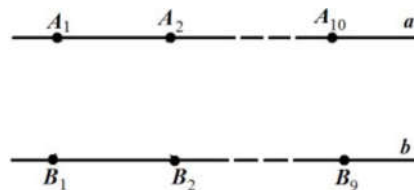
Practice 4. Five distinct points on line n (A,B,C,D,E) and six distinct points on line m (F,G,H,I,J,K) are chosen to maximize the number of intersections in the shaded region among the 30 unique line segments connecting one of the four points on n to one of the five points on m . Find the maximum number of intersections in the shaded region, excluding the intersections at points on lines m or n .

- (A)120 (B)132 (C)150 (D)167 (E)180



Practice 5. As shown in the figure, line a is parallel to line b . There are 10 points on line a and none points on line b . If we connect each point on a with each point on b , we get many lines. If no three of these line intersects at one point, what is the number of intersection points between a and b ?

- (A)1520 (B)1620 (C)1650 (D)1670 (E)1800

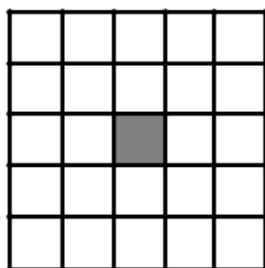


Practice 6. Lines L_1, L_2, \dots, L_{200} are distinct. All lines L_{4n} , n a positive integer, are parallel to each other. All lines L_{4n-3} , n a positive integer, pass through a given point A . The maximum number of points of intersection of pairs of lines from the complete set $\{L_1, L_2, \dots, L_{50}\}$ is

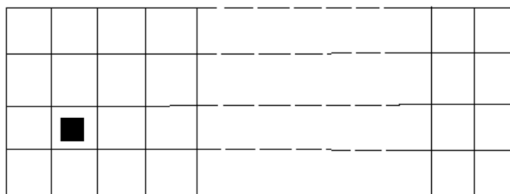
- (A)1024 (B)1082 (C)1100 (D)1200 (E)1030

Practice 7. The 5×5 grid shown contains a collection of rectangles. How many of these rectangles contain the black center square?

- (A)12 (B)15 (C)17 (D)81 (E)20



Practice 8. The 4×16 rectangular grid of squares shown below contains a shaded square. How many rectangular sub-regions contain the shaded square?



- (A) 120 (B) 150 (C) 170 (D) 180 (E) 190

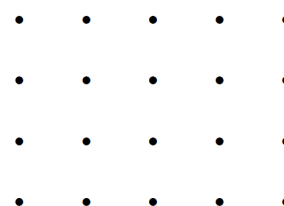
Practice 9. A set of four points is chosen randomly from the grid shown. Each four point set has the same probability of being chosen. What is the probability that the points form a square?

- (A) $1/21$ (B) $1/14$ (C) $2/21$ (D) $1/7$ (E) $2/7$



Practice 10. Twenty lattice points are arranged along the edges of a 4×3 rectangle as shown. How many triangles have all three of their vertices among these points?

- (A) 1056 (B) 1052 (C) 1036 (D) 1032 (E) 1012

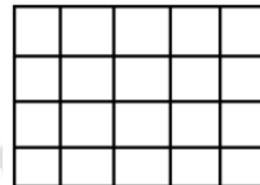


Practice 11. Find the number of triangles whose vertices are lattice points in the xy -plane satisfying $1 \leq x \leq 5$ and $1 \leq y \leq 5$.

- (A) 1650 (B) 2200 (C) 2270 (D) 2148 (E) 2160

Practice 12. A set of 20 square blocks is arranged into a 4×5 rectangle. How many different combinations of 2 blocks can be selected from that set so that the 2 blocks do not share a common side?

- (A) 100 (B) 125 (C) 159 (D) 155 (E) 160



Practice 13.

AMC10B 2002 / Problem 18

Four distinct circles are drawn in a plane. What is the maximum number of points where at least two of the circles intersect?

- A. 8 B. 9 C. 10 D. 12 E. 16

Practice 14.

UKMT-IMC 2009 / Problem 21

There are lots of ways of choosing three dots from this 4 by 4 array. How many triples of points are there where all three lie on a straight line (not necessarily equally spaced)?



- A. 8 B. 16 C. 20 D. 40 E. 44

Challenge-Practice 15. (2005, AIME, Problem 5)

Robert has 4 indistinguishable gold coins and 4 indistinguishable silver coins.

Each coin has an engraving of a face on one side, but not on the other.

He wants to stack the eight coins on a table into a single stack so that no two adjacent coins are face to face.

Find the number of possible distinguishable arrangements of the 8 coins.