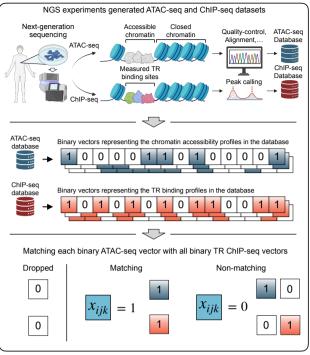
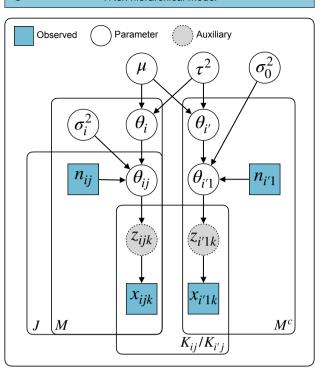
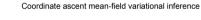
## а Data preprocessing and region mapping Next-generation Accessible Closed



## TRex hierarchical model



## Mean-field variational inference

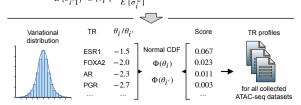


Mean-field variational family

$$q\left(\Theta\right)=q\left(\mu\right)q\left(\varepsilon^{2}\right)q\left(\sigma_{0}^{2}\right)\prod_{i=1}^{M}q\left(\sigma_{i}^{2}\right)\prod_{i=1}^{M}q\left(\theta_{i}\right)\prod_{i=1}^{M^{c}}q\left(\theta_{i'}\right)\times\\ \prod_{i=1}^{M}\prod_{j=1}^{J_{i}}q\left(\theta_{ij}\right)\prod_{i'=1}^{M^{c}}q\left(\theta_{i'1}\right)\prod_{i=1}^{M}\prod_{j=1}^{J_{i}}\prod_{k=1}^{K_{ij}}q\left(z_{ijk}\right)\prod_{i=1}^{M^{c}}\prod_{k=1}^{K_{i'1}}q\left(z_{i'1k}\right)$$
 Update the expectation of factors

$$E\left[z_{ijk}\right] = \begin{cases} E\left[\theta_{ij}\right] + \phi\left(E\left[\theta_{ij}\right]\right)/(1 - \Phi(E\left[\theta_{ij}\right])) & \text{use coordinate ascent to find optimal:} \\ \theta_{ij}^*(\theta_{ij}) = \phi\left(E\left[\theta_{ij}\right]\right)/(\Phi(E\left[\theta_{ij}\right])) & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{j}\right|\Theta_{-j},X\right)\right)\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{j}\right|\Theta_{-j},X\right)\right)\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{j}\right|\Theta_{-j},X\right)\right)\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{ij}\right|\Theta_{-j},X\right)\right)\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{ij}\right|\Theta_{-j},X\right)\right]\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{-j}\right),X\right]\right]\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{-j}\right),X\right]\right]\right\} \\ & \text{use } \left\{E_{-j}\left[\ln\left(p\left(\theta_{-j}\right),X\right]\right]\right\} \\ & \text{use }$$

Similarly for all factors 
$$E\left[\theta_{ij}\right] \quad E\left[\theta_{i}\right] \quad E\left[\mu\right] \\ E\left[z_{ijk}\right] \quad E\left[\theta_{i'1}\right] \quad E\left[\theta_{i'}\right] \quad E\left[\tau^{2}\right] \\ E\left[z_{i'1k}\right] \quad E\left[\theta_{i'1}^{2}\right] \quad E\left[\theta_{i}^{2}\right] \quad E\left[\sigma_{0}^{2}\right] \\ E\left[\theta_{i'1}^{2}\right] \quad E\left[\theta_{i'}^{2}\right] \quad E\left[\sigma_{i}^{2}\right] \end{cases}$$
 Minimize KL divergence:  $KL\left(q_{opt}|\mid p\left(\Theta\mid X\right)\right)$ 



## d Integration results for TRex online portal

