

R Package Development

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Chapter 1

Introduction

1.1 Abstract

This report discuss the development of the R package `rmcop`, an objective oriented financial option pricing package.

In chapter 2, fundamental technical concepts are introduced. These includes explanations on financial options and programming techniques in R that are essential for understanding the development phase described in chapter 4.

In chapter 3, the report enumerates multiple existing R packages for financial options pricing. We will discuss their functionalities and identify the advantages and limitations `rmcop` has comparing to them.

In chapter 4, we give detailed explanations on quantitative models in option pricing and their R implementations. This part will be roughly divided into two sections: deterministic methods and Monte Carlo methods.

In the last chapter, we will explain the current functionalities and limitations of `rmcop` comprehensively, and briefly discuss the possible extension of the package in the future.

1.2 Literature Review

The very first attempt of applying quantitative method in option pricing (perhaps in all finance) is by the French mathematician Louis Bachelier in 1900 [1]. In his paper “The Theory of Speculation,” he deducted deterministic formulas for pricing European (vanilla) call and put options as follows:

Being the earlist approach, Bachelier’s formula had already outlined the relationship between option price and asset price S , strike price X , and volatility measure σ , which are essential fragments in modern formulas. However, based on limited data, Bachelier’s solution was built under some unrealistic assumptions. The normality assumption violates the non-negativity of the stock price, and the formula’s discrete measure in time omitted the effect of continuous movements in the stock price. Also, the formula did not discount the effect of interest rate. These errors cause Bachelier’s model fails to price options accurately.

It wasn’t until 1960s had further improvement been made to quantitative option pricing. In 1961, Case Sprenkle [2] introduced the Sprenkle formula. The formula addressed the above issues by describing the stock price by the more suitable log-normal distribution and discounting for the effect of interest

rate, which successfully explained the time value of an option. In the following decade, improvements have been made by scholars such as Boness and Samuelson, who introduced empirical constants to increase the effectiveness of Sprenkle's model.

The model was finalised by Black and Scholes in 1973, who explained the stock price movement by General Brownian Motion (GBM) described by a Stochastic Differential Equation (SDE). The solution (derived through Itô's lemma) of Black-Scholes formula under an risk-neutral assumption eliminates the empirical measure of Sprenkle et al's model.

[3]

[4]

$$\sigma \tag{1.1}$$

Chapter 2

Concepts

2.1 Financial Options

2.1.1 Option Styles

2.1.2 Pricing of Option

2.2 R

2.2.1 R Package Development

2.2.2 Objective Oriented Programming in R

Existing packages in R ecosystem provides comprehensive pricing algorithms for financial derivatives. However, their function are based on Procedural Oriented Programming (POP). POP functions can be called directly by passing in required arguments. For simple options pricing cases, such as pricing individual options, using POP functions is intuitive. However, many real scenarios require pricing options in a complex formulation, such as compounded options (i.e. options with underlying assets being another option) and combination of options (i.e. spread, straddle, strangle, and other option strategies). In these situations, managing numerous arguments for POP functions can be difficult and inefficient.

The `rmcop` package proposed an Objective Oriented Programming (OOP) approach for pricing financial options in R. It encapsulates multiple arguments, such as option style, type, strike price, and maturity time, into an `option` class object. It also allows encapsulation of other market environment arguments, such as interest rate, dividend yield rate, and volatility measure into an `option.env` class object. The OOP structure enables easier variables managements and facilitates the comparison of prices among different sets of options and market environments.

The codes below demonstrates the calculation of an theoretical European vanilla call option with strike price $K = 20$, maturity $t = 0.75$, under the market condition such that the current price is $S = 20$, fixed interest rate is $r = 1\%$, and market volatility measured by $\sigma = 0.1$. We use Monte Carlo (i.e. `mc`) method with $n = 100$ replications and number of time steps per replication $steps = 1$.

OOP approach requires extra steps declaring objects before using the function, but once the declaration is completed, calling the pricing function is much simpler than the POP approach. As above, it

only required two (object) arguments, `obj` and `env`.

R provides two ways to perform OOP, the S3 and S4 methods. The S3 class objects are based on R `list` objects. An R list contains a `class` attribute, which can be customised into string (or vector of strings) that can be interpreted as a list's corresponding S3 class (i.e. so that the list itself became an object of that class). Other items within the list can be treated as object's properties under the OOP scope, and can be extracted using the `$` operator. Here is an example on how to implement OOP using S3 method in R.

```
1 John <- list(  
2   "age" = 20,  
3   "gender" = "male",  
4   "nation" = "UK"  
5 )  
6 class(John) <- "student"
```

We first define a new `list` object named "John", which contains three items (age, gender, and nationality). Then, we redefined the class of this list using the `class()` function to "student". Now, we have created a new object named "John" of the class "student" under the S3 scheme.

The S4 methods requires more rigorous class and object definition, as one would typically see within an OOP language such as Python and Java. The development of our pricing functions does not require rigorous OOP structure or defining generic functions, so S3 method is sufficient for its development.

Chapter 3

Existing Option Pricing Packages within R Ecosystem

3.1 Packages Review

3.1.1 derivmkt

3.1.2 fOptions

3.1.3 RQuantLib

An R interface to the QuantLib library, which embeds C++ programming.

3.2 General Comments

Chapter 4

Package Development

4.1 Package Structure

4.1.1 R Scripts

The package consists of 7 R scripts, with their contents defined as below:

File	Contents
<code>Option.R</code>	Methods creating and updating option and <code>option.env</code> objects
<code>Price.R</code>	Pricing functions takes objects input and calls specific pricing engines
<code>MonteCarlo.R</code>	Monte Carlo option pricing method engine functions
<code>BlackScholes.R</code>	Black-Scholes option pricing method engine functions
<code>Binomial.R</code>	Binomial option pricing method engine functions
<code>Trinomial.R</code>	Trinomial option pricing method engine functions
<code>Tools.R</code>	Other supplementary functions used in package

For the simplicity of user access, only four functions are exported, they are:

Function	Description
<code>option()</code>	Create new " <code>option</code> " class object, which represents the option of interest
<code>option.env()</code>	Create new " <code>option.env</code> " class object, which represents the market environment of interest
<code>update.option.env()</code>	Update the variables within a defined " <code>option.env</code> " class object
<code>price.option()</code>	Pricing the option based on specified option, market environment, and method input

4.2 Functions

4.3 Deterministic Methods

4.3.1 Black-Scholes Model

The movement of asset prices is intuitively described by an Geometric Brownian Motion (GBM). Through 1960s to 1970s, deterministic formula have been driven by numerous scholars.

Introduced by Fisher Black and Myron Scholes in 1973, the Black-Scholes model provides a deterministic method in valuing options under the assumption that the underlying asset's price is described by a Geometric Brownian Motion (GBM).

the Black-Scholes valuation formula provides a deterministic estimation for European option price.

Introduced by Fischer Black and Myron Scholes, the Black-Scholes model perceive the movement of the stock price as an Geometric Brownian Motion (GBM). The general form of the Brownian motion is specified by the following Stochastic Differential Equation (SDE) [5]:

$$\frac{dS(t)}{S(t)} = \mu(S(t), t)dt + \sigma dW(t) \quad (4.1)$$

Where μ is the drift term measuring the "direction" of the price movement at time t , σ measuring the volatility of the motion, and $W(t)$ the Standard Brownian Motion.

4.3.2 Binomial Lattice Tree

Introduced by Cox, Ross, and Rubinstein in 1979, the Binomial Model

4.3.3 Trinomial Lattice

Extending the Binomial model, the Trinomial Lattice model was introduced by Phelim Boyle in 1988 [6].

4.3.4 Discussion on Multinomial Option Pricing Models & Their Relationship with Binomial Model

4.4 Monte Carlo Methods

Due to the complexity of American option pricing using Monte Carlo method, the package (until now) has only includes European option pricing.

4.4.1 Vanilla Option Pricing

4.4.2 Asian Option Pricing

Different from a vanilla option whose payoff only depends on stock price at maturity (i.e. $t = T$), an Asian option's payoff is determined by the average stock price throughout the option's life \bar{S} and the strike price K . To calculate \bar{S} , we need to consider the price movement throughout $t \in [0, T]$, making the pricing of an Asian option path-dependent, i.e. we should store the price at any time $t \in [0, T]$ for each simulated price trajectory [7].

A generalised case of the stock pricing model is given by:

$$dS(t) = rS(t)dt + \sigma(S(t))S(t)dW(t) \quad (4.2)$$

4.4.3 Barrier Option Pricing

4.4.4 Binary Option Pricing

4.4.5 Lookback Option Pricing

Chapter 5

Discussion

5.1 Package Limitation

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