ECE 343 Lab #3: Power Supply and Voltage Regulator

1 Introduction

Learning Objectives:

- Circuit design using nonlinear circuit elements

- Making and justifying design choices based on requirements

- Simulate design power supply on LTSpice

- Evaluate performance parameters and compare with design requirements

- Build a AC-DC power supply

- Solder circuit on a PCB

- Compute DC-DC conversion efficiency of three circuits - voltage dividers, zener diode based on DC-DC conversion (ECE 110), power supply designed in this lab (ECE 343).

- Compare DC-DC conversion efficiency of designed voltage regulators with DC-DC conversion using a boost/buck converter (ECE 469)

Components Required:

- **Breadboard**

- **Resistors, Capacitors**: based on designs.

- **Diodes:** D1N750 (Zener Diode), D1N 4001/4002 (Rectifier Diodes).

- **BJT:** 2N3055, **OpAmp:** LM741

2   Introduction

In this lab we will design an AC/DC power supply. This project will be completed in three lab sessions and will call upon your knowledge of nonlinear circuit elements like diodes and the ability to make justified design choices. The design makes use of two different kinds of diodes - the basic silicon PB junction device, used as a rectifier in this case, and the zener diode, used to regulate the output DC voltage. Figure 1 shows the block diagram of a basic DC power supply.

The various components of the DC power supply are:

- **Transformer:** Transfers electrical energy from one circuit to another. It consists of two coils (primary and secondary) would on a magnetic core. The primary winding is connected to the **120** V (RMS) AC mains and the secondary winding is connected to the rectifier circuit.

- **Diode Rectifier:** The rectifier circuit converts the input AC signal V_s to a one sided signal. **(Lab 2)**.

- **Filter:** The output of rectifier is passed through a filter block to reduce ripple in the signal.

- **Zener-diode based regulator**: Used to further reduce the ripple in the voltage and to give a stable DC output voltage.

3 Design Specifications

The power supply will be designed to meet the following specifications,

- DC open circuit output voltage is 4.7V.

- Open circuit output voltage stays within 2% of the desired voltage as AC line voltage varies from 115 V (rms) to 125 V (rms).

- Ripple voltage at output is less than 2% of open circuit output DC voltage.

- The output current can vary from 0 to 20 mA.

4   Design Walk-through

4.1   AC power source and rectifier

For this design we will use the sine wave source for LTSpice simulations. The actual circuit will be tested using a transformer connected to AC mains. The input sine wave to the power supply is rectified using as shown below. There are two possible rectifier: (1) Half-wave rectifier (Fig. 2 (a)) and (2) Full-wave bridge rectifier (Fig. 2 (b))

- Give a sketch of voltage across resistor $\mathbf{R_1}$ and $\mathbf{R_2}$. Assume $\mathbf{V_{in}(t) = 25\sqrt{2}\sin(2\pi 60t)V}$. Clearly indicate the peak value of voltage in each case.
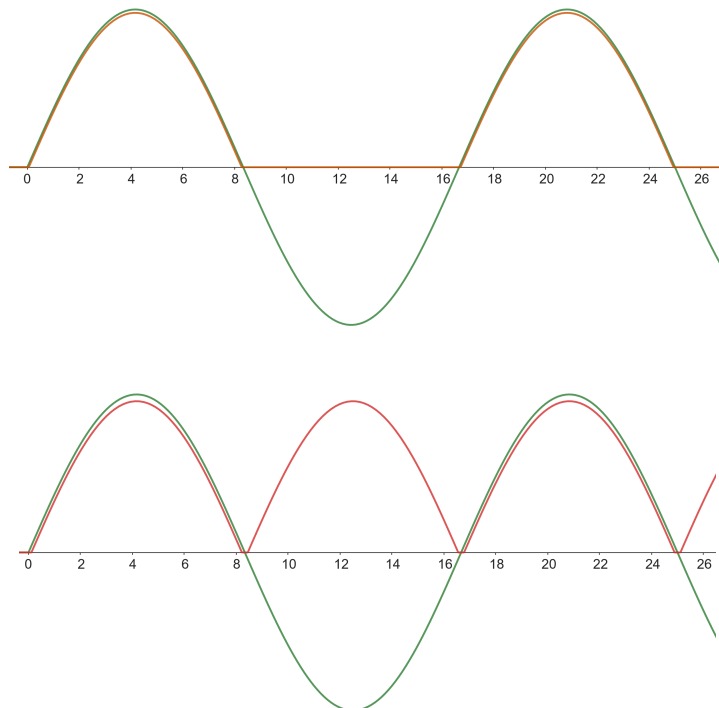
Suppose the diode has a forward voltage of V_F. The datasheet gives the following data:
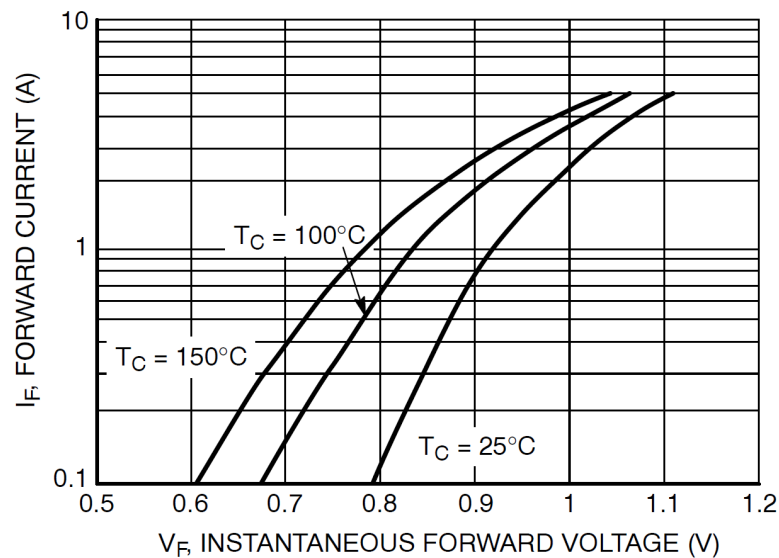
So we see that the forward voltage is around $0.8 - 1.1V$, but it could be smaller. In the LTSpice, a simulation with $R_1 = R_2 = 1000\Omega$ gives $V_F \approx 755\text{mV}$. Then the peak value of voltage is

$$\max(V_{R1}) = |V_{in}| - V_F \approx \boxed{34.60\text{V}}$$
$$\max(V_{R2}) = |V_{in}| - 2 \cdot V_F \approx \boxed{33.845\text{V}}$$

- What are the advantages/disadvantages of each circuit

> For the half-wave rectifier, as the name implies, you only get half of the entire waveform, which is will have a bigger ripple voltage compared to full-wave rectifier, but the peak voltage will be much closer to the peak voltage of the original waveform than a full-wave rectifier does. For whole-wave rectifier, you will get full input waveform, but your waveform will has less peak voltage when compared to half-wave rectifier, and each sine pulse in the waveform are separated by a small time gap.

- The average voltage value, $\langle \mathbf{V} \rangle$, of voltage $\mathbf{V(t)}$ is given by,

$$\langle \mathbf{V} \rangle = \frac{1}{T} \int_0^T \mathbf{V(t)} \, dt$$

Compute the average value of input voltage $\mathbf{V_{in}(t)}$, half wave rectified output $\mathbf{V_{R1}(t)}$, and full wave rectified output $\mathbf{V_{R2}(t)}$. You may assume the rectification is ideal and there is no voltage drop across the diodes.

> By symmetry, so
>
> $$\mathbf{V_{in}(t) = 0}V$$
>
> and doing the integral, we get
>
> $$\mathbf{V_{R1}(t)} = \frac{1}{T} \int_0^T \mathbf{A} \sin\left(\frac{2\pi}{T} t\right) dt = -\frac{A}{T} \frac{T}{2\pi} \cos\left(\frac{2\pi}{T} t\right)\Big|_0^{T/2} = \frac{A}{\pi} \approx 11.254V$$
>
> $$\mathbf{V_{R2}(t)} = \frac{1}{T} \int_0^T \mathbf{A} \sin\left(\frac{2\pi}{T} t\right) dt = -2 \cdot \frac{A}{T} \frac{T}{2\pi} \cos\left(\frac{2\pi}{T} t\right)\Big|_0^{T/2} = \frac{2A}{\pi} \approx 22.508V$$

4.2   Regulator

The regulator is simply a resistor and zenor-diode (Fig. 3), whose function is to hold the output voltage, $\mathbf{V_0}$, constant against variations in the load current and against variations in the AC line voltage. It also serves to reduce the ripple voltage that appears across the filter capacitor and would otherwise appear at the power supply output $\mathbf{V_0}$ as well.

4.3   Regulator Design

The regulator design mainly involves picking an appropriate **operating point** for the zener diode. The basic configuration of regulator is show in Fig. 3. Following considerations must be kept in mind:

1. Too much current will cause the diode to overheat.

2. Too little current will cause diode to sit in flat region of the I-V curve and lose regulation.

3. The resistor $\mathbf{R_s}$ limits the maximum current that can flow through the zener diode. This condition occurs when the load current $\mathbf{I_L = 0}$

Answering the following question will help you design the regulator circuit:

- Sketch the $\mathbf{I - V}$ characteristic of a reversed biased zener diode.
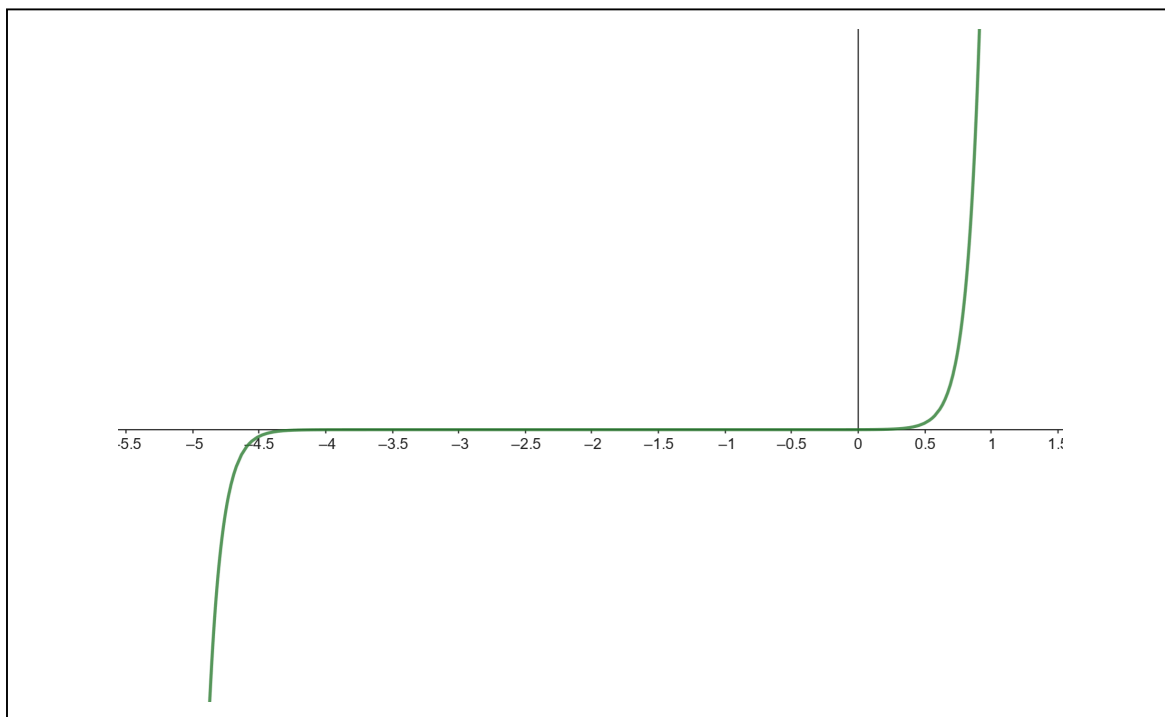
- Based on your sketch, give a short explanation of how reversed biased zener diode can function as a regulator. Also mention which part of the $\mathbf{I - V}$ curve should the diode be operated to operate as a regulator.

> The zenor diode should operate in breakdown region ($\mathrm{V} < \mathrm{V_Z}$). It could regulate variations in the AC line voltage $\mathrm{V_m}$, as $\mathrm{V_m}$ changes or has fluctuations, its current will vary greatly, but according to the graph, the V will sit close to $\mathrm{V_Z}$, so the output voltage is regulated. When the load current changes, its current voltage will vary greatly, but again according to the graph, the V will sit close to $\mathrm{V_Z}$.

- The zener voltage $\mathbf{V_Z}$ is fixed by the DC supply output voltage. What is the value of $\mathbf{V_Z}$ for this design.

> It should be $\boxed{\mathbf{V_Z = 4.7V}}$, as we want the DC supply voltage to be 4.7V

- The part number of zener diode used in this lab is **D1N750**. Refer to the device data sheet and note down the max power rating of the diode. Use **75**% of the maximum power to compute the maximum current that the diode can tolerate (This condition occurs when load current $\mathbf{I_L = 0}$)

> From the datasheet, we see that **maximum power dissipation** is 500mW. To use 75% of the maximum power, the maximum current have to be
> $I_{max} = (500\text{mW} \cdot 75\%)/4.7\text{V} = \boxed{79.79\text{mA}}$.

- What is the value of $\mathbf{R_S}$ required to ensure that current through the diode does not exceed the maximum allowed value. Assume $\mathbf{V_m = 25\sqrt{2}V}$.

> The zenor diode will have its maximum current when $I_L = 0$A. So in this case
>
> $$\mathbf{I_Z = I = (V_m - V_Z) \big/ R_s} \leq I_{max}$$
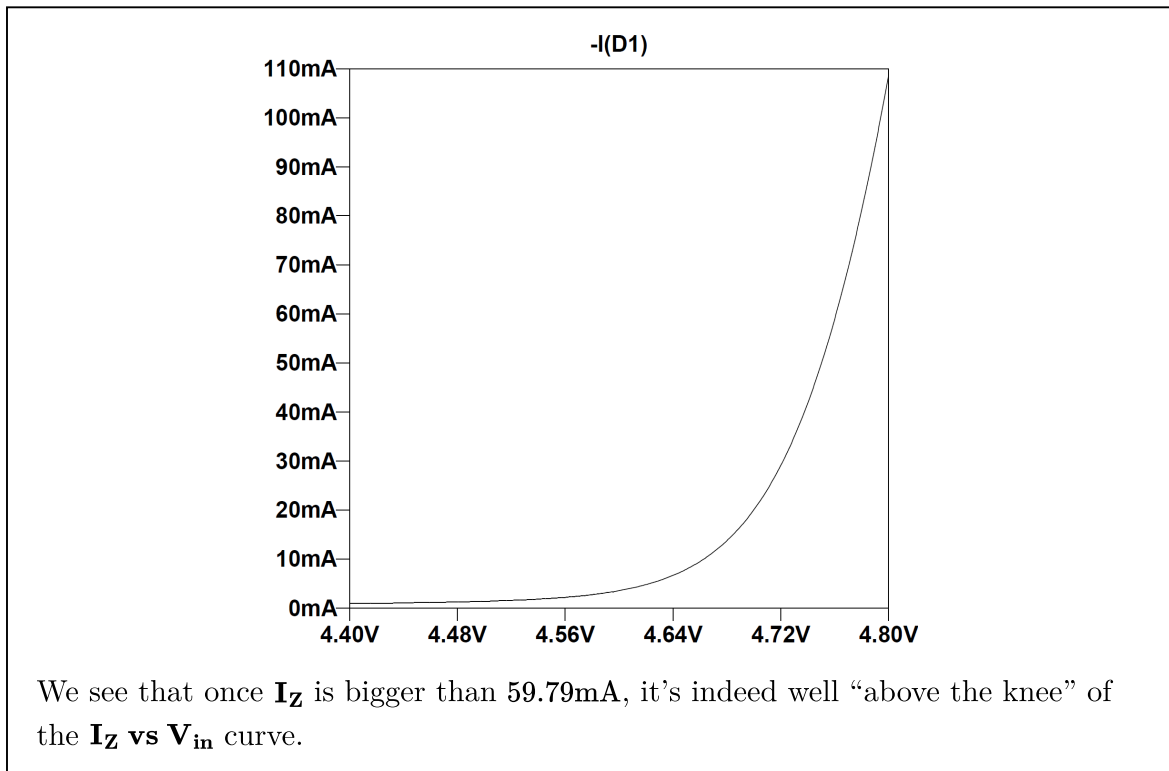>
> using ideal diode assumption. So
>
> $$\mathbf{R_s} \geq \frac{V_m - V_Z}{I_{max}} \approx \boxed{384.21\Omega}$$

- The current $\mathbf{I_Z}$ though will vary based on the load current ($\mathbf{I_L}$) that is drawn from the regulator. What is the minimum value of current $\mathbf{I_Z}$?

> Suppose we use the I_{max} calculated when $I_L = 0$A. We see that maximum $\mathbf{I_L}$ is **20mA**, so the minimum $\mathbf{I_Z = 79.79\text{mA} - 20\text{mA} = 59.79\text{mA}}$.

- At this point you must verify that the zener diode operates in the correct region of operation. Perform a DC sweep simulation of the circuit shown in Fig. 4. You can sweep voltage $\mathbf{V_{in}}$ from $\mathbf{4.4 - 4.8V}$. Plot $\mathbf{I_Z \text{ vs } V_{in}}$ and verify that the minimum current through the zener diode is above the knee of the $\mathbf{I_Z \text{ vs } V_{in}}$ curve.

-I(D1)

We see that once $\mathbf{I_Z}$ is bigger than **59.79mA**, it's indeed well "above the knee" of the $\mathbf{I_Z}$ **vs** $\mathbf{V_{in}}$ curve.

4.4   Filter

The filter block is used to reduce the ripple in the rectifier output. The filter section is **only a single capacitor** connected from the output of the rectifier circuit to ground. (Fig. 6.). The following points illustrate the role of the capacitor:

- The capacitor provides current to the load between peaks of rectified output.

- Between peaks of rectified voltage, the filter capacitor is discharging at a rate that depends upon the amount of current delivered to the regulator.

- The **ripple voltage**, $V_{\mathrm{ripple,\,C}}$, **across the capacitor (C)** can related to the value of the capacitance as follows,

$$\mathbf{V_{ripple,C}} = \frac{\mathbf{I_L}}{\mathbf{fC}}$$

where, $\mathbf{I_L}$ is the DC component of the load current and $\mathbf{f}$ is the frequency of the filter output.

- In order to use the expression to compute C, the output ripple voltage must be converted to the ripple across capacitor.

4.4.1   Picking the Capacitor

Using the maximum allowable **output ripple voltage** (from the specifications), we can work backwards to the maximum allowable ripple voltage at the filter. This is done by replacing the diode by its incremental model as shown below:

- Use the device data-sheet to obtain the incremental resistance of the diode

$$\boxed{R_{z,\,max} = 19\Omega}$$

  The actual R_z seems to be much smaller than the worst case situation, usually around 2Ω (from LTSpice simulation).

- Use the maximum allowable **output ripple voltage** to obtain the maximum allowable ripple across the capacitor.

  We therefore know that $V_{ripple,\,out} \leq 2\% \cdot 4.7V = 0.094V$, and it's obvious that

  $$V_{ripple,\,out} = \frac{R_z}{R_z + R_s} \cdot V_{ripple,\,C} = \frac{19\Omega}{384.21\Omega + 19\Omega} \cdot V_{ripple,\,C} \leq 0.094V$$

  and therefore

  $$V_{ripple,\,C} \leq 0.094V \cdot \frac{384.21\Omega + 19\Omega}{19\Omega} \approx \boxed{1.995V}$$
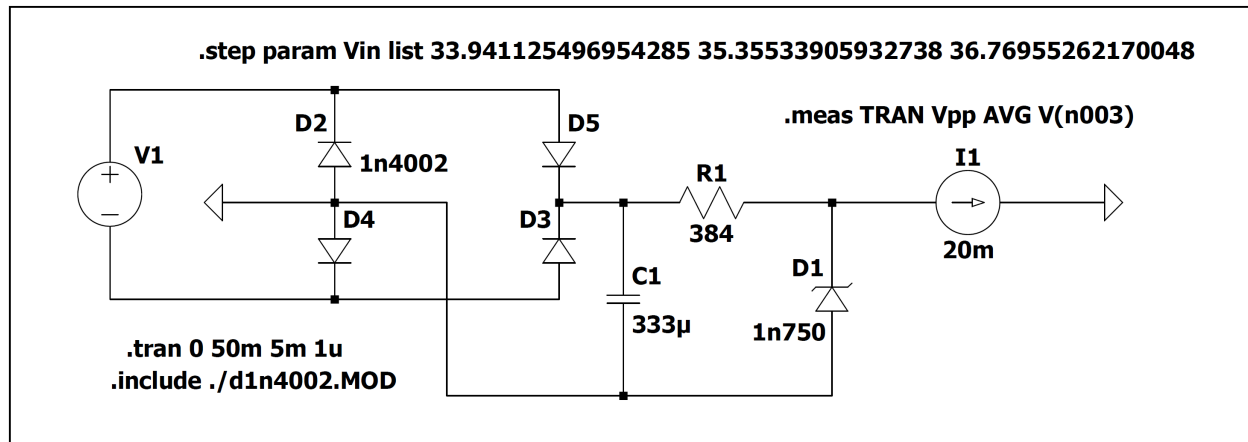
- Compute the capacitor value. Also mention the voltage rating of the capacitor . **Hint:** This is obtained from the maximum voltage difference across the capacitor.

  Using the formula, we know that for a half wave rectifier, the frequency **f** is roughly the same as the input frequency **60Hz**, for a full wave rectifier, the frequency **f** is roughly the twice of the input frequency **120Hz**. So,

  $$\mathbb{C}_{half} \geq \frac{I_{L,max}}{f \cdot V_{ripple,\,C}} = \frac{79.79mA}{60Hz \cdot 1.995V} = \boxed{666.6\mu F}$$

  $$\mathbb{C}_{full} \geq \frac{I_{L,max}}{f \cdot V_{ripple,\,C}} = \frac{79.79mA}{120Hz \cdot 1.995V} = \boxed{333.3\mu F}$$

4.5   Complete Design

Sketch the complete power supply circuit (based on bridge rectifier) you have designed. Include all the components and their values. For now you can replace the transformer circuit with sinusoidal input of appropriate value.

.step param Vin list 33.941125496954285 35.35533905932738 36.76955262170048

D2

V1   **D5**

1n4002   **.meas TRAN Vpp AVG V(n003)**

D4   **R1**   **I1**

D3   **384**   **20m**

C1   **D1**

333µ   **1n750**

.tran 0 50m 5m 1u
**.include ./d1n4002.MOD**

5 Simulations

- We will now verify the designed power supply using LTSpice. You are to construct the power supply and run simulations that will test the performance of the power supply over a variety of realistic situations like variable loading and dirty power.

V_{in} (V)	I_L (mA)	Ripple across C (V)	Output voltage ripple (mV)	Output DC voltage (V)
$24\sqrt{2}$	0	1.505	3.521	4.770
$26\sqrt{2}$	0	1.662	3.621	4.777
$25\sqrt{2}$	0	1.583	3.571	4.774
$25\sqrt{2}$	20	1.584	4.557	4.754

- Also save the output plots for each case.
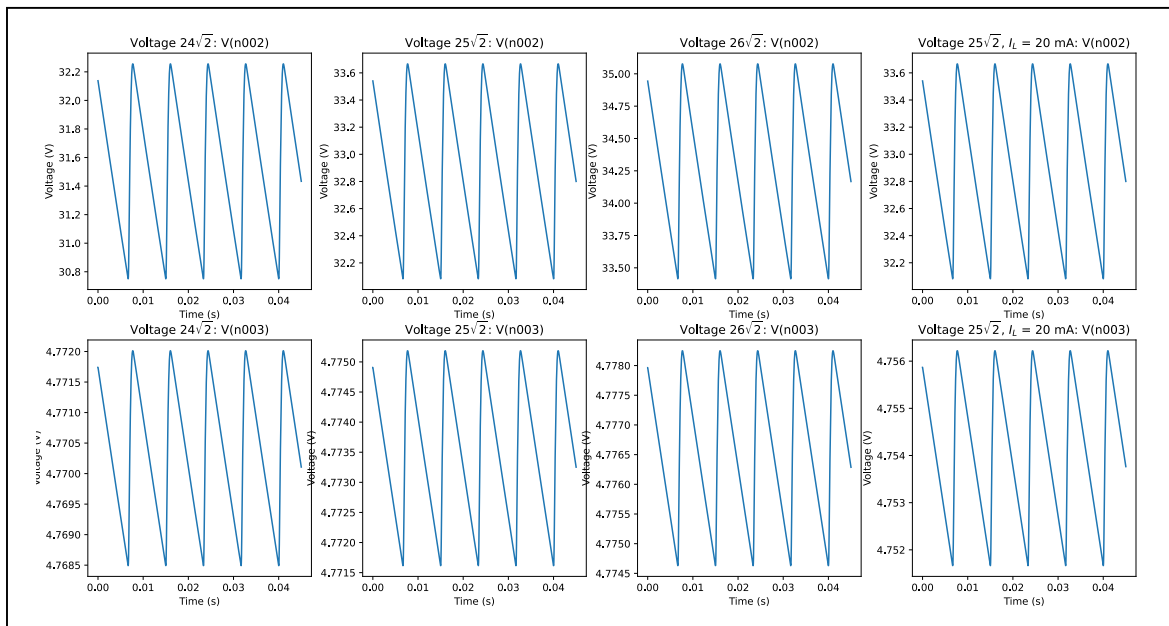
6 Bench Test

Build the circuit you have tested in simulations. Complete the following table to verify its operation. **Please note:** ask your TA to verify your circuit before you test it.

V_{in} (V)	I_L (mA)	Ripple across C (V)	Output voltage ripple (mV)	Output DC voltage (V)
$125\sqrt{2}$	0	1.89	47.7	4.8475

7   Increasing the supply voltage

7.1   Design and Calculation

The first step is to increase the output voltage of the power supply to approximately **10V**. Consider the circuit shown below:

- Compute gain of the circuit $\mathbf{A_V = V_{out}} \big/ \mathbf{V_{in}}$ and fix the ratio $\mathbf{R_1} \big/ \mathbf{R_2}$ to obtain $\mathbf{A_V \approx 2}$.

From ideal Op-Amp assumption, we have

$$\mathbf{A_V} = \frac{\mathbf{V_{out}}}{\mathbf{V_{in}}} = \left(1 + \frac{\mathbf{R_1}}{\mathbf{R_2}} \right) \approx 2$$

Therefore,

$$\frac{\mathbf{R_1}}{\mathbf{R_2}} \approx 1$$

- Compute the maximum power dissipated in the resistor $\mathbf{R_1}$ and $\mathbf{R_2}$. While performing bench test of the designed circuit, the resistors you pick must be rated for this power. **Hint:** Determine the condition under which max power dissipation occurs.

If the $\mathbf{I_{out}}$ is **0**, then the resistors will have maximum dissipated power. In this case, the power for them is
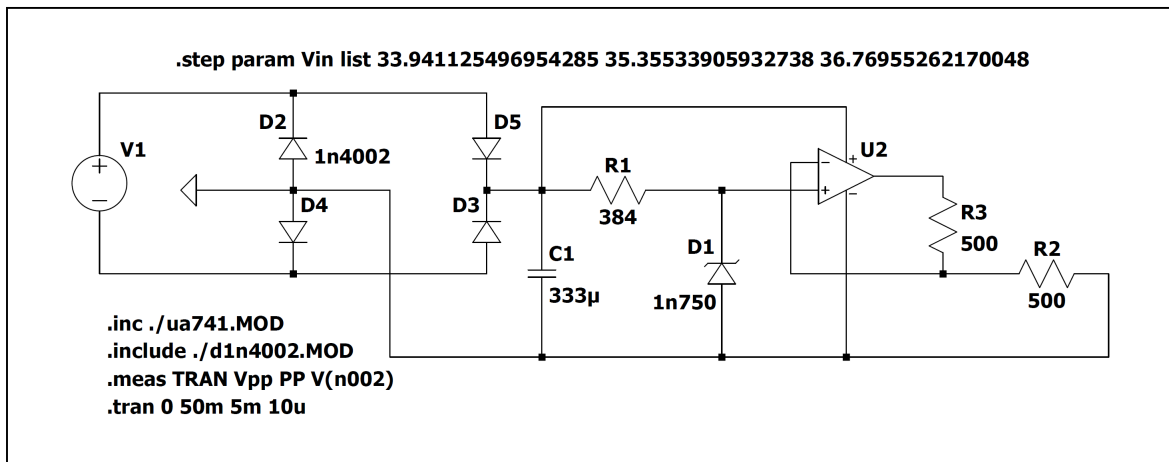
$$P_{max,\,1} = P_{max,\,2} = \frac{V_{out}^2}{4 \cdot \mathbf{R_1}} = \frac{V_{out}^2}{4 \cdot \mathbf{R_2}}$$

- The Op-Amp circuit shown in Fig. 9 will be used to increase the output voltage of the DC power supply you designed. **The rail voltages for the Op-Amp can be taken from the terminals of filter capacitor**. You must ensure that this satisfies the maximum allowed rail voltages for LM 741 IC (ref: Datasheet). Note down the maximum allowed rails voltages from the device datasheet and then justify if voltage across the plates of capacitor satisfies this requirement.

$\mathbf{V_{amp,max}}$ (V)	$\mathbf{V_{c,max}}$ (V)
$\pm 22\text{V} \sim 44\text{V}$	35.36V

This should work, as the maximum voltage difference $\mathbf{V_{c,max}}$ is smaller than the Op-Amp maximum.

- Sketch the new circuit that includes Op-Amp in negative feedback configuration to increase the power supply output. **Note:** The rail voltage V_+ can be taken from the terminals of filter capacitor and V_- can be at ground.

```
.step param Vin list 33.941125496954285 35.35533905932738 36.76955262170048
```

D2 1n4002 D5 U2
V1 R1 384
D4 D3 R3 500 R2
C1 333µ D1 1n750 500

```
.inc ./ua741.MOD
.include ./d1n4002.MOD
.meas TRAN Vpp PP V(n002)
.tran 0 50m 5m 10u
```

7.2   LTSpice Simulation

- Simulate your circuit using LTSpice. Complete the following table to verify its operation. **Please Note:** Ask your TA to verify your circuit before you test it.

V_{in} (V)	I_L (mA)	Ripple across C (V)	Output voltage ripple (mV)	Output DC voltage (V)
$24\sqrt{2}$	0	1.540	7.269	9.541
$26\sqrt{2}$	0	1.700	7.478	9.553
$25\sqrt{2}$	0	1.620	7.373	9.547
$25\sqrt{2}$	5	1.620	7.374	9.548
$25\sqrt{2}$	20	1.620	7.474	9.548
$25\sqrt{2}$	80	1.620	4.470e-5	0.184

- Is the output DC voltage maintained at the designed value for different load currents? Justify your answer. **Hint: Device Datasheet can give you a clue**

> Seems like that at 80mA, the circuit fails to maintain its voltage. The datasheet said that LM741 have a maximum short circuit output current of 25mA, so it's not able to sustain 80mA output.

- Note down the maximum power dissipated by resistors R_1, R_2 and R_s under no load conditions and $V_{in} = 25\sqrt{2}$
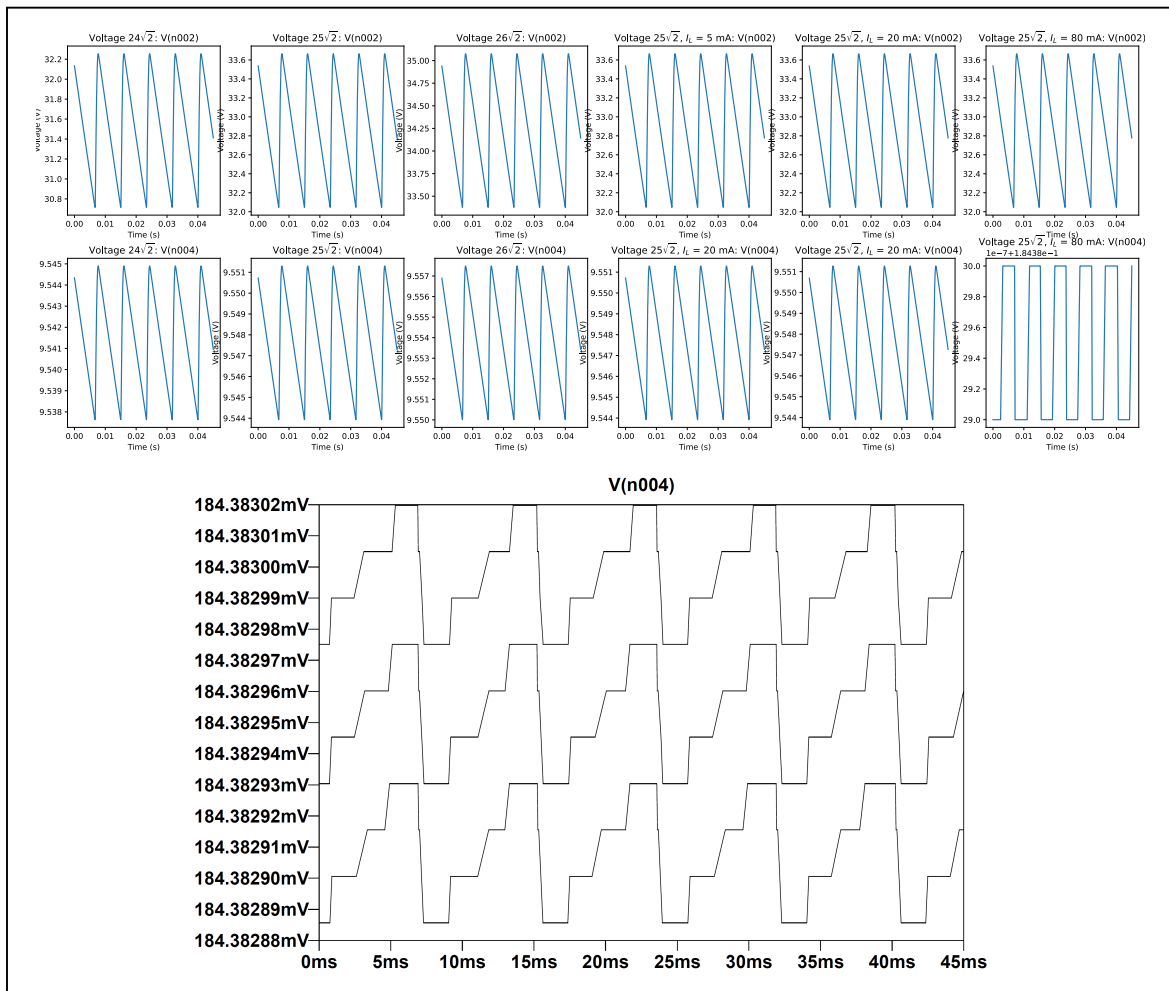
$$\mathbf{R_1} = 45.58\text{mW}$$

$$\mathbf{R_2} = 45.58\text{mW}$$

$$\mathbf{R_s} = 2.061\text{W}$$

- Save simulation plots showing DC output voltage and ripple.

  Note, there is a error is y axis for last simulation in the first plot, the correct one for the last simulation is the middle trace in the second plot.

8 Increasing output current rating

8.1 Design and Calculation

In this section you will make further modifications to your circuit to meet the output current specifications of the power supply. Consider the BJT shown below:

- Give a brief explanation of how the BJT can be used to provided DC current gain

> The output current $I_E = (1 + \beta) I_B$, and β is a big constant, so we see that DC current get amplified.

- Consider now the circuit shown in Fig. 11 below. Compute the maximum power dissipated by the BJT in the circuit shown in Fig. 11. Compare with the specifications in device data sheet.

$P_{\text{max, datasheet}}$ (W)	$P_{\text{max, calculated}}$ (W)
115W	2.0768W

> As the BJT power could be approximated as $I_E \cdot V_{CE}$ where $V_{\text{max, CE}} = 35.36V - 9.4V = 25.96V$, and $I_{\text{max, E}} = 80mA$. The calculated power is way smaller than the maximum power rating in datasheet, so we should be fine in this case.

- Sketch the complete power supply unit:
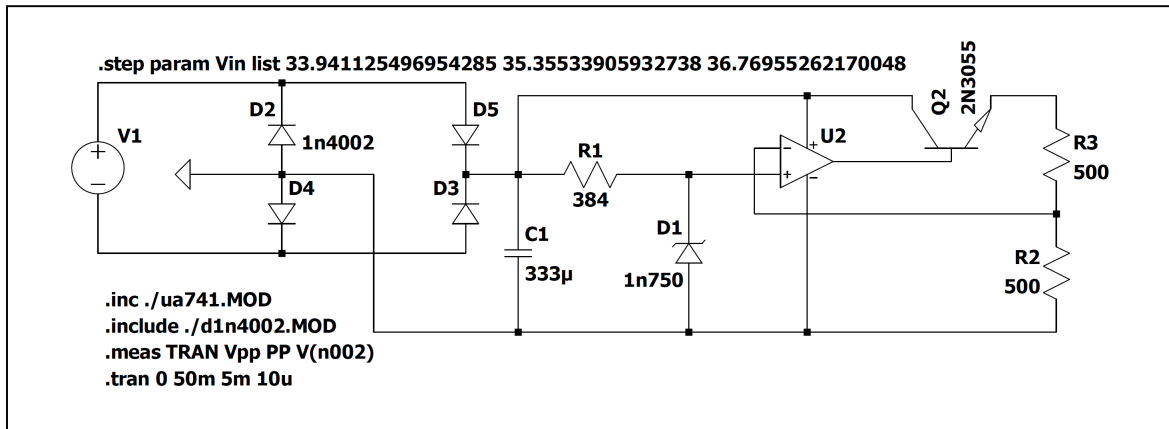
8.2 LTSpice Simulation

- Simulate your circuit using LTSpice. Complete the following table to verify its operation.

V_{in} (V)	I_L (mA)	Ripple across C (V)	Output voltage ripple (mV)	Output DC voltage (V)
$24\sqrt{2}$	0	1.729	8.183	9.541
$26\sqrt{2}$	0	1.888	8.329	9.553
$25\sqrt{2}$	0	1.808	8.253	9.547
$25\sqrt{2}$	5	1.906	8.712	9.547
$25\sqrt{2}$	20	2.198	10.084	9.547
$25\sqrt{2}$	80	3.326	15.509	9.544

- Note down the power dissipated by the transistor ($\mathbf{P_T}$) and power delivered to the load ($\mathbf{P_L}$) under maximum load conditions and $\mathbf{V_{in} = 25\sqrt{2}V}$

$$P_T = 1.989W \quad P_L = 764mW$$
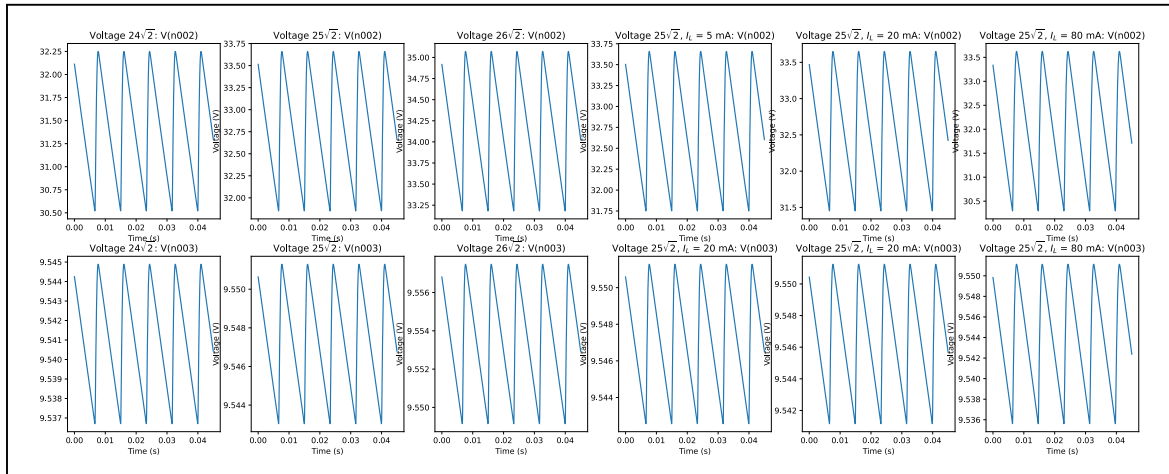
9 Bench Test

Build the circuit you have tested in simulations. Complete the following table to verify its operation. **Please Note:** Ask your TA to verify your circuit before you test it.

$\mathbf{V_{in}}$ (V)	$\mathbf{I_L}$ (mA)	Output DC voltage (V)
$115\sqrt{2}$	0	9.588
$120\sqrt{2}$	0	9.637
$125\sqrt{2}$	0	9.650