Instructions:

Please answer the questions below. Show all your work. This is an open-book test. NO discussion/collaboration is allowed.

Problem 1. (10 points)

Consider the perceptron algorithm and let us re-write the weight updates as follows:

 $\begin{aligned} &\text{Initialization}: w_1^+ = w_1^- = 0\\ &\text{Mistakes on positive}: w_{t+1}^+ = w_t^+ + x\\ &\text{Mistakes on negative}: w_{t+1}^- = w_t^- - x\\ &\text{Weight update}: w_{t+1} = w_{t+1}^+ + w_{t+1}^- \end{aligned}$

If the inputs are images from two categories: apple (positive) and banana (negative). What would the final weights of w_T^+ and w_T^- look like as an image after T iterations, and why? What about w_T ?

Problem 2. (10 points)

Consider a multiclass logistic regression with L1 regularization as follows:

$$z_{l} = \sum_{j=1}^{2} w_{lj} x_{j} + b_{l}, l = 1, 2$$

$$y_{k} = \frac{e^{z_{k}}}{\sum_{l} e^{z_{l}}}, k = 1, 2$$

$$\mathcal{L} = -\sum_{k} t_{k} \log y_{k} + \lambda \sum_{i=1}^{2} \sum_{j=1}^{2} ||w_{ij}||_{1} + \gamma \sum_{l=1}^{2} ||b_{l}||_{1}$$

Draw a computational graph for this network and its loss. Note each node should be a scalar in this graph.

Write down the forward pass based on the graph you have built.