

Pseudo-code:

```
For i to size - 1
    Grab point 1 & point 2 and calculate distance(pt1,pt2) initialize result struct
    For j (j=i+1) to size-1
        Distance = dis (pt[i],pt[j])
        If(distance < result.distance)
            Result.distance = distance
            Clear vector which store the shortest pair of points
            Push pt[i],pt[i+1] to vector
        else if (distance == result.distance)
            push finded pairs to vector
    End for
End for
```

Asymptotic Analysis of run time:

For the out for loop it iterates through all elements of the points array who has n elements, so it will execute n times. Inner loop go through element from index i + 1 to 0, so it will go through 1 times, 2 times, ... n-1 times. When out loop go through n times, total times for inner loops execution is $1 + 2 + 3 + \dots + n - 1 = (1 + n - 1) * n / 2 = n^2 / 2$.

When $n \rightarrow \infty$, $T(n) = n^2 / 2$, which divider 2 is not import, due to the n^2 domain it. $n^2 / 2 < n^2$, so $T(n) = O(n^2)$. The time complexity of Brute force would be $O(n^2 / 2)$.

Empirical analysis and plotting:

| NumInputs(100)\times | 1st | 2nd | 3rd | 4th | 5th |
|----------------------|-----------|-----------|-----------|-----------|------------------|
| Runtime | 0.000159s | 0.000149s | 0.000155s | 0.000170s | 0.000148s |
| -- | 6th | 7th | 8th | 9th | 10 th |
| -- | 0.000162s | 0.000150s | 0.000175s | 0.000149s | 0.000149s |

Average: 0.000157s

| NumInputs(1000)\times | 1st | 2nd | 3rd | 4th | 5th |
|-----------------------|-----------|-----------|-----------|-----------|------------------|
| Runtime | 0.014481s | 0.014158s | 0.014113s | 0.014336s | 0.014153s |
| -- | 6th | 7th | 8th | 9th | 10 th |
| -- | 0.014154s | 0.013996s | 0.013928s | 0.013956s | 0.013961s |

Average: 0.014248s

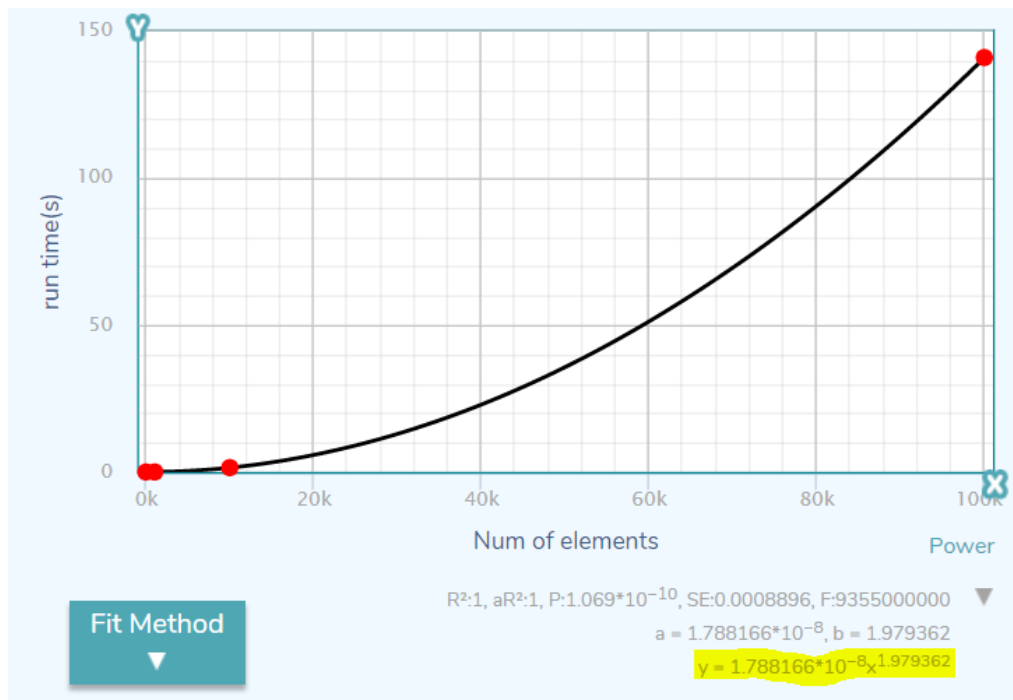
| NumInputs(10000)\times | 1st | 2nd | 3rd | 4th | 5th |
|------------------------|-----------|-----------|-----------|-----------|------------------|
| Runtime | 1.424536s | 1.451141s | 1.554845s | 1.533729s | 1.411581s |
| -- | 6th | 7th | 8th | 9th | 10 th |
| -- | 1.592131s | 1.407556s | 1.409005s | 1.589402s | 1.412498s |

Average: 1.4786474s

| NumInputs(100000)\times | 1st | 2nd | 3rd | 4th | 5th |
|-------------------------|------|------|------|------|------------------|
| Runtime | 141s | 142s | 140s | 140s | 142s |
| -- | 6th | 7th | 8th | 9th | 10 th |
| -- | 139s | 140s | 141s | 141s | 142s |

Average: 140.8s

Plot:



After we plug the points into the curve fitting tools, I get this curve and whose formula almost same as $y = x^2$.