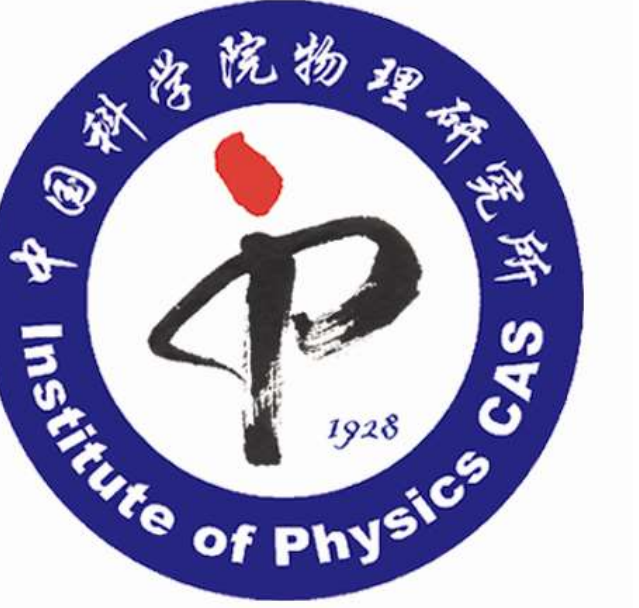


Tianyi Zhang,<sup>1</sup> Caihua Wan,<sup>1,\*</sup> and Xiufeng Han<sup>1,\*</sup>

<sup>1</sup>Beijing National Laboratory for Condensed Matter Physics,  
Institute of Physics, Chinese Academy of Sciences, Beijing 100190, China



**Abstract** Spin-orbit torque (SOT) is a promising technique for next-generation magnetic random-access memory. Recent experiments have shown that materials with low-symmetry crystalline or magnetic structures can generate anomalous SOT with an out-of-plane component, which is crucial for switching the perpendicular magnetization of adjacent ferromagnetic (FM) layers in a field-free condition. In this study, we derive the threshold current for field-free perpendicular magnetization switching using anomalous SOT and numerically calculate the magnetic moment trajectory in an FM free layer for currents smaller and greater than the threshold. We also investigate the dependence of switching time and energy consumption on applied current, finding that the minimum energy consumption decreases with an increasing out-of-plane torque proportion. Additionally, we explore the relationships between the threshold current and anisotropy strength, out-of-plane torque proportion, FM free-layer thickness, and Gilbert damping constant. The results show a negative correlation between the threshold current and out-of-plane torque proportion, and positive correlations with the other three parameters. Finally, we demonstrate that even when the applied current is smaller than the threshold current, it can still add an effective exchange bias field  $H_{bias}$  on the FM free layer. The  $H_{bias}$  is proportional to the applied current  $J_{SOT}$ , facilitating the determination of anomalous SOT efficiency. Our findings provide insights into the design of spintronic devices that favor field-free switching of perpendicular magnetization using anomalous SOT and offer a means of adjusting the exchange bias field to control FM layer magnetization depinning.

## Results

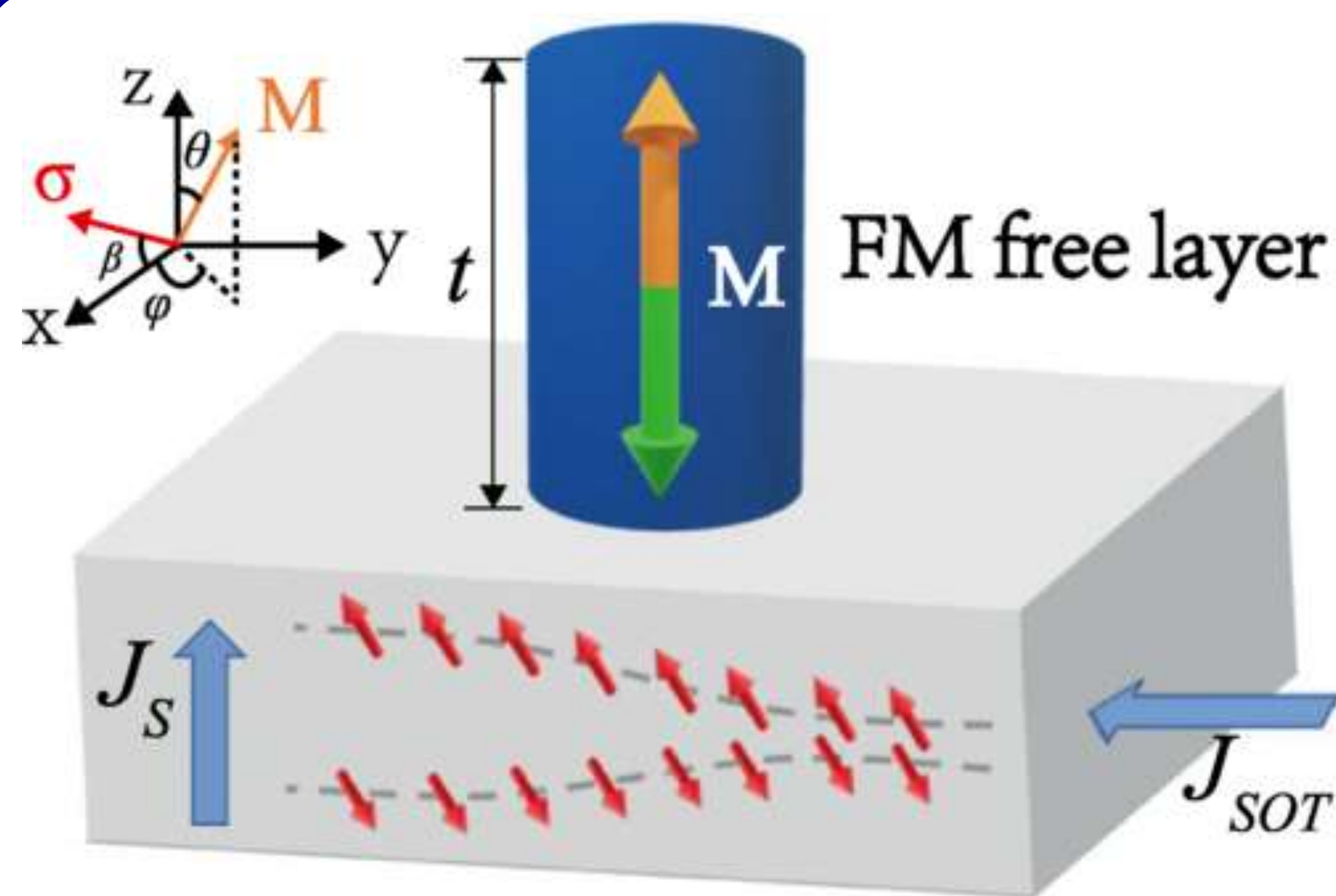


FIG. 1. A schematic diagram of the FM free-layer magnetization switch driven by an anomalous SOT with both in-plane and out-of-plane components. The applied electron current  $J_{SOT}$  is along the  $-y$  direction and generates a spin current  $J_s$  propagating along the  $z$  direction. The spin current diffuses into the FM free layer with the perpendicular magnetic anisotropy to drive its magnetization dynamics.

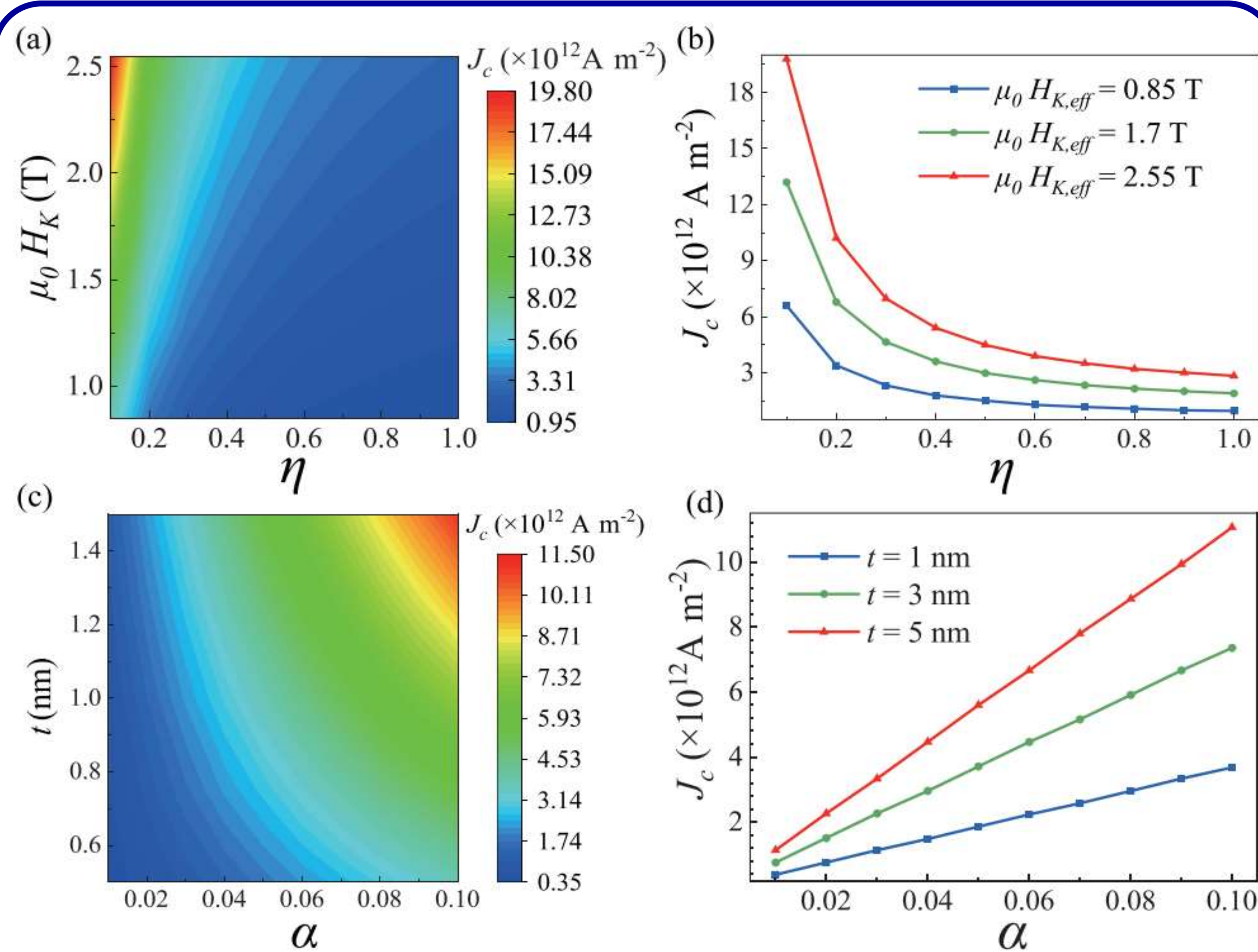


FIG. 4. (a) The dependence of  $J_c$  on the anisotropic field  $H_K$  and anomalous ratio  $\eta$ . (b) The  $\eta$  dependence of  $J_c$  under  $\alpha = 0.015$ ,  $t = 1$  nm extracted from Fig. 4(a). (c) The dependence of  $J_c$  on the thickness  $t$  and Gilbert damping  $\alpha$ . (d) The  $\eta$  dependence of  $J_c$  under  $\mu_0 H_K = 0.85$  T,  $\eta = 0.75$  extracted from Fig. 4(c).

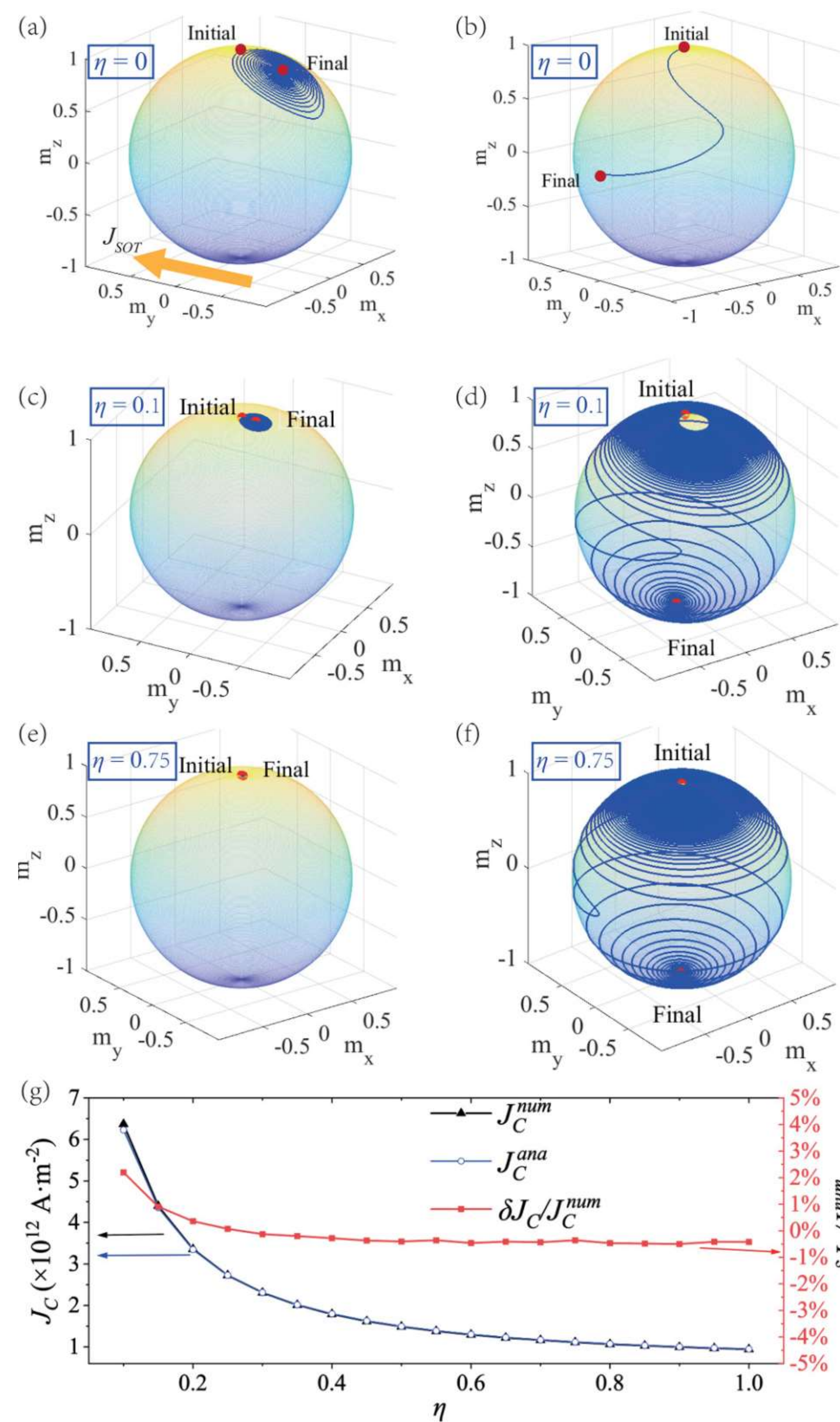


FIG. 2. (a)–(f) The magnetization trajectory with different  $\eta$  and  $J_{SOT}$ . The two parameters are shown as follows.  $\eta = 0$ , (a)  $J_{SOT} = 1.8 \times 10^{13}$  A m $^{-2}$  and (b)  $J_{SOT} = 1.9 \times 10^{13}$  A m $^{-2}$ ;  $\eta = 0.1$ , with threshold current value  $J_c = 6.23 \times 10^{12}$  A m $^{-2}$ , (c)  $J_{SOT} = 6.2 \times 10^{12}$  A m $^{-2}$ , and (d)  $J_{SOT} = 6.37 \times 10^{12}$  A m $^{-2}$ ;  $\eta = 0.75$ , with threshold current value  $J_c = 1.116 \times 10^{12}$  A m $^{-2}$ , (e)  $J_{SOT} = 1.1 \times 10^{12}$  A m $^{-2}$ , and (f)  $J_{SOT} = 1.12 \times 10^{12}$  A m $^{-2}$ . (g) The  $\eta$  dependence of analytical threshold current  $J_c^{ana}$ , numerical threshold current  $J_c^{num}$ , and error  $\delta J_c/J_c^{num} = (J_c^{num} - J_c^{ana})/J_c^{num}$ .

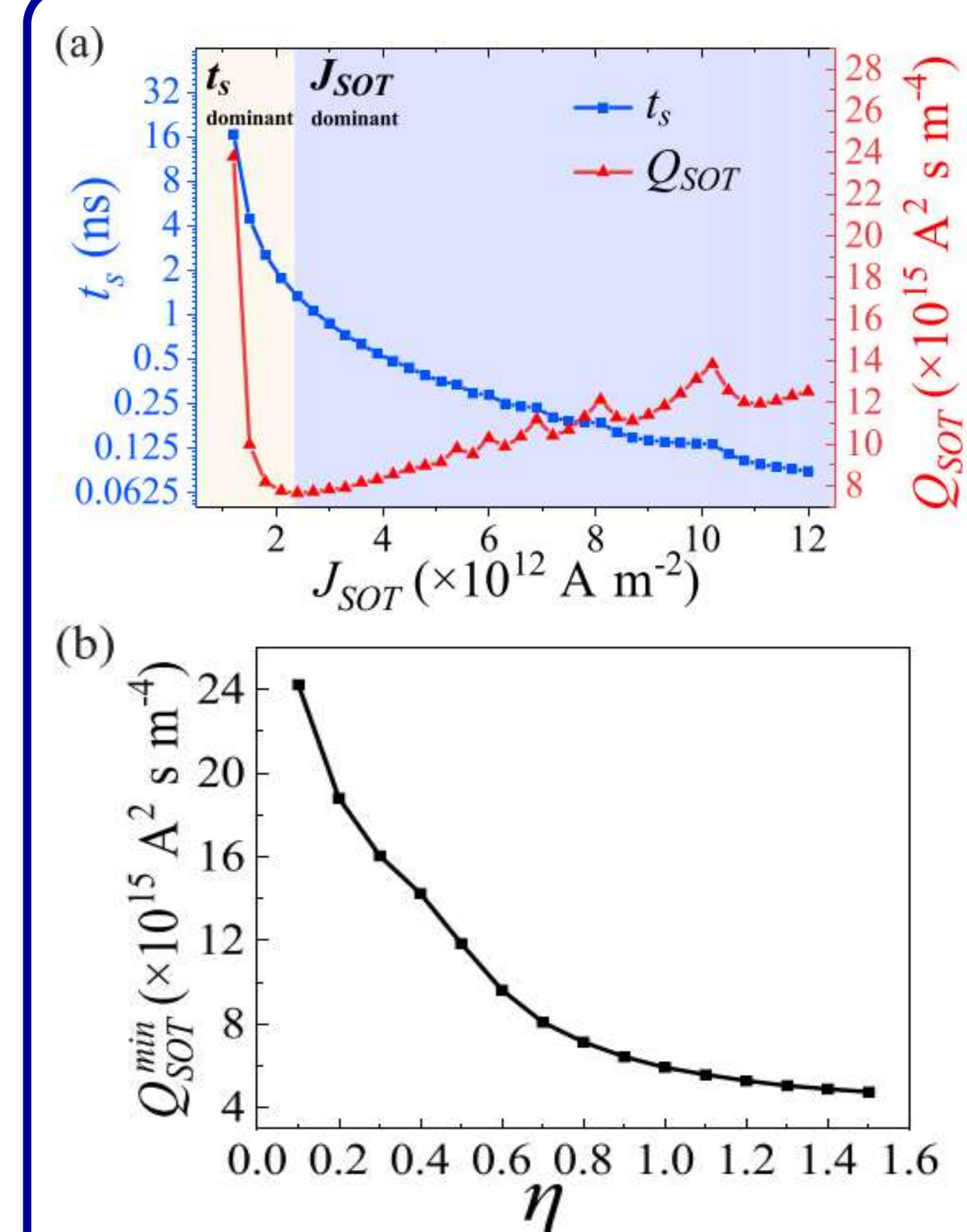


FIG. 3. (a) The  $J_{SOT}$  dependence of the switching time  $t_s$  and the switching energy consumption  $Q_{SOT}$ . (b) The  $\eta$  dependence of minimum energy loss  $Q_{SOT}^{min}$ . In the regime of  $\eta \leq 0.8$ , the increase in  $\eta$  can significantly reduce the value of  $Q_{SOT}^{min}$ .

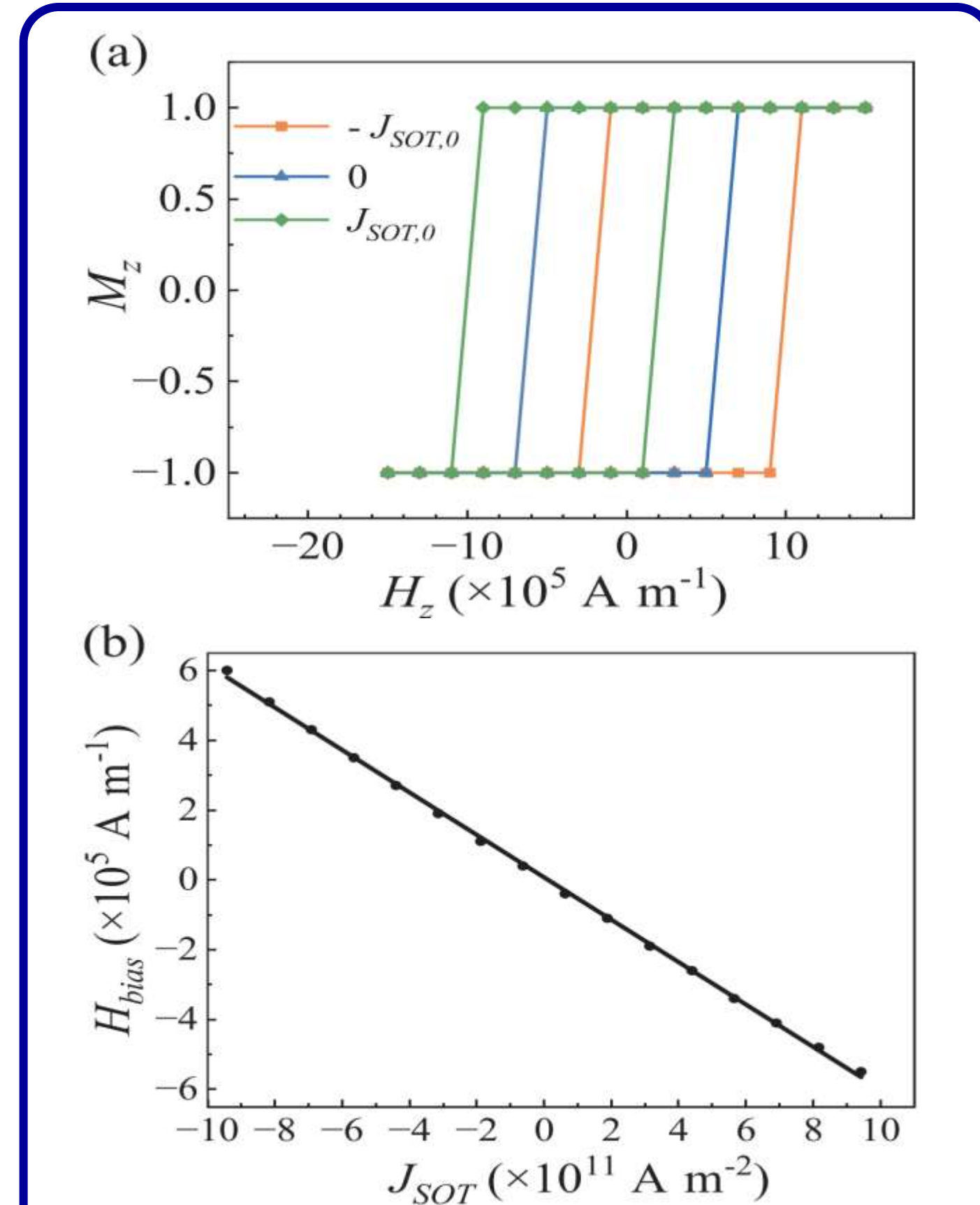


FIG. 5. (a) Hysteresis loop of FM free layer under different applied currents  $J_{SOT}$ . (b) Relationship between equivalent exchange bias field  $H_{bias}$  and applied current  $J_{SOT}$ . Here  $\eta = 0.75$ .