

WMD

$$d(w_i, w_j) = \|w_i - w_j\|_2$$

$$d(s_1, s_2) \swarrow \nearrow$$

$$\downarrow$$

$$\sum_{i,j} \hat{T}_{ij} d(w_i, w_j)$$

sWMD
(forward)

$$d(w_i, w_j; M) = (w_i - w_j)^T M (w_i - w_j)$$

$$d(s_1, s_2; M) \swarrow \nearrow$$

$$\downarrow$$

$$\sum_{i,j} \hat{T}_{ij} d(w_i, w_j; M)$$

SWMD
(learning)

$$M^{(t)}$$

$$d(w_i, w_j; M^{(t)}) = (w_i - w_j)^T M^{(t)} (w_i - w_j)$$

$$d(s_1, s_2; M^{(t)})$$

$$\sum_{i,j} \hat{T}_{ij}^{(t)} d(w_i, w_j; M^{(t)})$$

监督学习 (利用Margin Loss 对M的优化)

内嵌局部优化 (WMD的线性规划)

$$l(M^{(t)}) = \lambda \sum_{u=1}^N \sum_{v \in \text{pos}(u)} d(s_u, s_v; M^{(t)})$$

$$+ (1-\lambda) \sum_{u=1}^N \sum_{v \in \text{pos}(u)} \sum_{w \in \text{neg}(u)} \max\{0, d(u, v; M^{(t)}) + \eta - d(u, w; M^{(t)})\}$$

$$M^{(t+1)} = M^{(t)} - \alpha \frac{\partial l(M^{(t)})}{\partial M^{(t)}}$$