Assignment 1: Tabular Reinforcement Learning

CS260R 2023Fall: Reinforcement Learning. Department of Computer Science at University of California, Los Angeles. Course Instructor: Professor Bolei ZHOU. Assignment author: Zhenghao PENG, Yiran WANG.

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Welcome to the assignment 1 of our reinforcement learning course. The objective of this assignment is for you to understand the classic methods used in tabular RL.

This assignment has the following sections:

- Section 1: Warm-up on the RL environment (35 points)
- Section 2: Implementation of the model-based family of algorithms: policy iteration and value iteration. (65 points)

You need to go through this self-contained notebook, with dozens of **TODO**s are scattered in the cells. You need to finish all TODOs.

You are encouraged to add more code on extra cells at the end of each section to investigate the problems you think interesting. At the end of the file, we leave a place for you to write comments optionally (Yes, please give us either negative or positive rewards so that we can keep improving the assignment!).

Please report any code bugs to us via **GitHub issues**.

Before you get start, remember to follow the instruction at https://github.com/ucla-rlcourse/assignment-2022fall/tree/main/assignment0 to set up your python environment.

Dependencies

This assignment requires the following dependencies:

```
1. gymnasium==0.29.1
```

- 2. numpy
- 3. scipy

You can install all of them through the following cell:

```
In [1]: # If you already installed everything, you don't need to run this cell.
# Install dependencies to your current python environment.

!pip install -U pip
!pip install mediapy numpy scipy "gymnasium==0.29.1" "gymnasium[toy-text]==0.29.1"

Requirement already satisfied: pip in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (23.2.1)
Collecting pip
    Obtaining dependency information for pip from https://files.pythonhosted.org/packages/47/6a/453160888fab7c6a432a6e25f8afe6256
d0d9f2cbd25971021da6491d899/pip-23.3.1-py3-none-any.whl.metadata
    Using cached pip-23.3.1-py3-none-any.whl.metadata (3.5 kB)
Using cached pip-23.3.1-py3-none-any.whl (2.1 MB)

ERROR: To modify pip, please run the following command:
    C:\Users\yuzha\AppData\Local\Programs\Python\Python311\python.exe -m pip install -U pip

[notice] A new release of pip is available: 23.2.1 -> 23.3.1
[notice] To update, run: python.exe -m pip install --upgrade pip
```

```
Requirement already satisfied: mediapy in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (1.1.9)
Requirement already satisfied: numpy in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (1.26.0)
Requirement already satisfied: scipy in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (1.11.3)
Requirement already satisfied: gymnasium==0.29.1 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages
(0.29.1)
Requirement already satisfied: cloudpickle>=1.2.0 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages
(from gymnasium==0.29.1) (2.2.1)
Requirement already satisfied: typing-extensions>=4.3.0 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-pack
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Requirement already satisfied: pygame>=2.1.3 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from
gymnasium==0.29.1) (2.5.2)
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y) (8.15.0)
Requirement already satisfied: matplotlib in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from med
iapy) (3.8.0)
Requirement already satisfied: Pillow in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from mediap
y) (10.0.1)
Requirement already satisfied: backcall in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from ipyth
on->mediapy) (0.2.0)
Requirement already satisfied: decorator in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from ipyt
hon->mediapy) (5.1.1)
Requirement already satisfied: jedi>=0.16 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from ipy
thon->mediapy) (0.19.0)
Requirement already satisfied: matplotlib-inline in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (f
rom ipython->mediapy) (0.1.6)
Requirement already satisfied: pickleshare in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from ip
ython->mediapy) (0.7.5)
Requirement already satisfied: prompt-toolkit!=3.0.37,<3.1.0,>=3.0.30 in c:\users\yuzha\appdata\local\programs\python\python311
\lib\site-packages (from ipython->mediapy) (3.0.39)
Requirement already satisfied: pygments>=2.4.0 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (fro
m ipython->mediapy) (2.16.1)
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python->mediapy) (5.9.0)
Requirement already satisfied: colorama in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from ipyth
on->mediapy) (0.4.6)
Requirement already satisfied: contourpy>=1.0.1 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (fr
om matplotlib->mediapy) (1.1.1)
```

```
Requirement already satisfied: cycler>=0.10 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from m
atplotlib->mediapy) (0.12.1)
Requirement already satisfied: fonttools>=4.22.0 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (f
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Requirement already satisfied: kiwisolver>=1.0.1 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (f
rom matplotlib->mediapy) (1.4.5)
Requirement already satisfied: packaging>=20.0 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (fro
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Requirement already satisfied: pyparsing>=2.3.1 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (fr
om matplotlib->mediapy) (3.1.1)
Requirement already satisfied: python-dateutil>=2.7 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages
(from matplotlib->mediapy) (2.8.2)
Requirement already satisfied: parso<0.9.0,>=0.8.3 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages
(from jedi>=0.16->ipython->mediapy) (0.8.3)
Requirement already satisfied: wcwidth in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from prompt
-toolkit!=3.0.37,<3.1.0,>=3.0.30->ipython->mediapy) (0.2.6)
Requirement already satisfied: six>=1.5 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from pytho
n-dateutil>=2.7->matplotlib->mediapy) (1.16.0)
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om stack-data->ipython->mediapy) (1.2.0)
Requirement already satisfied: asttokens>=2.1.0 in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (fr
om stack-data->ipython->mediapy) (2.4.0)
Requirement already satisfied: pure-eval in c:\users\yuzha\appdata\local\programs\python\python311\lib\site-packages (from stac
k-data->ipython->mediapy) (0.2.2)
[notice] A new release of pip is available: 23.2.1 -> 23.3.1
[notice] To update, run: python.exe -m pip install --upgrade pip
```

Now start running the cells sequentially (by ctrl + enter or shift + enter) to avoid unnecessary errors by skipping some cells.

Section 1: Warm-up on the RL environment

(35/100 points)

In this section, we will go through the basic concepts of RL environments using OpenAI Gym. Besides, you will get the first sense of the toy environment we will use in the rest of the assignment.

Every Gym environment should contain the following attributes:

- 1. env.step(action) To advance the environment by one time step through applying action. Will return four things: observation, reward, terminated, truncated, info, wherein terminated is a boolean value indicating whether this episode is finished either by the agent successfully finishes the task or makes something wrong so the episode is not valid (like the agent dies), truncated is a boolean value indicating whether this episode reach the maximum step limit. We sometime use done = terminated or truncated as an indicator that an episode is ended. info is a dict containing some information the user is interested in.
- 2. env.reset() To reset the environment, back to the initial state. Will return the initial observation of the new episode.
- 3. env.render() To render the current state of the environment for human-being
- 4. env.action_space The allowed action format. In our case, it is Discrete(4) which means the action is an integer in the range [0, 1, 2, 3]. Therefore, the action for step(action) should obey the limit of the action space.
- 5. env.observation_space The observation space.

Note that the word **episode** means the process that an agent interacts with the environment from the initial state to the terminal state. Within one episode, the agent will only receive one done=True, when it goes to the terminal state (the agent is dead or the game is over).

We will use FrozenLake8x8-v1 as our environment. In this environment, the agent controls the movement of a *character* in a grid world. Some tiles of the grid are walkable, and others are not, making to the agent falling into the water. Additionally, the movement direction of the agent is uncertain and only partially depends on the chosen direction. The agent is rewarded for finding a walkable path to a goal tile. The meaning of each character:

1. S: starting point, safe

2. F: frozen surface, safe

3. H: hole, fall to your doom

4. G: goal, where the frisbee is located

In [2]: # Run this cell without modification
import time
from typing import List, Callable

Import some packages that we need to use
import gymnasium as gym

```
import numpy as np
# Prepare some useful functions
from IPython.display import clear output
import mediapy as media
import matplotlib.pyplot as plt
%matplotlib inline
def wait(sleep=0.2):
          clear output(wait=True)
          time.sleep(sleep)
def print table(data):
          if data.ndim == 2:
                   for i in range(data.shape[1]):
                            print("\n=== The state value for action {} ===".format(i))
                            print table(data[:, i])
                   return
          assert data.ndim == 1, data
         if data.shape[0] == 16: # FrozenLake-v0
                   text = "+----+\n" \
                                   "|----+\n"
                  for row in range(4):
                           tmp = "| {} | {:.3f}|{:.3f}|{:.3f}|{n" }
                                          "+----+\n" \
                                         "".format(
                                     row, *[data[row * 4 + col] for col in range(4)]
                            text = text + tmp
          else:
                  text = "+----+\n" \
                                   "| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |\n" \
                                   "|----+----|\n"
                  for row in range(8):
                           tmp = "| {} | {:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|{:.3f}|
                                         ":.3f}|\n" \
                                          "+----+\n" \
```

```
"".format(
                row, *[data[row * 8 + col] for col in range(8)]
            text = text + tmp
    print(text)
def test random policy(policy, env):
    acts = set()
    for i in range(1000):
        act = policy(0)
        acts.add(act)
        assert env.action space.contains(act), "Out of the bound!"
    if len( acts) != 1:
        print(
            "[HINT] Though we call self.policy 'random policy', "
            "we find that generating action randomly at the beginning "
            "and then fixing it during updating values period lead to better "
            "performance. Using a stochastic policy is not even work! "
```

Section 1.1: Make the environment

You need to know

- 1. How to make an environment
- 2. How to set the random seed of environment
- 3. What is observation space and action space

```
In [3]: # Solve the TODOs and remove `pass`

# TODO: Just a reminder. Do you add your name and student
# ID in the table at top of the notebook?

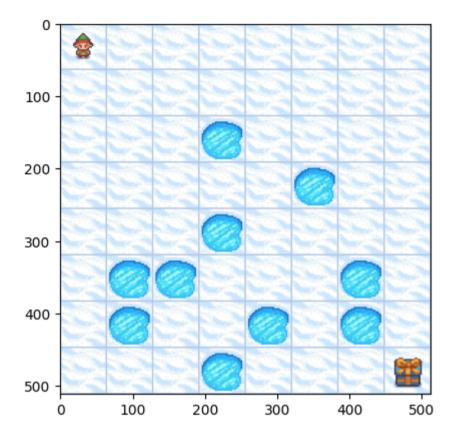
# Create the environment
env = gym.make('FrozenLake8x8-v1', render_mode="ansi")
```

```
# You need to reset the environment immediately after instantiating env.
env.reset(seed=0) # TODO: uncomment this line

print("Current observation space: {}".format(env.observation_space))
print("Current action space: {}".format(env.action_space))
print("0 in action space? {}".format(env.action_space.contains(0)))
print("5 in action space? {}".format(env.action_space.contains(5)))

Current observation space: Discrete(64)
Current action space: Discrete(4)
0 in action space: True
5 in action space? False

In [4]: # Run this cell without modification to get a sense of the environment.
tmp_env = gym.make('FrozenLake8x8-v1', render_mode="rgb_array")
tmp_env.reset()
_ = plt.imshow(tmp_env.render())
```



Section 1.2: Play the environment with random actions

You need to know

- 1. How to step the environment;
- 2. How to rollout a complete episode.

```
In [5]: # Solve the TODOs and remove `pass`

# Run 1000 steps for test, terminate if done.
# You can run this cell multiples times.
env.reset(seed=0)
```

```
while True:
     # Take random action
     # TODO: Uncomment next two Lines
     observation, reward, terminated, truncated, info = env.step(env.action space.sample())
     done = terminated or truncated
     # Render the environment.
     # You will see the visualization of the behaviors of the agent
     # if you are using local machine to run this notebook.
     print(env.render())
     print("Current observation: {}\nCurrent reward: {}\n"
           "Whether we are done: {}\ninfo: {}".format(
         observation, reward, done, info
     ))
     wait(sleep=0.1)
     # TODO: Terminate the loop if done
     if done:
         break
  (Left)
SFFFFFF
FFFFFFF
FFFHFFF
FFFFFHFF
FFFHFFF
FHHFFFHF
FHFFHFHF
FFFHFFFG
Current observation: 46
Current reward: 0.0
Whether we are done: True
```

Section 1.3: Define the evaluation function to value the random baseline

Now we need to define an evaluation function to evaluate a given policy.

As a reminder, you should create a FrozenLake8x8-v1 environment instance by default, reset it after each episode (and at the beginning), step the environment, and terminate the episode if done. According to Gym v26 update,

After implementing the evaluate function, run the next cell to check whether the function is working.

```
In [6]: # Solve the TODOs and remove `pass`
        def render helper(env):
            print(env.render())
            wait(sleep=0.05)
        def evaluate(
            policy: Callable,
            num episodes: int,
            seed: int = 0,
            env name: str = 'FrozenLake8x8-v1',
            render: bool = False,
            render mode: str = 'ansi',
        ) -> float:
            """This function evaluates the given policy and returns the
            average episodic return across #num episodes episodes.
            We use `seed` argument for testing purpose.
            You should pass the tests in the next cell.
            :param policy: a function whose input is an integer (observation)
            :param num episodes: number of episodes you wish to run
            :param seed: an integer, used for testing.
             :param env name: the name of the environment
            :param render: a boolean flag. If true, please call render helper
            function.
            :param render mode: a string specifies the render mode if render=True.
            :return: the averaged episode reward of the given policy.
            0.00
            # Create environment (according to env name, we will use env other than 'FrozenLake8x8-v1')
            env = gym.make(env name, render mode=render mode if render else None)
            # Build inner loop to run.
```

Only terminate episode (reset environment) when done = True.

For each episode, do not set the limit.

```
# The episode reward is the sum of all rewards happen within one episode.
            # Call the helper function `render(env)` to render
            rewards = []
            for i in range(num_episodes):
                # reset the environment
                obs, info = env.reset(seed=seed + i)
                action = policy(obs)
                ep reward = 0
                while True:
                    # TODO: run the environment and terminate it if done, collect the
                    # reward at each step and sum them to the episode reward.
                    obs, reward, terminated, truncated, = env.step(action)
                    done = np.logical or(terminated, truncated) # here use the logical or, one can use terminal
                    action = policy(obs)
                    ep reward += reward
                    if render:
                        render helper(env)
                    if done:
                        break
                rewards.append(ep reward)
            return float(np.mean(rewards))
        # TODO: Run next cell to test your implementation!
In [7]: # Run this cell without modification
        # Run this cell to test the correctness of your implementation of `evaluate`.
        LEFT = 0
        DOWN = 1
        RIGHT = 2
        UP = 3
        def expert(obs):
```

```
"""Go down if agent at the right edge, otherwise go right."""
    return DOWN if (obs + 1) % 8 == 0 else RIGHT
def assert equal(seed, value, env name):
    ret = evaluate(expert, 1000, seed, env name=env name)
    assert ret == value, \
        "When evaluate on seed {}~{} in {} environment, the " \
        "averaged reward should be {}. But you get {}." \
        "".format(seed, seed + 1000, env name, value, ret)
assert equal(0, 0.046, 'FrozenLake8x8-v1')
assert equal(1000, 0.047, 'FrozenLake8x8-v1')
assert equal(2000, 0.065, 'FrozenLake8x8-v1')
assert equal(0, 0.024, 'FrozenLake-v1')
assert equal(1000, 0.034, 'FrozenLake-v1')
assert equal(2000, 0.035, 'FrozenLake-v1')
print("Test Passed!")
print("\nAs a baseline, the mean episode reward of a hand-craft "
      "agent is: ", evaluate(expert, 1000))
```

Test Passed!

As a baseline, the mean episode reward of a hand-craft agent is: 0.046

Congratulation! You have finished section 1 (if and only if not error happens above).

Section 2: Model-based Tabular RL

(65/100 points)

We have learned how to use the Gym environment to run an episode, as well as how to interact between the agent (policy) and environment via env.step(action) to collect observation, reward, done, and possible extra information.

Now we need to build the basic tabular RL algorithm to solve this environment. **Note that compared to the model-free methods** in the Sec.3, the algorithms in this section needs to access the internal information of the environment, namely the transition dynamics.

In our case, given a state and an action, we need to know which state current environment will jump to, the probability of this transition, and the reward of the transition. You will find that we provide you a helper function self._get_transitions(state, action) that takes state and action as input and return you a list of possible transitions.

First, we will implement an abstract class to represent a Trainer. Though this seems to be over-complex for tabular RL, we will use the same framework in the future assignments. So it would be helpful for you to get familiar with how to implement an RL algorithm in the class-oriented programming style.

```
In [8]: # Run this cell without modification
        class TabularRLTrainerAbstract:
            """This is an abstract class for tabular RL trainer. We will subclass this class
             to implement specific algorithm, so that we can reuse the codes like
            getting the dynamic of the environment (self. get transitions()) or rendering the
            learned policy (self.render())."""
            def init (self, env name='FrozenLake8x8-v1', model based=True):
                self.env name = env name
                self.env = gym.make(self.env name)
                self.action dim = self.env.action space.n
                self.obs dim = self.env.observation space.n
                self.model based = model based
                # Define the policy as function that returns the selected action given a state.
                self.policy = None
                # Define the value table as a numpy array.
                self.value table = None
            def get transitions(self, state: int, act: int) -> List:
                """Query the environment to get the transition probability,
                reward, the next state, and done given a pair of state and action.
                We implement this function for you. But you need to know the
```

```
return format of this function.
    .....
    self. check env name()
   assert self.model based, "You should not use get transitions in " \
                             "model-free algorithm!"
   # call the internal attribute of the environments.
   # `transitions` is a list contain all possible next states and the
    # probability, reward, and termination indicator corresponding to it
   transitions = self.env.unwrapped.P[state][act]
   # Given a state-action pair, it is possible
   # to have multiple transitions, since the
   # environment is not deterministic.
   # The return of this function: a list of dicts
   for prob, next state, reward, done in transitions:
        ret.append({
            "prob": prob,
            "next state": next state,
            "reward": reward,
            "done": done
       })
    return ret
def check env name(self):
   assert self.env name.startswith('FrozenLake')
def print table(self):
    """print beautiful table, only work for FrozenLake8X8-v1 env. We
   write this function for you."""
   self. check env name()
    print table(self.value table)
def train(self):
    """Conduct one iteration of learning."""
   raise NotImplementedError("You need to override the "
                              "Trainer.train() function.")
def evaluate(self, seed=1000):
    """Use the function you write to evaluate current policy.
```

```
Return the mean episode reward of 1000 episodes when seed=0."""
result = evaluate(self.policy, seed=seed, num_episodes=1000, env_name=self.env_name)
return result

def render(self, seed=1000):
    """Reuse your evaluate function, render current policy
    for one episode when seed=0"""
    evaluate(self.policy, seed=seed, num_episodes=1, render=True, env_name=self.env_name)
```

```
In [9]: # Run this cell without modification

# Run trainer._get_transitions and give you a sense of how it works.

test_trainer = TabularRLTrainerAbstract()

transitions = test_trainer._get_transitions(state=0, act=0)

print(f"The return transitions is a {type(transitions)}.\n\n{transitions}")
```

The return transitions is a <class 'list'>.

Section 2.1: Policy Iteration

Recall the process of policy iteration:

- 1. Update the state value function, given all possible transitions at current state of the environment.
- 2. Find the best policy that earns the highest value under current state value function.
- 3. If the best policy is identical to the previous one then stop the training. Otherwise, return to step 1.

In step 1, update the state value function by

$$v_{k+1} = E_{s'}[r(s,a) + \gamma v_k(s')]$$

wherein the a is given by current policy, s' is next state, r is the reward, $v_k(s')$ is the next state value given by the old (not updated yet) value function. The expectation is computed among all possible transitions given a state and action pair (As the environment is not deterministic, it's possible to transit to different next states even given the same state-action pair). Note that the new value v_{k+1} should be temporarily stored at some places, instead of

In step 2, the best policy is the one that takes the action with maximal expected return given a state:

```
a = argmax_a E_{s'}[r(s,a) + \gamma v_k(s')]
```

Policy iteration algorithm has an outer loop (update policy, step 1 to 3) and an inner loop (fit the value function, within step 1).

In each outer loop, we call once trainer.train(), where we call trainer.update_value_function() once to update the value function (the state value table).

After that we call trainer.update_policy() to update the current policy.

trainer object has a trainer policy attribute, which is a function that takes observation as input and returns an action.

You should implement the trainer following the framework we already wrote for you. Please carefully go through the codes and finish all TODO in it.

```
In [10]: # Solve the TODOs and remove `pass`
         class PolicyIterationTrainer(TabularRLTrainerAbstract):
             def init (self, gamma=1.0, eps=1e-10, env name='FrozenLake8x8-v1'):
                 super(PolicyIterationTrainer, self). init (env name)
                 # Discount factor
                 self.gamma = gamma
                 # Value function convergence criterion
                 self.eps = eps
                 # The **value table** for each possible observation
                 self.value table: np.ndarray = np.zeros((self.obs dim,))
                 # TODO: you need to implement a uniform random policy at the beginning.
                 # self.policy is a python function that takes an integer (the observation)
                 # as input and return an integer (action).
                 # You can use self.action dim to get the dimension (range)
                 # of the action. An action is an integer in range
                 # [0, ..., self.action dim - 1]
                 # Note: policy should be a deterministic function. That is, given a state,
```

```
# it should also return the same action.
   self.policy = lambda obs: DOWN if (obs + 1) % 8 == 0 or (obs + 8) < 64 else RIGHT
   # test your random policy
   test random policy(self.policy, self.env)
def train(self):
    """Conduct one iteration of learning."""
   # TODO: self.value table may be need to be reset to zeros.
   # If you think it should, than do it. If not, then go ahead.
   # self.table = np.zeros((self.obs dim,))
    self.update value function()
    self.update policy()
def update value function(self):
   count = 0 # count the steps of value updates
   while True:
        old table = self.value table.copy()
       for state in range(self.obs_dim):
            action = self.policy(state)
            transition list = self. get transitions(state, action)
            state_value = 0
            # Iterate over all possible next states given a state-action pair.
            for transition in transition list:
                prob = transition['prob']
                reward = transition['reward']
               next state = transition['next state']
               done = transition['done']
               # TODO: compute state value
               # hint: you should use reward, self.gamma, old table, prob,
               # and next state to compute the state value
               state_value += prob * (reward + self.gamma * old_table[next_state])
            # update the state value
            self.value_table[state] = state_value
        # TODO: Compare the old table and current table to
```

```
# decide whether to break the value update process.
        # hint: you should use self.eps, old table and self.value table
        should break = np.sum(np.abs(old table - self.value table)) < self.eps</pre>
        # pass
       if should break:
            print("[DEBUG]\tThe value table was updated for {} steps. "
                  "Difference between new and old table is: {:.4f}".format(
                count, np.sum(np.abs(old table - self.value table))
            ))
            break
        count += 1
       if count > 6000:
            raise ValueError("Clearly your code has problem. Check it!")
def update policy(self):
    """You need to define a new policy function, given current
    value function. The best action for a given state is the one that
   has the highest expected return.
    To optimize computing efficiency, we introduce a policy table,
    which is a numpy array taking state as index and return the action given a state.
    .....
    policy table: np.ndarray = np.zeros([self.obs dim, ], dtype=int)
   for state in range(self.obs dim):
        state action values = [0] * self.action dim
       # TODO: assign the action with greatest state-action value
        # to policy table[state].
        # Hint:
        # You should use the value table, gamma, reward, as well as
        # the return from self. get transitions() to compute the
       # state-action value first before getting the action.
        # Bellman equation may help.
       best action = None
       for action in range(self.action dim):
            transition list = self. get transitions(state, action)
            for transition in transition list:
                prob = transition['prob']
                reward = transition['reward']
```

Now we have built the Trainer class for policy iteration algorithm. In the following few cells, we will train the agent to solve the problem and evaluate its performance.

```
In [11]: # Solve the TODOs and remove `pass`
         # Managing configurations of your experiments is important for your research.
         default pi config = dict(
             max iteration=1000,
             evaluate interval=1,
             gamma=1.0,
             eps=1e-10
         def policy iteration(train config=None):
             # Prepare a config dict
             config = default pi config.copy()
             if train config is not None:
                 config.update(train config)
             # Initialize the trainer
             trainer = PolicyIterationTrainer(gamma=config['gamma'], eps=config['eps'])
             # Initialize an array as the policy mapping obs to action.
             old policy = np.zeros(trainer.obs dim, dtype=int)
             old policy.fill(-1)
             for i in range(config['max iteration']):
                 # train the agent
```

```
trainer.train()
   # TODO: compare the new policy with old policy to check whether
    # we should stop. If new and old policy have same output given any
   # observation, then we consider the algorithm is converged and
    # should be stopped.
   new policy = {
        state: trainer.policy(state) for state in range(trainer.obs dim)
   should stop = np.array equal(new policy, old policy)
   if should stop:
        print("We found policy is not changed anymore at "
              "iteration {}. Current mean episode reward "
             "is {}. Stop training.".format(i, trainer.evaluate()))
       break
    old policy = new policy
   # evaluate the result
   if i % config['evaluate interval'] == 0:
        print(
           "[INFO]\tAfter {} iterations, current policy has mean episode reward {}."
           "".format(i, trainer.evaluate()))
       if i > 20:
           print("You sure your codes is OK? It shouldn't take so many "
                  "({}) iterations to train a policy iteration "
                  "agent.".format(i))
assert trainer.evaluate() > 0.8, \
    "We expect to get the mean episode reward greater than 0.8. " \
    "But you get: {}. Please check your codes.".format(trainer.evaluate())
return trainer
```

```
In [12]: # Run this cell without modification

# It may be confusing to call a trainer agent. But that's what we normally do.
pi_agent = policy_iteration()
```

```
[DEBUG] The value table was updated for 76 steps. Difference between new and old table is: 0.0000
        [INFO] After 0 iterations, current policy has mean episode reward 0.837.
        [DEBUG] The value table was updated for 1553 steps. Difference between new and old table is: 0.0000
        [INFO] After 1 iterations, current policy has mean episode reward 0.818.
        [DEBUG] The value table was updated for 821 steps. Difference between new and old table is: 0.0000
        [INFO] After 2 iterations, current policy has mean episode reward 0.788.
        [DEBUG] The value table was updated for 1050 steps. Difference between new and old table is: 0.0000
        [INFO] After 3 iterations, current policy has mean episode reward 0.705.
        [DEBUG] The value table was updated for 1298 steps. Difference between new and old table is: 0.0000
        [INFO] After 4 iterations, current policy has mean episode reward 0.841.
        [DEBUG] The value table was updated for 89 steps. Difference between new and old table is: 0.0000
        [INFO] After 5 iterations, current policy has mean episode reward 0.882.
        [DEBUG] The value table was updated for 0 steps. Difference between new and old table is: 0.0000
        We found policy is not changed anymore at iteration 6. Current mean episode reward is 0.882. Stop training.
In [13]: # Run this cell without modification
         print("Your policy iteration agent achieve {} mean episode reward. The optimal score "
               "should be > 0.8.".format(pi agent.evaluate()))
        Your policy iteration agent achieve 0.882 mean episode reward. The optimal score should be > 0.8.
In [14]: # Run this cell without modification
         pi agent.render()
          (Right)
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        FHHFFFHF
        FHFFHFHF
        FFFHFFF
In [15]: # Run this cell without modification
         pi agent.print table()
```

+				State \	/alue N	1apping	g		+
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	1	1.000	1.000	1.000 	1.000	1.000	1.000	1.000	1.000
	2	1.000	0.978	0.926 	0.000	0.857	0.946	0.982	 1.000
	3	1.000	0.935	0.801 	0.475	0.624	0.000	0.945	 1.000
	4	1.000	0.826	0.542	0.000	0.539	0.611	0.852	1.000
	5	1.000	0.000	0.000	0.168	0.383	0.442	0.000	1.000
	6	1.000	0.000	0.195 	0.121	0.000	0.332	0.000	1.000
	7	1.000	0.732	0.463	0.000	0.277	0.555	0.777	0.000

Congratulations! You have successfully implemented the policy iteration trainer (if and only if no error happens at the above cells).

Here are few further problems for you to investigate:

- 1. What is the impact of the discount factor gamma?
- 2. What is the impact of the value function convergence criterion epsilon?

If you are interested in doing more investigation (not limited to these two), feel free to open new cells at the end of this notebook and left a clear trace of your thinking and coding, which leads to extra credit if you do a good job. It's an optional job, and you can ignore it.

Now let's continue our journey!

Section 2.2: Value Iteration

Recall the idea of value iteration. We update the state value:

$$v_{k+1}(s) = \max_a E_{s'}[r(s,a) + \gamma v_k(s')]$$

wherein the s' is next state, r is the reward, $v_k(s')$ is the next state value given by the old (not updated yet) value function. The expectation is computed among all possible transitions (given a state and action pair, it is possible to have many next states, since the environment is not deterministic).

The value iteration algorithm does not require an inner loop. It computes the expected return of all possible actions at a given state and uses the maximum of them as the state value. You can imagine it "pretends" we already have the optimal policy and run policy iteration based on it. Therefore, we do not need to maintain a policy object in a trainer. We only need to retrieve the optimal policy using the same rule as policy iteration, given current value function.

You should implement the trainer following the framework we already wrote for you. Please carefully go through the code and finish all TODO in it.

```
class ValueIterationTrainer(PolicyIterationTrainer):
    """Note that we inherit Policy Iteration Trainer, to reuse the
    code of update_policy(). It's same since it get optimal policy from
    current state-value table (self.table).
    """

def __init__(self, gamma=1.0, env_name='FrozenLake8x8-v1'):
        super(ValueIterationTrainer, self).__init__(gamma, None, env_name)

def train(self):
    """Conduct one iteration of learning.""
    # TODO: self.value_table may be need to be reset to zeros.
    # If you think it should, than do it. If not, then move on.
```

```
# self.table = np.zeros((self.obs dim,))
   # In value iteration, we do not explicit require a
    # policy instance to run. We update value function
   # directly based on the transitions. Therefore, we
   # don't need to run self.update policy() in each step.
    self.update value function()
def update value function(self):
   old table = self.value table.copy()
   for state in range(self.obs dim):
        state value = 0
       # TODO: Compute the new state value.
        # Hint: try to compute the state-action value first
       act = self.policy(state)
       transition list = self. get transitions(state, act)
       for transition in transition list:
            prob = transition['prob']
            reward = transition['reward']
            next state = transition['next state']
            done = transition['done']
            state value += prob * (reward + self.gamma * old table[next state])
        self.value table[state] = state value
   # Till now the one-step value update is finished.
   # You can see that we do not use an inner loop to update
   # the value function like what we did in the policy iteration.
   # This is because to compute the state value, which is
   # an expectation among all possible action given by a
   # specified policy, we **pretend** we already have the optimal
   # policy (the max operation). Therefore we don't need to
    # compute the state-action values for those actions that will not
    # be selected by the policy.
def evaluate(self):
    """Since in value iteration we do not maintain a policy function,
   so we need to retrieve it when we need it."""
    self.update policy()
```

```
return super().evaluate()

def render(self):
    """Since in value iteration we do not maintain a policy function,
    so we need to retrieve it when we need it."""
    self.update_policy()
    return super().render()

# Solve the TODOs and remove `pass`
```

```
In [17]: # Solve the TODOs and remove `pass`
         # Managing configurations of your experiments is important for your research.
         default vi config = dict(
             max iteration=10000,
             evaluate interval=100, # don't need to update policy each iteration
             gamma=1.0,
             eps=1e-10
         def value iteration(train config=None):
             config = default vi config.copy()
             if train config is not None:
                 config.update(train config)
             # TODO: initialize Value Iteration Trainer. Remember to pass
             # config['gamma'] to it.
             trainer: TabularRLTrainerAbstract = ValueIterationTrainer(gamma=config['gamma'])
             old state value table = trainer.value table.copy()
             for i in range(config['max iteration']):
                 old policy = {
                     obs: trainer.policy(obs) for obs in range(trainer.obs dim)
                 # train the agent
                 trainer.train()
                 # evaluate the result
                 if i % config['evaluate interval'] == 0:
                     print("[INFO]\tIn {} iteration, current "
```

```
"mean episode reward is {}.".format(
           i, trainer.evaluate()
        ))
        # TODO: Compare the new policy with old policy to check should
        # we stop.
        # Hint: If new and old policy have same output given any
        # observation, them we consider the algorithm is converged and
        # should be stopped.
        new policy = {
            obs: trainer.policy(obs) for obs in range(trainer.obs dim)
        should stop = (new policy == old policy)
        if should stop:
            print("We found policy is not changed anymore at "
                  "iteration {}. Current mean episode reward "
                  "is {}. Stop training.".format(i, trainer.evaluate()))
            break
        if i > 3000:
            print("You sure your codes is OK? It shouldn't take so many "
                  "({}) iterations to train a policy iteration "
                  "agent.".format(
                i))
assert trainer.evaluate() > 0.8, \
    "We expect to get the mean episode reward greater than 0.8. " \
    "But you get: {}. Please check your codes.".format(trainer.evaluate())
return trainer
```

```
In [18]: # Run this cell without modification
vi_agent = value_iteration()
```

```
[INFO] In 0 iteration, current mean episode reward is 0.0.
        [INFO] In 100 iteration, current mean episode reward is 0.0.
        [INFO] In 200 iteration, current mean episode reward is 0.0.
        [INFO] In 300 iteration, current mean episode reward is 0.0.
        [INFO] In 400 iteration, current mean episode reward is 0.0.
        [INFO] In 500 iteration, current mean episode reward is 0.616.
        [INFO] In 600 iteration, current mean episode reward is 0.86.
        [INFO] In 700 iteration, current mean episode reward is 0.871.
        [INFO] In 800 iteration, current mean episode reward is 0.882.
        [INFO] In 900 iteration, current mean episode reward is 0.882.
        [INFO] In 1000 iteration, current mean episode reward is 0.882.
        [INFO] In 1100 iteration, current mean episode reward is 0.882.
        We found policy is not changed anymore at iteration 1100. Current mean episode reward is 0.882. Stop training.
In [19]: # Run this cell without modification
         print("Your value iteration agent achieve {} mean episode reward. The optimal score "
               "should be > 0.8.".format(vi agent.evaluate()))
        Your value iteration agent achieve 0.882 mean episode reward. The optimal score should be > 0.8.
In [20]: # Run this cell without modification
         vi agent.render()
          (Right)
        SFFFFFF
        FFFFFFF
        FFFHFFF
        FFFFFHFF
        FFFHFFF
        FHHFFFHF
        FHFFHFHF
        FFFHFFF
In [21]: # Run this cell without modification
         vi agent.print table()
```

			+	state v	/alue N	งappıng	g			H
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) 	 1.000 	 1.000 	 1.000 	 1.000 	1.000	1.000	1.000	+ 1.000 	
1	.	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	
2	<u> </u>	0.999	0.977 	0.926 	0.000	0.857	0.946	0.982	1.000	
3 +	} 	0.998 	0.933 	0.800 	0.475 	0.623	0.000 	0.945	1.000 	
4 +	 	0.998	0.824 	0.541 	0.000	0.539	0.611	0.852	1.000 	
5 	; 	0.997	0.000 	0.000 	0.168	0.383	0.442	0.000	1.000 	
6	; 	0.997 	0.000 	 0.194 	0.121	0.000	0.332	0.000	1.000	
7 	, 	0.997 	0.729 	0.461 	0.000 	0.277	0.555 	0.777	0.000 	 -

Congratulation! You have successfully implemented the value iteration trainer (if and only if no error happens at the above cells). Few further problems for you to investigate:

- 1. Do you see that some iteration during training yields better rewards than the final one? Why does that happen?
- 2. What is the impact of the discount factor gamma?
- 3. What is the impact of the value function convergence criterion epsilon?

If you are interested in doing more investigation (not limited to these two), feel free to open new cells at the end of this notebook and left a clear trace of your thinking and coding, which leads to extra credit if you do a good job. It's an optional job, and you can ignore it.

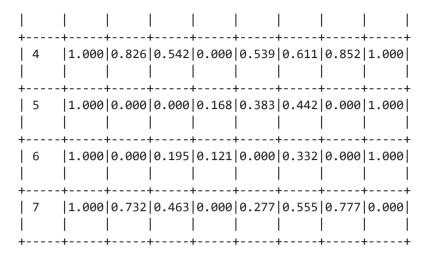
Now let's continue our journey!

Section 2.3: Compare two model-based agents

Now we have two agents: pi_agent and vi_agent . They are believed to be the optimal policies in this environment.

```
In [22]: # Solve the TODO and remove `pass`
         # TODO: Print the value tables of these two policies and see if they match each other.
         vi agent.print table()
         pi agent.print table()
         flag = True
         for row in pi agent.value table:
             if np.sum(np.abs(pi agent.value table - vi agent.value table)) >= 0.1:
                 print("\nTwo table does not match")
                 flag = False
                 break
         if flag:
             print("\nTwo table match")
         # table match = np.allclose(pi agent.value table, vi agent.value table)
         # if table match:
               print("\nTwo table match")
         # else:
               print("\nTwo table does not match")
```

++State Value Mapping+								
	0	1	2	3	4	5		7
0	1.000	1.000	1.000	1.000 	1.000	1.000 	1.000	1.000
1 1	1.000 	 1.000 	1.000	 1.000 		 1.000 	1.000	1.000
2 +	0.999 	0.977 +	 0.926 	0.000 	0.857 	0.946 	 0.982 	 1.000
3 +	0.998 	0.933 	0.800 	0.475 	0.623 	0.000 	 0.945 	 1.000
4 +	0.998	0.824 	0.541 	0.000 	0.539 	0.611 	0.852 	 1.000
5 5 	0.997 	0.000 	0.000 	0.168 	0.383 	0.442 	0.000 	1.000
6 	0.997 	0.000 	0.194 	0.121 	0.000 	0.332 	0.000 	1.000
7 +	0.997 	0.729 	0.461 	0.000 +	0.277 	0.555 	0.777 	0.000
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0	1.000	1.000 	1.000 	1.000 	1.000 	1.000 	1.000	1.000
1	1.000	1.000 	1.000	1.000	1.000	1.000	1.000	1.000
2	1.000	0.978	0.926	0.000 	0.857	0.946 	0.982	1.000
3	1.000	0.935	0.801	0.475	0.624	0.000	0.945	1.000



Two table match

You can do more investigation here if you wish. Leave it blank if you don't.

1. For policy iteration:

a. What is the impact of the discount factor gamma?

The discount factor gamma determines the trade-off between immediate and future rewards.

Higher gamma values favor long-term rewards, while lower values focus on immediate gains.

b. What is the impact of the value function convergence criterion epsilon?

The value function convergence criterion epsilon sets the threshold for convergence. Smaller epsilon values demand higher precision, leading to slower but more accurate convergence, while larger epsilons result in faster but potentially less precise policy iteration.

2. For policy iteration:

a. Do you see that some iteration during training yields better rewards than the final one? Why does that happen? Yes, this can occur when value iteration overshoots the optimal policy briefly, only to converge to a better long-term solution later.

b. What is the impact of the discount factor gamma?

The discount factor gamma in value iteration influences the trade-off between immediate and future rewards.

Higher gamma values emphasize long-term planning, while lower values prioritize immediate gains.

c. What is the impact of the value function convergence criterion epsilon?

The value function convergence criterion epsilon determines the threshold for convergence.

Smaller epsilon values demand higher precision, leading to slower but more accurate convergence, while larger epsilons result in faster but potentially less precise value iteration.

Conclusion and Discussion

In this assignment, we learn how to use the gym (now Gymnasium) library, how to use Object Oriented Programming to build a basic tabular RL algorithm.

Follow the submission instruction in the README to submit your assignment. Thank you!

•••