CS 577: Introduction to Algorithms

Program 2 - Crossing Lines

Out: February 9, 2021 Due: February 16, 2021

Coding Question:

Reminders:

- Must be coded individually in your choice of either Python, Java, C, C++, or C#
- There are hidden testcases
- Submitted through Gradescope
- There is a class-wide runtime leaderboard on Gradescope
- We encourage the use of Piazza for debugging help
- · Please do not cheat

Problem:

Suppose you are given two sets of n points, one set $\{p_1, p_2, \ldots, p_n\}$ on the line y = 0 and the other set $\{q_1, q_2, \ldots, q_n\}$ on the line y = 1. Create a set of n line segments by connecting each point p_i to the corresponding point q_i . Your goal is to develop an algorithm to determine how many pairs of these line segments intersect. Your algorithm should take the 2n points as input, and return the number of intersections. Using divide-and-conquer, you should be able to develop an algorithm that runs in $O(n \log n)$ time.

Hint: What does this problem have in common with the problem of counting inversions in a list?

Input should be read in from stdin. The first line will contain the number of pairs of points (n). The next n lines each contain the location of a point q_i on the top line. The final n lines each contain the location of the corresponding point p_i on the bottom line. For the example shown in Fig 1, the input is properly formatted in the first test case below.

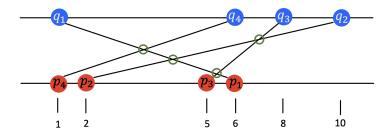


Figure 1: An example for the line intersection problem where the answer is 4

Constraints:

- $1 \le n \le 10^6$
- For each point, its location x is a positive integer such that $1 \le x \le 10^6$
- No two points are placed at the same location on the top line, and no two points are placed at the same location on the bottom line.
- Note that in C\C++, the results of some of the test cases may not fit in a 32-bit integer. If you are using C\C++, make sure you use a 'long long' to store your final answer.

Sample Test Cases:

| input: | input: |
|--------|--------|
| 4 | 5 |
| 1 | 9 |
| 10 | 21 |
| 8 | 1 |
| 6 | 5 |
| 6 | 18 |
| 2 | 2 |
| 5 | 4 |
| 1 | 6 |
| | 10 |
| | 1 |
| | |

expected output: expected output: 4 7