	9	
Out: 03/09/21		Due: 03/16/21
Nama	Wise ID:	

Homework 5

Ground Rules

- Answer the questions in the boxes provided on the question sheets. If you run out of room for an answer, add a page to the end of the document. Do **not** feel obligated to fill the entire solution box. The size of the box does **not** correspond to the intended solution length.
- The homework is to be done and submitted individually. You may discuss the homework with others in either section but you must write up the solution *on your own*.
- You are not allowed to consult any material outside of assigned textbooks and material the instructors post on the course websites. In particular, consulting the internet will be considered plagiarism and penalized appropriately.
- The homework is due at 11:59 PM CST on the due date. No extensions to the due date will be given under any circumstances.
- Homework must be submitted electronically on Gradescope.

CS 577: Introduction to Algorithms

Problem 1:

Recall that in Problem 1 of the midterm, you were given a fully parenthesized numerical expression with n numbers, and your goal was to find the maximum and minimum possible values of the expression by filling in + or - for each of the n-1 operators. Denote the sequence of these n numbers as a₁,..., a_n, and the sequence of the n-1 operators as o_{1,2}, o_{2,3},..., o_{i,i+1},..., o_{n-1,n}, where o_{i,i+1} is the operator placed between a_i and a_{i+1}.
Now consider the problem where you are given the number sequence a₁,..., a_n, but the choices of these n-1 operators and positions of parentheses are both undetermined. Moreover, you can set each of the n-1 operators to be either +, -, or ×. Your goal is to find the **maximum** possible value the numerical expression

$$[a_1]o_{1,2}[a_2]o_{2,3}\dots[a_{n-1}]o_{n-1,n}[a_n]$$

can evaluate to when you fill in +, -, or \times for these n-1 operators and insert pairs of parentheses. Note that you should not change the ordering of numbers in $a_1...a_n$ but you may give precedence to some operations with appropriate parenthesizing. For example, the following number sequence of

$$[-3]$$
? $[-4]$? $[-5]$

can achieve a maximum value of 35 by filling in $o_{1,2}$ to $o_{2,3}$ and adding parentheses in the following way:

$$([-3] + [-4]) \times [-5]$$

Problem 2:

2. You have a collection of boxes and want to pack them in your attic. Every box i has a width w_i , a height h_i and contains items of total value v_i . Your attic has the shape of a right angled isosceles triangle with two sides of length H. You want to stack the boxes and place them in the attic. You may choose the order in which to stack the boxes but you are not allowed to rotate them and you cannot place two boxes side by side. However, not all boxes can fit in the attic. In order for a box to fit, its width must be at most H minus its height and the heights of all the boxes below it in the stack. Figure 1, illustrates how boxes are packed to fit in the attic. Your goal is to maximize the value of the boxes placed in the attic.

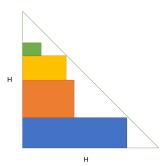


Figure 1: How boxes are stacked and placed in the attic.

Input: A set of n boxes with box i having width w_i , height h_i and value v_i , the height of the attic H, where all heights h_i s and H are integers.

Your goal is to maximize the value of the boxes placed in the attic.

