Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [9]:
       ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc_net import *
        from nndl.layers import *
        from utils.data_utils import get_CIFAR10_data
        from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradien
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipytho
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

```
In [10]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y_test: (1000,)
```

Dropout forward pass

Implement the training and test time dropout forward pass, dropout_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [11]: x = np.random.randn(500, 500) + 10
         for p in [0.3, 0.6, 0.75]:
           out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
           out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})
           print('Running tests with p = ', p)
           print('Mean of input: ', x.mean())
           print('Mean of train-time output: ', out.mean())
           print('Mean of test-time output: ', out_test.mean())
           print('Fraction of train-time output set to zero: ', (out == 0).mean())
           print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
        Running tests with p = 0.3
        Mean of input: 9.997837261359429
       Mean of train-time output: 10.01426645162686
       Mean of test-time output: 9.997837261359429
        Fraction of train-time output set to zero: 0.699504
        Fraction of test-time output set to zero: 0.0
        Running tests with p = 0.6
       Mean of input: 9.997837261359429
        Mean of train-time output: 10.008206169146657
       Mean of test-time output: 9.997837261359429
        Fraction of train-time output set to zero: 0.399472
        Fraction of test-time output set to zero: 0.0
        Running tests with p = 0.75
       Mean of input: 9.997837261359429
       Mean of train-time output: 10.006821115667954
        Mean of test-time output: 9.997837261359429
        Fraction of train-time output set to zero: 0.249384
        Fraction of test-time output set to zero: 0.0
```

Dropout backward pass

Implement the backward pass, dropout_backward, in nndl/layers.py . After that, test your gradients by running the following cell:

dx relative error: 5.44560859772755e-11

Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
Running check with dropout = 0
Initial loss: 2.3051948273987857
W1 relative error: 2.5272575344376073e-07
W2 relative error: 1.5034484929313676e-05
W3 relative error: 2.753446833630168e-07
b1 relative error: 2.936957476400148e-06
b2 relative error: 5.051339805546953e-08
b3 relative error: 1.1740467838205477e-10
Running check with dropout = 0.25
Initial loss: 2.3126468345657742
W1 relative error: 1.483854795975875e-08
W2 relative error: 2.3427832149940254e-10
W3 relative error: 3.564454999162522e-08
b1 relative error: 1.5292167232408546e-09
b2 relative error: 1.842268868410678e-10
b3 relative error: 1.4026015558098908e-10
Running check with dropout = 0.5
Initial loss: 2.302437587710995
W1 relative error: 4.553387957138422e-08
W2 relative error: 2.974218050584597e-08
W3 relative error: 4.3413247403122424e-07
b1 relative error: 1.872462967441693e-08
b2 relative error: 5.045591219274328e-09
b3 relative error: 8.009887154529434e-11
```

Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```
In [14]: # Train two identical nets, one with dropout and one without
         num train = 500
         small_data = {
            'X_train': data['X_train'][:num_train],
            'y_train': data['y_train'][:num_train],
            'X val': data['X val'],
            'y_val': data['y_val'],
         solvers = {}
         dropout choices = [0, 0.6]
         for dropout in dropout choices:
           model = FullyConnectedNet([100, 100, 100], dropout=dropout)
           solver = Solver(model, small_data,
                            num_epochs=25, batch_size=100,
                            update_rule='adam',
                            optim config={
                              'learning_rate': 5e-4,
```

```
verbose=True, print_every=100)
solver.train()
solvers[dropout] = solver
```

```
(Iteration 1 / 125) loss: 2.300804
(Epoch 0 / 25) train acc: 0.220000; val_acc: 0.168000
(Epoch 1 / 25) train acc: 0.188000; val_acc: 0.147000
(Epoch 2 / 25) train acc: 0.266000; val_acc: 0.200000
(Epoch 3 / 25) train acc: 0.338000; val acc: 0.262000
(Epoch 4 / 25) train acc: 0.378000; val_acc: 0.278000
(Epoch 5 / 25) train acc: 0.428000; val_acc: 0.297000
(Epoch 6 / 25) train acc: 0.468000; val_acc: 0.323000
(Epoch 7 / 25) train acc: 0.494000; val_acc: 0.287000
(Epoch 8 / 25) train acc: 0.566000; val_acc: 0.328000
(Epoch 9 / 25) train acc: 0.572000; val_acc: 0.322000
(Epoch 10 / 25) train acc: 0.622000; val_acc: 0.324000
(Epoch 11 / 25) train acc: 0.670000; val_acc: 0.279000
(Epoch 12 / 25) train acc: 0.710000; val_acc: 0.338000
(Epoch 13 / 25) train acc: 0.746000; val_acc: 0.319000
(Epoch 14 / 25) train acc: 0.792000; val acc: 0.307000
(Epoch 15 / 25) train acc: 0.834000; val_acc: 0.297000
(Epoch 16 / 25) train acc: 0.876000; val acc: 0.327000
(Epoch 17 / 25) train acc: 0.886000; val_acc: 0.320000
(Epoch 18 / 25) train acc: 0.918000; val_acc: 0.314000
(Epoch 19 / 25) train acc: 0.922000; val_acc: 0.290000
(Epoch 20 / 25) train acc: 0.944000; val_acc: 0.306000
(Iteration 101 / 125) loss: 0.156105
(Epoch 21 / 25) train acc: 0.968000; val_acc: 0.302000
(Epoch 22 / 25) train acc: 0.978000; val_acc: 0.302000
(Epoch 23 / 25) train acc: 0.976000; val_acc: 0.289000
(Epoch 24 / 25) train acc: 0.986000; val_acc: 0.285000
(Epoch 25 / 25) train acc: 0.978000; val_acc: 0.311000
(Iteration 1 / 125) loss: 2.301328
(Epoch 0 / 25) train acc: 0.154000; val_acc: 0.143000
(Epoch 1 / 25) train acc: 0.214000; val_acc: 0.195000
(Epoch 2 / 25) train acc: 0.252000; val_acc: 0.217000
(Epoch 3 / 25) train acc: 0.276000; val_acc: 0.200000
(Epoch 4 / 25) train acc: 0.308000; val acc: 0.254000
(Epoch 5 / 25) train acc: 0.316000; val_acc: 0.241000
(Epoch 6 / 25) train acc: 0.322000; val acc: 0.282000
(Epoch 7 / 25) train acc: 0.354000; val_acc: 0.273000
(Epoch 8 / 25) train acc: 0.364000; val_acc: 0.276000
(Epoch 9 / 25) train acc: 0.408000; val_acc: 0.282000
(Epoch 10 / 25) train acc: 0.454000; val acc: 0.302000
(Epoch 11 / 25) train acc: 0.472000; val acc: 0.297000
(Epoch 12 / 25) train acc: 0.498000; val_acc: 0.318000
(Epoch 13 / 25) train acc: 0.510000; val_acc: 0.309000
(Epoch 14 / 25) train acc: 0.534000; val_acc: 0.315000
(Epoch 15 / 25) train acc: 0.546000; val_acc: 0.331000
(Epoch 16 / 25) train acc: 0.584000; val_acc: 0.302000
(Epoch 17 / 25) train acc: 0.626000; val acc: 0.332000
(Epoch 18 / 25) train acc: 0.614000; val_acc: 0.327000
(Epoch 19 / 25) train acc: 0.626000; val_acc: 0.325000
(Epoch 20 / 25) train acc: 0.656000; val_acc: 0.338000
(Iteration 101 / 125) loss: 1.299296
(Epoch 21 / 25) train acc: 0.676000; val acc: 0.329000
(Epoch 22 / 25) train acc: 0.684000; val_acc: 0.325000
(Epoch 23 / 25) train acc: 0.730000; val_acc: 0.343000
(Epoch 24 / 25) train acc: 0.736000; val_acc: 0.321000
(Epoch 25 / 25) train acc: 0.768000; val_acc: 0.333000
```

```
# Plot train and validation accuracies of the two models
 train_accs = []
 val_accs = []
 for dropout in dropout_choices:
   solver = solvers[dropout]
   train_accs.append(solver.train_acc_history[-1])
   val_accs.append(solver.val_acc_history[-1])
 plt.subplot(3, 1, 1)
 for dropout in dropout_choices:
    plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % dropo
 plt.title('Train accuracy')
 plt.xlabel('Epoch')
 plt.ylabel('Accuracy')
 plt.legend(ncol=2, loc='lower right')
 plt.subplot(3, 1, 2)
 for dropout in dropout choices:
    plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % dropout
 plt.title('Val accuracy')
 plt.xlabel('Epoch')
 plt.ylabel('Accuracy')
 plt.legend(ncol=2, loc='lower right')
 plt.gcf().set_size_inches(15, 15)
 plt.show()
                                          Train accuracy
  1.0
  0.8
  0.6
  0.4

    0.60 dropout

    0.00 dropout

                                             Epoch
 0.350
 0.300
 0.275
 0.250
Ų 0.225
 0.200
```

Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

10

Epoch

15

0.175

0.00 dropout

20

0.60 dropout

25

Answer:

Yes. As depicted in the two figures above, despite the model employing dropout exhibiting lower training accuracies, its performance on the validation set closely mirrors that of the model without dropout. This suggests that dropout serves as a regularization technique, effectively mitigating overfitting of the training data.

Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
In [19]: | # ------ #
       # YOUR CODE HERE:
       # Implement a FC-net that achieves at least 55% validation accuracy
         on CIFAR-10.
       model = FullyConnectedNet(
          [100, 100, 100],
          weight_scale=0.01,
          use_batchnorm=True,
          dropout=0.9,
       solver = Solver(
          model,
          data,
          num epochs=10,
          batch_size=100,
          update_rule="adam",
          optim_config={
            "learning rate": 5e-4,
          lr_decay=0.9,
          verbose=True,
          print_every=4900,
       solver.train()
       y_test_pred = np.argmax(model.loss(data["X_test"]), axis=1)
       y_val_pred = np.argmax(model.loss(data["X_val"]), axis=1)
       print("Validation set accuracy: {}".format(np.mean(y_val_pred == data["y_val"]))
       print("Test set accuracy: {}".format(np.mean(y_test_pred == data["y_test"])))
       # END YOUR CODE HERE
```

```
(Iteration 1 / 4900) loss: 2.313523
       (Epoch 0 / 10) train acc: 0.125000; val_acc: 0.130000
       (Epoch 1 / 10) train acc: 0.487000; val_acc: 0.469000
       (Epoch 2 / 10) train acc: 0.494000; val_acc: 0.487000
       (Epoch 3 / 10) train acc: 0.517000; val_acc: 0.514000
       (Epoch 4 / 10) train acc: 0.565000; val acc: 0.510000
       (Epoch 5 / 10) train acc: 0.570000; val_acc: 0.535000
       (Epoch 6 / 10) train acc: 0.544000; val_acc: 0.532000
       (Epoch 7 / 10) train acc: 0.581000; val_acc: 0.565000
       (Epoch 8 / 10) train acc: 0.626000; val_acc: 0.550000
       (Epoch 9 / 10) train acc: 0.605000; val_acc: 0.543000
       (Epoch 10 / 10) train acc: 0.601000; val acc: 0.556000
       Validation set accuracy: 0.564
       Test set accuracy: 0.546
In [ ]: #fc_net.py
        import numpy as np
        import pdb
        from .layers import *
        from .layer_utils import *
        This code was originally written for CS 231n at Stanford University
        (cs231n.stanford.edu). It has been modified in various areas for use in the
        ECE 239AS class at UCLA. This includes the descriptions of what code to
        implement as well as some slight potential changes in variable names to be
        consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
        permission to use this code. To see the original version, please visit
        cs231n.stanford.edu.
        class TwoLayerNet(object):
          A two-layer fully-connected neural network with ReLU nonlinearity and
          softmax loss that uses a modular layer design. We assume an input dimension
          of D, a hidden dimension of H, and perform classification over C classes.
          The architecure should be affine - relu - affine - softmax.
          Note that this class does not implement gradient descent; instead, it
          will interact with a separate Solver object that is responsible for running
          optimization.
          The learnable parameters of the model are stored in the dictionary
          self.params that maps parameter names to numpy arrays.
          def init (self, input dim=3*32*32, hidden dims=100, num classes=10,
                       dropout=0, weight_scale=1e-3, reg=0.0):
            Initialize a new network.
            Inputs:
            - input_dim: An integer giving the size of the input
            - hidden dims: An integer giving the size of the hidden layer
            - num_classes: An integer giving the number of classes to classify
            - dropout: Scalar between 0 and 1 giving dropout strength.
            - weight_scale: Scalar giving the standard deviation for random
              initialization of the weights.
```

```
- reg: Scalar giving L2 regularization strength.
 self.params = {}
 self.reg = reg
 # VOUR CODE HERE .
 # Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
   self.params['W2'], self.params['b1'] and self.params['b2']. The
    biases are initialized to zero and the weights are initialized
 # so that each parameter has mean 0 and standard deviation weight_scale.
   The dimensions of W1 should be (input_dim, hidden_dim) and the
 # dimensions of W2 should be (hidden_dims, num_classes)
 self.params['W1'] = weight_scale * np.random.randn(input_dim, hidden_dim)
 self.params['b1'] = np.zeros(hidden_dim)
 self.params['W2'] = weight_scale * np.random.randn(hidden_dim, num_classes)
 self.params['b2'] = np.zeros(num_classes)
 # END YOUR CODE HERE
 def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 Inputs:
 - X: Array of input data of shape (N, d_1, ..., d_k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns:
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
   scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - grads: Dictionary with the same keys as self.params, mapping parameter
  names to gradients of the loss with respect to those parameters.
 scores = None
 # YOUR CODE HERE:
 # Implement the forward pass of the two-layer neural network. Store
 # the class scores as the variable 'scores'. Be sure to use the layers
 # you prior implemented.
 W1, b1 = self.params['W1'], self.params['b1']
 W2, b2 = self.params['W2'], self.params['b2']
 N, D = X.shape
 hidden layer = np.maximum(0, X.dot(W1) + b1)
 # Output Layer
 scores = hidden_layer.dot(W2) + b2
 # END YOUR CODE HERE
```

```
# If y is None then we are in test mode so just return scores
   if y is None:
     return scores
   loss, grads = 0, \{\}
   # =========== #
   # YOUR CODE HERE:
      Implement the backward pass of the two-layer neural net. Store
      the loss as the variable 'loss' and store the gradients in the
      'grads' dictionary. For the grads dictionary, grads['W1'] holds
   # the gradient for W1, grads['b1'] holds the gradient for b1, etc.
      i.e., grads[k] holds the gradient for self.params[k].
   # Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
   # for each W. Be sure to include the 0.5 multiplying factor to
      match our implementation.
   #
   # And be sure to use the layers you prior implemented.
   scores -= np.max(scores, axis=1, keepdims=True) # For numerical stability
   exp_scores = np.exp(scores)
   probs = exp_scores / np.sum(exp_scores, axis=1, keepdims=True)
   correct_logprobs = -np.log(probs[range(N), y])
   data_loss = np.sum(correct_logprobs) / N
   reg_loss = 0.5 * self.reg * (np.sum(W1 * W1) + np.sum(W2 * W2))
   loss = data_loss + reg_loss
   # Backward pass
   grads = \{\}
   dscores = probs
   dscores[range(N), y] -= 1
   dscores /= N
   grads['W2'] = hidden layer.T.dot(dscores)
   grads['b2'] = np.sum(dscores, axis=0)
   dhidden = dscores.dot(W2.T)
   dhidden[hidden layer <= 0] = 0</pre>
   grads['W1'] = X.T.dot(dhidden)
   grads['b1'] = np.sum(dhidden, axis=0)
   grads['W2'] += self.reg * W2
   grads['W1'] += self.reg * W1
   # END YOUR CODE HERE
   return loss, grads
class FullyConnectedNet(object):
 A fully-connected neural network with an arbitrary number of hidden layers,
 ReLU nonlinearities, and a softmax loss function. This will also implement
 dropout and batch normalization as options. For a network with L layers,
 the architecture will be
 {affine - [batch norm] - relu - [dropout]} x (L - 1) - affine - softmax
```

```
where batch normalization and dropout are optional, and the {...} block is
repeated L - 1 times.
Similar to the TwoLayerNet above, learnable parameters are stored in the
self.params dictionary and will be learned using the Solver class.
def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10,
            dropout=0, use_batchnorm=False, reg=0.0,
            weight_scale=1e-2, dtype=np.float32, seed=None):
 Initialize a new FullyConnectedNet.
 - hidden_dims: A list of integers giving the size of each hidden layer.
 - input_dim: An integer giving the size of the input.
 - num_classes: An integer giving the number of classes to classify.
 - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=0 then
   the network should not use dropout at all.
 - use batchnorm: Whether or not the network should use batch normalization.
 - reg: Scalar giving L2 regularization strength.
 - weight_scale: Scalar giving the standard deviation for random
   initialization of the weights.
 - dtype: A numpy datatype object; all computations will be performed using
   this datatype. float32 is faster but less accurate, so you should use
   float64 for numeric gradient checking.
 - seed: If not None, then pass this random seed to the dropout layers. This
   will make the dropout layers deteriminstic so we can gradient check the
   model.
 self.use batchnorm = use batchnorm
 self.use_dropout = dropout > 0
 self.reg = reg
 self.num layers = 1 + len(hidden dims)
 self.dtype = dtype
 self.params = {}
 # YOUR CODE HERE:
    Initialize all parameters of the network in the self.params dictionary.
    The weights and biases of layer 1 are W1 and b1; and in general the
     weights and biases of layer i are Wi and bi. The
 # biases are initialized to zero and the weights are initialized
     so that each parameter has mean 0 and standard deviation weight_scale.
 #
 #
     BATCHNORM: Initialize the gammas of each layer to 1 and the beta
 # parameters to zero. The gamma and beta parameters for layer 1 should
    be self.params['gamma1'] and self.params['beta1']. For layer 2, they
     should be gamma2 and beta2, etc. Only use batchnorm if self.use batchnor
     is true and DO NOT do batch normalize the output scores.
 layer dims = [input dim] + hidden dims + [num classes]
 # fc Layers
 for i in range(self.num layers):
     self.params["W" + str(i + 1)] = weight\_scale * np.random.randn(
         layer_dims[i], layer_dims[i + 1]
     self.params["b" + str(i + 1)] = np.zeros(layer_dims[i + 1])
```

```
# bn Layers
 if self.use_batchnorm:
     for i in range(self.num_layers - 1):
         self.params["gamma" + str(i + 1)] = np.ones(layer_dims[i + 1])
         self.params["beta" + str(i + 1)] = np.zeros(layer_dims[i + 1])
 # END YOUR CODE HERE
 # When using dropout we need to pass a dropout param dictionary to each
 # dropout layer so that the layer knows the dropout probability and the mode
 # (train / test). You can pass the same dropout_param to each dropout layer.
 self.dropout_param = {}
 if self.use_dropout:
   self.dropout_param = {'mode': 'train', 'p': dropout}
   if seed is not None:
     self.dropout_param['seed'] = seed
 # With batch normalization we need to keep track of running means and
 # variances, so we need to pass a special bn_param object to each batch
 # normalization layer. You should pass self.bn_params[0] to the forward pass
 # of the first batch normalization layer, self.bn_params[1] to the forward
 # pass of the second batch normalization layer, etc.
 self.bn_params = []
 if self.use_batchnorm:
   self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1
 # Cast all parameters to the correct datatype
 for k, v in self.params.items():
   self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
 Compute loss and gradient for the fully-connected net.
 Input / output: Same as TwoLayerNet above.
 X = X.astype(self.dtype)
 mode = 'test' if y is None else 'train'
 # Set train/test mode for batchnorm params and dropout param since they
 # behave differently during training and testing.
 if self.dropout_param is not None:
   self.dropout param['mode'] = mode
 if self.use batchnorm:
   for bn_param in self.bn_params:
     bn param[mode] = mode
 scores = None
 # ------ #
 # YOUR CODE HERE:
    Implement the forward pass of the FC net and store the output
     scores as the variable "scores".
     BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
     between the affine forward and relu forward layers. You may
```

```
also write an affine_batchnorm_relu() function in layer_utils.py.
#
#
  DROPOUT: If dropout is non-zero, insert a dropout layer after
# every ReLU layer.
caches = {}
for i in range(self.num_layers - 1):
   W = self.params["W" + str(i + 1)]
   b = self.params["b" + str(i + 1)]
   if self.use batchnorm:
      gamma = self.params["gamma" + str(i + 1)]
      beta = self.params["beta" + str(i + 1)]
      fc_cache, bn_cache, relu_cache = None, None, None
      out, fc_cache = affine_forward(X, W, b)
      out, bn_cache = batchnorm_forward(out, gamma, beta, self.bn_params[i
      out, relu_cache = relu_forward(out)
      X, cache = out, (fc_cache, bn_cache, relu_cache)
   else:
      X, cache = affine_relu_forward(X, W, b)
   caches[i + 1] = cache
   if self.use_dropout:
      X, cache = dropout_forward(X, self.dropout_param)
      caches["dropout" + str(i + 1)] = cache
# forward last layer with softmax
W = self.params["W" + str(self.num_layers)]
b = self.params["b" + str(self.num_layers)]
scores, cache = affine forward(X, W, b)
caches[self.num_layers] = cache
# END YOUR CODE HERE
# ========== #
# If test mode return early
if mode == 'test':
 return scores
loss, grads = 0.0, {}
# YOUR CODE HERE:
  Implement the backwards pass of the FC net and store the gradients
  in the grads dict, so that grads[k] is the gradient of self.params[k]
# Be sure your L2 regularization includes a 0.5 factor.
  BATCHNORM: Incorporate the backward pass of the batchnorm.
#
# DROPOUT: Incorporate the backward pass of dropout.
loss, dout = softmax_loss(scores, y)
for i in range(self.num_layers):
   W = self.params["W" + str(i + 1)]
```

```
loss += 0.5 * self.reg * (W * W).sum()
dout, dw, grads["b" + str(self.num_layers)] = affine_backward(dout, caches[s
W = self.params["W" + str(self.num_layers)]
grads["W" + str(self.num_layers)] = dw + self.reg * W
for i in range(self.num_layers - 2, -1, -1):
   if self.use dropout:
       dout = dropout_backward(dout, caches["dropout" + str(i + 1)])
   if self.use_batchnorm:
       fc_cache, bn_cache, relu_cache = caches[i + 1]
       dout = relu_backward(dout, relu_cache)
       dout, dgamma, dbeta = batchnorm_backward(dout, bn_cache)
       dx, dw, db = affine_backward(dout, fc_cache)
       dout, dbeta = dx, dbeta
       grads["gamma" + str(i + 1)] = dgamma
      grads["beta" + str(i + 1)] = dbeta
   else:
       dout, dw, db = affine_relu_backward(dout, caches[i + 1])
   W = self.params["W" + str(i + 1)]
   grads["W" + str(i + 1)] = dw + self.reg * W
   grads["b" + str(i + 1)] = db
# ------ #
# FND YOUR CODE HERE
return loss, grads
```

```
In [ ]: #layers.py
        import numpy as np
        import pdb
        This code was originally written for CS 231n at Stanford University
        (cs231n.stanford.edu). It has been modified in various areas for use in the
        ECE 239AS class at UCLA. This includes the descriptions of what code to
        implement as well as some slight potential changes in variable names to be
        consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
        permission to use this code. To see the original version, please visit
        cs231n.stanford.edu.
        def affine_forward(x, w, b):
          Computes the forward pass for an affine (fully-connected) layer.
          The input x has shape (N, d_1, ..., d_k) and contains a minibatch of N
          examples, where each example x[i] has shape (d 1, ..., d k). We will
          reshape each input into a vector of dimension D = d_1 * ... * d_k, and
          then transform it to an output vector of dimension M.
          Inputs:
          - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
          - w: A numpy array of weights, of shape (D, M)
          - b: A numpy array of biases, of shape (M,)
```

```
Returns a tuple of:
 - out: output, of shape (N, M)
 - cache: (x, w, b)
 Calculate the output of the forward pass. Notice the dimensions
   of w are D x M, which is the transpose of what we did in earlier
 # assignments.
 out = np.dot(x.reshape(x.shape[0], -1), w) + b
 # END YOUR CODE HERE
 cache = (x, w, b)
 return out, cache
def affine_backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
 - cache: Tuple of:
   - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
  - w: A numpy array of weights, of shape (D, M)
  - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., d k)
 - dw: Gradient with respect to w, of shape (D, M)

    db: Gradient with respect to b, of shape (M,)

 x, w, b = cache
 dx, dw, db = None, None, None
 # YOUR CODE HERE:
   Calculate the gradients for the backward pass.
 # Notice:
 # dout is N x M
 # dx should be N x d1 x ... x dk; it relates to dout through multiplication
   dw should be D x M; it relates to dout through multiplication with x, which
   db should be M; it is just the sum over dout examples
 x flatten = x.reshape(x.shape[0], -1)
 dx = np.dot(dout, w.T).reshape(x.shape)
 dw = np.dot(x_flatten.T, dout)
 db = np.sum(dout, axis=0)
 # ------ #
 # END YOUR CODE HERE
```

```
return dx, dw, db
def relu_forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # =================== #
 # YOUR CODE HERE:
 # Implement the ReLU forward pass.
 # ----- #
 out = x.copy()
 out[out < 0] = 0
 # END YOUR CODE HERE
 cache = x
 return out, cache
def relu backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 Input:
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 x = cache
 # ----- #
 # YOUR CODE HERE:
   Implement the ReLU backward pass
 dx = dout * (x >= 0)
 # END YOUR CODE HERE
 return dx
def batchnorm_forward(x, gamma, beta, bn_param):
 Forward pass for batch normalization.
 During training the sample mean and (uncorrected) sample variance are
 computed from minibatch statistics and used to normalize the incoming data.
```

```
During training we also keep an exponentially decaying running mean of the mea
and variance of each feature, and these averages are used to normalize data
at test-time.
At each timestep we update the running averages for mean and variance using
an exponential decay based on the momentum parameter:
running mean = momentum * running mean + (1 - momentum) * sample mean
running_var = momentum * running_var + (1 - momentum) * sample_var
Note that the batch normalization paper suggests a different test-time
behavior: they compute sample mean and variance for each feature using a
large number of training images rather than using a running average. For
this implementation we have chosen to use running averages instead since
they do not require an additional estimation step; the torch7 implementation
of batch normalization also uses running averages.
Input:
- x: Data of shape (N, D)
- gamma: Scale parameter of shape (D,)
- beta: Shift paremeter of shape (D,)
- bn_param: Dictionary with the following keys:
 - mode: 'train' or 'test'; required
 - eps: Constant for numeric stability
 - momentum: Constant for running mean / variance.
 - running_mean: Array of shape (D,) giving running mean of features
 - running_var Array of shape (D,) giving running variance of features
Returns a tuple of:
- out: of shape (N, D)
- cache: A tuple of values needed in the backward pass
mode = bn_param['mode']
eps = bn_param.get('eps', 1e-5)
momentum = bn param.get('momentum', 0.9)
N, D = x.shape
running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
out, cache = None, None
if mode == 'train':
 # YOUR CODE HERE:
 # A few steps here:
 #
       (1) Calculate the running mean and variance of the minibatch.
      (2) Normalize the activations with the running mean and variance.
       (3) Scale and shift the normalized activations. Store this
 #
           as the variable 'out'
       (4) Store any variables you may need for the backward pass in
          the 'cache' variable.
 batch mean = x.mean(axis=0)
 batch_var = x.var(axis=0)
 x_centralized = x - batch_mean
 x_normalized = x_centralized / (batch_var + eps) ** 0.5
 out = gamma * x_normalized + beta
```

```
# update running mean and var
   running_mean = momentum * running_mean + (1 - momentum) * batch_mean
   running_var = momentum * running_var + (1 - momentum) * batch_var
   # update cache
   cache = {
      "batch_var": batch_var,
      "x_centralized": x_centralized,
      "x_normalized": x_normalized,
      "gamma": gamma,
      "eps": eps,
   }
   # END YOUR CODE HERE
   elif mode == 'test':
   # ------ #
   # YOUR CODE HERE:
   # Calculate the testing time normalized activation. Normalize using
     the running mean and variance, and then scale and shift appropriately.
     Store the output as 'out'.
   out = gamma * (x - running_mean) / (running_var + eps) ** 0.5 + beta
   # END YOUR CODE HERE
   # ----- #
 else:
   raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
 # Store the updated running means back into bn param
 bn param['running mean'] = running mean
 bn_param['running_var'] = running_var
 return out, cache
def batchnorm backward(dout, cache):
 Backward pass for batch normalization.
 For this implementation, you should write out a computation graph for
 batch normalization on paper and propagate gradients backward through
 intermediate nodes.
 - dout: Upstream derivatives, of shape (N, D)
 - cache: Variable of intermediates from batchnorm_forward.
 Returns a tuple of:
 - dx: Gradient with respect to inputs x, of shape (N, D)
 - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
 - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
 dx, dgamma, dbeta = None, None, None
```

```
# YOUR CODE HERE:
   Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
 N = dout.shape[0]
 # unpack cache
 batch_var = cache.get("batch_var")
 x_centralized = cache.get("x_centralized")
 x_normalized = cache.get("x_normalized")
 gamma = cache.get("gamma")
 eps = cache.get("eps")
 # calculate dx
 dx_hat = dout * gamma
 batch_sqrt_var = (batch_var + eps) ** 0.5
 dx_mu1 = dx_hat / batch_sqrt_var
 dsqrt var = -(dx hat * x centralized).sum(axis=0) / (batch var + eps)
 dvar = dsqrt_var * 0.5 / batch_sqrt_var
 dx_mu2 = 2 * x_centralized * dvar * np.ones_like(dout) / N
 dx1 = dx_mu1 + dx_mu2
 dx2 = -dx1.sum(axis=0) * np.ones_like(dout) / N
 dx = dx1 + dx2
 # calculate dgamma and dbeta
 dbeta = dout.sum(axis=0)
 dgamma = (dout * x_normalized).sum(axis=0)
 # END YOUR CODE HERE
 # ----- #
 return dx, dgamma, dbeta
def dropout forward(x, dropout param):
 Performs the forward pass for (inverted) dropout.
 Inputs:
 - x: Input data, of any shape
 - dropout param: A dictionary with the following keys:
   - p: Dropout parameter. We drop each neuron output with probability p.
   - mode: 'test' or 'train'. If the mode is train, then perform dropout;
     if the mode is test, then just return the input.
   - seed: Seed for the random number generator. Passing seed makes this
     function deterministic, which is needed for gradient checking but not in
     real networks.
 Outputs:
 - out: Array of the same shape as x.
 - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
   mask that was used to multiply the input; in test mode, mask is None.
 p, mode = dropout param['p'], dropout param['mode']
 if 'seed' in dropout_param:
   np.random.seed(dropout param['seed'])
 mask = None
 out = None
```

```
if mode == 'train':
  # YOUR CODE HERE:
    Implement the inverted dropout forward pass during training time.
   Store the masked and scaled activations in out, and store the
    dropout mask as the variable mask.
  mask = (np.random.rand(*x.shape) < p) / p</pre>
  out = x * mask
  # END YOUR CODE HERE
  elif mode == 'test':
  # YOUR CODE HERE:
   Implement the inverted dropout forward pass during test time.
 # ------ #
  # END YOUR CODE HERE
  cache = (dropout_param, mask)
out = out.astype(x.dtype, copy=False)
 return out, cache
def dropout_backward(dout, cache):
 Perform the backward pass for (inverted) dropout.
Inputs:
 - dout: Upstream derivatives, of any shape
 - cache: (dropout_param, mask) from dropout_forward.
 dropout_param, mask = cache
mode = dropout param['mode']
 dx = None
 if mode == 'train':
  # ------ #
  # YOUR CODE HERE:
   Implement the inverted dropout backward pass during training time.
 dx = dout * mask
  # END YOUR CODE HERE
  elif mode == 'test':
  # YOUR CODE HERE:
    Implement the inverted dropout backward pass during test time.
  dx = dout
  # END YOUR CODE HERE
  # ------ #
 return dx
```

```
def svm_loss(x, y):
  Computes the loss and gradient using for multiclass SVM classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
    0 \leftarrow y[i] \leftarrow C
  Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
  N = x.shape[0]
  correct_class_scores = x[np.arange(N), y]
  margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
  margins[np.arange(N), y] = 0
  loss = np.sum(margins) / N
  num_pos = np.sum(margins > 0, axis=1)
  dx = np.zeros_like(x)
  dx[margins > 0] = 1
  dx[np.arange(N), y] -= num_pos
  dx /= N
  return loss, dx
def softmax_loss(x, y):
  Computes the loss and gradient for softmax classification.
 Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
    0 \leftarrow y[i] \leftarrow C
  Returns a tuple of:
  - loss: Scalar giving the loss
  - dx: Gradient of the loss with respect to x
  0.00
  probs = np.exp(x - np.max(x, axis=1, keepdims=True))
  probs /= np.sum(probs, axis=1, keepdims=True)
  N = x.shape[0]
  loss = -np.sum(np.log(probs[np.arange(N), y])) / N
  dx = probs.copy()
  dx[np.arange(N), y] -= 1
  dx /= N
  return loss, dx
```