

Homework 1

Computer Engineering 303

Problem 1. (25 Points, CMOS Technology)

- (a) (15 Points) If the number of transistors per unit area (i.e., on the same chip size) doubles every 24 months, what is the annual scaling factor s for the length of the side of a transistor, assuming the area occupied by one transistor is a square?

Total chip area at the start of a two year cycle = A_{initial}

Total number of transistors on chip at the start of a two year cycle = N

Initial Length of one side of the square shaped transistor area = L

Annual transistor scaling factor = s

Derive the answer by solving the following steps:

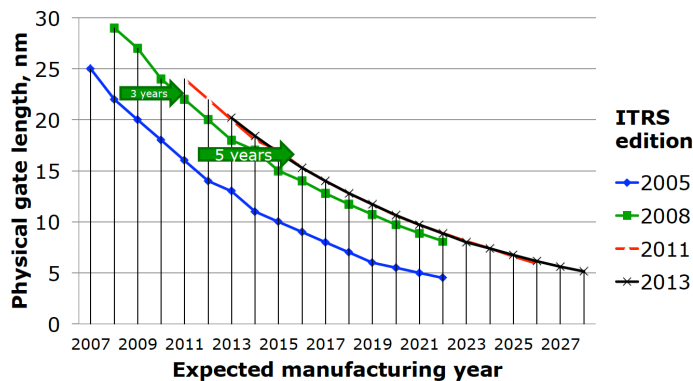
$A_{\text{initial}} =$

$A_{\text{one_year}} =$

Using the equations above derive the value for annual scaling factor $s =$

- (b) (10 Points) The International Technology Roadmap for Semiconductors published the trends depicted in the figure below. Starting with 18.4nm in 2014 what would be the transistor size according to the scaling trend s you calculated above in 2021? How does it compare to the predicted 10nm size in the report?

ITRS projections for gate lengths (nm)
for 2005, 2008 and 2011 editions



Problem 2. (30 Points, 10 Points for each part) Switch Representation of Digital Circuits:

Draw the CMOS circuit diagrams using NMOS and PMOS transistors for the following functions.

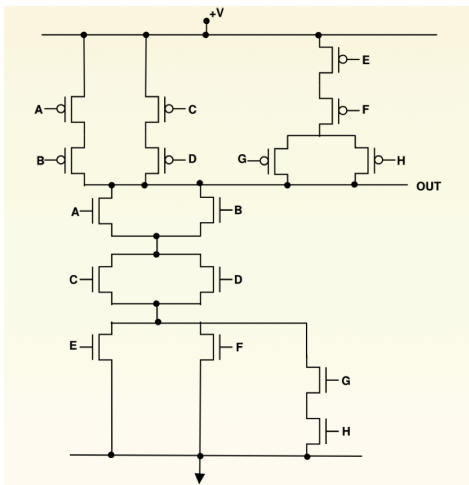
(1)

$$F = \overline{(AB+C)D}$$

(2)

$$F = \overline{(A+B)(BC+D)}$$

(3) What is the logic equation describing the behavior of the complex CMOS gate depicted in the figure below?



Problem 3. (25 Points) For the function f with the minterms $\{ABC'D, ABC'D', A'BC'D, A'B'C'D, ABCD, ABCD', A'B'CD\}$

CD \ AB	00	01	11	10
00				
01				
11				
10				

a. (20 Points) Using the K-Map layout above, identify all Prime Implicants

b. (5 Points) Identify the Essential Prime Implicants

Problem 4. (25 Points) Find all Prime Implicants for the following functions by applying the first step of the QM Method

- a. $F(A, B, C, D) = \text{minterms of the ON-Set: } \{m_1, m_5, m_7, m_9, m_{11}, m_{12}, m_{14}, m_{15}\}$
- b. $F(A, B, C, D) = \text{minterms of the ON-Set: } \{m_0, m_1, m_3, m_5, m_6, m_7, m_8, m_{10}, m_{14}, m_{15}\}$