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In[14]:=  $\alpha L = 1.3 \times 10^5;$ 
 $\beta R = 1.0 \times 10^5;$ 
 $AL = 0.1^2 \pi / 4;$ 
 $AR = 0.09^2 \pi / 4;$ 
 $\kappa = 1.4; R = 287; cV = \frac{R}{\kappa - 1};$ 
 $\rho 0 = 1.2;$ 

In[1]:= Eq1 = pL +  $\rho L$  aL vL -  $\alpha L$ ;
Eq2 = pR -  $\rho R$  aR vR -  $\beta R$ ;
Eq3 =  $\rho L$  AL vL -  $\rho R$  AR vR;
Eq4 =  $\rho L$  AL vL2 + pL AR - ( $\rho R$  AR vR2 + pR AR);
Eq5 = ( $\rho L$  eL vL + pL vL) AL - ( $\rho R$  eR vR + pR vR) AR;
Eq6 = aL -  $\sqrt{\kappa R TL}$ ;
Eq7 = aR -  $\sqrt{\kappa R TR}$ ;
Eq8 = eL - (cV TL + vL2 / 2);
Eq9 = eR - (cV TR + vR2 / 2);
Eq10 = pL -  $\rho L$  R TL;
Eq11 = pR -  $\rho R$  R TR;
Eq12 =  $\rho R$  -  $\rho 0$ ;

In[20]:= sols = NSolve[{Eq1 == 0, Eq2 == 0, Eq3 == 0, Eq4 == 0, Eq5 == 0,
Eq6 == 0, Eq7 == 0, Eq8 == 0, Eq9 == 0, Eq10 == 0, Eq11 == 0, Eq12 == 0},
{pL, pR, vL, vR, aL, aR,  $\rho L$ ,  $\rho R$ , eL, eR, TL, TR}];
sols[[3]]

Out[21]= { $\rho R \rightarrow 1.2$ , TL  $\rightarrow 338.209$ , TR  $\rightarrow 337.971$ , aR  $\rightarrow 368.506$ , eR  $\rightarrow 243182.$ , aL  $\rightarrow 368.636$ ,
eL  $\rightarrow 243114.$ , pL  $\rightarrow 116714.$ , pR  $\rightarrow 116397.$ ,  $\rho L \rightarrow 1.20242$ , vR  $\rightarrow 37.0806$ , vL  $\rightarrow 29.975$ }

In[13]:= {Eq1, Eq2, Eq3, Eq4, Eq5, Eq6, Eq7, Eq8, Eq9, Eq10, Eq11, Eq12} /. {vL  $\rightarrow 0$ , vR  $\rightarrow 0$ }

Out[13]= {pL -  $\alpha L$ , pR -  $\beta R$ , 0, AR pL - AR pR, 0, aL -  $\sqrt{R TL \kappa}$ ,
aR -  $\sqrt{R TR \kappa}$ , eL - cV TL, eR - cV TR, pL - R TL  $\rho L$ , pR - R TR  $\rho R$ , - $\rho 0$  +  $\rho R$ }

Eq4 = mp vL + pL AR - (mp vL + pR AR);

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