

## FISH 559: Example Application I (Fitting growth curves)

Two commonly applied curves relating length to age are the logistic function (Eqn 1a) and the von Bertalanffy curve (Eqn 1b)<sup>1</sup>:

$$L_a = L_\infty \left( 1 + \exp \left[ -\ln 19 \frac{(a - a_{50})}{\Delta} \right] \right)^{-1} \quad (1a)$$

$$L_a = L_\infty (1 - \exp(-\kappa(a - a_0))) \quad (1b)$$

where  $L_\infty$  is the asymptotic size,  $a_{50}$  is the age at which length is half of  $L_\infty$ ,  $\Delta$  is the difference between age at which length is 95% of  $L_\infty$  and  $a_{50}$ ,  $\kappa$  is the growth rate parameter, and  $a_0$  is the age corresponding to zero length. You can assume that the errors measuring length-at-age are normally distributed with mean 0 and standard deviation  $\sigma$ .

Given the data file EX1.DAT:

- fit models 1a and 1b using TMB;
- print out the model predictions for ages 0-20 ;
- write an R function to plot the data and the two sets of model predictions;
- use AIC to (a) select a best model and (b) compute AIC-weights; and
- find a model-averaged estimate for  $L_\infty$ .

Hints:

- Write down the negative log-likelihood function first
- To keep parameters positive, estimate them in log-space
- You should have one CPP file and use the map option to ensure that you only estimate the correct number of parameters.

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<sup>1</sup> Both of these curves are special cases of Schnute's (1981) generalized growth model.