Let $X = QR$, and extend Q to an $n \times n$ ON matrix $[Q, \tilde{Q}]$.
Write $y = QQ^T y + \tilde{Q}\tilde{Q}^T y$.