

Part 1

(a)  $w_1$

(b)  $w_1$

(c)  $f(x) = \frac{1}{12}x - \frac{1}{4}$

$$\therefore P(\text{error} | w) = \int_3^{5.1} \left( \frac{1}{12}x - \frac{1}{4} \right) dx = 0.18375$$

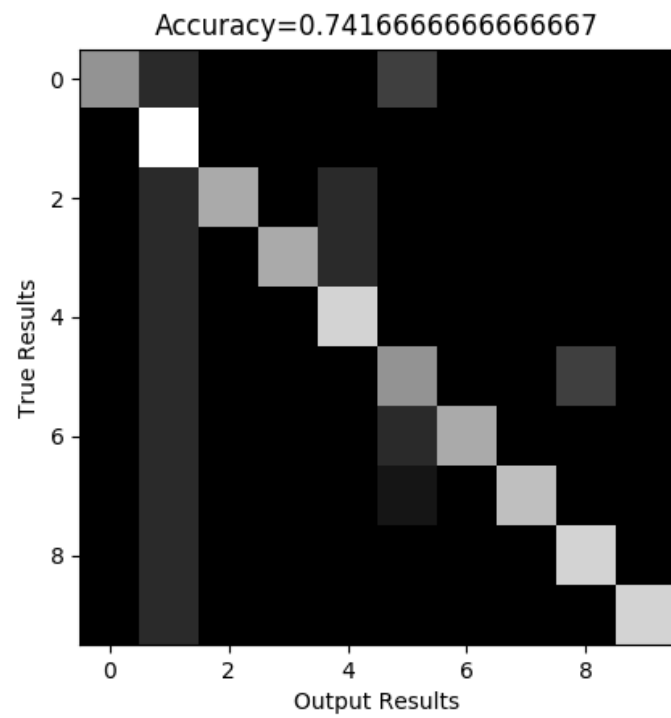
(d) 
$$\begin{cases} y = \frac{1}{12}x - \frac{1}{4} \\ y = -\frac{1}{6}x + \frac{5}{6} \end{cases} \Rightarrow \begin{cases} x = \frac{13}{3} \\ y = \frac{1}{9} \end{cases}$$

set a threshold  $x^* = \frac{13}{3}$

if  $x \geq x^*$  then decide  $w_2$ , else decide  $w_1$

## Part 2

### 1. PCA confusion matrix



### 2. Eigenfaces and mean face

Eigenface 1



Eigenface 2



Eigenface 3



Eigenface 4



Eigenface 5



Eigenface 6



Eigenface 7



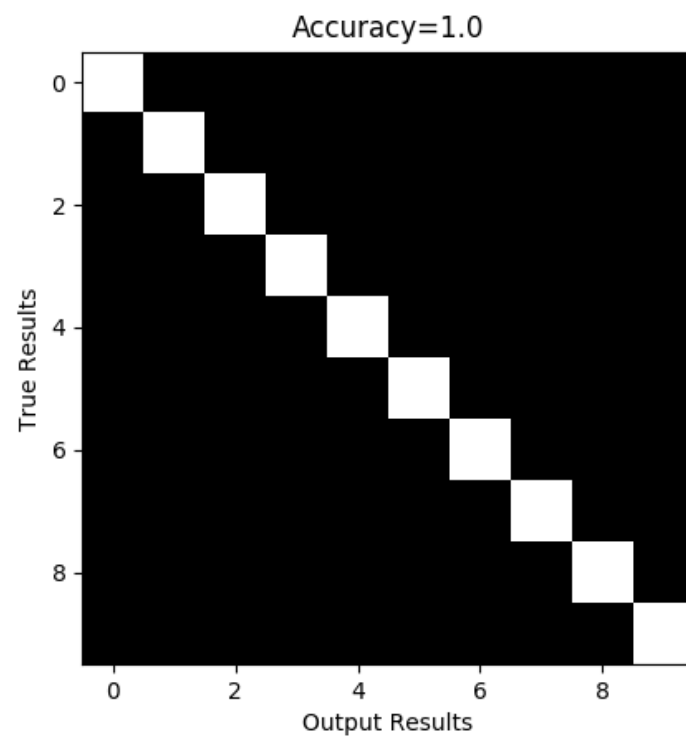
Eigenface 8



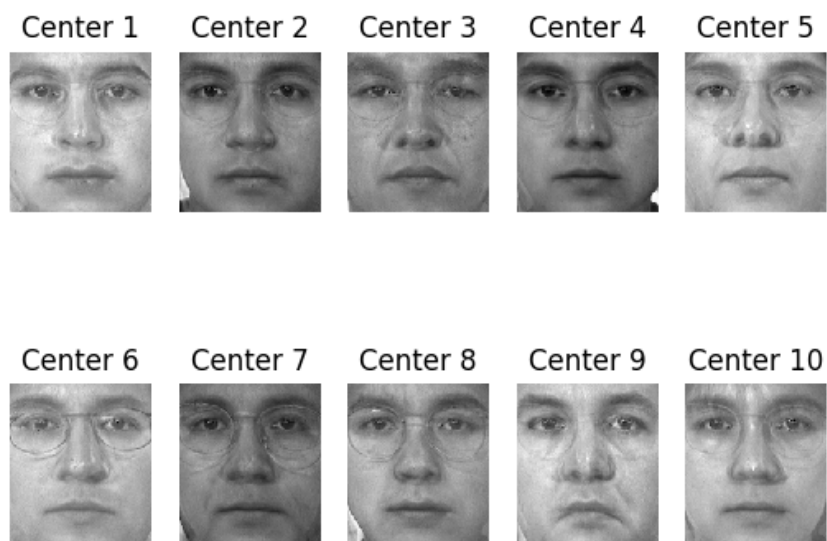
Mean



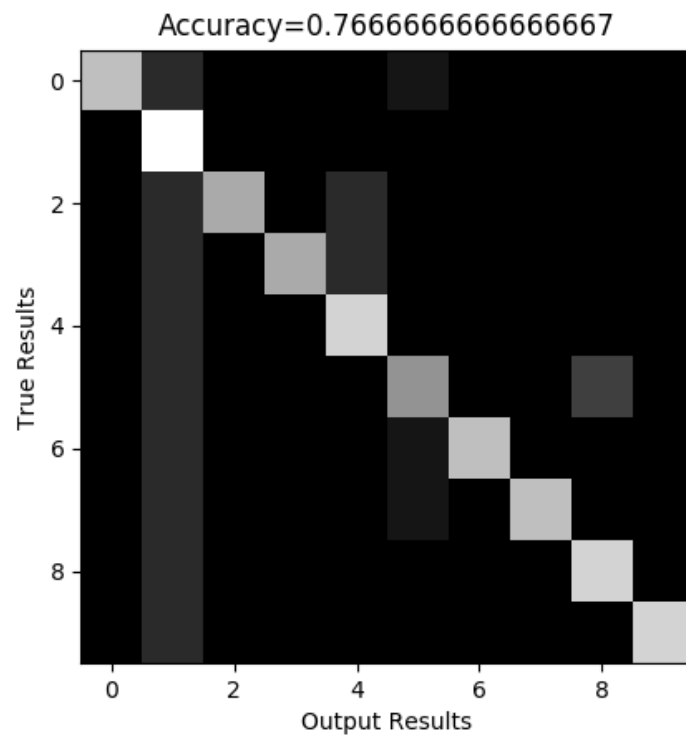
3. LDA confusion matrix



4. LDA centers



5. Fusion scheme confusion matrix



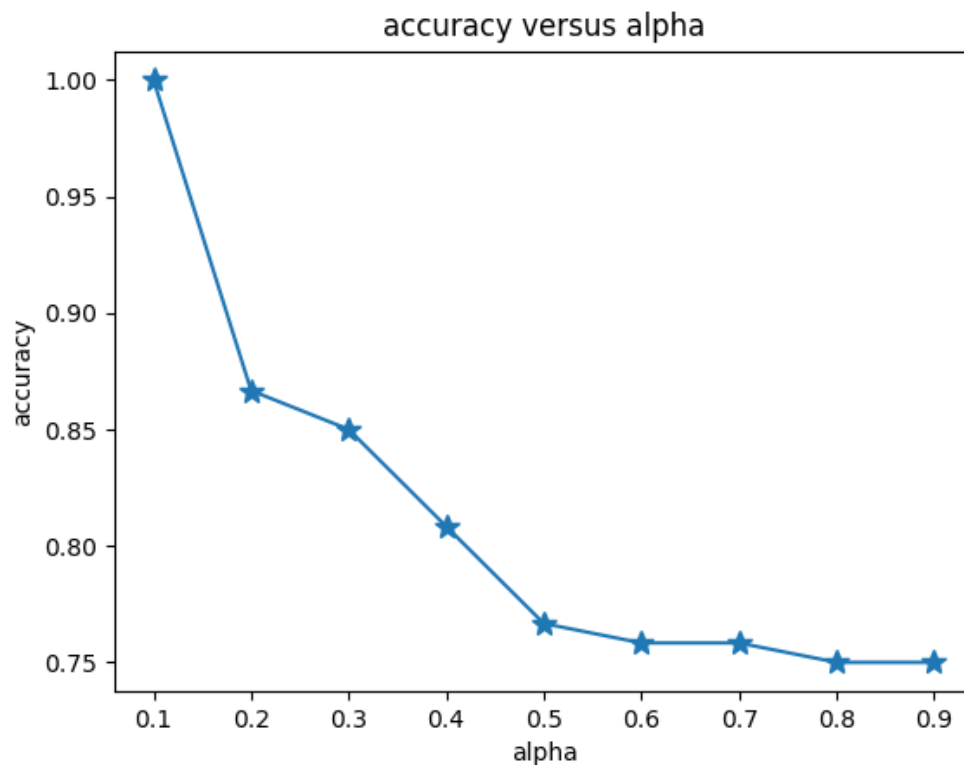
Q: Compare the results for PCA feature and LDA feature, which feature is better? Why?

A: LDA feature is better. In this problem, PCA just projects the data to the axis which is easy to present and it doesn't use the information of classes within the data. So classes are mixed up which makes it difficult to classify. However, LDA finds the most suitable way to project the data so that classes are well separated. Thus, in this face recognition problem, LDA performs better.

Q: Let  $\alpha = 0.1; 0.2; \dots; 0.9$ . Retrain your identifier for fused feature and re-calculate its accuracy for each  $\alpha$ . Plot accuracy versus  $\alpha$  for different  $\alpha$ . Submit this plot.

What do you observe?

A:



I find that with  $\alpha$  increasing, the accuracy rate keeps dropping. When  $\alpha$  tends to be 0, the accuracy tends to be 100% and when  $\alpha$  tends to be 1, the accuracy tends to be 74%. For all the  $\alpha$  between 0 and 1, the accuracy rate monotonically decreases.

Q: Does the fused feature outperform both PCA feature and LDA feature? Why?

A: No. This may be because I just implement fusion scheme in feature level and it just does the combination of two feature vectors. Thus, the accuracy, unsurprisingly, is just between two methods and the limiting cases meet the results which I get above.