



# **COMP9321:**

## **Data services engineering**

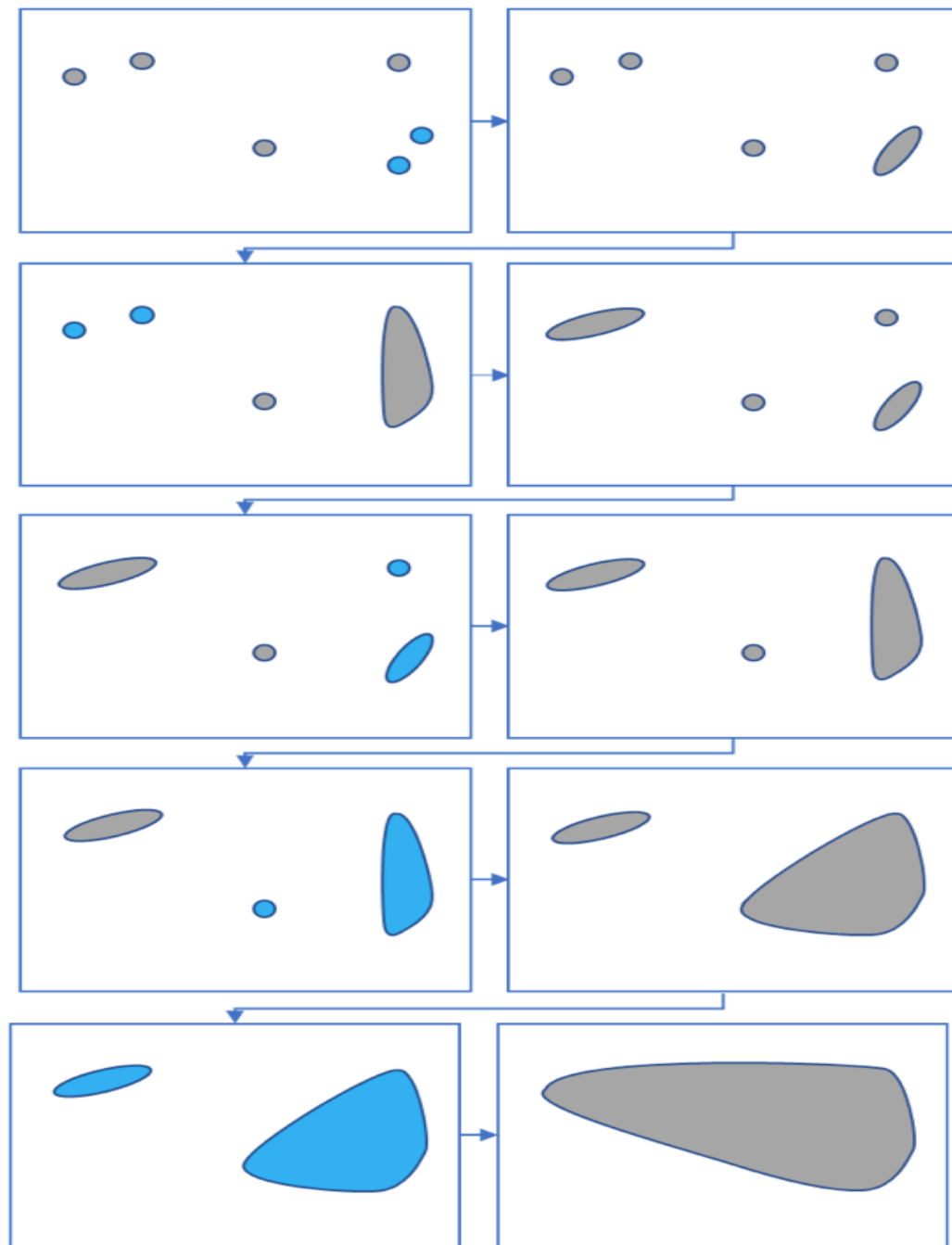
### **Week 9: Hierarchal Clustering and ML Model Evaluation**

**Term 1, 2020**

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# Hierarchal Clustering

- What is it?
  - Unsupervised machine learning.
  - It is essentially building a hierarchy of clusters
- Types of Hierarchal Clustering
  - Agglomerative hierarchical clustering
  - Divisive Hierarchical clustering



# Linkage Criteria

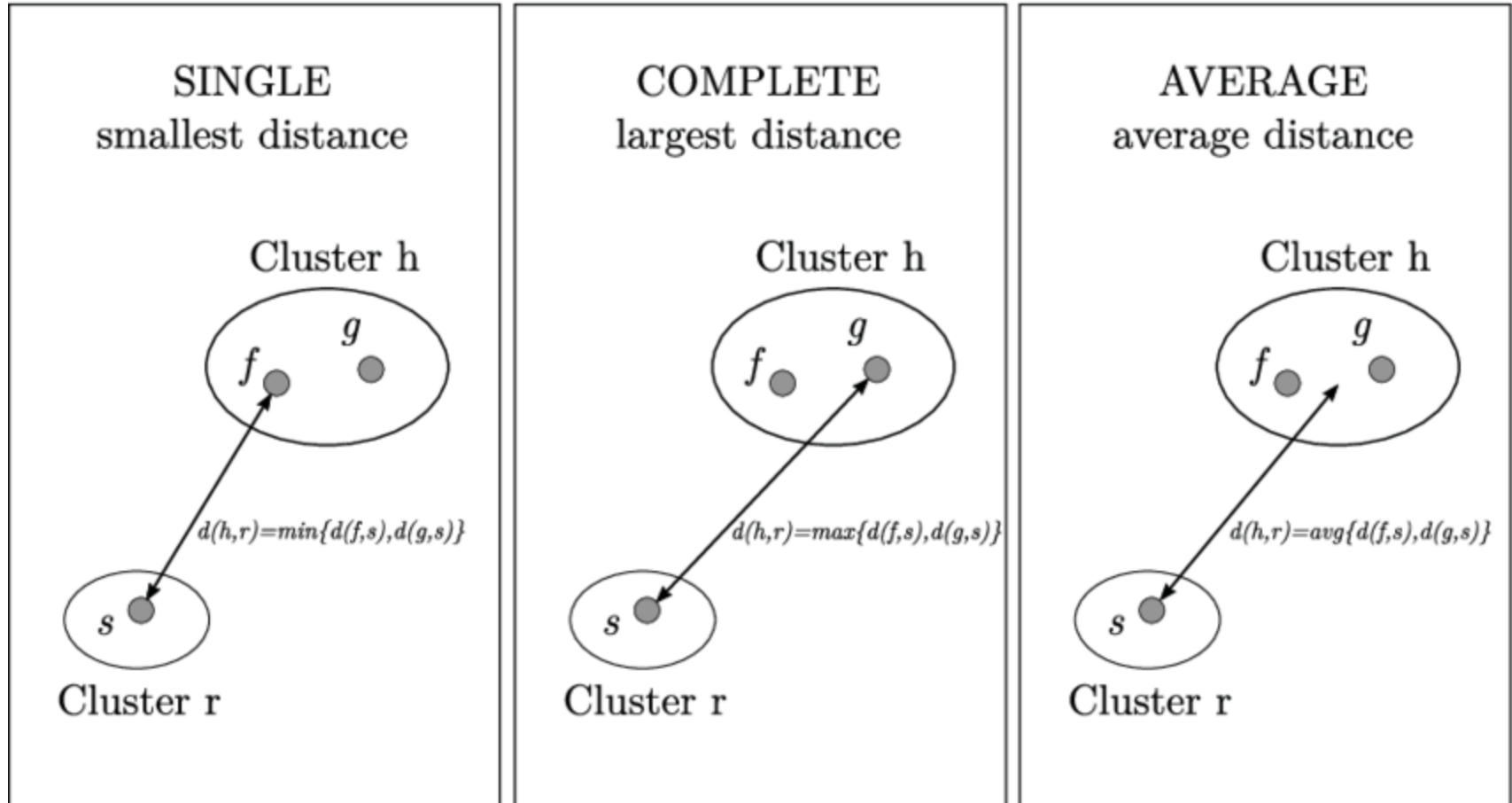
- It is necessary to determine from where distance is computed in cluster.
- Your options
  - It can be computed between the two most similar parts of a cluster (*single-linkage*)
  - the two least similar bits of a cluster (*complete-linkage*)
  - the center of the clusters (*mean or average-linkage*)
  - or some other criterion

从两个cluster里取距离最短的两个点当作cluster的距离

从两个cluster里取距离最长的两个点当作cluster的距离

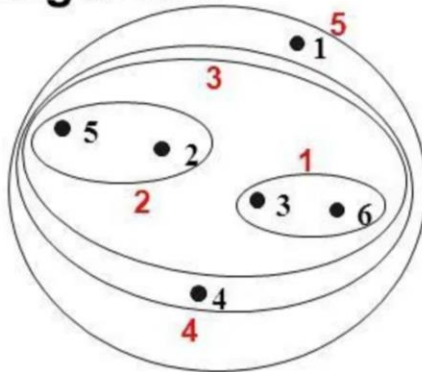
从两个cluster里的两个中点当作cluster的距离

# Linkage Criteria

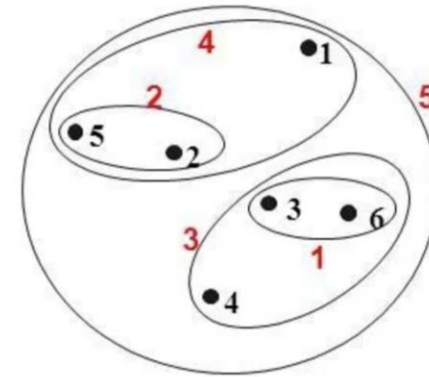


# Linkage Criteria Comparison

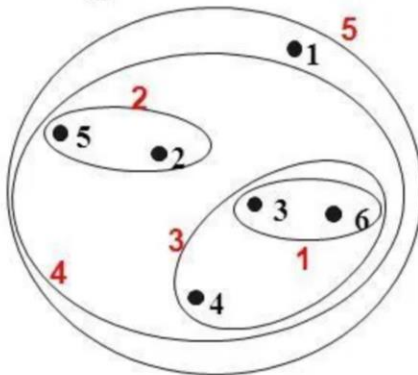
**Single-link**



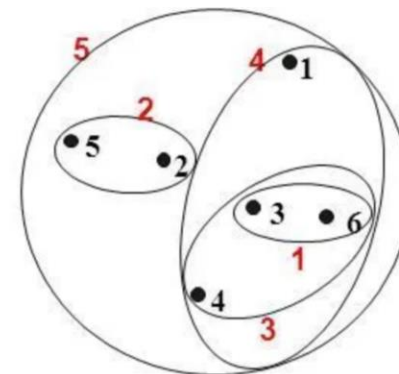
**Complete-link**



**Average-link**



**Centroid distance**

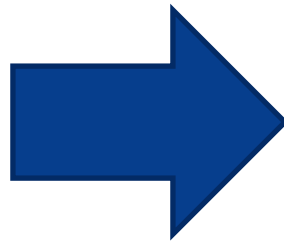


# Agglomerative Clustering Algorithm

1. Compute the proximity matrix
2. Let each data point be a cluster
3. Repeat: Merge the two closest clusters and update the proximity matrix
4. Until only a single cluster remains

# Agglomerative Clustering Example

Student_ID	Marks
1	10
2	7
3	28
4	20
5	35



ID	1	2	3	4	5
1	0	3	18	10	25
2	3	0	21	13	28
3	18	21	0	8	7
4	10	13	8	0	15
5	25	28	7	15	0

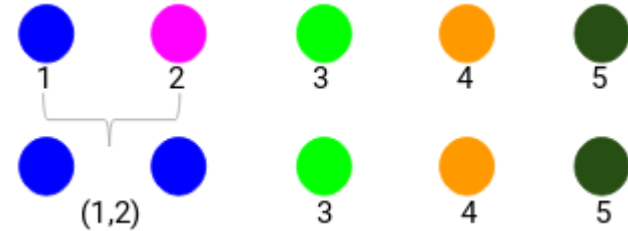
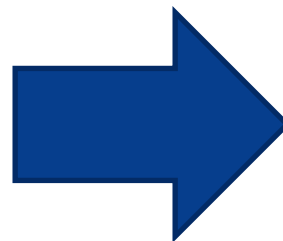
Proximity Matrix



# Agglomerative Clustering Example



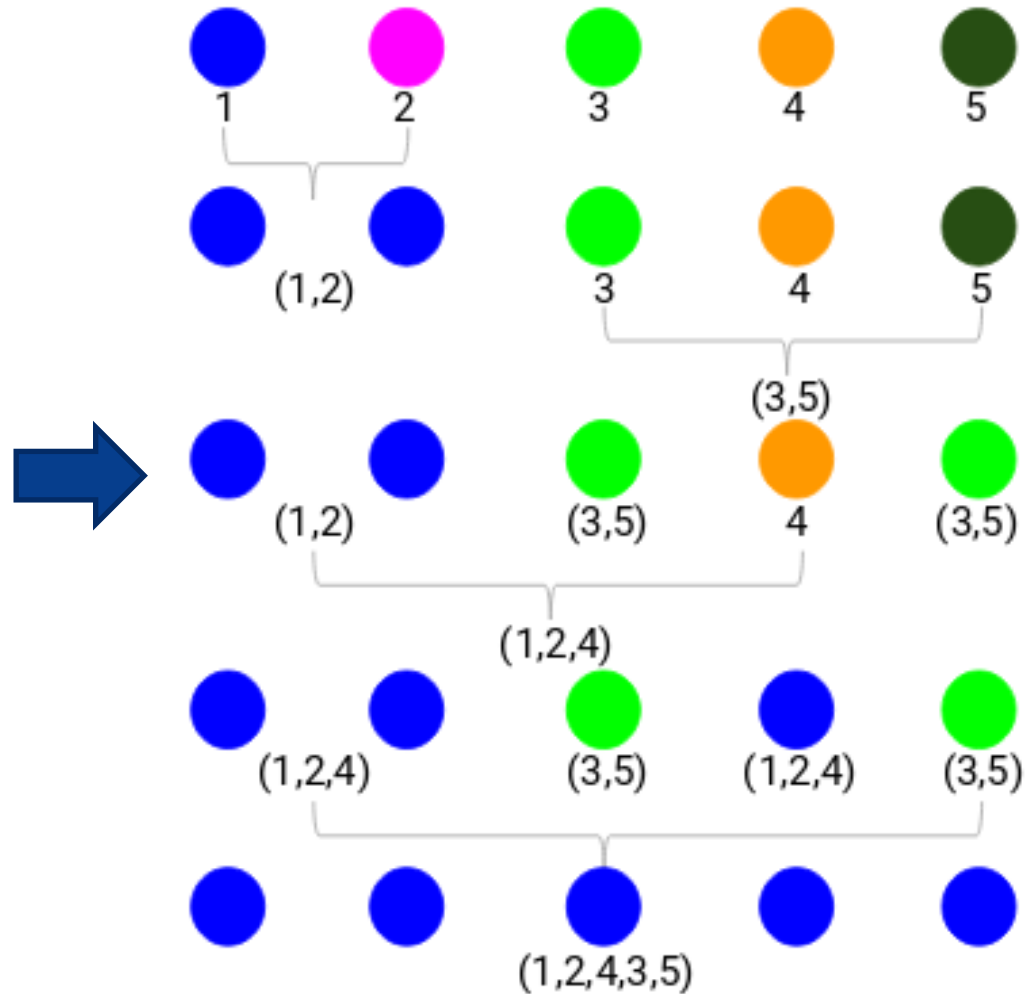
ID	1	2	3	4	5
1	0	3	18	10	25
2	3	0	21	13	28
3	18	21	0	8	7
4	10	13	8	0	15
5	25	28	7	15	0



Student_ID	Marks
(1,2)	10
3	28
4	20
5	35

# Agglomerative Clustering Example

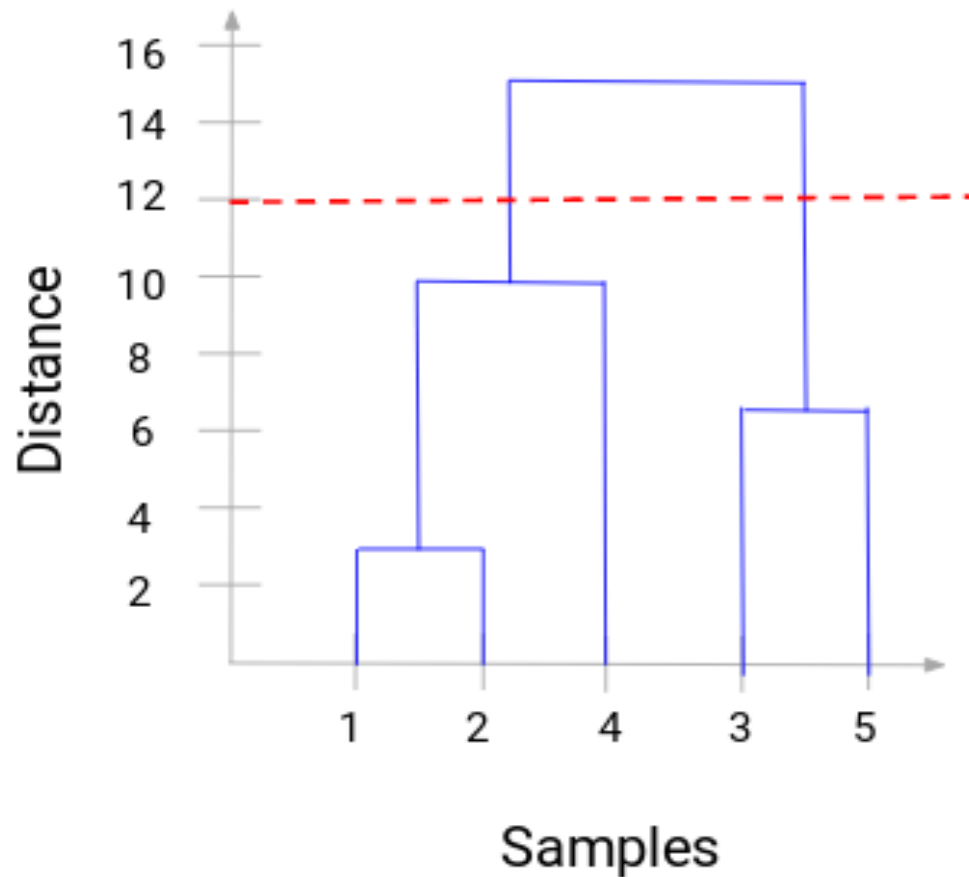
ID	(1,2)	3	4	5
(1,2)	0	18	10	25
3	18	0	8	7
4	10	8	0	15
5	25	7	15	0



# How Can we Choose the Number of Clusters?

- Using a Dendrogram
- A dendrogram is a tree-like diagram that records the sequences of merges or splits
- Whenever two clusters are merged, we will join them in this dendrogram and the height of the join will be the distance between these points
- We set a threshold distance and draw a horizontal line (try to set the threshold in such a way that it cuts the tallest vertical line)
- The number of clusters will be the number of vertical lines which are being intersected by the line drawn using the threshold

# How Can we Choose the Number of Clusters?

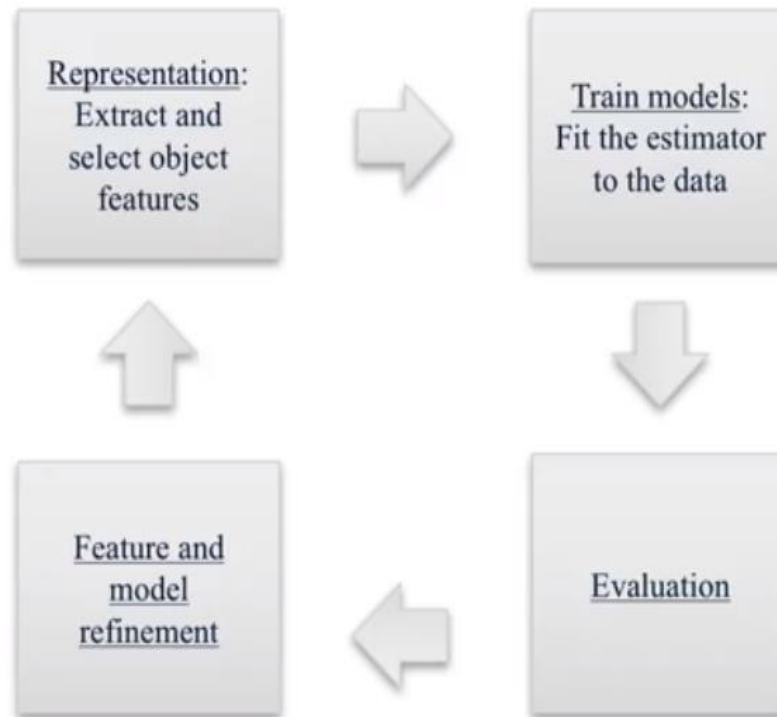


# Advantages and Disadvantages of Hierarchical Clustering

- Advantages
  - Easy to Implement
  - No Need to decide the number of clusters beforehand.
- Disadvantages
  - Not suitable for large datasets
  - Sensitive to Outliers
  - Initial Seeds have strong impact of final results
  - Linkage criteria and Distance measure are selected most of the time arbitrary.

# Refresher

## Represent / Train / Evaluate / Refine Cycle



# Machine Learning Evaluation

- There are various metrics and methods to evaluate machine learning algorithms
- They differ according to the algorithm being supervised or unsupervised and they differ according to the task
- Let's look at some of the metrics and concepts regarding evaluation

# Accuracy

- This is the simplest metric
- Number of correct predictions divided by the total number of predictions, multiplied by 100.

$$\text{Accuracy} = \frac{\text{\#correct predictions}}{\text{\#total instances}}$$



# Accuracy with Imbalanced Classes

- Suppose you have two classes:
  - The positive class
  - The negative class
- Out of 1000 randomly selected items, on average:
- One item belong to the positive class
- The rest of items (999 of them) belong to the negative class
- The Accuracy will be

$$\text{Accuracy} = \frac{\text{\#correct predictions}}{\text{\#total instances}}$$

# Accuracy with Imbalanced Classes

- When you build a classifier to predict the items (positive or negative), you may find out that the accuracy on the test set is 99.9%.
- Be aware that this is not an actual presentation of how good your classifier is.
- For comparison, if we have a “dummy” classifier that does not consider the features at all but rather blindly predicts according to the most frequent class

# Accuracy with Imbalanced Classes

- If we use the same dataset mentioned in the previous slide (the 1000 data instance with 999 negative and 1 positive). What do you think the accuracy of the dummy classifier would be?

**Answer:**

$$\text{Accuracy}_{\text{Dummy}} = 999/1000 = 99.9\%$$

- Hence the accuracy alone sometime not a good metric to measure how good the model is

# Dealing with Imbalanced Classes

- Data pre-processing
  - Random Under Sampling
  - Random Over Sampling
  - Cluster-Based Over Sampling
  - Synthetic Minority Over-sampling
- Select More suitable Metrics to Evaluate Imbalanced Classes
  - Precision and Recall
  - F1-Score
  - Log-Loss

# Precision and Recall

**FN: the classifier predict it negative, but it is actually positive!**

## Precision

**Precision** attempts to answer the following question:

**FP: the classifier predict it positive, but it is actually negative!**

What proportion of positive identifications was actually correct?

Precision is defined as follows:

$$\text{Precision} = \frac{TP}{TP + FP}$$

TP: True Positive

**FP: False Positive**

FN: False Negative

## Recall

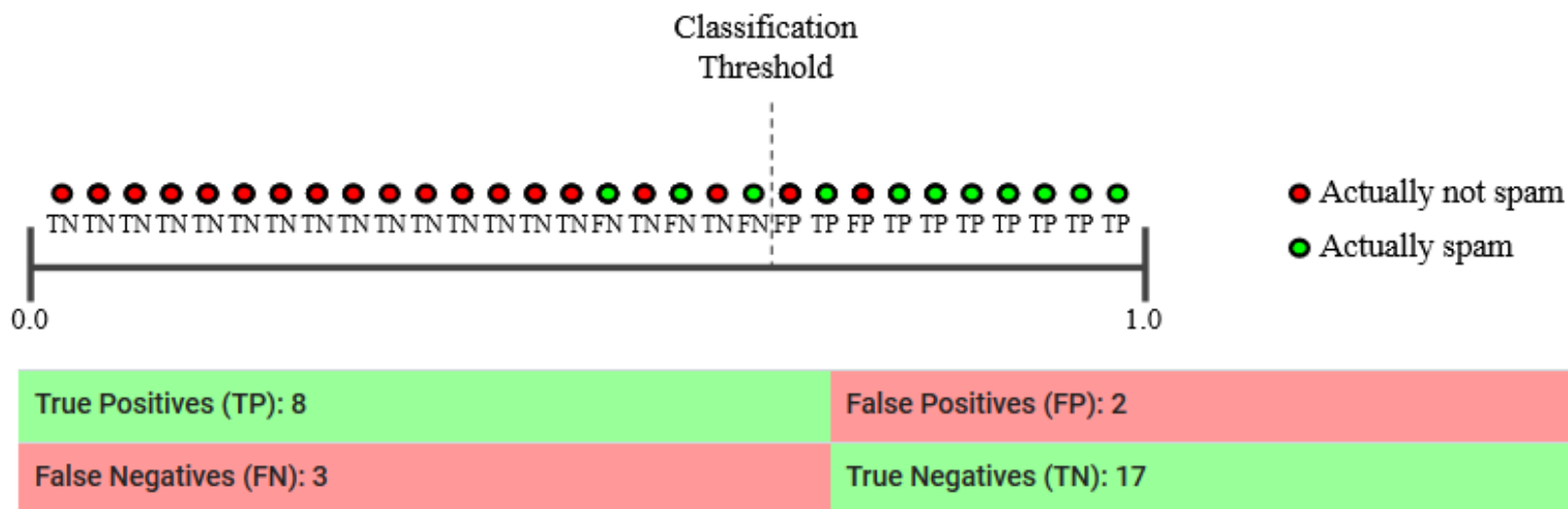
**Recall** attempts to answer the following question:

What proportion of actual positives was identified correctly?

Mathematically, recall is defined as follows:

$$\text{Recall} = \frac{TP}{TP + FN}$$

# Precision and Recall



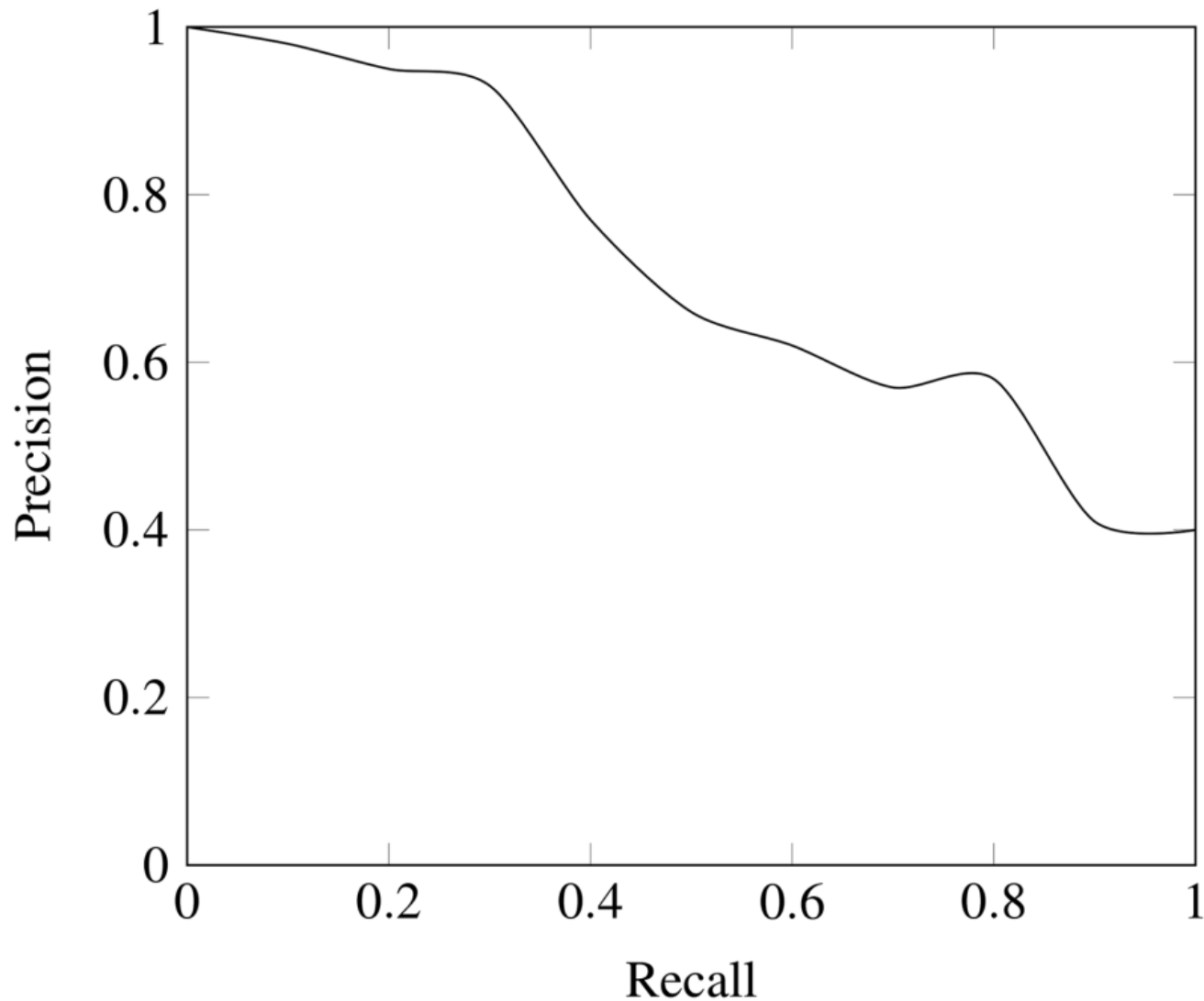
Precision measures the percentage of **emails flagged as spam** that were correctly classified—that is, the percentage of dots to the right of the threshold line that are green

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{8}{8 + 2} = 0.8$$

Recall measures the percentage of **actual spam emails** that were correctly classified—that is, the percentage of green dots that are to the right of the threshold line

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{8}{8 + 3} = 0.73$$

# Precision and Recall



# F1 Score

- A metric which combines precision and recall
- Harmonic mean of precision and recall

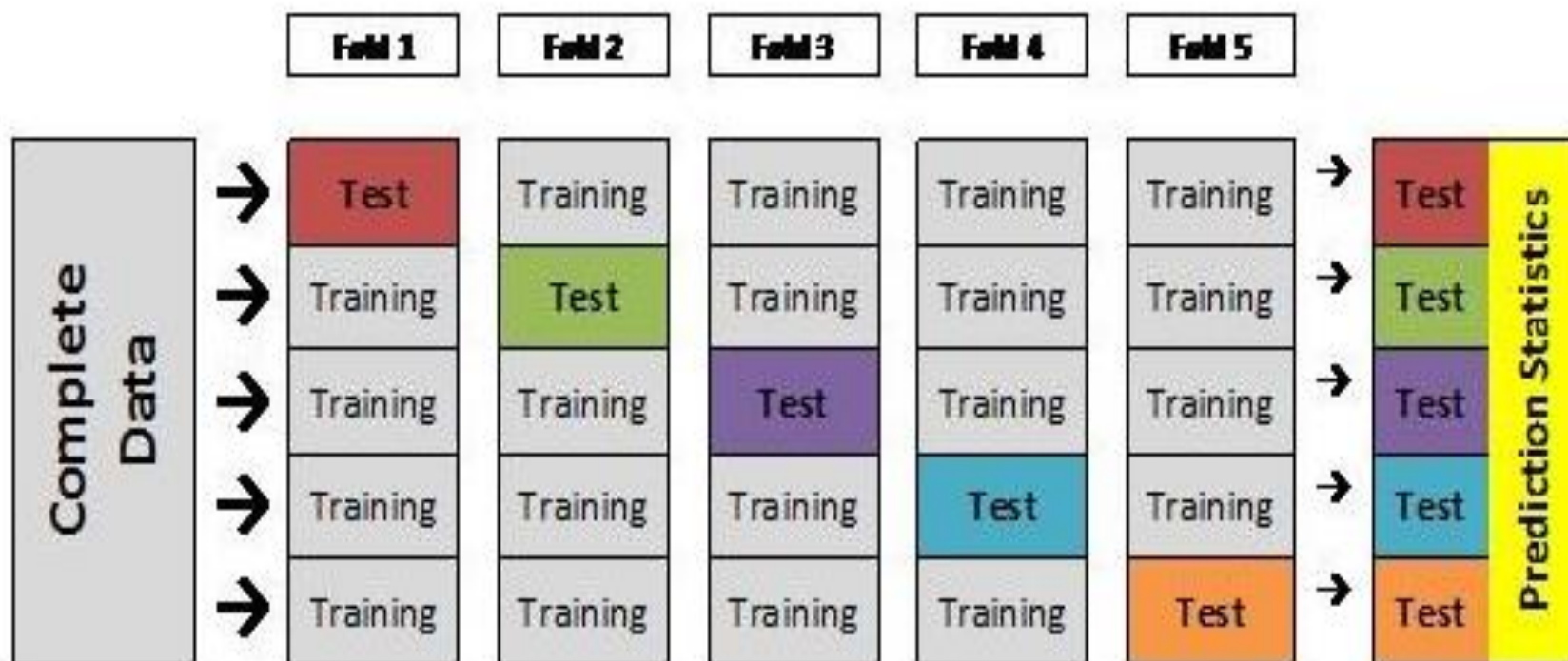
$$\text{F1-score} = 2 * \text{Precision} * \text{Recall} / (\text{Precision} + \text{Recall})$$



# Cross-validation

- Cross-validation is a resampling procedure used to evaluate machine learning models on a limited data sample.
- The procedure has a single parameter called  $k$  that refers to the number of groups that a given data sample is to be split into. As such, the procedure is often called  $k$ -fold cross-validation.
- When a specific value for  $k$  is chosen, it may be used in place of  $k$  in the reference to the model, such as  $k=5$  becoming 5-fold cross-validation.

# Cross Validation Examples (5-fold)



# Stratified Cross-validation

fruit_label	fruit_name
1	Apple
1	Apple
1	Apple
1	Apple
1	Apple
2	Mandarin
...	...
3	Orange
...	...
4	Lemon
4	Lemon
4	Lemon
4	Lemon
4	Lemon

(Folds and dataset shortened for illustration purposes.)

Example has 20 data samples  
= 4 classes with 5 samples each.

5-fold CV: 5 folds of 4 samples each.

Fold 1 uses the first 20% of the dataset as the test set,  
which only contains samples from class 1.

Classes 2, 3, 4 are missing entirely from test set and so  
will be missing from the evaluation.

# Stratified Cross-validation

- Stratification is a technique where we rearrange the data in a way that each fold has a good representation of the whole dataset
- It forces each fold to have at least  $m$  instances of each class.  $T$
- This approach ensures that one class of data is not overrepresented especially when the target variable is unbalanced.

# Useful Resources

<https://towardsdatascience.com/understanding-the-concept-of-hierarchical-clustering-technique-c6e8243758ec>

<https://heartbeat.fritz.ai/introduction-to-machine-learning-model-evaluation-fa859e1b2d7f>

<https://machinelearningmastery.com/tour-of-evaluation-metrics-for-imbalanced-classification/>

<https://www.analyticsvidhya.com/blog/2017/03/imbalanced-data-classification/>

<https://medium.com/james-blogs/handling-imbalanced-data-in-classification-problems-7de598c1059f>

# Q&A