

Exploratory data analysis on impact of weather on marathon performance across age and gender

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Introduction

Marathon running is a physically demanding sport which requires a combination of endurance, strength, and mental fortitude. Runners characteristics shaped the performance as Men are more likely than women to slow over the course of a marathon(DEANER et al. 2015). And older runners tend to have less pace variance in a marathon than younger runners(Nikolaidis and Knechtle 2017). Research has shown adverse weather condition(High temperature, humidity, etc) can have a negative impact on marathon performance on both elite(Knechtle et al. 2021) and recreational runners(ELY et al. 2007). But the effect diminish among females compare to male(Vihma 2009). One of the many reasons that explain the negative relation between weather condition and marathon performance is that the body's ability to release heat is reduced in hot environments, which can lead to heat stress and reduce the body's ability to perform at its best. Aging further compromises thermoregulation and heat tolerance (Kenney and Munce 2003), but it remains unclear whether this translates directly to decreased running performance in hot environments and whether the effects of aging differ between sexes.

This report aim to examine effects of increasing age on marathon performance in men and women by using percentage off record as the measurement metrics, explore the impact of environmental conditions on marathon performance, and whether the impact differs across age and gender, identify the weather parameters (WBGT, Flag conditions, temperature, etc) that have the largest impact on marathon performance and evaluate the impact of air quality on marathon performance. The analysis is carried out in R (version 4.4.0) using `ggplot2`, `dplyr`, `lubridate`, `kableExtra`, `gtsummary`, `stringr`, `ggpubr`, `RColorBrewer`, `gridExtra` and `latex2exp` packages.

Data collection and preprocessing

Data are provided by Dr. Brett Romano Ely and Dr. Matthew Ely from the Department of Health Sciences at Providence College. The data set contains 3 separate file that contains the marathon performance of each year of age across male and female in different races, course record of races and air quality index (AQI) values of the marathon location in the given years. The marathon performance file contains 11564 records with 14 variables. Each row represent the fastest finishing time among men or women at a year of age, compared with the percentage off course record (%CR) among Boston, Chicago, New York, Twin Cities, Grandma's Marathons for 17 to 24 years, 1993-2016, and the corresponding weather conditions.

The participants are range from age 14 to 91 for men, and 14 to 88 for women. The distribution of the weather conditions (represented by `Flag`, a variable that indicates the wet bulb globe temperature(WBGT)) is shown in Table 1. WBGT is the Weighted average of dry bulb, wet bulb, and globe temperature (measured in celsius), which measure the heat stress considering temperature, humidity and solar radiation. Therefore, `Flag` is a reasonable proxy for the weather conditions of marathons, with `White` indicating WBGT is lower than 10 degrees, `Green` indicating WBGT is between 10 and 18 degrees, `Yellow` indicating WBGT is between 18 and 23 degrees, and `Red` indicating WBGT is between 20 and 28 degrees, and `Black` indicating WBGT is higher than 28 degrees. Table 1 shows that the distribution of weather condition is not balanced, with more than 40% of records are in `Green` flag and only 5% of records are in `Red` flag. No races were held in `Black` flag condition. There are 491 records (4%) missing the `Flag` information, as long as other weather conditions, which is because the race was canceled due to weather conditions. However, these records still contains the information of the fastest finishing time. The details of the races with missing weather conditions are: Chicago Marathon, New York City Marathon, Twin Cities Marathon in 2011 and Grandma's Marathon in 2012. Excluding those records from our analysis may bring bias as it's anticipated that the weather conditions may have an impact on the marathon performance. However, considering the relative small portion of missingness, we will exclude them from the analysis.

Table 1: Summary of Flag variable in the dataset

Flag	Count	Percentage (%)
	491	4.25
Green	4706	40.70
Red	592	5.12
White	3753	32.45
Yellow	2022	17.49

The data set also include a separate file contains the course record of the marathon in the given years, but with different coding for the races and sex. We first unified the coding system of the two files by converting the coding of the course record file to the same as the marathon

performance file. We then merged the two files by the race, year and sex. Another file in the data set contains the air quality index (AQI) values with different sampling duration and measured units of the marathon location in the given years. The inspection of the data shows that the AQI values are missing for sampling duration: “1 HOUR”. Since the both 1 hour duration and 8 hour duration shares the same measuring unit: “Parts per million”, and there are no missing values for 8 hour duration, it was assumed that the missing value of 1 hour duration can be ignored and the information of the 8 hour duration can be used to represent the air quality of the marathon location. Therefore, we will only use AQI records measured in 8 hours duration from the analysis.

Examine effects of increasing age on marathon performance in men and women

It is proposed that aging will have a negative impact on marathon performance as older individuals will have reduced ability to tolerate heat stress. However, whether this assumption translate to decreased running performance in hot environments and does the effect of aging differ between men and women remains unknown. We compared the fastest finish time against age between men and women. Since different races may take different time to finish, we compared the performance among different races across different years by calculating smoothed conditional means. Our result (Figure 1) shows that both men and women have a U-shaped relationship between age and fastest finish time, with women have a higher finish time compare to men across all ages. The fastest finish time first drop as age increase until 23 - 33 years old, then increase as age increase, for both men and women. The detail about peak performance are summarized in Table 2. It need to be noticed that the slope of the curve changed after 52 years old, with the fastest finish time increase faster as age increase. The slope of the curve is roughly the same between men and women before 75 years old, but the slope varies among different races after 75 years old. The result indicates that aging have a negative impact on marathon performance, with the impact is more significant after 52 years old. Eventhough the fastest finish time drop as age increase until roughly 28 years old, considering the fact that body function is not going to drop at such a young age, this may only due to the fact that young runner may not have enough experience to run a marathon.

Table 2: Summary of the peak performance of marathon runners

Sex	Marathon	Minimum finish time (Hr)	Age
Female	Boston Marathon	2.32	33
Female	Chicago Marathon	2.29	28
Female	Grandma’s Marathon	2.44	23
Female	New York City Marathon	2.38	27
Female	Twin Cities Marathon	2.45	36
Male	Boston Marathon	2.05	29
Male	Chicago Marathon	2.06	29

Male	Grandma's Marathon	2.15	26
Male	New York City Marathon	2.13	25
Male	Twin Cities Marathon	2.15	28

The result also suggest that the effect of aging on marathon performance is consistent between gender until 75 years old. But the effect after age 75 varies across races. The effect decrease after 75 years old for both gender in New York City Marathon, and stayed the same for Chicago Marathon. While in Boston Marathon, the effect only decrease among women, and in Twin Cities Marathon, only among men. In Grandma's Marathon, the effect decrease for men and first decrease, then increase among women.

Explore the impact of environmental conditions on marathon performance, and whether the impact differs across age and gender.

In order to examine the effect of environmental conditions on marathon performance, we first define what should be the variable to represent the marathon performance. The fastest finish time can serve as a good proxy for marathon performance, but as described earlier and shown in Figure 1, the fastest finish time differs among different races. To make the comparison fair, we will utilize the percentage off record, $\%CR$ to represent the marathon performance as the difference of $\%CR$ should remain the same among different races condition on all other factors remain the same. We compare the smoothed conditional means of $\%CR$ against age among different weather conditions. The result (Figure 2) shows similar pattern as the fastest finish time, with the $\%CR$ first drop as age increase until 26 years old, then increase as age increase. The smoothed conditional means is roughly the same among different weather conditions, until 75 years old, where slope of the mean start to decrease while the others remain the same. But this can not guarantee that the effect of aging start to be less effective when the weather temperature is high as there are only little data points collected for the senior persons (represented by the scatter dots). A slightly bigger difference among different weather conditions can be observed among runner age between 52 and 75 years old, but in general, the effect of weather conditions on marathon performance is not significant.

It can be shown that among the times that the record is broken, the percentage of **Green** flag is higher than the percentage of **Green** flag in the data by more than 10 percentage points and the percentage of **Yellow** flag is lower than the percentage of **Yellow** flag in the data by more than 10 percentage points too.

Since we have already described the relationship between age and marathon performance that in general, marathon performance decrease as age increase. Defining a new way to represent marathon performance, which will show no difference among age is crucial so that we can compare the effect of weather conditions on marathon performance. We will use

$$\frac{\%CR - E[\%CR|Age, Sex]}{E[\%CR|Age, Sex]}$$

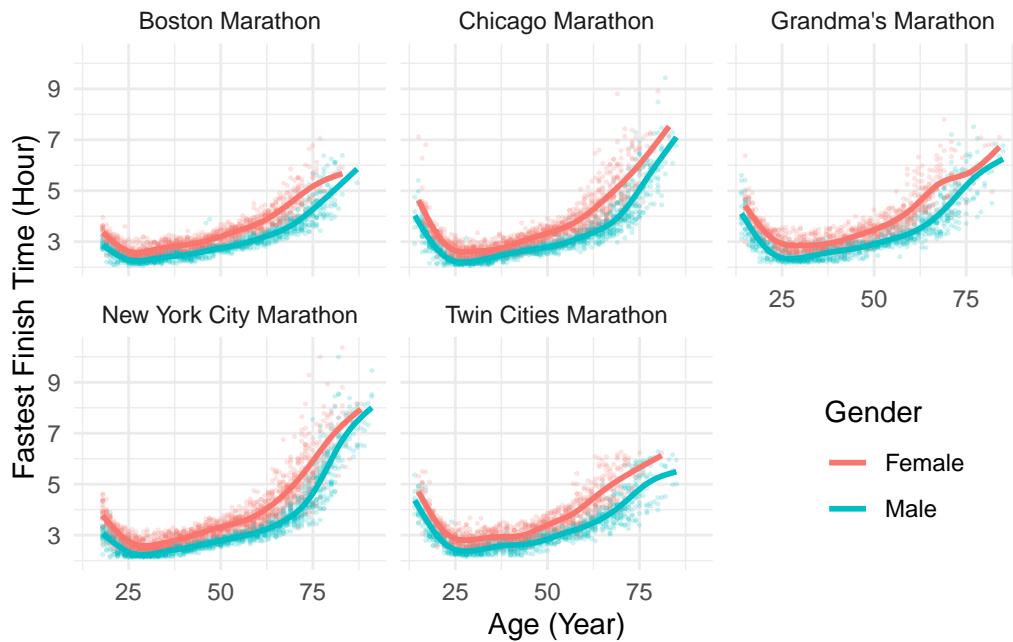


Figure 1: Scatter plot of marathon performance against age among different races

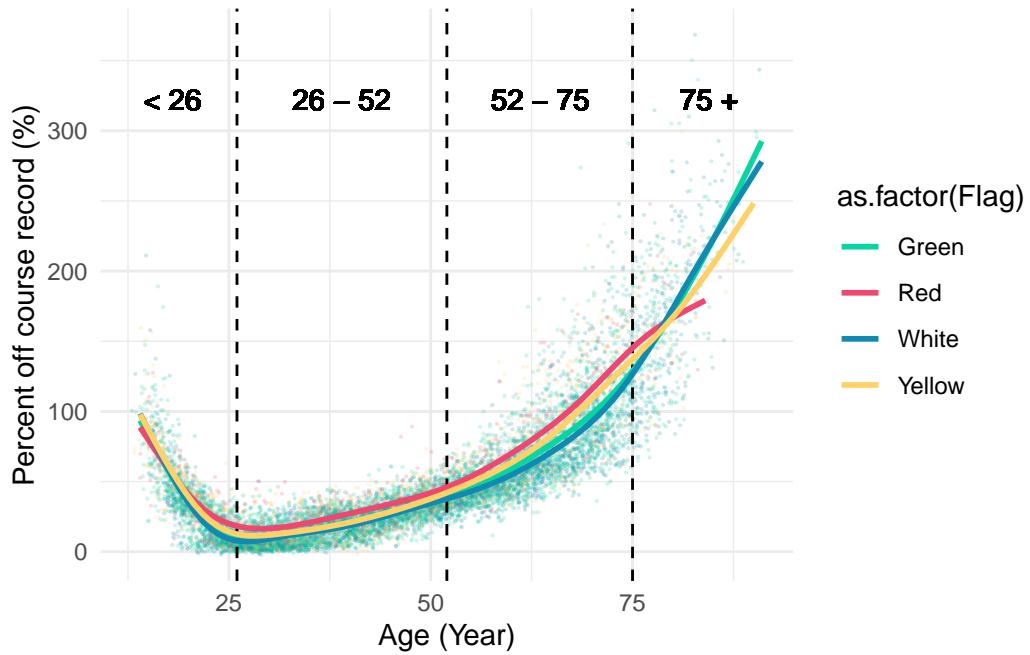


Figure 2: Scatter plot of marathon performance against age among different weather conditions

the normalized difference between the $\%CR$ and the expectation of $\%CR$ given the age, to represent the marathon performance of each rows, where $E[\%CR|Age, Sex]$ is the expectation of $\%CR$ given the age and sex. This new variable is the percentage of $\%CR$ that is off the expectation of $\%CR$ given the age, and under the assumption that weather condition has no effect on $\%CR$, then:

$$E\left[\frac{\%CR - E[\%CR|Age, Sex]}{E[\%CR|Age, Sex]}\right] = 0$$

The expectation of the new metric will be 0 across all ages and sex under this assumption. There for, this metric can exclude the effect of aging and sex on marathon performance and only focus on the effect of weather conditions on marathon performance. A natural way to estimate $E[\%CR|Age, Sex]$ is by calculating the means, stratified by age. However, as shown in Table 1, the distribution of weather conditions is not balanced. If the assumption that weather do have effect on marathon performance is true, then the arithmetic mean will be biased. To address this issue, we will use the weighted mean to estimate $E[\%CR|Age, Sex]$, where the weight is the proportion of each weather condition in the data set. With this new variable, we can compare the marathon performance among different weather conditions, and examine whether the impact of weather conditions on marathon performance differs across age and sex. In Figure 3, we separate the records into 2 groups, below average marathon performance and above average marathon performance, corresponding to whether the normalized difference is below or above 0. We also compare the difference of using weighted mean and arithmetic mean to estimate $E[\%CR|Age]$. The result shows that the temperature of 4 different measurements are all higher in those records with above average marathon performance. It also shows that there is little difference between using weighted mean and arithmetic mean to estimate $E[\%CR|Age, Sex]$. Nonetheless, we still adopt weighted mean to estimate $E[\%CR|Age]$ because it can avoid bias by theory.

Table 3 shows that the mean of all weather conditions are significantly different between above and below average marathon performance records, except for the Percent relative humidity. The average of temperature, solar radiation and dew point are all higher in the records with above average marathon performance, while the average of wind speed is lower in the records with above average marathon performance. The result indicates that the weather conditions do have an impact on marathon performance, with higher temperature, solar radiation and dew point and lower wind speed are associated with better marathon performance.

Table 3: Siginificant test of the difference of the average weather conditions between above and below average marathon performance records

Characteristic	Above average N = 5,386¹	Below average N = 5,687¹	p-value²
Flag			<0.001
White	1,552 (29%)	2,201 (39%)	
Green	2,263 (42%)	2,443 (43%)	

Yellow	1,162 (22%)	860 (15%)	
Red	409 (7.6%)	183 (3.2%)	
Td..C	14.2 (9.0, 19.3)	12.0 (8.3, 15.7)	<0.001
Tw..C	10.0 (5.7, 14.3)	8.2 (5.2, 12.9)	<0.001
Tg..C	26 (20, 31)	23 (19, 29)	<0.001
WBGT	13.4 (9.1, 18.2)	11.9 (7.6, 15.8)	<0.001
X.rh	53 (1, 64)	52 (1, 64)	0.5
SR.W.m2	513 (390, 627)	513 (354, 602)	<0.001
DP	7 (2, 12)	4 (0, 10)	<0.001
Wind	9.8 (7.0, 11.7)	10.0 (7.6, 12.2)	<0.001

¹n (%); Median (Q1, Q3)

²Pearson's Chi-squared test; Wilcoxon rank sum test

To determine whether the effect of weather conditions on marathon performance differs across age and sex, we stratify the records by `flag` to represent for different weather conditions. As shown in Figure 4, runner are more likely to have bad performance (positive normalized difference) when WBGT is higher than 23 degrees (Red flag), especially for runner between 20 to 30 years old, where the normalized difference reaches it's peak to 0.5 (50% worse than average performance). After 30 years old, the normalized difference decrease as age increase, and Female runnner experienced a faster decrease than male runner, indicating that the effect of weather conditions on marathon performance is weaker in female runners than male runner after 30 years old. The result also shows that runners performance is roughly the same as the average performance when WBGT is between 10-18 degrees (Green flag). The performance ise slightly worse when WBGT is between 18-23 degrees (Yellow flag) and better when WBGT is lower than 10 degrees (White flag).

By stratifying the records by age group, we can see that the effect of weather conditions on marathon performance is more significant among older runners. The age group is defined as < 26, 26–52, 52–75, 75 +. The groups are selected by different slopes based on Figure 2. The result (Figure 5) shows a similar result with Figure 4, with the effect of weather conditions on marathon performance is more significant among runners between 26 and 52 years old, male runners experience a stronger effect by weather conditions and the effect is weaker among older runners.

Identify the weather parameters (WBGT, Flag conditions, temperature, etc) that have the largest impact on marathon performance.

To determine the largest impact on marathon performance, we calculated the correlation between the normalized difference and the significant weather parameters identified in Table 3. The results (Figure 6) show that temperature-related variables (e.g., Dew Point, Dry Bulb, Wet Bulb) exhibit similar patterns. The correlation increases until around age 60 and then

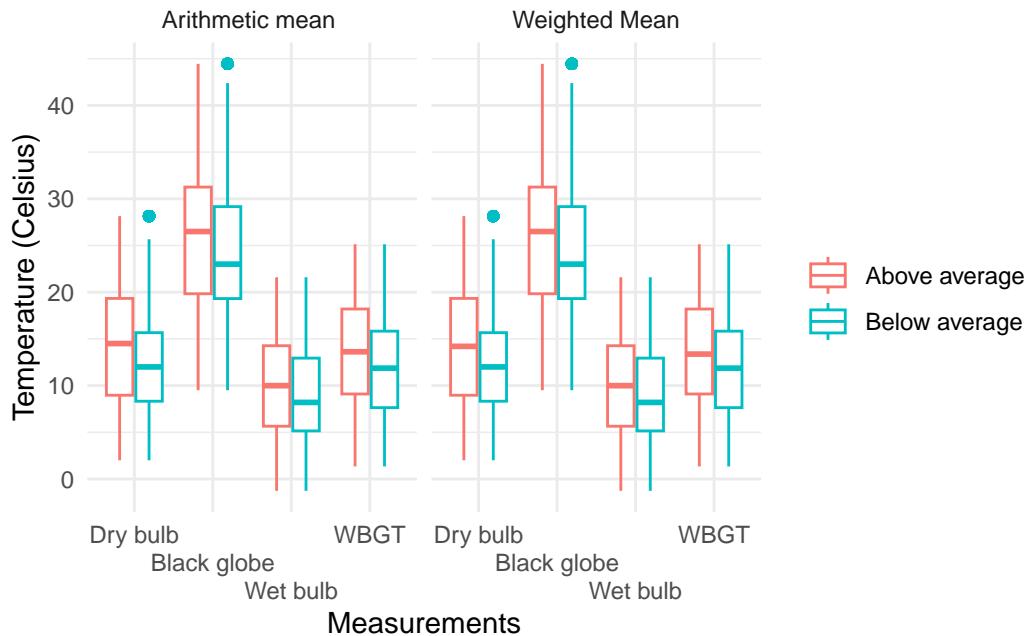


Figure 3: Boxplot of temperatures measured in different equipment between above and below average marathon performance records.

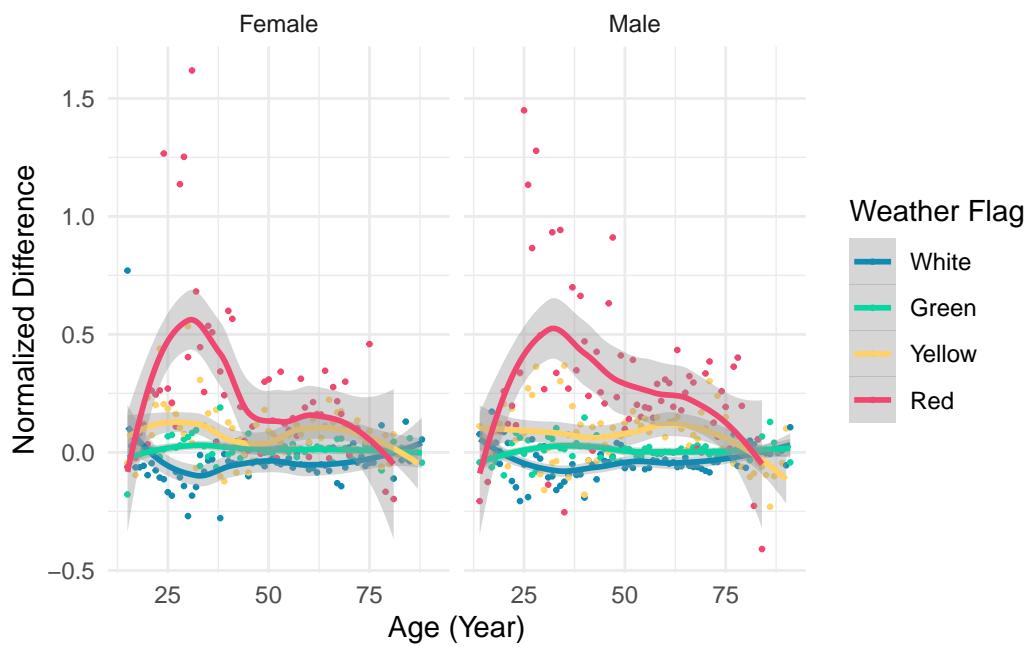


Figure 4: Scatter plot of normalized difference against age among different weather conditions

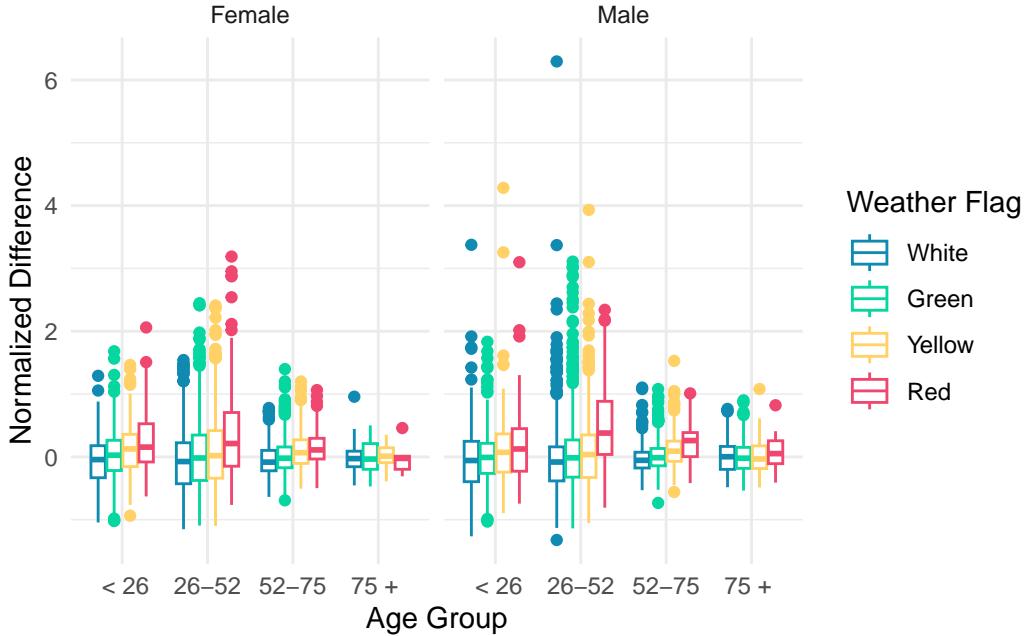


Figure 5: Boxplot of normalized difference against age group among different weather conditions

begins to decrease. In contrast, wind shows the opposite trend, with the correlation decreasing until around age 60 before increasing. Solar radiation has the lowest correlation among all weather parameters, remaining relatively constant across all ages. These correlations measure the strength of the linear relationship between weather parameters and marathon performance, where a positive correlation indicates that an increase in the weather parameter is associated with worse performance (higher normalized difference) and vice versa. The magnitude of the correlation reflects the potential impact of the weather parameter on marathon performance. The results suggest that temperature, adjusted or unadjusted by other conditions, has the most significant effect, and older runners are more likely to be affected by weather conditions than younger runners.

The age-stratified results (Figure 7) reveal a similar pattern but highlight increased variance among runners over 75 years old. This suggests that the observed decreasing effect of weather conditions on older runners, shown in Figure 6, may be unreliable due to higher variability in this age group.

In the previous sections, we analyzed weather effects primarily through WBGT flags. To evaluate whether WBGT flags accurately represent weather conditions, we fit three linear models: a full model that included all weather parameters and their interactions (after applying AIC-based stepwise selection), a WBGT-only model, and a flag-only model. The full model demonstrated the best fit, achieving the lowest MSE (Table 4). However, the WBGT and flag

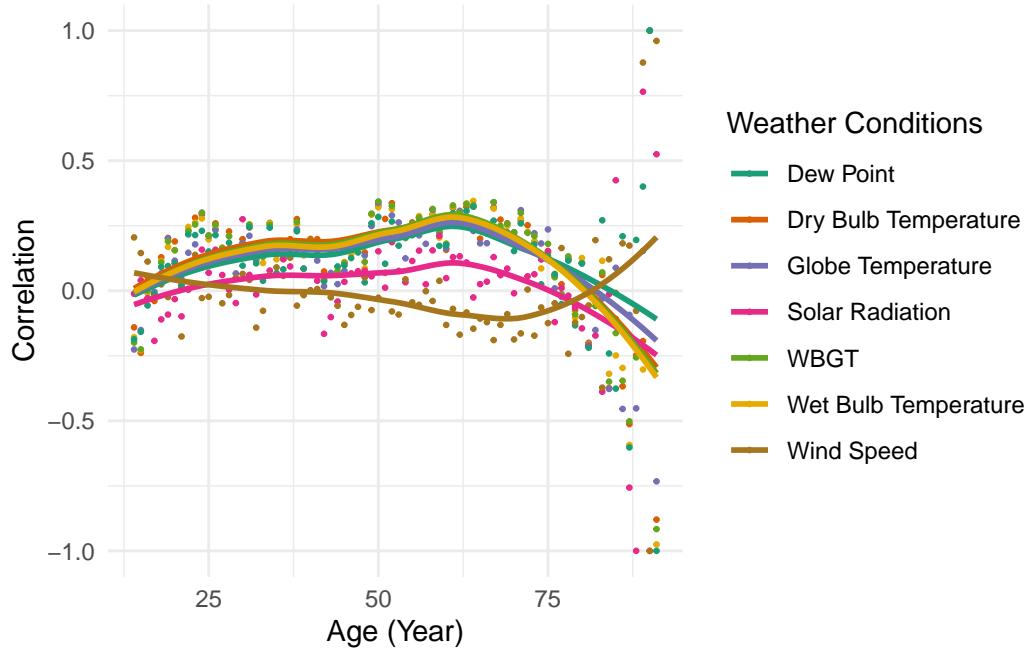


Figure 6: Scatter plot of correlation between weather parameters and normalized difference against age

models showed only slightly higher MSEs, suggesting that both can still effectively capture the impact of weather on marathon performance. Since WBGT itself is a combination of various temperature measurements—already shown to be highly correlated with marathon performance—we can conclude that using the flag to represent weather conditions is a practical and effective choice.

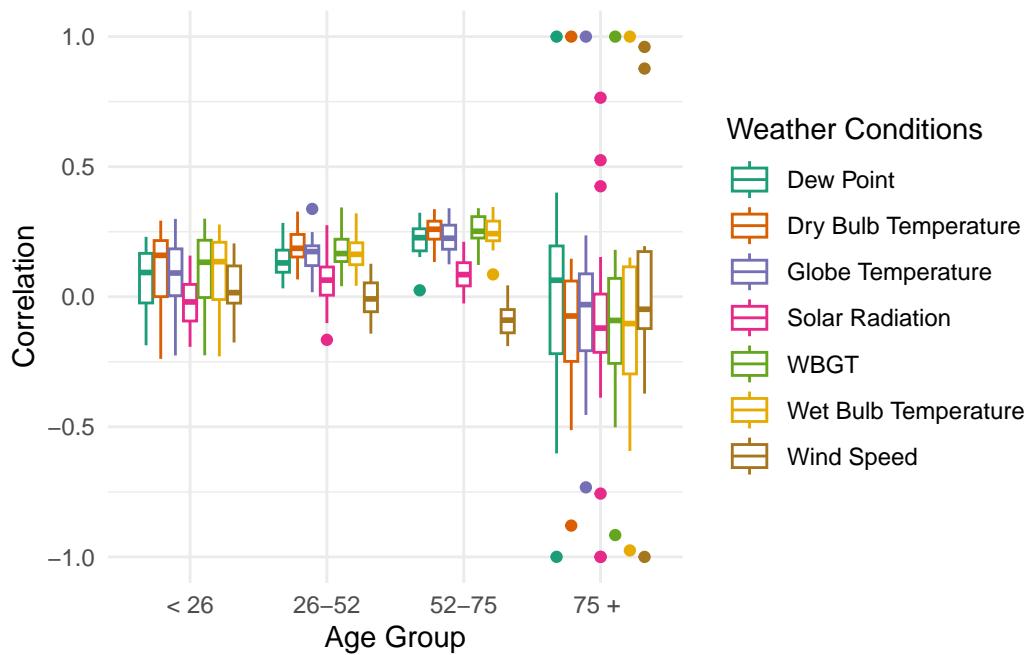
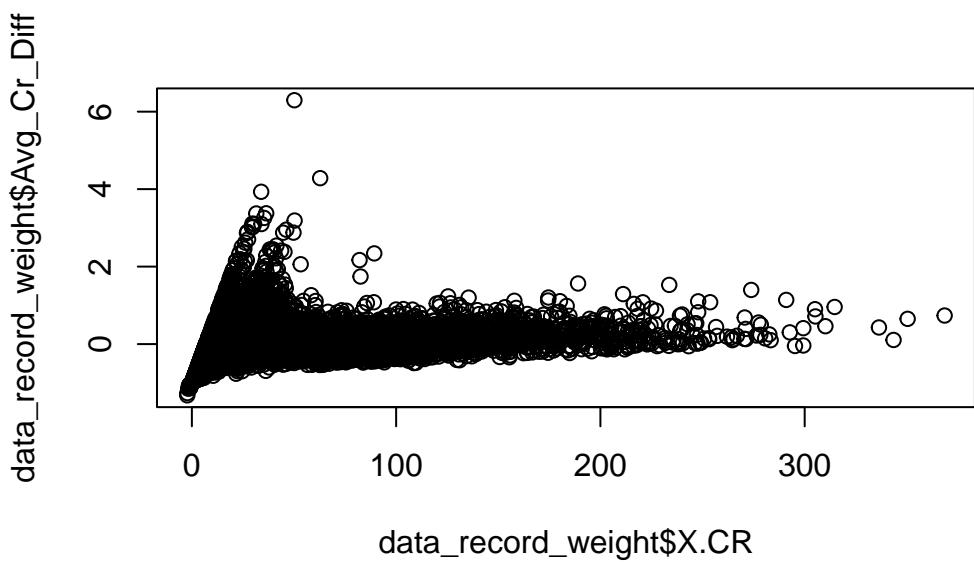
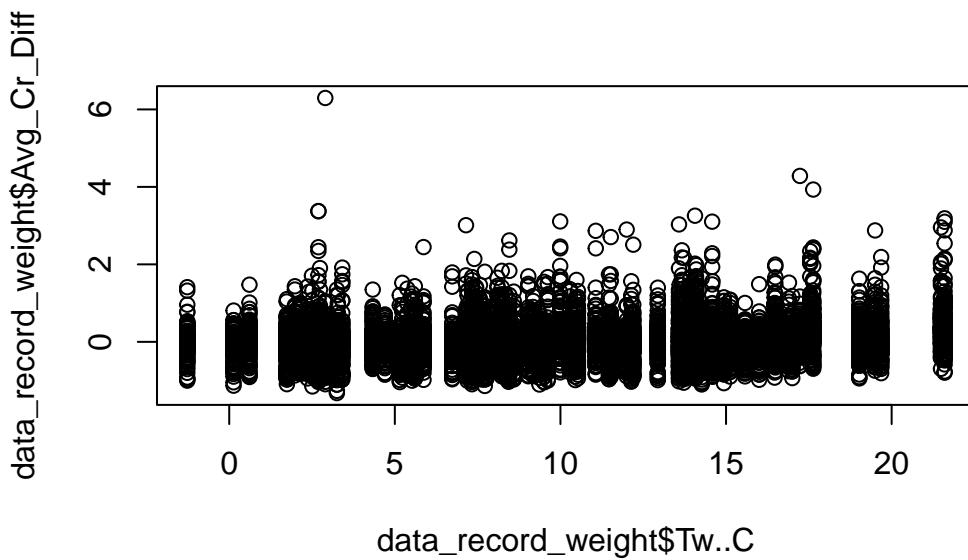
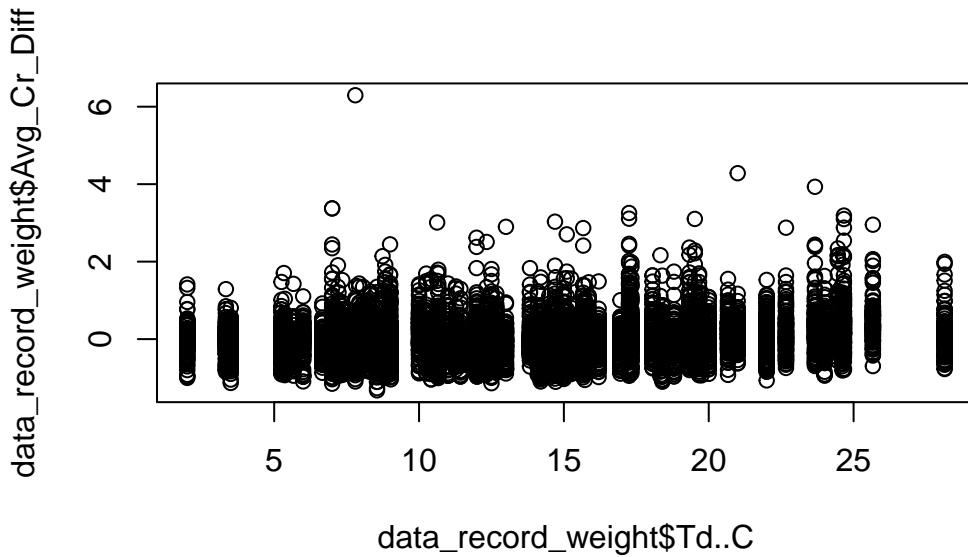
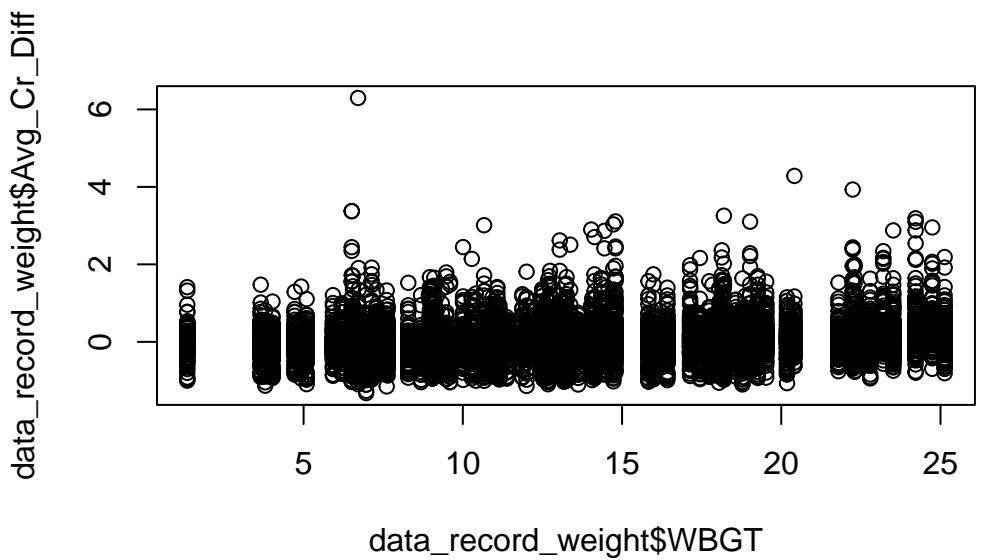
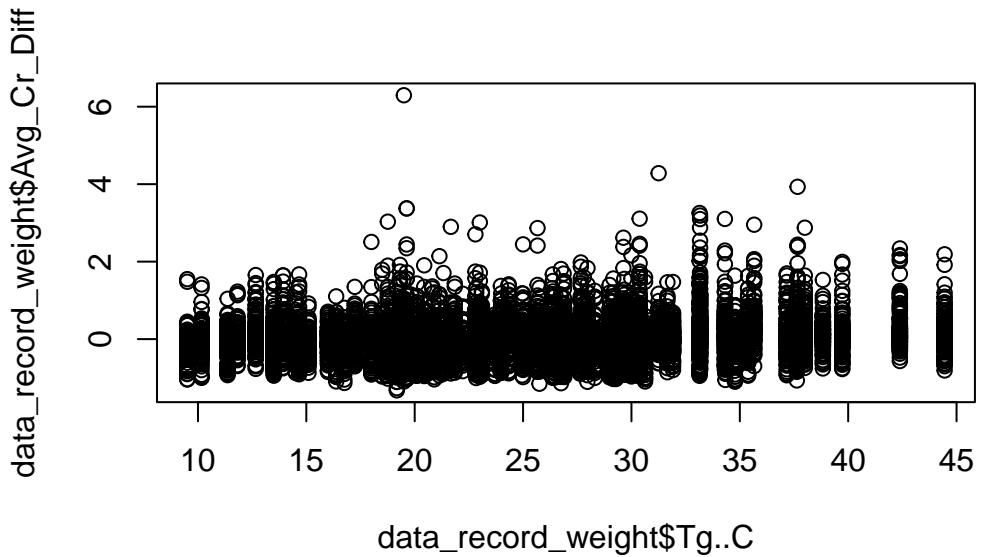
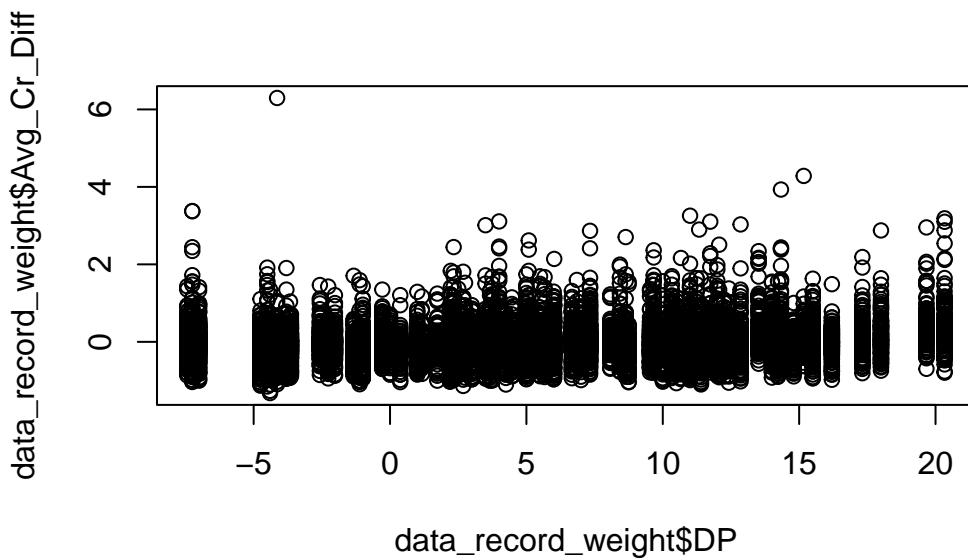
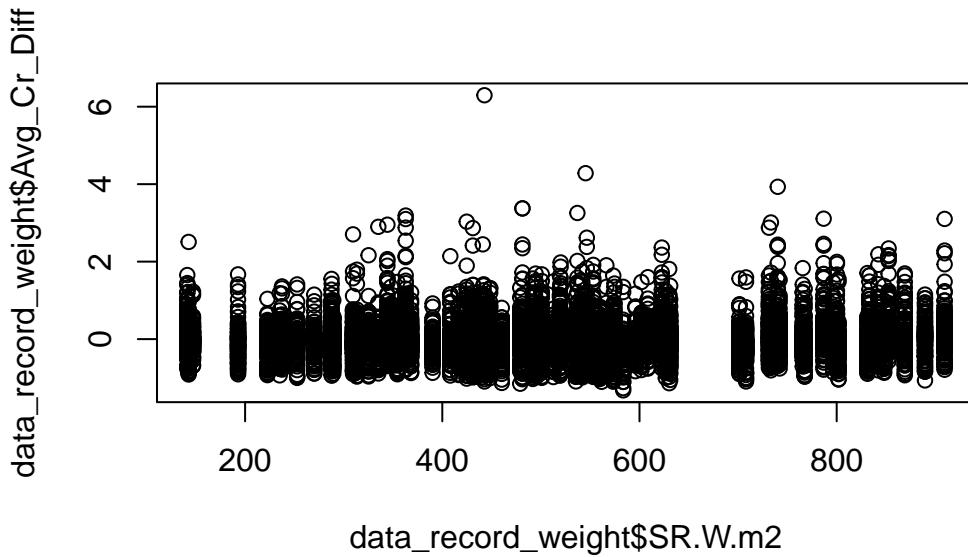


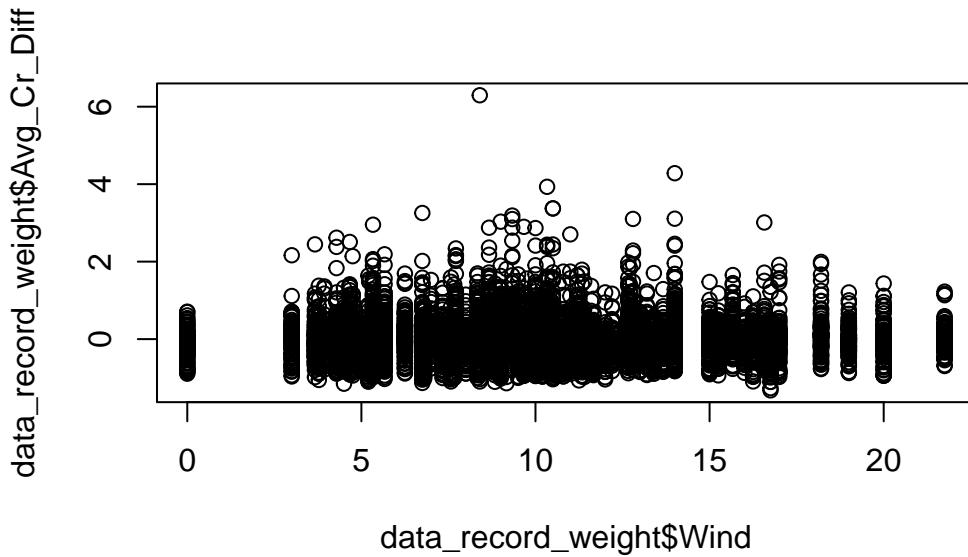
Figure 7: Boxplot of correlation between weather parameters and normalized difference against age group











Start: AIC=-17518.97
 $\text{Avg_Cr_Diff} \sim \text{Td..C} + \text{Tw..C} + \text{Tg..C} + \text{SR.W.m2} + \text{DP} + \text{Wind}$

	Df	Sum of Sq	RSS	AIC
+ Td..C:DP	1	16.5011	2256.5	-17598
+ Td..C:Tw..C	1	15.1174	2257.9	-17591
+ Tw..C:DP	1	11.5893	2261.4	-17574
+ Tg..C:DP	1	8.4945	2264.5	-17558
+ Tw..C:Tg..C	1	8.0248	2265.0	-17556
+ Td..C:Tg..C	1	6.6119	2266.4	-17549
+ SR.W.m2:DP	1	3.1207	2269.9	-17532
+ Tw..C:SR.W.m2	1	2.7830	2270.2	-17530
+ Td..C:SR.W.m2	1	2.5360	2270.5	-17529
+ Tg..C:Wind	1	0.8442	2272.2	-17521
- Td..C	1	0.0035	2273.0	-17521
- Tg..C	1	0.3099	2273.3	-17520
+ Tg..C:SR.W.m2	1	0.4681	2272.6	-17519
+ Td..C:Wind	1	0.4466	2272.6	-17519
<none>		2273.0		-17519
- Wind	1	0.5109	2273.5	-17518
- SR.W.m2	1	0.7060	2273.7	-17518
+ DP:Wind	1	0.0969	2272.9	-17517
+ SR.W.m2:Wind	1	0.0388	2273.0	-17517

+ Tw..C:Wind	1	0.0312	2273.0	-17517
- Tw..C	1	1.3493	2274.4	-17514
- DP	1	1.6003	2274.6	-17513

Step: AIC=-17597.64

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP

	Df	Sum of Sq	RSS	AIC
+ Tw..C:DP	1	6.4865	2250.0	-17628
+ Tg..C:DP	1	2.2270	2254.3	-17607
+ Tw..C:Tg..C	1	1.6795	2254.8	-17604
+ DP:Wind	1	0.7303	2255.8	-17599
+ Td..C:SR.W.m2	1	0.7054	2255.8	-17599
- Tg..C	1	0.1915	2256.7	-17599
- SR.W.m2	1	0.1939	2256.7	-17599
- Tw..C	1	0.1945	2256.7	-17599
+ Td..C:Tg..C	1	0.4964	2256.0	-17598
<none>		2256.5		-17598
- Wind	1	0.4248	2256.9	-17598
+ Tw..C:Wind	1	0.2684	2256.3	-17597
+ Tw..C:SR.W.m2	1	0.2496	2256.3	-17597
+ SR.W.m2:Wind	1	0.0855	2256.4	-17596
+ Tg..C:Wind	1	0.0842	2256.4	-17596
+ SR.W.m2:DP	1	0.0586	2256.5	-17596
+ Td..C:Tw..C	1	0.0417	2256.5	-17596
+ Td..C:Wind	1	0.0141	2256.5	-17596
+ Tg..C:SR.W.m2	1	0.0045	2256.5	-17596
- Td..C:DP	1	16.5011	2273.0	-17519

Step: AIC=-17627.52

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP + Tw..C:DP

	Df	Sum of Sq	RSS	AIC
+ Tg..C:DP	1	3.6402	2246.4	-17643
+ Tw..C:Tg..C	1	3.6084	2246.4	-17643
+ Td..C:Tg..C	1	1.8569	2248.2	-17635
- Tg..C	1	0.0027	2250.0	-17630
+ Td..C:Tw..C	1	0.8001	2249.2	-17630
- SR.W.m2	1	0.1426	2250.2	-17629
+ DP:Wind	1	0.4573	2249.6	-17628
<none>		2250.0		-17628
- Wind	1	0.4955	2250.5	-17627

+ SR.W.m2:DP	1	0.3131	2249.7	-17627
+ SR.W.m2:Wind	1	0.2889	2249.8	-17627
+ Tw..C:Wind	1	0.2016	2249.8	-17626
+ Td..C:SR.W.m2	1	0.1848	2249.8	-17626
+ Tg..C:SR.W.m2	1	0.0475	2250.0	-17626
+ Tg..C:Wind	1	0.0469	2250.0	-17626
+ Td..C:Wind	1	0.0211	2250.0	-17626
+ Tw..C:SR.W.m2	1	0.0100	2250.0	-17626
- Tw..C:DP	1	6.4865	2256.5	-17598
- Td..C:DP	1	11.3983	2261.4	-17574

Step: AIC=-17643.45

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
Tw..C:DP + Tg..C:DP

	Df	Sum of Sq	RSS	AIC
+ Td..C:SR.W.m2	1	2.8326	2243.6	-17655
+ Tw..C:SR.W.m2	1	2.4416	2244.0	-17654
+ SR.W.m2:DP	1	1.3794	2245.0	-17648
+ Td..C:Tw..C	1	1.3698	2245.0	-17648
+ Tg..C:SR.W.m2	1	0.6061	2245.8	-17644
+ Tg..C:Wind	1	0.5568	2245.8	-17644
<none>		2246.4		-17643
- SR.W.m2	1	0.4149	2246.8	-17643
+ Tw..C:Tg..C	1	0.3003	2246.1	-17643
+ Td..C:Wind	1	0.2910	2246.1	-17643
+ Tw..C:Wind	1	0.1873	2246.2	-17642
+ Td..C:Tg..C	1	0.1571	2246.2	-17642
+ DP:Wind	1	0.0627	2246.3	-17642
+ SR.W.m2:Wind	1	0.0345	2246.4	-17642
- Wind	1	1.2358	2247.6	-17639
- Tg..C:DP	1	3.6402	2250.0	-17628
- Tw..C:DP	1	7.8997	2254.3	-17607
- Td..C:DP	1	15.0369	2261.4	-17572

Step: AIC=-17655.42

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2

	Df	Sum of Sq	RSS	AIC
+ Td..C:Tw..C	1	3.9187	2239.7	-17673
+ Tw..C:Tg..C	1	3.0510	2240.5	-17668
+ Td..C:Tg..C	1	2.9901	2240.6	-17668

+ Tw..C:Wind	1	2.3183	2241.2	-17665
+ Td..C:Wind	1	1.9319	2241.6	-17663
+ DP:Wind	1	1.9128	2241.7	-17663
+ Tg..C:SR.W.m2	1	1.7237	2241.8	-17662
+ Tg..C:Wind	1	0.8772	2242.7	-17658
<none>			2243.6	-17655
+ SR.W.m2:Wind	1	0.2153	2243.3	-17654
+ Tw..C:SR.W.m2	1	0.0003	2243.6	-17653
+ SR.W.m2:DP	1	0.0000	2243.6	-17653
- Wind	1	1.6254	2245.2	-17649
- Td..C:SR.W.m2	1	2.8326	2246.4	-17643
- Tg..C:DP	1	6.2881	2249.8	-17626
- Tw..C:DP	1	6.9440	2250.5	-17623
- Td..C:DP	1	16.2251	2259.8	-17578

Step: AIC=-17672.78

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
 Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2 + Td..C:Tw..C

	Df	Sum of Sq	RSS	AIC
+ DP:Wind	1	2.8965	2236.8	-17685
+ Tw..C:Wind	1	2.5768	2237.1	-17684
+ Td..C:Tw..C:DP	1	1.7250	2237.9	-17679
+ Tg..C:SR.W.m2	1	1.6210	2238.0	-17679
+ SR.W.m2:DP	1	1.2311	2238.4	-17677
+ Td..C:Wind	1	1.2192	2238.4	-17677
+ Tw..C:SR.W.m2	1	1.0519	2238.6	-17676
+ SR.W.m2:Wind	1	0.5998	2239.1	-17674
<none>		2239.7		-17673
+ Tg..C:Wind	1	0.2555	2239.4	-17672
+ Td..C:Tg..C	1	0.0209	2239.6	-17671
+ Tw..C:Tg..C	1	0.0080	2239.6	-17671
- Wind	1	3.0667	2242.7	-17660
- Td..C:Tw..C	1	3.9187	2243.6	-17655
- Td..C:SR.W.m2	1	5.3815	2245.0	-17648
- Tg..C:DP	1	9.1292	2248.8	-17630
- Tw..C:DP	1	9.3760	2249.0	-17628
- Td..C:DP	1	16.7275	2256.4	-17592

Step: AIC=-17685.11

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
 Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2 + Td..C:Tw..C + DP:Wind

	Df	Sum of Sq	RSS	AIC
+ Tg..C:SR.W.m2	1	1.9139	2234.8	-17693
+ Td..C:Tw..C:DP	1	1.1594	2235.6	-17689
<none>			2236.8	-17685
+ SR.W.m2:Wind	1	0.3132	2236.4	-17685
+ Td..C:Tg..C	1	0.2010	2236.6	-17684
+ Tg..C:Wind	1	0.1149	2236.6	-17684
+ Tw..C:Tg..C	1	0.0550	2236.7	-17683
+ Tw..C:Wind	1	0.0267	2236.7	-17683
+ SR.W.m2:DP	1	0.0194	2236.7	-17683
+ Td..C:Wind	1	0.0046	2236.8	-17683
+ Tw..C:SR.W.m2	1	0.0020	2236.8	-17683
- DP:Wind	1	2.8965	2239.7	-17673
- Td..C:Tw..C	1	4.9023	2241.7	-17663
- Td..C:SR.W.m2	1	8.2579	2245.0	-17646
- Tw..C:DP	1	10.8869	2247.6	-17633
- Tg..C:DP	1	11.4848	2248.2	-17630
- Td..C:DP	1	19.6163	2256.4	-17590

Step: AIC=-17692.59

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP + Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2 + Td..C:Tw..C + DP:Wind + Tg..C:SR.W.m2

	Df	Sum of Sq	RSS	AIC
+ Td..C:Tw..C:DP	1	1.5328	2233.3	-17698
+ SR.W.m2:DP	1	1.1809	2233.7	-17696
+ Tw..C:SR.W.m2	1	0.8925	2233.9	-17695
<none>			2234.8	-17693
+ Tw..C:Wind	1	0.3613	2234.5	-17692
+ Tw..C:Tg..C	1	0.3010	2234.5	-17692
+ Td..C:Wind	1	0.2656	2234.6	-17692
+ Td..C:Tg..C	1	0.1142	2234.7	-17691
+ SR.W.m2:Wind	1	0.0951	2234.7	-17691
+ Tg..C:Wind	1	0.0471	2234.8	-17691
- Tg..C:SR.W.m2	1	1.9139	2236.8	-17685
- DP:Wind	1	3.1894	2238.0	-17679
- Td..C:Tw..C	1	4.8381	2239.7	-17671
- Td..C:SR.W.m2	1	8.0283	2242.9	-17655
- Tw..C:DP	1	9.0036	2243.8	-17650
- Tg..C:DP	1	11.7493	2246.6	-17636
- Td..C:DP	1	18.3884	2253.2	-17604

Step: AIC=-17698.18

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2 + Td..C:Tw..C + DP:Wind +
Tg..C:SR.W.m2 + Td..C:Tw..C:DP

	Df	Sum of Sq	RSS	AIC
+ SR.W.m2:DP	1	1.4003	2231.9	-17703
+ Tw..C:SR.W.m2	1	1.3609	2231.9	-17703
<none>			2233.3	-17698
+ SR.W.m2:Wind	1	0.3541	2232.9	-17698
+ Tg..C:Wind	1	0.3214	2233.0	-17698
+ Td..C:Tg..C	1	0.1232	2233.2	-17697
+ Tw..C:Tg..C	1	0.0967	2233.2	-17697
+ Tw..C:Wind	1	0.0799	2233.2	-17697
+ Td..C:Wind	1	0.0362	2233.3	-17696
- Td..C:Tw..C:DP	1	1.5328	2234.8	-17693
- Tg..C:SR.W.m2	1	2.2874	2235.6	-17689
- DP:Wind	1	2.5459	2235.8	-17688
- Td..C:SR.W.m2	1	9.0926	2242.4	-17655
- Tg..C:DP	1	10.8992	2244.2	-17646

Step: AIC=-17703.13

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2 + Td..C:Tw..C + DP:Wind +
Tg..C:SR.W.m2 + SR.W.m2:DP + Td..C:Tw..C:DP

	Df	Sum of Sq	RSS	AIC
+ Td..C:SR.W.m2:DP	1	6.8935	2225.0	-17735
+ Tg..C:SR.W.m2:DP	1	6.3537	2225.6	-17733
- DP:Wind	1	0.2243	2232.1	-17704
<none>			2231.9	-17703
+ Tg..C:Wind	1	0.1598	2231.7	-17702
+ SR.W.m2:Wind	1	0.1376	2231.8	-17702
+ Tw..C:Wind	1	0.1208	2231.8	-17702
+ Td..C:Wind	1	0.0630	2231.8	-17701
+ Tw..C:SR.W.m2	1	0.0185	2231.9	-17701
+ Td..C:Tg..C	1	0.0129	2231.9	-17701
+ Tw..C:Tg..C	1	0.0081	2231.9	-17701
- Tg..C:DP	1	1.3860	2233.3	-17698
- SR.W.m2:DP	1	1.4003	2233.3	-17698
- Td..C:Tw..C:DP	1	1.7522	2233.7	-17696
- Tg..C:SR.W.m2	1	3.6680	2235.6	-17687
- Td..C:SR.W.m2	1	8.1911	2240.1	-17665

Step: AIC=-17735.38

Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind + Td..C:DP +
 Tw..C:DP + Tg..C:DP + Td..C:SR.W.m2 + Td..C:Tw..C + DP:Wind +
 Tg..C:SR.W.m2 + SR.W.m2:DP + Td..C:Tw..C:DP + Td..C:SR.W.m2:DP

	Df	Sum of Sq	RSS	AIC
<none>			2225.0	-17735
+ Td..C:Tg..C	1	0.2909	2224.7	-17735
+ Tg..C:Wind	1	0.1344	2224.9	-17734
+ Tw..C:Wind	1	0.0934	2224.9	-17734
+ Tg..C:SR.W.m2:DP	1	0.0930	2224.9	-17734
+ Tw..C:Tg..C	1	0.0895	2224.9	-17734
+ SR.W.m2:Wind	1	0.0810	2224.9	-17734
+ Td..C:Wind	1	0.0608	2224.9	-17734
+ Tw..C:SR.W.m2	1	0.0152	2225.0	-17734
- DP:Wind	1	1.0460	2226.1	-17732
- Tg..C:DP	1	2.4588	2227.5	-17725
- Tg..C:SR.W.m2	1	2.7509	2227.8	-17724
- Td..C:Tw..C:DP	1	3.1206	2228.1	-17722
- Td..C:SR.W.m2:DP	1	6.8935	2231.9	-17703

Table 4: Mean squared error of different models

Model	MSE
Full model	0.2009401
WBGT model	0.2059512
Flag model	0.2050398

Evaluate the impact of air quality on marathon performance

Except for the weather conditions, air quality may also have an effect on marathon performance. We will explore the impact of air quality on marathon performance by examining the correlation between the air quality index (AQI) and the normalized difference. The AQI of each race is calculated by averaging the AQI of all hours measured by 8-HR RUN AVERAEG BEGIN HOUR. The data set provides other kinds of measurements of air quality, but only records measured by 8-HR RUN AVERAEG BEGIN HOUR have no missing value and are measured in the same way across all locations and years.

The result (Figure 8) shows that the correlation between AQI and the normalized difference is roughly the same across all ages, with the average correlation is only 0.05. To further

explore the effect of air quality, we also fit a linear model to examine the effect of other weather parameters on marathon performance, condition on air quality. The model is fitted by $Diff \sim \beta_0 + \beta_1 X + \beta_2 * AQI + \beta_3 * X * AQI$, where $Diff$ is the normalized difference, X is the weather parameter, and AQI is the air quality index. The estimated coefficient of β_1 and β_3 , and the corresponding p-value are reported in Table 5. The result shows that, only the effect of Solar Radiation is not significantly associated with air quality, and after condition on air quality, the effect of relative humidity is still not significant. The estimated value of β_3 for other weather parameters are all significantly above 0, indicating that the effect of weather parameters on marathon performance is stronger when AQI is higher (worse air quality).

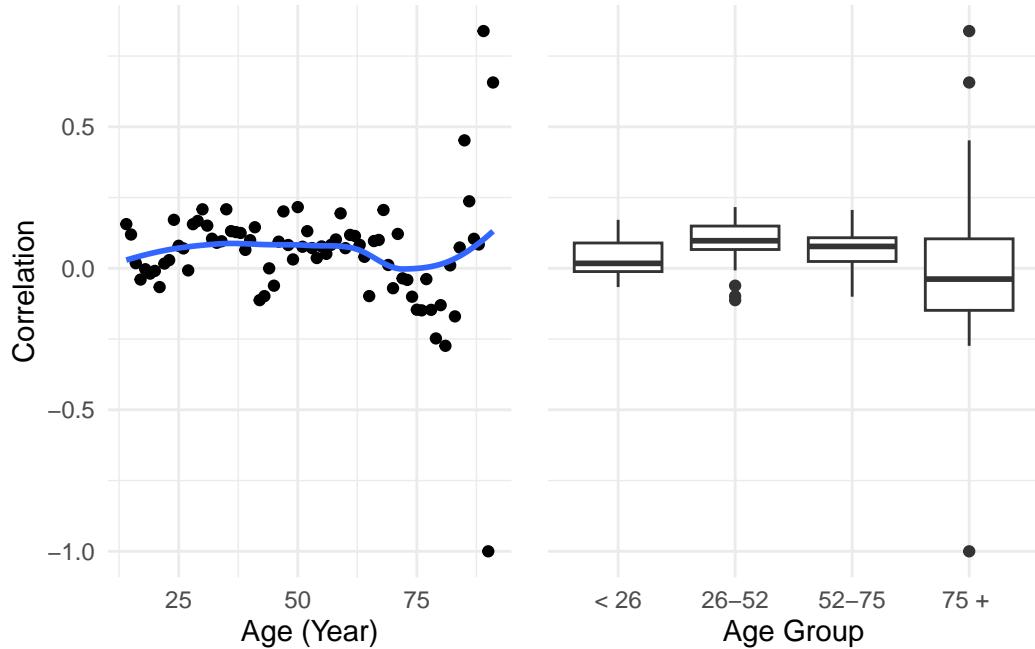


Figure 8: Scatter plot and box plot of correlation between air quality index and normalized difference against age

Table 5: Estimated coefficient and p-value of weather parameters on normalized difference, condition on air quality

Parameter	Estimate	P-value
Dry bulb temperature	0.009	< 0.001*
Dry bulb temperature * Aqi	< 0.001	0.001*
Wet bulb temperature	-0.004	0.116
Wet bulb temperature * Aqi	0.001	< 0.001*
Black globe temperature	0.006	< 0.001*

Black globe temperature * Aqi	< 0.001	0.011*
Wet Bulb Globe Temperature	0.002	0.252
Wet Bulb Globe Temperature * Aqi	< 0.001	< 0.001*
Solar Radiation	< 0.001	0.012*
Solar Radiation * Aqi	< 0.001	0.146
Dew Point	-0.009	< 0.001*
Dew Point * Aqi	0.001	< 0.001*
Wind Speed	0.004	0.113
Wind Speed * Aqi	< 0.001	0.002*
Relative Humidity	< 0.001	0.477
Relative Humidity * Aqi	< 0.001	0.089

Conclusion and discussion

Our analysis shows that aging have an overall negative impact on marathon performance, in terms of fastest finish time and percentage off course record. All weather conditions except for the relative humidity have a significant impact on marathon performance, in terms of normalized difference, with higher temperature, solar radiation and dew point and lower wind speed are associated with worse marathon performance. Runners around 26 years old are the fastest runner compare to all other age, and effect of aging start to accelerate around 53 years old (Figure 1 and Figure 2). Wet Bulb Globe Temperature only have effect on marathon performance when the temperature is over 23 degrees (Red Flag). The effect of Wet Bulb Globe Temperature varies across age and sex, where the effect is stronger among younger runners (between 20 to 30 years old) and among male runners (Figure 4). Even though young runners suffered the biggest effect of bad weather conditions, old runners are more likely to be affected by the weather conditions (Figure 6). Temperatures measured in all kinds of way(Dry bulb, wet bulb, etc.) are the mostly related to marathon performance. AQI value, on it's own, has little effect on marathon performance, but it can amplify the effect of other weather parameters on marathon performance. The effect of weather parameters on marathon performance is stronger when AQI is higher.

The observation that young runners are most susceptible to weather effects, while older runners are more likely to be affected, is not contradictory. Consider the thermoregulation system's efficacy as a value between 0 and 1. As age increases, this efficacy decreases monotonically. This means that older runners have less room for their thermoregulation to be impacted by weather, as the efficacy cannot fall below 0 (negative thermoregulation efficacy). While younger runners can tolerate a significant decrease in thermoregulation efficacy, they are also more likely to experience stronger effects from weather conditions on marathon performance. Conversely, young runners may have such strong thermoregulation that ideal weather conditions do not fully utilize their system's capacity, making them less susceptible to adverse weather conditions.

Even though the analysis shows that there is little correlation between relative humidity and marathon performance, and there is no significant association between 2. This result can not be drawn to the conclusion that relative humidity has no effect on marathon performance. First of all, dew point and wet bulb temperature, which are both related to relative humidity, are significantly associated with marathon performance. Second, the report only inspect the linear relationship between weather parameters and marathon performance, and the effect of relative humidity on marathon performance may be non-linear. Third, the effect of relative humidity on marathon performance may be mediated by other weather parameters, and the effect of relative humidity may be significant when condition on other weather parameters.

The analysis has several limitations that should be considered. First, the dataset focuses exclusively on the speed records of the fastest runners, which may introduce bias and limit the generalizability of the findings to the broader population of marathon participants. Slower runners or those with different characteristics may exhibit different patterns or relationships with the variables studied. Second, the impact of our newly proposed variable has not yet been fully examined. Further analysis is needed to understand its role and potential interactions with other variables, as well as its overall contribution to explaining marathon performance. Addressing these limitations in future studies could enhance the robustness and applicability of the results.

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Code Appendix

```
# load libraries
library(dplyr)
library(tidyr)
library(kableExtra)
library(gtsummary)
library(lubridate)
library(ggplot2)
library(stringr)
library(latex2exp)
library(ggpubr)
library(RColorBrewer)
library(gridExtra)
# Read data
data <- read.csv("../Data/project1.csv")
air <- read.csv("../Data/aqi_values.csv")
# change column name to make it easier to understand
colnames(data)[[1]] <- 'Race'
colnames(data)[[3]] <- 'Sex'

# Table 1
df1 <- data.frame(Flag = names(table(data$Flag)),
                    Count = as.numeric(table(data$Flag)),
                    Percentage = round(as.numeric(table(data$Flag))/sum(table(data$Flag)) * 100))
kable(df1, col.names = c('Flag', 'Count', 'Percentage (%)')) %>%
  kable_styling()
# Missing record summary

data_na <- data[data$Flag == '',]
data <- data[data$Flag != '',]

data_na$location <- case_when(data_na$Race == 0 ~ 'Boston Marathon',
                                data_na$Race == 1 ~ 'Chicago Marathon',
                                data_na$Race == 2 ~ 'New York City Marathon',
                                data_na$Race == 3 ~ 'Twin Cities Marathon',
                                data_na$Race == 4 ~ 'Grandma's Marathon')
```

```

data_na$marathon <- paste(data_na$location, data_na$Year, sep = ' in ')
na_df <- unique(data_na$marathon)
na_df <- str_split(na_df, ' in ')
na_df <- as.data.frame(do.call(rbind, na_df))
colnames(na_df) <- c('Race', 'Year')
# na_df %>%
#   kable() %>%
#   kable_styling()
# Course record data
record <- read.csv("../Data/course_record.csv")
record$Race <- case_when(
  record$Race == 'B' ~ 0,
  record$Race == 'C' ~ 1,
  record$Race == 'NY' ~ 2,
  record$Race == 'TC' ~ 3,
  record$Race == 'D' ~ 4
)

colnames(record)[[4]] <- 'Sex'
record$seconds <- period_to_seconds(hms(record$CR))
record$Sex <- ifelse(record$Sex == 'M', 1, 0)

# Merge data
data_record <- left_join(data, record, by = c('Race', 'Year', 'Sex'))

# fastest running time
data_record$Time <- data_record$seconds + (data_record$X.CR/100) * data_record$seconds
data_record$locations <- case_when(data_record$Race == 0 ~ 'Boston Marathon',
                                     data_record$Race == 1 ~ 'Chicago Marathon',
                                     data_record$Race == 2 ~ 'New York City Marathon',
                                     data_record$Race == 3 ~ 'Twin Cities Marathon',
                                     data_record$Race == 4 ~ 'Grandma's Marathon')

# Fig 1
ggplot(data_record, aes(x = Age..yr., y = Time, color = as.factor(Sex))) +
  geom_point(size = 0.2, alpha = 0.2) +
  geom_smooth(se = F) +
  scale_color_discrete(name = 'Gender', label = c('Female','Male'))+
  scale_y_continuous(breaks = c(10800,18000, 25200, 32400),
                     labels = c(3,5,7,9),
                     name = 'Fastest Finish Time (Hour)') +
  scale_x_continuous(name = 'Age (Year)')+
  facet_wrap(~locations) +

```

```

theme_minimal() +
  theme(legend.position = c(.85,.2))
data_record %>%
  group_by(Sex, locations) %>%
  mutate(Sex = ifelse(Sex == 1, 'Male', 'Female')) %>%
  summarise(min_time = round(min(Time)/60**2,2), age = Age..yr.[which.min(Time)]) %>%
  kable(col.names = c('Sex', 'Marathon', 'Minimum finish time (Hr)', 'Age')) %>%
  kable_styling()
# Figure 2
ggplot(data_record, aes(x = Age..yr., y = X.CR)) +
  geom_point(aes(color = as.factor(Flag)),
             size = 0.05, alpha = 0.2, position = position_jitter(width = 1)) +
  geom_vline(xintercept = c(26, 52, 75), linetype = 'dashed') +
  geom_text(x = 18, y = 300, label = '< 26', vjust = -1) +
  geom_text(x = 39, y = 300, label = '26 - 52', vjust = -1) +
  geom_text(x = 63.6, y = 300, label = '52 - 75', vjust = -1) +
  geom_text(x = 85, y = 300, label = '75 + ', vjust = -1) +
  geom_smooth(aes(color = as.factor(Flag)), se = F) +
  scale_color_manual(values = c('#06d6a0', '#ef476f', '#118ab2', '#ffd166')) +
  scale_y_continuous(name = 'Percent off course record (%)') +
  scale_x_continuous(name = 'Age (Year)') +
  theme_minimal()

# Record breaking summary
# won't be shown in the final report
record_flag <- left_join(record, data[,1:4], by = c('Race', 'Year', 'Sex'))
record_flag <- record_flag[!is.na(record_flag$Flag),]
record_break <- record_flag %>%
  distinct(CR, .keep_all = T)

flag_break_record <- round(as.numeric(summary(as.factor(record_break$Flag)))*100/nrow(record_break))
flag_data <- round(as.numeric(summary(as.factor(data$Flag)))*100/nrow(data)),3

flag_df <- data.frame(Flag = c('Green', 'Red', 'White', 'Yellow'),
                      Record = flag_break_record,
                      Data = flag_data)
# flag_df %>%
#   kable(col.names = c('Flag', 'Percentage in record breaking cases (%)', 'Percentage in Data'))
#   kable_styling()
# calculate mean and weighted mean

Avg_CR_unweighted <- data_record %>% #unweighted mean

```

```

group_by(Sex, Age..yr.) %>%
  summarise(mean_CR_unweight = mean(X.CR))

Flag_Weight <- data_record %>% # calculate weight based on flags
  group_by(Flag) %>%
    summarise(weight = n()/nrow(data_record))

data_record_weight <- left_join(data_record, Flag_Weight, by = 'Flag')

# weighted mean
Avg_CR_weighted <- data_record_weight %>%
  group_by(Sex, Age..yr.) %>%
  summarise(mean_CR_weighted = weighted.mean(X.CR, w = weight),
            mean_TdC_weighted = weighted.mean(Td..C, w = weight),
            mean_TwC_weighted = weighted.mean(Tw..C, w = weight),
            mean_TgC_weighted = weighted.mean(Tg..C, w = weight),
            mean_WBGT_weighted = weighted.mean(WBGT, w = weight),
            mean_SR.W.m2_weighted = weighted.mean(SR.W.m2, w = weight),
            mean_DP_weighted = weighted.mean(DP, w = weight),
            mean_Wind_weighted = weighted.mean(Wind, w = weight))

# merge data
data_record_weight <- left_join(data_record_weight,
                                  Avg_CR_weighted,
                                  by = c('Sex', 'Age..yr.'))
data_record_weight <- left_join(data_record_weight,
                                  Avg_CR_unweighted,
                                  by = c('Sex', 'Age..yr.))

data_record_weight$below_avg <- ifelse(data_record_weight$X.CR < data_record_weight$mean_CR_unweight, 1, 0)
data_record_weight$below_avg_w <- ifelse(data_record_weight$X.CR < data_record_weight$mean_CR_unweight, 1, 0)

#converge data to long format for Fig 3
data_weight_long <- pivot_longer(data_record_weight,
                                   cols = c('Td..C', 'Tw..C', 'Tg..C', 'WBGT'),
                                   names_to = 'Type', values_to = 'Temp')

data_weight_long <- pivot_longer(data_weight_long,
                                   cols = c('below_avg', 'below_avg_w'),
                                   names_to = 'Cr_type',
                                   values_to = 'Below_avg_CR')
data_weight_long$Cr_type <- ifelse(data_weight_long$Cr_type == 'below_avg', 1, 0)

```

```

        'Arithmetic mean',
        'Weighted Mean')
data_weight_long$Below_avg_CR <- ifelse(data_weight_long$Below_avg_CR == 1,
                                         'Below average',
                                         'Above average')

# Fig3
ggplot(data_weight_long, aes(x = Type, y = Temp, color = as.factor(Below_avg_CR))) +
  geom_boxplot() +
  scale_color_discrete(name = '') +
  scale_x_discrete(name = 'Measurements',
                    labels = c('Dry bulb', 'Black globe', 'Wet bulb', 'WBGT'),
                    guide = guide_axis(n.dodge=3)) +
  scale_y_continuous(name = 'Temperature (Celsius)') +
  facet_wrap(~Cr_type) +
  theme_minimal()

# normalized difference
data_record_weight$Avg_Cr_Diff <- (data_record_weight$X.CR -
                                       data_record_weight$mean_CR_weighted)/
                                     data_record_weight$mean_CR_weighted

data_record_weight$Flag <- factor(data_record_weight$Flag,
                                    ordered = T,
                                    levels = c('White', 'Green', 'Yellow', 'Red'))
data_record_weight$below_avg_w <- ifelse(data_record_weight$below_avg_w == 1,
                                           'Below average',
                                           'Above average')

# table 2
tbl_summary(data_record_weight, by = below_avg_w,
            include = c(Flag, Td..C, Tw..C, Tg..C, WBGT, X.rh, SR.W.m2, DP, Wind)) %>%
  add_p()
# Tg flag
# not used in the final report
data_record_weight$Tg_flag <- case_when(data_record_weight$Tg..C < 19.475000 ~ 1,
                                         data_record_weight$Tg..C < 24.955556 ~ 2,
                                         data_record_weight$Tg..C < 30.000000 ~ 3,
                                         TRUE ~ 4)
data_record_weight$Tg_flag <- as.factor(data_record_weight$Tg_flag)

data_record_weight$Avg_Cr_Diff <- (data_record_weight$X.CR -

```

```

            data_record_weight$mean_CR_weighted) /
data_record_weight$mean_CR_weighted

data_record_weight$Sex <- ifelse(data_record_weight$Sex == 1, 'Male', 'Female')

# Fig 4
data_record_weight %>%
  group_by(Sex, Age..yr., Flag) %>%
  summarise(mean_cr = mean(Avg_Cr_Diff)) %>%
  ggplot(aes(x = Age..yr., y = mean_cr, color = as.factor(Flag))) +
  geom_point(size= 0.5) +
  geom_smooth(se = T) +
  scale_color_manual(values = c('#118ab2', '#06d6a0', '#ffd166', '#ef476f'),
                     name = 'Weather Flag') +
  scale_y_continuous(name = 'Normalized Difference') +
  scale_x_continuous(name = 'Age (Year)') +
  facet_wrap(~Sex) +
  theme_minimal()

# Age group
data_record_weight$Age_grp <- case_when(data_record_weight$Age..yr. < 26 ~ ' < 26',
                                         data_record_weight$Age..yr. < 52 ~ '26-52',
                                         data_record_weight$Age..yr. < 75 ~ '52-75',
                                         TRUE ~ '75 + ')

# Fig 5
ggplot(data_record_weight, aes(x = Age_grp, y = Avg_Cr_Diff, color = as.factor(Flag))) +
  geom_boxplot() +
  scale_color_manual(values = c('#118ab2', '#06d6a0', '#ffd166', '#ef476f'),
                     name = 'Weather Flag') +
  scale_y_continuous(name = 'Normalized Difference') +
  scale_x_discrete(name = 'Age Group') +
  facet_wrap(~Sex) +
  theme_minimal()

# Normalized difference of weather parameters
# not used in the final report
data_record_weight <-data_record_weight %>%
  mutate(TdC_diff = (Td..C - mean_TdC_weighted)/mean_TdC_weighted,
         TwC_diff = (Tw..C - mean_TwC_weighted)/mean_TwC_weighted,
         TgC_diff = (Tg..C - mean_TgC_weighted)/mean_TgC_weighted,
         WBGT_diff = (WBGT - mean_WBGT_weighted)/mean_WBGT_weighted,
         SR_diff = (SR.W.m2 - mean_SR.W.m2_weighted)/mean_SR.W.m2_weighted,

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DP_diff = (DP - mean_DP_weighted)/mean_DP_weighted,
Wind_diff = (Wind - mean_Wind_weighted)/mean_Wind_weighted)

# Correlation
cor_df <- data_record_weight %>%
  group_by(Age..yr.) %>%
  summarise(Dry_T = cor(TdC_diff, Avg_Cr_Diff, use = 'complete.obs'),
            Wet_T = cor(TwC_diff, Avg_Cr_Diff, use = 'complete.obs'),
            Goble_T = cor(TgC_diff, Avg_Cr_Diff, use = 'complete.obs'),
            WBGT = cor(WBGT_diff, Avg_Cr_Diff, use = 'complete.obs'),
            SR = cor(SR_diff, Avg_Cr_Diff, use = 'complete.obs'),
            Dp = cor(DP_diff, Avg_Cr_Diff, use = 'complete.obs'),
            Wind = cor(Wind_diff, Avg_Cr_Diff, use = 'complete.obs'))

# convert to long format for Fig 6
cor_df_long <- pivot_longer(cor_df,
                             cols = c(Dry_T, Wet_T, Goble_T, WBGT, SR, Dp, Wind),
                             names_to = 'Type', values_to = 'Correlation')
cor_df_long$Type <- factor(cor_df_long$Type,
                            levels = c('Dry_T', 'Wet_T', 'Goble_T', 'WBGT',
                                      'SR', 'Dp', 'Wind'))

cor_df_long$Type <- case_when(cor_df_long$Type == 'Dry_T' ~ 'Dry Bulb Temperature',
                               cor_df_long$Type == 'Wet_T' ~ 'Wet Bulb Temperature',
                               cor_df_long$Type == 'Goble_T' ~ 'Globe Temperature',
                               cor_df_long$Type == 'WBGT' ~ 'WBGT',
                               cor_df_long$Type == 'SR' ~ 'Solar Radiation',
                               cor_df_long$Type == 'Dp' ~ 'Dew Point',
                               cor_df_long$Type == 'Wind' ~ 'Wind Speed')

# Fig6
ggplot(cor_df_long, aes(x = Age..yr., y = Correlation, color = as.factor(Type))) +
  geom_point(size = 0.5) +
  geom_smooth(se = F) +
  scale_color_brewer(palette = 'Dark2', name = 'Weather Conditions') +
  scale_y_continuous(name = 'Correlation') +
  scale_x_continuous(name = 'Age (Year)') +
  theme_minimal()

#Age group
cor_df_long$Age_grp <- case_when(cor_df_long$Age..yr. < 26 ~ '< 26',
                                    cor_df_long$Age..yr. < 52 ~ '26-52',
                                    cor_df_long$Age..yr. < 75 ~ '52-75',

```

```

TRUE ~ '75 + ')

# Fig 7
ggplot(cor_df_long, aes(x = Age_grp, y = Correlation, color = as.factor(Type))) +
  geom_boxplot() +
  scale_color_brewer(palette = 'Dark2', name = 'Weather Conditions') +
  scale_y_continuous(name = 'Correlation') +
  scale_x_discrete(name = 'Age Group') +
  theme_minimal()
plot(data_record_weight$X.CR ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$Td..C ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$Tw..C ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$Tg..C ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$WBGT ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$SR.W.m2 ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$DP ,data_record_weight$Avg_Cr_Diff)
plot(data_record_weight$Wind ,data_record_weight$Avg_Cr_Diff)

low_scope <- lm(Avg_Cr_Diff ~ 1, data = data_record_weight)
high_scope <- lm(Avg_Cr_Diff ~ Td..C * Tw..C * Tg..C * SR.W.m2 * DP * Wind, data = data_record_weight)
mod <- lm(Avg_Cr_Diff ~ Td..C + Tw..C + Tg..C + SR.W.m2 + DP + Wind, data = data_record_weight)
mod <- step(mod, scope = list(lower = low_scope, upper = high_scope), direction = 'both')
mod_WBGT <- lm(Avg_Cr_Diff ~ WBGT, data = data_record_weight)
mod_Flag <- lm(Avg_Cr_Diff ~ Flag, data = data_record_weight)

mse_mod <- mean((data_record_weight$Avg_Cr_Diff - predict(mod))^2)
mse_mod_WBGT <- mean((data_record_weight$Avg_Cr_Diff - predict(mod_WBGT))^2)
mse_mod_Flag <- mean((data_record_weight$Avg_Cr_Diff - predict(mod_Flag))^2)
# Table 3
mse_df <- data.frame(Model = c('Full model', 'WBGT model', 'Flag model'),
                       MSE = c(mse_mod, mse_mod_WBGT, mse_mod_Flag))
mse_df %>%
  kable() %>%
  kable_styling()
# air quality data
air <- air[!is.na(air$aqi),]
air_avg <- air %>%
  group_by(date_local, marathon) %>%
  filter(sample_duration == "8-HR RUN AVG BEGIN HOUR") %>%
  summarise(mean_aqi = mean(aqi))

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air_avg$Year <- as.numeric(substr(air_avg$date_local, 1, 4))
air_avg$Race <- case_when(
  air_avg$marathon == 'Boston' ~ 0,
  air_avg$marathon == 'Chicago' ~ 1,
  air_avg$marathon == 'NYC' ~ 2,
  air_avg$marathon == 'Twin Cities' ~ 3,
  air_avg$marathon == 'Grandmas' ~ 4
)

# merge air data with record data
data_record_weight_air <- left_join(data_record_weight, air_avg,
                                      by = c('Year', 'Race'))
# correlation between air and marathon performance
cor_air_df <- data_record_weight_air %>%
  group_by(Age..yr.) %>%
  summarise(Aqi_cor = cor(mean_aqi, Avg_Cr_Diff, use = 'complete.obs'))

cor_air_df$Age_grp <- case_when(cor_air_df$Age..yr. < 26 ~ '< 26',
                                  cor_air_df$Age..yr. < 52 ~ '26-52',
                                  cor_air_df$Age..yr. < 75 ~ '52-75',
                                  TRUE ~ '75 + ')

# fig 8
p1 <- ggplot(cor_air_df, aes(x = Age..yr., y = Aqi_cor)) +
  geom_point() +
  scale_y_continuous(name = 'Correlation') +
  scale_x_continuous(name = 'Age (Year)') +
  geom_smooth(se = F) +
  theme_minimal()

p2 <- ggplot(cor_air_df, aes(x = Age_grp, y = Aqi_cor)) +
  geom_boxplot() +
  scale_x_discrete(name = 'Age Group') +
  theme_minimal() +
  theme(axis.title.y = element_blank(),
        axis.text.y = element_blank(),
        axis.ticks.y = element_blank())
grid.arrange(p1, p2, ncol=2)
# linear model of weather parameters on marathon performance, condition on air quality
m_tdc <- lm(Avg_Cr_Diff ~ Td..C * mean_aqi, data = data_record_weight_air)
m_twc <- lm(Avg_Cr_Diff ~ Tw..C * mean_aqi, data = data_record_weight_air)
m_tgc <- lm(Avg_Cr_Diff ~ Tg..C * mean_aqi, data = data_record_weight_air)

```

```

m_WBGT <- lm(Avg_Cr_Diff ~ WBGT * mean_aqi, data = data_record_weight_air)
m_SR <- lm(Avg_Cr_Diff ~ SR.W.m2 * mean_aqi, data = data_record_weight_air)
m_DP <- lm(Avg_Cr_Diff ~ DP * mean_aqi, data = data_record_weight_air)
m_Wind <- lm(Avg_Cr_Diff ~ Wind * mean_aqi, data = data_record_weight_air)
m_rh <- lm(Avg_Cr_Diff ~ X.rh * mean_aqi, data = data_record_weight_air)

# select beta1 and beta3
coef_df <- round(summary(m_tdc)$coefficient[c(2,4),c(1,4)],3)
coef_df <- rbind(coef_df, round(summary(m_twc)$coefficient[c(2,4),c(1,4)],3))
coef_df <- rbind(coef_df, round(summary(m_tgc)$coefficient[c(2,4),c(1,4)],3))
coef_df <- rbind(coef_df, round(summary(m_WBGT)$coefficient[c(2,4),c(1,4)],3))
coef_df <- rbind(coef_df, round(summary(m_SR)$coefficient[c(2,4),c(1,4)],3))
coef_df <- rbind(coef_df, round(summary(m_DP)$coefficient[c(2,4),c(1,4)],3))
coef_df <- rbind(coef_df, round(summary(m_Wind)$coefficient[c(2,4),c(1,4)],3))
coef_df <- rbind(coef_df, round(summary(m_rh)$coefficient[c(2,4),c(1,4)],3))
rownames(coef_df) <- c('Dry bulb temperature', 'Dry bulb temperature * Aqi',
                       'Wet bulb temperature ', 'Wet bulb temperature * Aqi',
                       'Black globe temperature', 'Black globe temperature * Aqi',
                       'Wet Bulb Globe Temperature', 'Wet Bulb Globe Temperature * Aqi',
                       'Solar Radiation', 'Solar Radiation * Aqi',
                       'Dew Point', 'Dew Point * Aqi',
                       'Wind Speed', 'Wind Speed * Aqi',
                       'Relative Humidity', 'Relative Humidity * Aqi')

#table3
coef_df <- as.data.frame(coef_df)
coef_df$Estimate <- ifelse(coef_df$Estimate ==0, '< 0.001', coef_df$Estimate)
coef_df`Pr(>|t|)` <- ifelse(coef_df`Pr(>|t|)` == 0, '< 0.001', coef_df`Pr(>|t|)` )
coef_df`Pr(>|t|)` <- ifelse(coef_df`Pr(>|t|)` < 0.05,
                               paste0(coef_df`Pr(>|t|)` , '*'), coef_df`Pr(>|t|)` )
coef_df$Estimate <- as.character(coef_df$Estimate)
coef_df`Pr(>|t|)` <- as.character(coef_df`Pr(>|t|)` )
coef_df %>%
  kable(align = 'ccc', col.names = c('Parameter', 'Estimate', 'P-value')) %>%
  kable_styling()

```