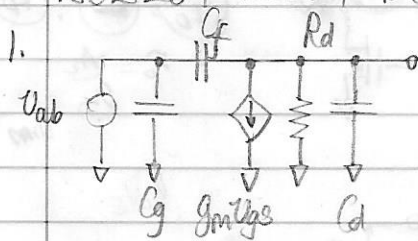


ECE264 Lect 7 Blackman's Impedance Relation



$$\begin{aligned} \textcircled{1} \quad Z_{ab}^0 &= \left(\frac{R_d}{1+sC_d R_d} + \frac{1}{sC_g} \right) \parallel \frac{1}{sC_g} \\ &= \frac{Z_d + \frac{1}{sC_g}}{1+sC_g \left(Z_d + \frac{1}{sC_g} \right)} \\ &= \frac{1+sC_g Z_d}{sC_g + sC_g (1+sC_g Z_d)} \\ &= \frac{R_d}{1+sC_g (1+sC_d R_d)} \\ &= \frac{1+sC_g (1+sC_d R_d)}{sC_g + sC_g (1+sC_g \frac{R_d}{1+sC_d R_d})} \\ &= \frac{(1+sC_d R_d) + sC_g R_d}{sC_g (1+sC_d R_d) + sC_g (1+sC_d R_d + sC_g R_d)} \end{aligned}$$

$$v_t = - \frac{\frac{R_d}{1+sC_d R_d}}{1+s \frac{C_g R_d}{C_g + C_g} \frac{R_d}{1+sC_d R_d}} i_t$$

$$= - \frac{R_d (C_g + C_d)}{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d} i_t$$

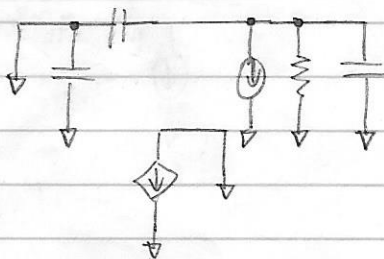
$$x_c = - \frac{\frac{1}{sC_g}}{\frac{1}{sC_g} + \frac{1}{sC_g}} v_t$$

$$= \frac{sC_g}{sC_g + sC_g} \frac{-R_d (C_g + C_d)}{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d} i_t$$

$$= \frac{-R_d C_g}{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d} i_t$$

$$T_x = g_m x_c = - \frac{g_m R_d C_g}{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d} i_t$$

② T_{sc}

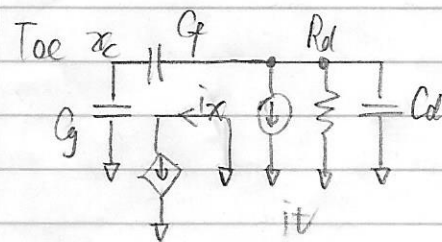


$$T_{sc} = 0$$

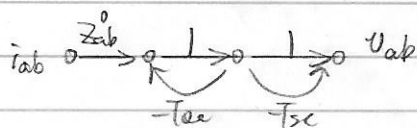
$$\begin{aligned} \textcircled{4} \quad Z_{ab} &= \frac{1+sC_d R_d + sC_g R_d}{sC_g (1+sC_d R_d) + sC_g (1+sC_d R_d + sC_g R_d)} \\ &= \frac{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d}{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d + g_m R_d C_g} \\ &= \frac{1}{s} \frac{1+sC_g (1+sC_d R_d) R_d}{(C_g + C_d) (1+sC_d R_d) + sC_g C_g R_d + g_m R_d C_g} \end{aligned}$$

$$Z_d = \frac{R_d}{1+sC_d R_d}$$

③



$$Z_{ab} = Z_{ab}^0 \frac{1-T_{sc}}{1-T_{sc}}$$

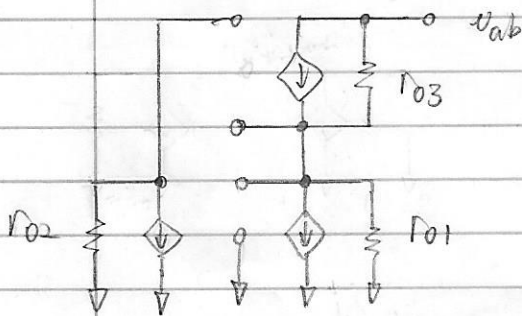
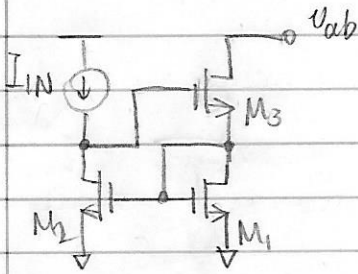


$$v_t = - \left(R_d \parallel \frac{1}{sC_d} \parallel \left(\frac{1}{sC_g} + \frac{1}{sC_g} \right) \right) i_t$$

$$= - \left(Z_d \parallel \frac{s(C_g + C_d)}{s^2 C_g C_d} \right) i_t \quad \text{or} \quad - \left(Z_d \parallel \frac{1}{sC_m} \right) i_t = \frac{-Z_d}{1+sC_m Z_d} i_t$$

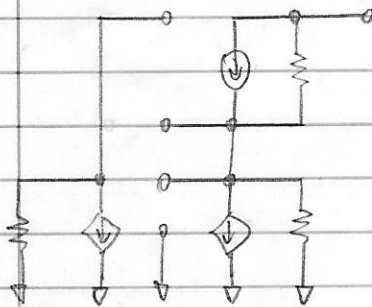
ECE 264A Leet 7

2. Wilson



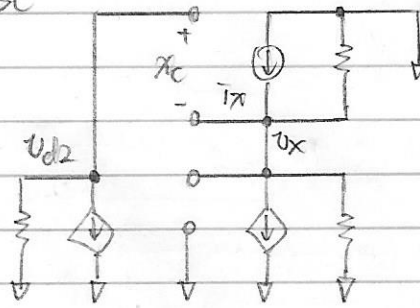
$$\textcircled{1} \quad Z_{ab}^0 = r_{o3} + \left(\frac{1}{g_{m1}} \parallel r_{o1} \right) \approx r_{o3}$$

② T_{oe}



$$T_{oe} = 0$$

③ T_{sc}



$$v_t \approx \frac{1}{g_{m1}} i_t$$

$$v_{d2} = -A_{o2} v_t$$

$$x_c = v_{d2} - v_t \approx -A_{o2} v_t \approx -\frac{g_{m2} r_{o2}}{g_{m1}} i_t$$

$$i_x = g_{m3} x_c = -\frac{g_{m3} g_{m2} r_{o2}}{g_{m1}} i_t$$

$$\textcircled{4} \quad Z_{ab} = Z_{ab}^0 (1 - T_{sc})$$

$$\approx r_{o3} \left(1 + \frac{g_{m3} A_{o2}}{g_{m1}} \right)$$

$$= \frac{g_{m1} r_{o3} + A_{o2} A_{o3}}{g_{m1}}$$

$$\begin{aligned} & r_{o1} + r_{o2} + g_{m2} r_{o2} r_{o1} \\ & r_{o2} (g_{m2} r_{o1} + 1) \end{aligned}$$