



Step 1:

$$R(i,j,k+1) = R(i,j,k) + R(i,k,k) \cdot R(k,k,k)^* \cdot R(k,j,k)$$

$$\text{find } L(M) = R(1,2,5) + R(1,3,5)$$

$$R(1,1,1) = b+e$$

$$R(1,2,1) = a$$

$$R(1,3,1) = \emptyset$$

$$R(1,4,1) = \emptyset$$

$$R(2,1,1) = \emptyset$$

$$R(2,2,1) = e$$

$$R(2,3,1) = b$$

$$R(2,4,1) = a$$

$$R(3,1,1) = \emptyset$$

$$R(3,2,1) = \emptyset$$

$$R(3,3,1) = a+b+e$$

$$R(3,4,1) = \emptyset$$

$$R(4,1,1) = \emptyset$$

$$R(4,2,1) = \emptyset$$

$$R(4,3,1) = \emptyset$$

$$R(4,4,1) = a+b+e$$

Step 2:

Step 2:

$$R(1,2,5) = R(1,2,4) + R(1,4,4) \cdot R(4,4,4)^* \cdot R(4,2,4)$$

$$= b^*a + b^*aa \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,2,5) = b^*a$$

$$R(1,2,4) = R(1,2,3) + R(1,3,3) \cdot R(3,3,3)^* \cdot R(3,2,3)$$

$$= b^*a + b^*ab \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,2,4) = b^*a$$

$$R(1,2,3) = R(1,2,2) + R(1,2,2) \cdot R(2,2,2)^* \cdot R(2,2,2)$$

$$= b^*a + b^*a \cdot e^* \cdot e$$

$$R(1,2,3) = b^*a$$

$$R(1,2,2) = R(1,2,1) + R(1,1,1) \cdot R(1,1,1)^* \cdot R(1,2,1)$$

$$= a + (b+e) \cdot (b+e)^* \cdot a$$

$$= a + b^*a$$

$$R(1,2,2) = b^*a$$

$$R(2,2,2) = R(2,2,1) + R(2,1,1) \cdot R(1,1,1)^* \cdot R(1,2,1)$$

$$= e + \emptyset \cdot (b+e)^* \cdot a$$

$$R(2,2,2) = e$$

$$R(1,3,3) = R(1,3,2) + R(1,2,2) \cdot R(2,2,2)^* \cdot R(2,3,2)$$

$$= \emptyset + (a + b^*a) \cdot e^* \cdot b$$

$$R(1,3,3) = (a + b^*a)b$$

$$R(1,3,2) = R(1,3,1) + R(1,1,1) \cdot R(1,1,1)^* \cdot R(1,3,1)$$

$$= \emptyset + (b+e) \cdot (b+e)^* \cdot \emptyset$$

$$R(1,3,2) = \emptyset$$

$$R(2,3,2) = R(2,3,1) + R(2,1,1) \cdot R(1,1,1)^* \cdot R(1,3,1)$$

$$= b + \emptyset \cdot (b+e)^* \cdot \emptyset$$

$$R(2,3,2) = b$$

$$R(3,3,3) = R(3,3,2) + R(3,2,2) \cdot R(2,2,2)^* \cdot R(2,3,2)$$

$$= (a+b+e) + \emptyset \cdot e^* \cdot b$$

$$R(3,3,3) = a+b+e$$

$$R(3,3,2) = R(3,3,1) + R(3,1,1) \cdot R(1,1,1)^* \cdot R(1,3,1)$$

$$= (a+b+e) + \emptyset \cdot (b+e)^* \cdot \emptyset$$

$$R(3,3,2) = a+b+e$$

$$\begin{aligned} R(3,2,2) &= R(3,2,1) + R(3,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,1,1) \\ &= \emptyset + \emptyset \cdot (b+e)^* \cdot (b+e) \end{aligned}$$

$$R(3,2,2) = \emptyset$$

$$\begin{aligned} R(3,2,3) &= R(3,2,2) + R(3,2,2) \cdot R(2,2,2)^* \cdot \\ R(2,2,2) \\ &= \emptyset + \emptyset \cdot e^* \cdot e \end{aligned}$$

$$R(3,2,3) = \emptyset$$

$$\begin{aligned} R(1,4,4) &= R(1,4,3) + R(1,3,3) \cdot R(3,3,3)^* \cdot \\ R(3,4,3) \\ &= b^*aa + b^*ab \cdot (a+b+e)^* \cdot \emptyset \end{aligned}$$

$$R(1,4,4) = b^*aa$$

$$\begin{aligned} R(1,4,3) &= R(1,4,2) + R(1,2,2) \cdot R(2,2,2)^* \cdot \\ R(2,4,2) \\ &= \emptyset + b^*a \cdot e^* \cdot a \end{aligned}$$

$$R(1,4,3) = b^*aa$$

$$\begin{aligned} R(1,4,2) &= R(1,4,1) + R(1,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,4,1) \\ &= \emptyset + (b+e) \cdot (b+e)^* \cdot \emptyset \end{aligned}$$

$$R(1,4,2) = \emptyset$$

$$\begin{aligned} R(2,4,2) &= R(2,4,1) + R(2,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,4,1) \\ &= a + \emptyset \cdot (b+e)^* \cdot \emptyset \end{aligned}$$

$$R(2,4,2) = a$$

$$\begin{aligned} R(3,4,3) &= R(3,4,2) + R(3,2,2) \cdot R(2,2,2)^* \cdot \\ R(2,4,2) \\ &= \emptyset + \emptyset \cdot e^* \cdot a \end{aligned}$$

$$R(3,4,3) = \emptyset$$

$$\begin{aligned} R(3,4,2) &= R(3,4,1) + R(3,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,4,1) \\ &= \emptyset + \emptyset \cdot (b+e)^* \cdot \emptyset \end{aligned}$$

$$R(3,4,2) = \emptyset$$

$$\begin{aligned} R(4,4,4) &= R(4,4,3) + R(4,3,3) \cdot R(3,3,3)^* \cdot \\ R(3,4,3) \\ &= (a+b+e) + \emptyset \cdot (a+b+e)^* \cdot \emptyset \end{aligned}$$

$$R(4,4,4) = a+b+e$$

$$\begin{aligned} R(4,4,3) &= R(4,4,2) + R(4,2,2) \cdot R(2,2,2)^* \cdot \\ R(2,4,2) \end{aligned}$$

$$= (a+b+e) + \emptyset \cdot e^* \cdot a$$

$$R(4,4,3) = a+b+e$$

$$\begin{aligned} R(4,4,2) &= R(4,4,1) + R(4,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,4,1) \end{aligned}$$

$$= (a+b+e) + \emptyset \cdot (b+e)^* \cdot \emptyset$$

$$R(4,4,2) = a+b+e$$

$$\begin{aligned} R(4,2,2) &= R(4,2,1) + R(4,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,2,1) \end{aligned}$$

$$= \emptyset + \emptyset \cdot (b+e)^* \cdot a$$

$$R(4,2,2) = \emptyset$$

$$\begin{aligned} R(4,3,3) &= R(4,3,2) + R(4,2,2) \cdot R(2,2,2)^* \cdot \\ R(2,3,2) \end{aligned}$$

$$= \emptyset + \emptyset \cdot e^* \cdot b$$

$$R(4,3,3) = \emptyset$$

$$\begin{aligned} R(4,3,2) &= R(4,3,1) + R(4,1,1) \cdot R(1,1,1)^* \cdot \\ R(1,3,1) \end{aligned}$$

$$= \emptyset + \emptyset \cdot (b+e)^* \cdot \emptyset$$

$$R(4,3,2) = \emptyset$$

$$\begin{aligned} R(4,2,4) &= R(4,2,3) + R(4,3,3) \cdot R(3,3,3)^* \cdot \\ R(3,2,3) \end{aligned}$$

$$= \emptyset + \emptyset \cdot (a+b+e)^* \cdot \emptyset$$

$$R(4,2,4) = \emptyset$$

$$\begin{aligned} R(4,2,3) &= R(4,2,2) + R(4,2,2) \cdot R(2,2,2)^* \cdot \\ R(2,2,2) \end{aligned}$$

$$= \emptyset + \emptyset \cdot e^* \cdot e$$

$$R(4,2,3) = \emptyset$$

$$\begin{aligned} R(1,3,5) &= R(1,3,4) + R(1,4,4) \cdot R(4,4,4)^* \cdot \\ R(4,3,4) \end{aligned}$$

$$= b^*ab(a+b)^* + b^*aa \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,3,5) = b^*ab(a+b)^*$$

$$\begin{aligned} R(1,3,4) &= R(1,3,3) + R(1,3,3) \cdot R(3,3,3)^* \cdot \\ R(3,3,3) \end{aligned}$$

$$= b^*ab + b^*ab \cdot (a+b+e)^* \cdot (a+b+e)$$

$$= b^*ab + b^*ab(a+b)^*$$

$$R(1,3,4) = b^*ab(a+b)^*$$

$$R(4,3,4) = R(4,3,3) + R(4,3,3) \cdot R(3,3,3)^* \cdot R(3,3,3)$$

$$= \emptyset + \emptyset \cdot (a+b+e)^* \cdot (a+b+e)$$

$$R(4,3,4) = \emptyset$$

$$L(M) = R(1,2,5) + R(1,3,5)$$

$$L(M) = b^*a + b^*ab(a+b)^*$$

$L = \{w \in \{a,b\}^* \mid w \text{ consists of zero or more } b\text{'s and ends in } a, \text{ or } w \text{ starts with zero or more } b\text{'s that are followed by } ab\}$

$L = \{w \in \{a,b\}^* \mid w \text{ consists of zero or more } b\text{'s and ends in } a, \text{ or } w \text{ starts with zero or more } b\text{'s that are followed by } ab\}$

$L = \{w \in \{a,b\}^* \mid w \text{ starts with zero or more } b\text{'s that are not followed by } aa\}$

$L = \{w \in \{a,b\}^* \mid w \text{ starts with 0 or more } b\text{'s that are followed by exactly 1 } a\}$

(Di ko sure sa last)

Scratch:

$$\cdot (b+e)^* \cdot$$

$$R(1,2,5) = b^*a$$

$$R(1,3,5) = b^*ab(a+b)^*$$

$$R(1,2,4) = b^*a$$

$$R(1,3,4) = b^*ab(a+b)^*$$

$$R(1,4,4) = b^*aa$$

$$R(4,2,4) = \emptyset$$

$$R(4,4,4) = a+b+e$$

$$\cdot (a+b+e)^* \cdot$$

$$R(1,2,3) = b^*a$$

$$R(1,3,3) = b^*ab$$

$$R(1,4,3) = b^*aa$$

$$R(3,2,3) = \emptyset$$

$$R(3,3,3) = a+b+e$$

$$\cdot (a+b+e)^* \cdot$$

$$R(3,4,3) = \emptyset$$

$$R(4,3,3) = \emptyset$$

$$R(4,4,3) = a+b+e$$

$$R(1,2,2) = b^*a$$

$$R(1,3,2) = \emptyset$$

$$R(1,4,2) = \emptyset$$

$$R(2,2,2) = e$$

$$\cdot e^* \cdot$$

$$R(2,3,2) = b$$

$$R(2,4,2) = a$$

$$R(3,2,2) = \emptyset$$

$$R(3,3,2) = a+b+e$$

$$R(3,4,2) = \emptyset$$

$$R(4,2,2) = \emptyset$$

$$R(4,3,2) = \emptyset$$

$$R(4,4,2) = a+b+e$$

$$R(1,2,5) = R(1,2,4) + R(1,4,4) \cdot R(4,4,4)^* \cdot R(4,2,4)$$

$$= b^*a + b^*aa \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,2,5) = b^*a$$

$$R(1,2,4) = R(1,2,3) + R(1,3,3) \cdot R(3,3,3)^* \cdot R(3,2,3)$$

$$= b^*a + b^*ab \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,2,4) = b^*a$$

$$R(1,4,4) = R(1,4,3) + R(1,3,3) \cdot R(3,3,3)^* \cdot R(3,4,3)$$

$$= b^*aa + b^*ab \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,4,4) = b^*aa$$

$$R(4,4,4) = R(4,4,3) + R(4,3,3) \cdot R(3,3,3)^* \cdot R(3,4,3)$$

$$= (a+b+e) + \emptyset \cdot (a+b+e)^* \cdot \emptyset$$

$$R(4,4,4) = a+b+e$$

$$R(4,2,4) = R(4,2,3) + R(4,3,3) \cdot R(3,3,3)^* \cdot R(3,2,3)$$

$$= \emptyset + \emptyset \cdot (a+b+e)^* \cdot \emptyset$$

$$R(4,2,4) = \emptyset$$

$$R(1,3,5) = R(1,3,4) + R(1,4,4) \cdot R(4,4,4)^* \cdot$$

$$R(4,3,4)$$

$$= b^*ab(a+b)^* + b^*aa \cdot (a+b+e)^* \cdot \emptyset$$

$$R(1,3,5) = b^*ab(a+b)^*$$

$$R(1,3,4) = R(1,3,3) + R(1,3,3) \cdot R(3,3,3)^* \cdot$$

$$R(3,3,3)$$

$$= b^*ab + b^*ab \cdot (a+b+e)^* \cdot (a+b+e)$$

$$= b^*ab + b^*ab(a+b)^*$$

$$R(1,3,4) = b^*ab(a+b)^*$$

