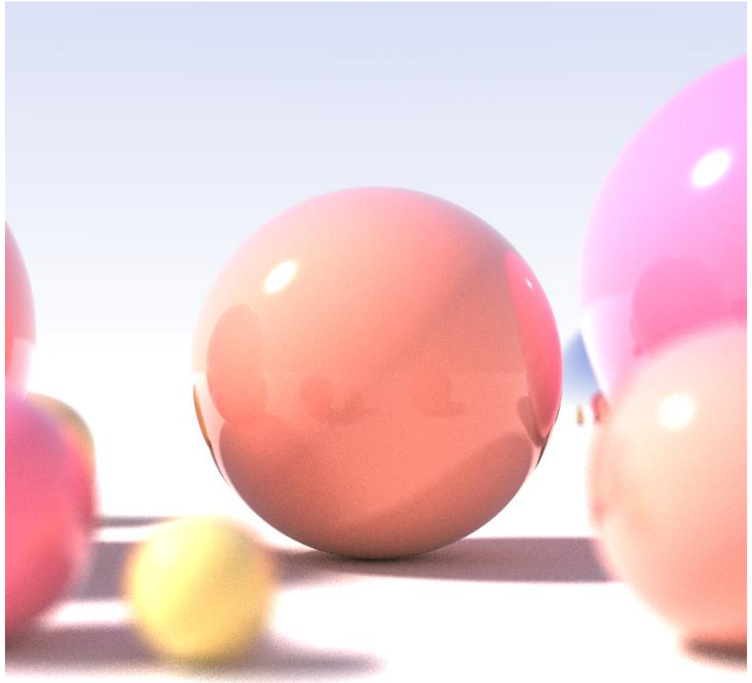
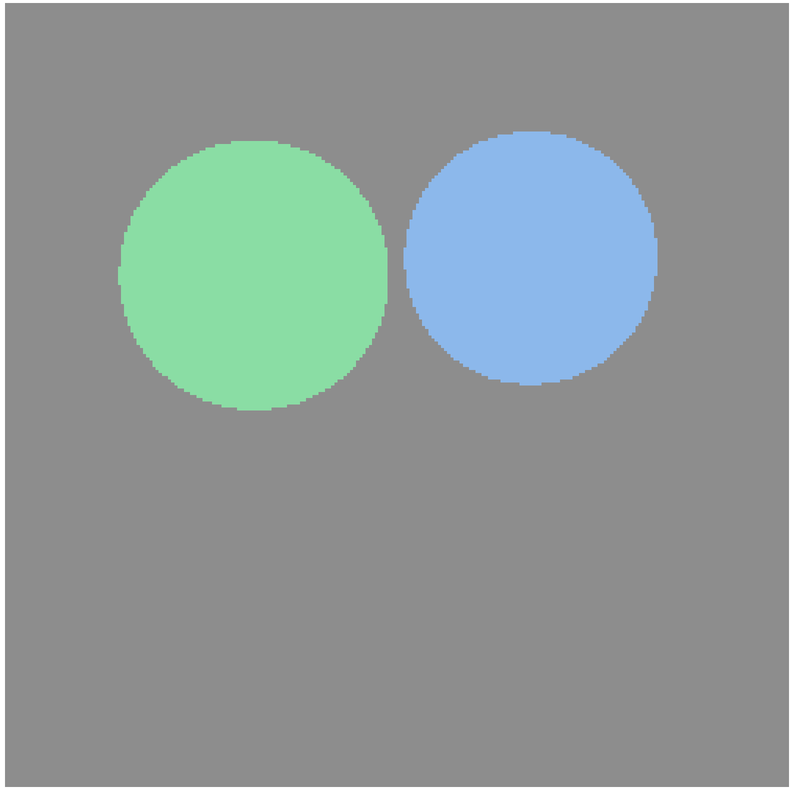
Ray Tracing



Some Slides/Images adapted from Marschner and Shirley and David Levin

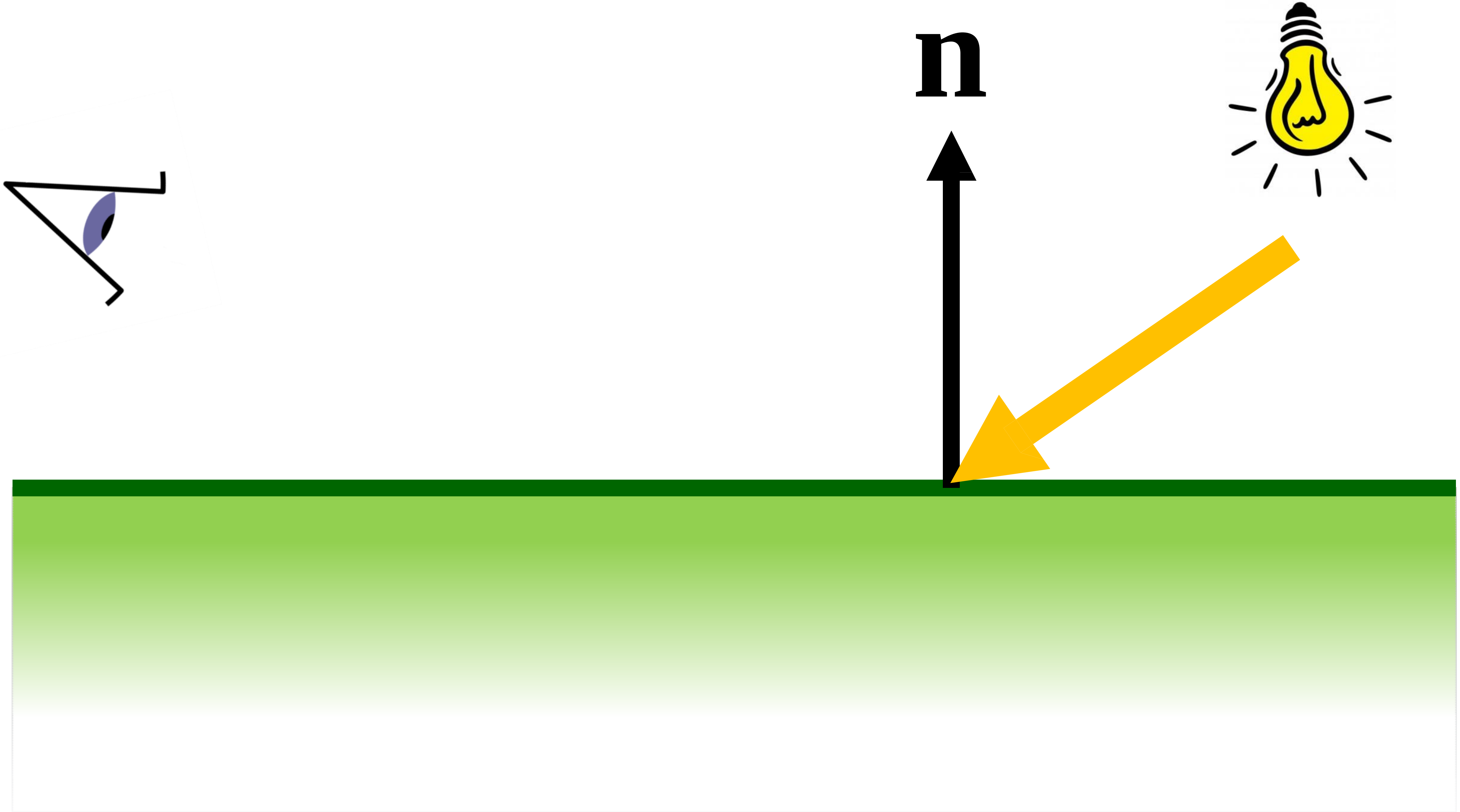
Ray Casting

```
for 0 <= iy < ny
    for 0 <= ix < nx
  {
        ray = camera.getRay(ix, iy);
        firstSurface = scene.intersect(result,ray);
        if (firstSurface)
            image.set(ix, iy, firstSurface.color);
        else
            image.set(ix, iy, background.color);
   }
```

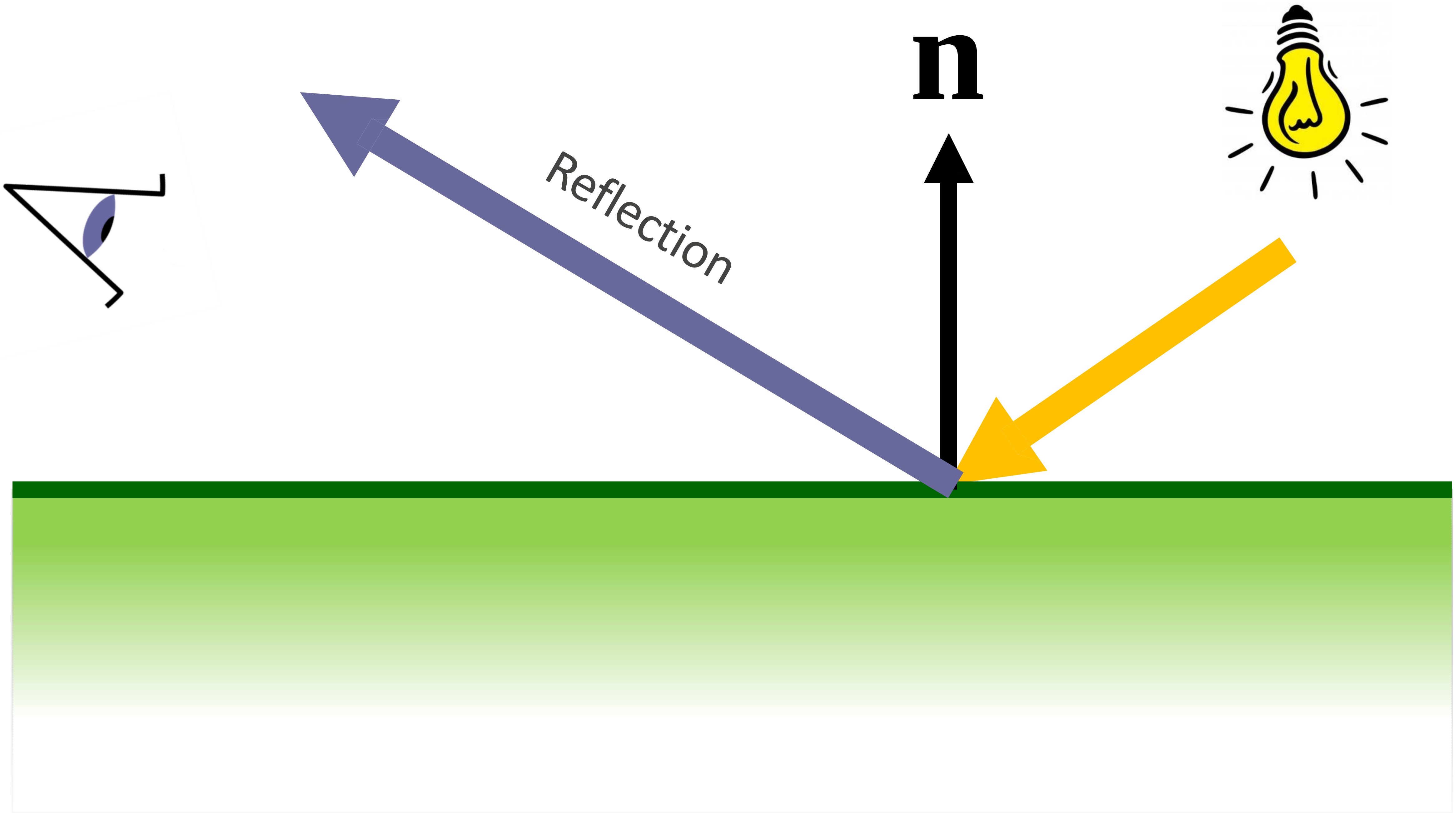


Light and Surfaces

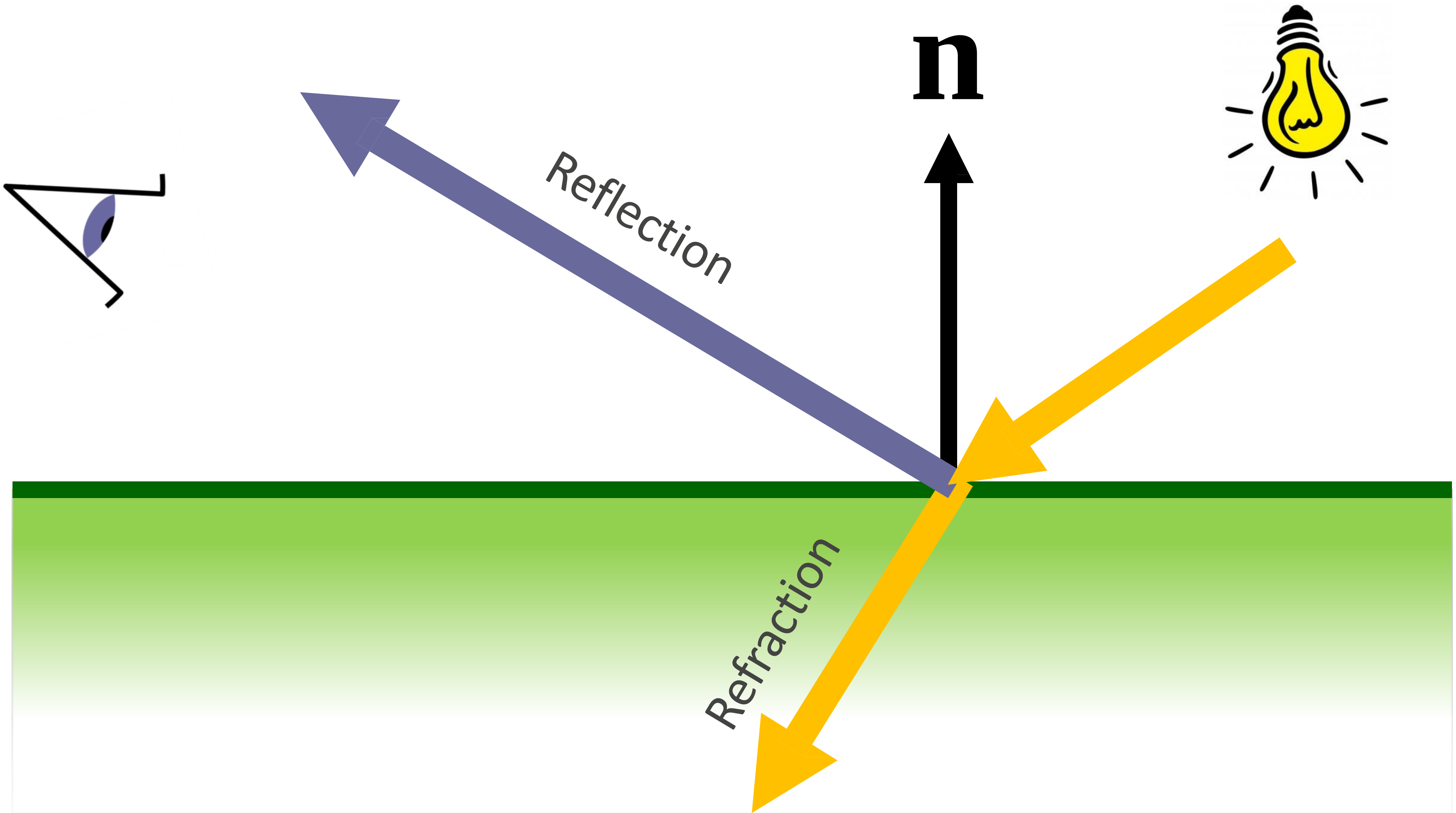
Light and Surfaces



Light and Surfaces

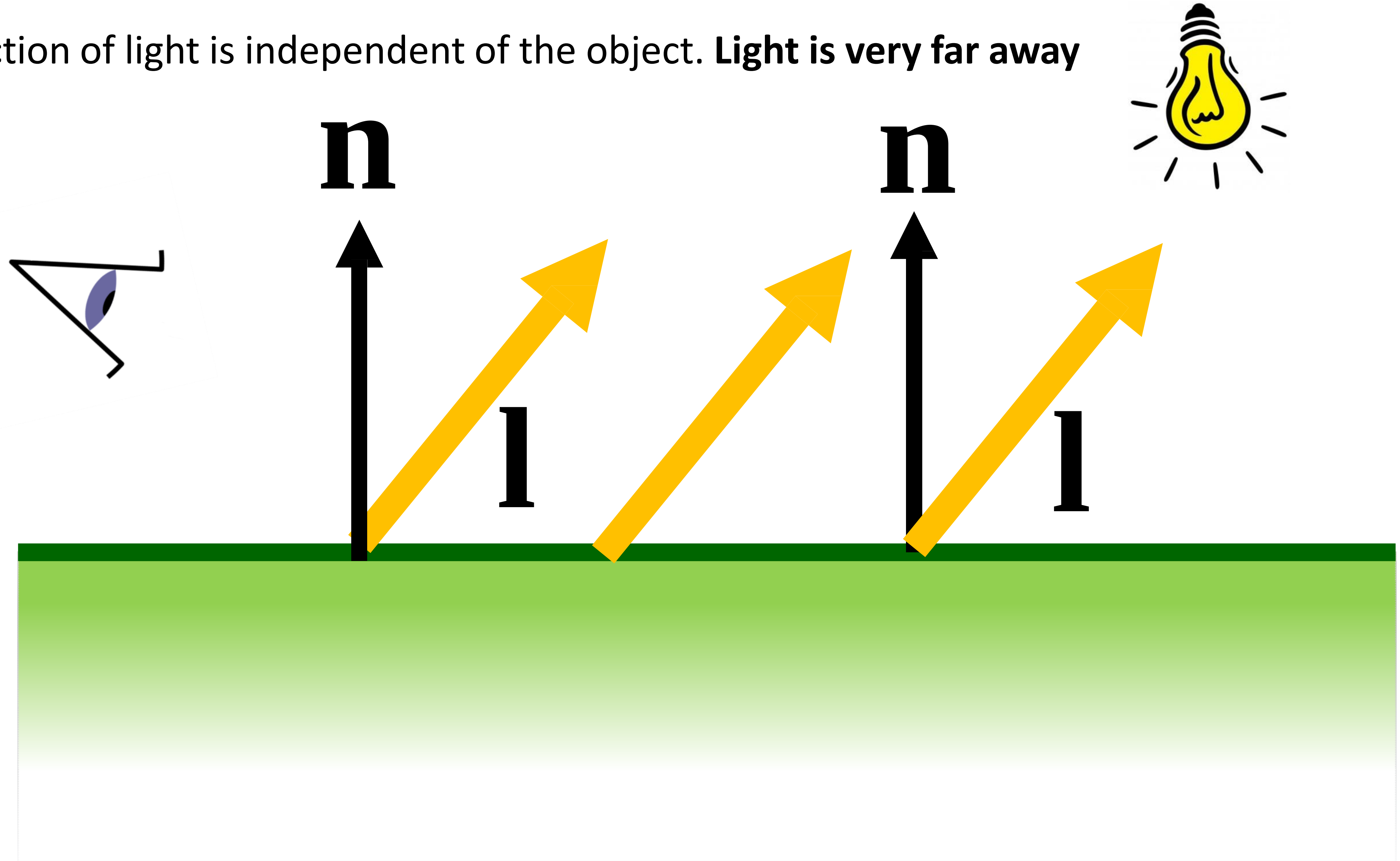


Light and Surfaces



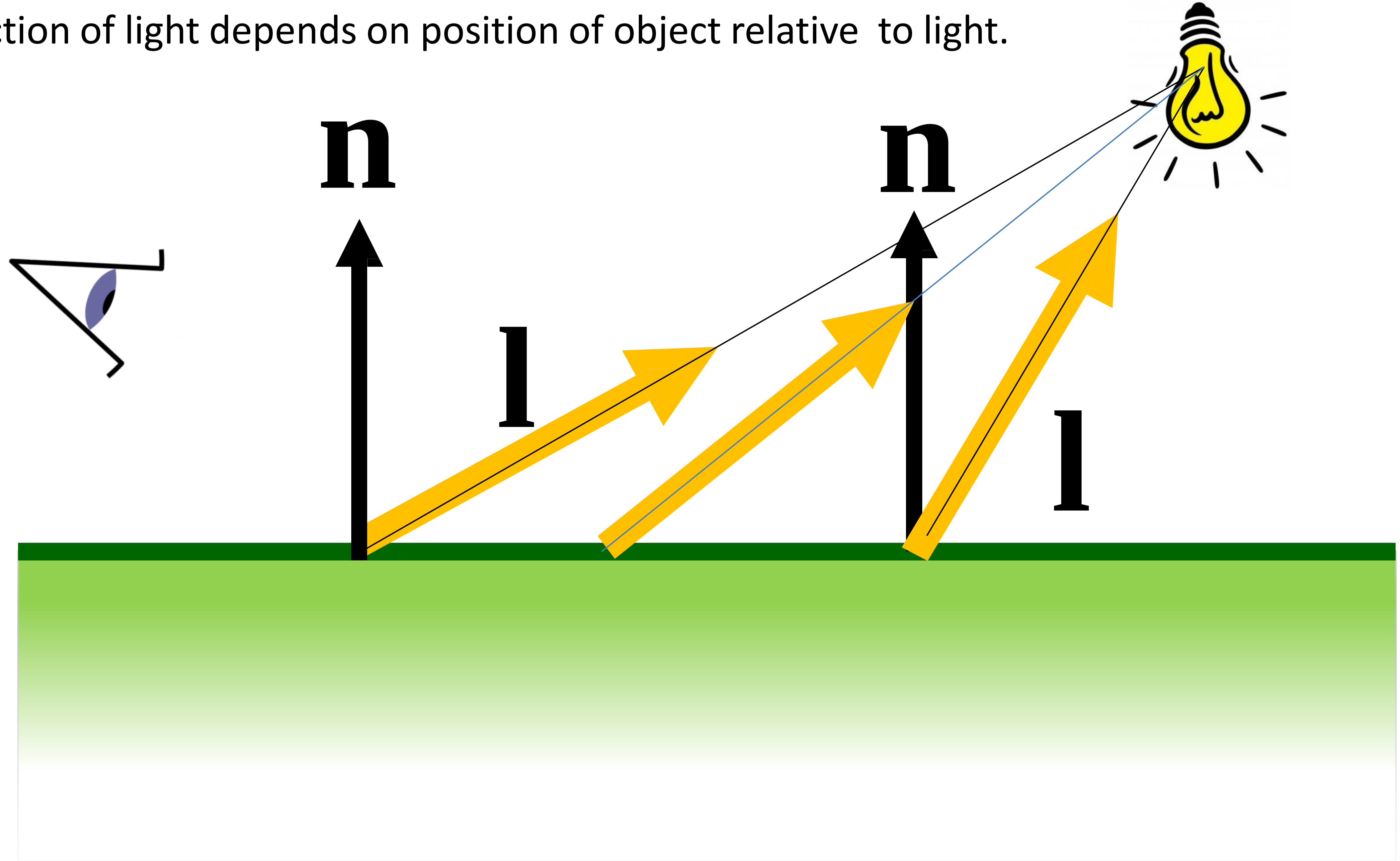
Directional Light

Direction of light is independent of the object. **Light is very far away**



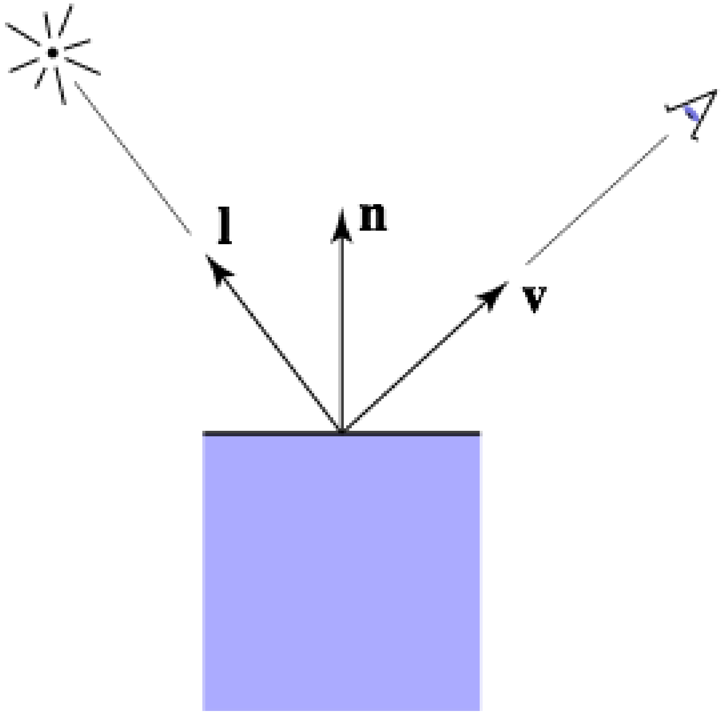
Point Light

Direction of light depends on position of object relative to light.



Shading

- Compute light reflected toward camera
- Inputs:
  - – eye direction
  - – light direction
    (for each of many lights)
  - – surface normal
  - – surface parameters
    (color, shininess, …)



Computing the Normal at a Hit Point

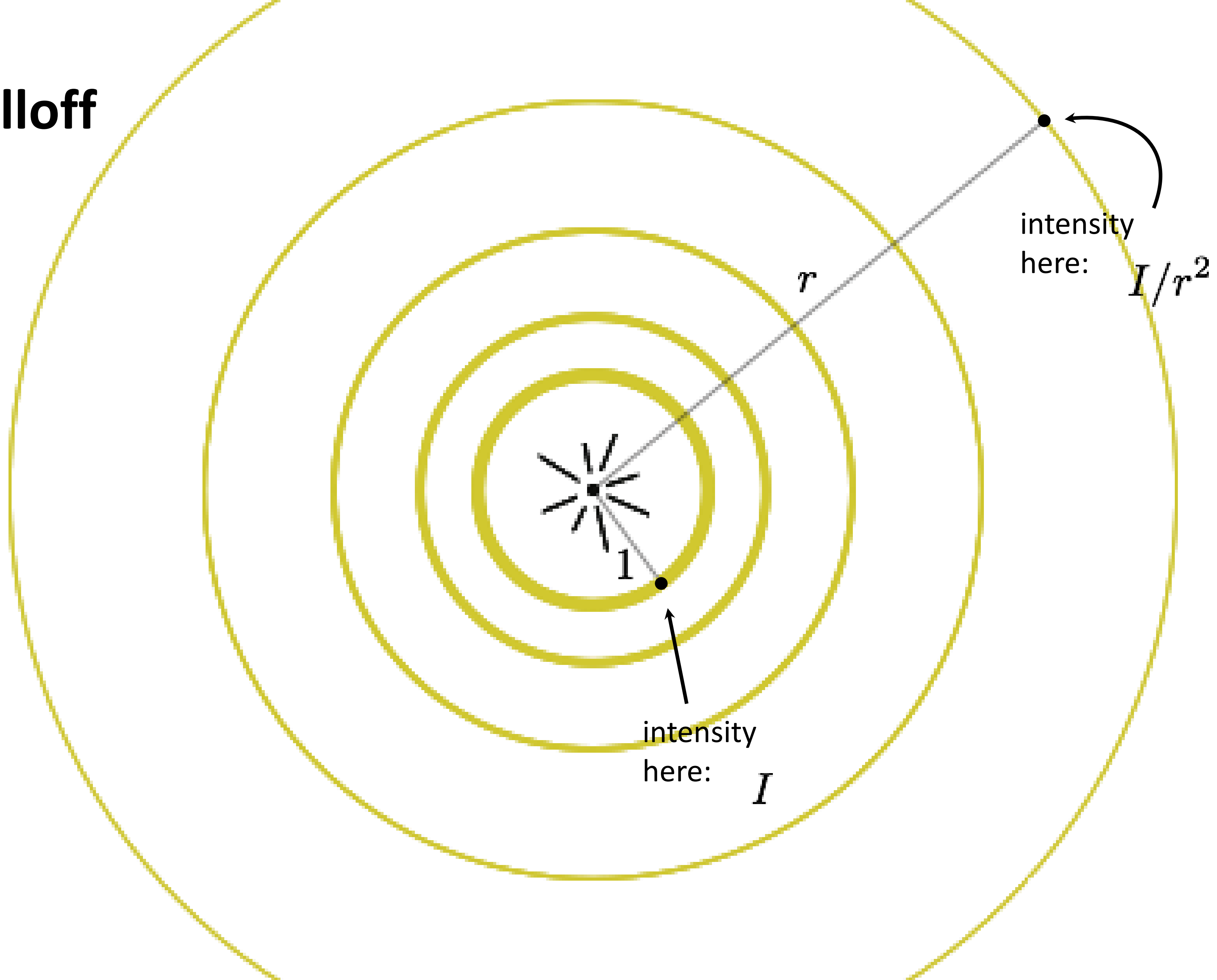
- Polygon normal: cross product of two non-collinear edges.
- Implicit surface normal $f(p)=0$:

  $$gradient(f)(p).$$

- Explicit parametric surface $f(a,b)$:

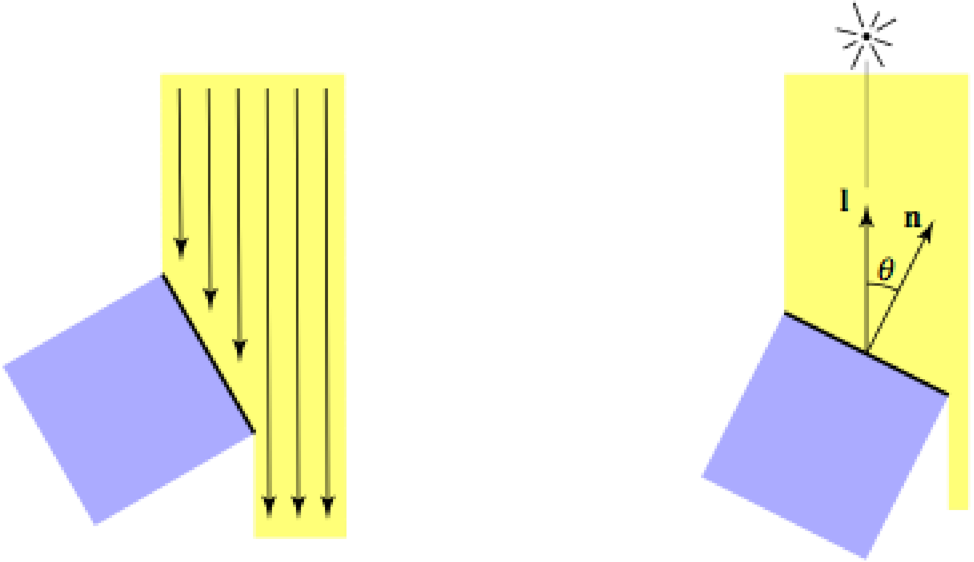
  $$\delta f(s,b)/ \delta s \ X \ \delta f(a,t)/ \delta t.$$

Light falloff



Diffuse reflection

- Light is scattered uniformly in all directions
  - the surface color is the same for all viewing directions
- Lambert's cosine law



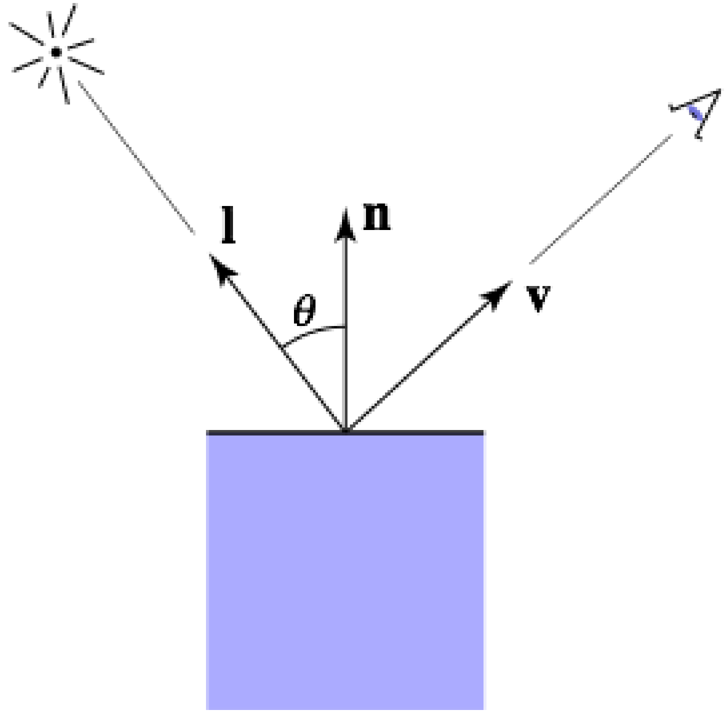
Top face of cube receives a certain amount of light

Top face of 60º rotated cube intercepts half the light

In general, light per unit area is proportional to $\boxed{\cos\theta = l \bullet n}$

Lambertian shading

Shading independent of view direction



illumination from source

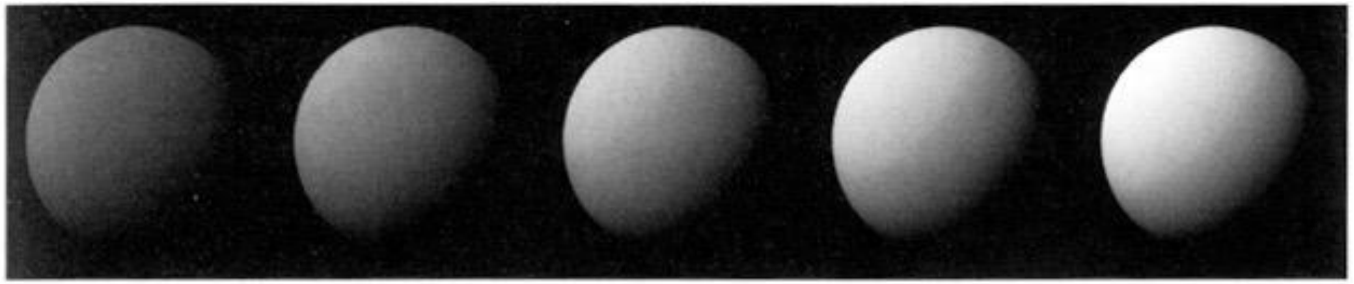
$$L_d = k_d\,(I/r^2)\max(0, \mathbf{n}\cdot\mathbf{l})$$

diffusely reflected light

diffuse coefficient

Lambertian shading

Produces a matte appearance



$k_d \longrightarrow$

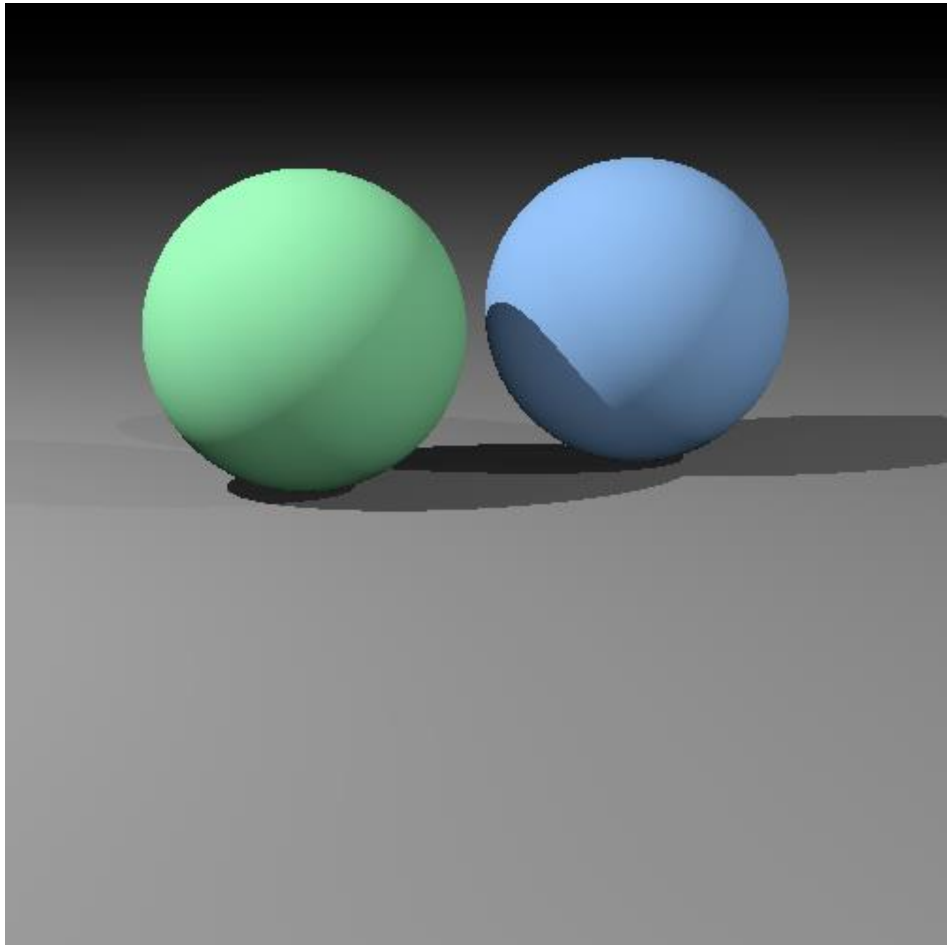


Image without shading

```
for 0 <= iy < ny
    for 0 <= ix < nx
   {
        ray = camera.getRay(ix, iy);
        firstSurface = scene.intersect(result,ray);
        if (firstSurface)
            image.set(ix, iy, firstSurface.color);
        else
            image.set(ix, iy, background.color);
    }
```

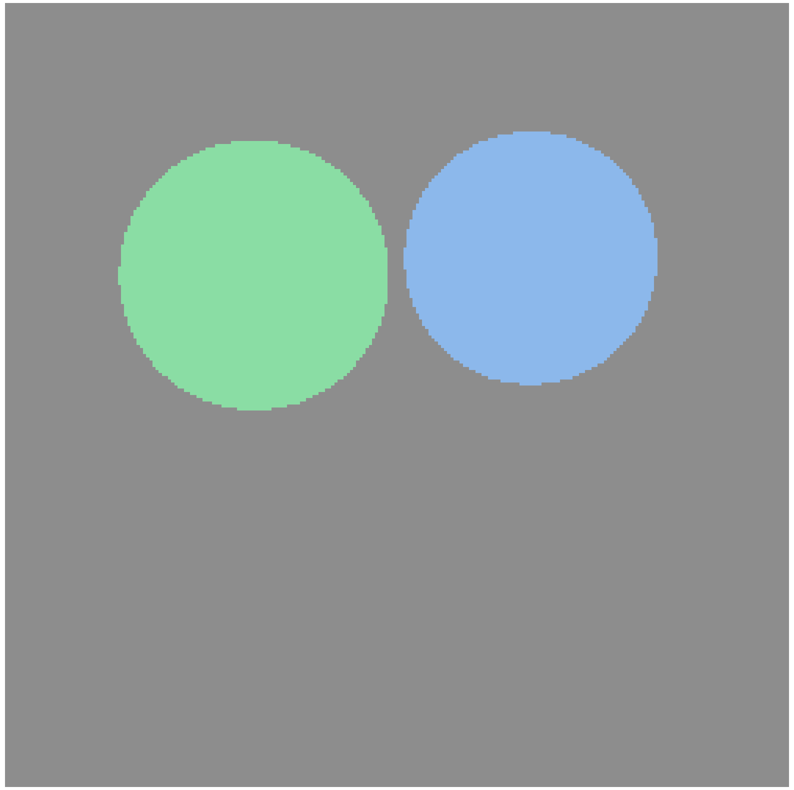
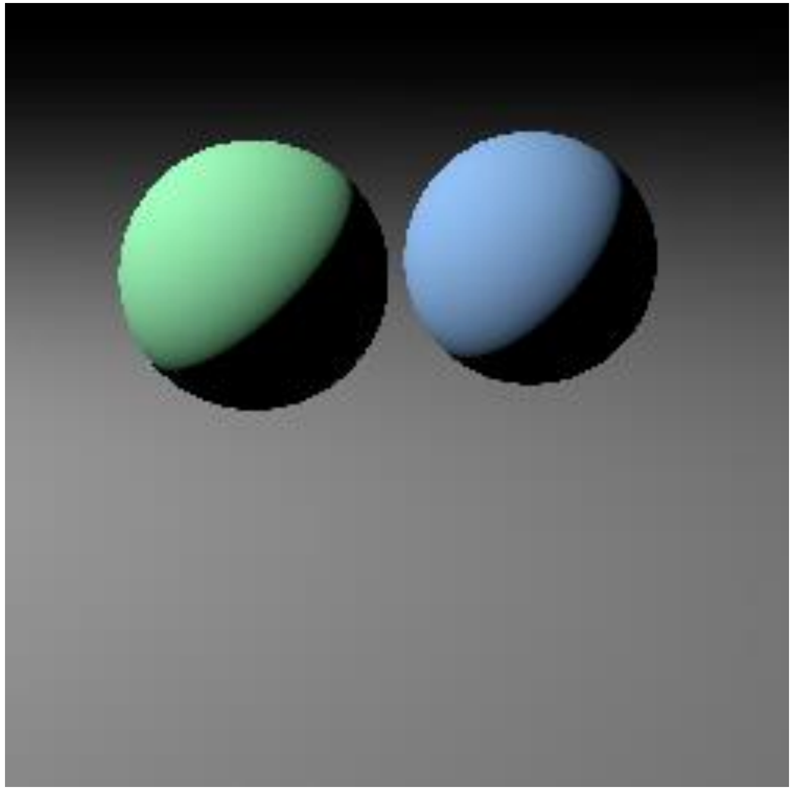


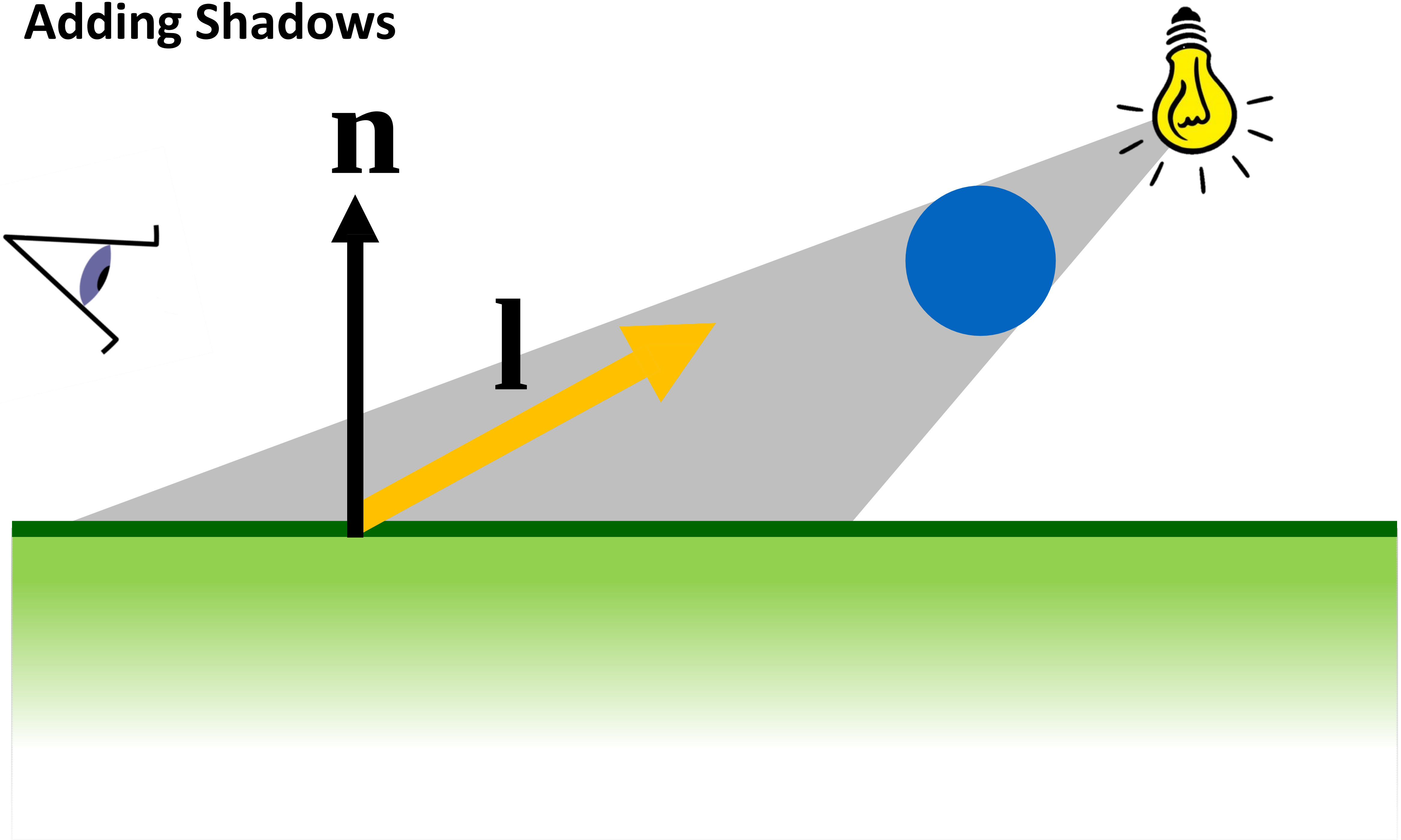
Image with shading

```
for 0 <= iy < ny
   for 0 <= ix < nx
  {
      ray = camera.getRay(ix, iy);
      firstSurface = scene.intersect(result,ray);
      image.set(ix, iy,
               firstSurface.shade(ray,light,result.point,
                        result.normal);
      else
         image.set(ix, iy, background.color);
   }
```



```
Surface.shade(ray,light,point,normal) {
            l=light.pos-position;
            it= surface.k*light.intensity*max(0,normal.l);
            return surface.color*it;
}
```

Adding Shadows

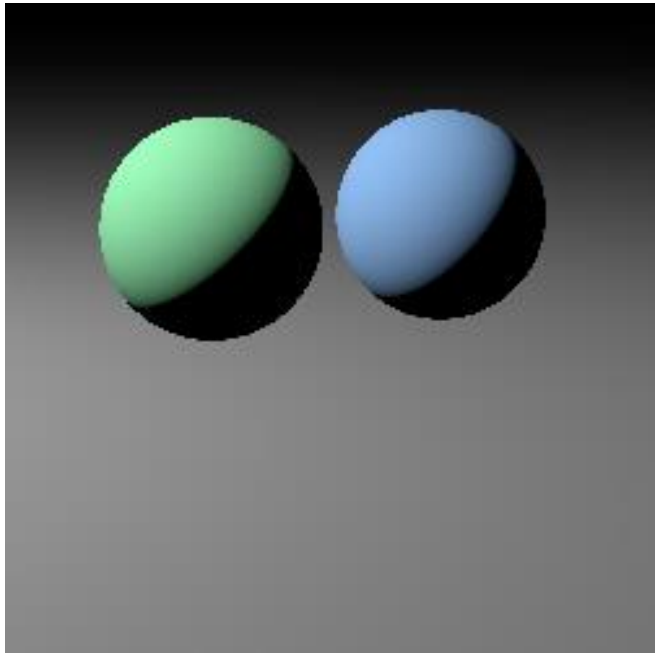


Shadows

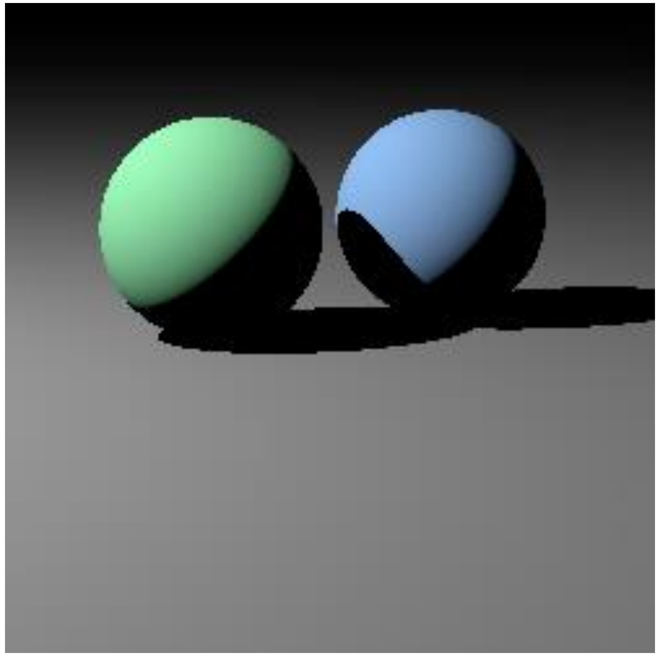
- Surface is only illuminated if nothing blocks its view of the light.
- With ray tracing it's easy to check if a point in the scene is in shadow.

  just shoot a ray from the point to the light and intersect it with the scene!

```
Surface.shade(ray,light,point,normal) {
        l=light.pos-position;
        shadowray=(point,l);
        if  !scene.intersect(result,shadowray)
        {
            it= surface.k*light.intensity*
                    max(0,normal.l);
            return surface.color*it;
        }
        else
            return black;
}
```



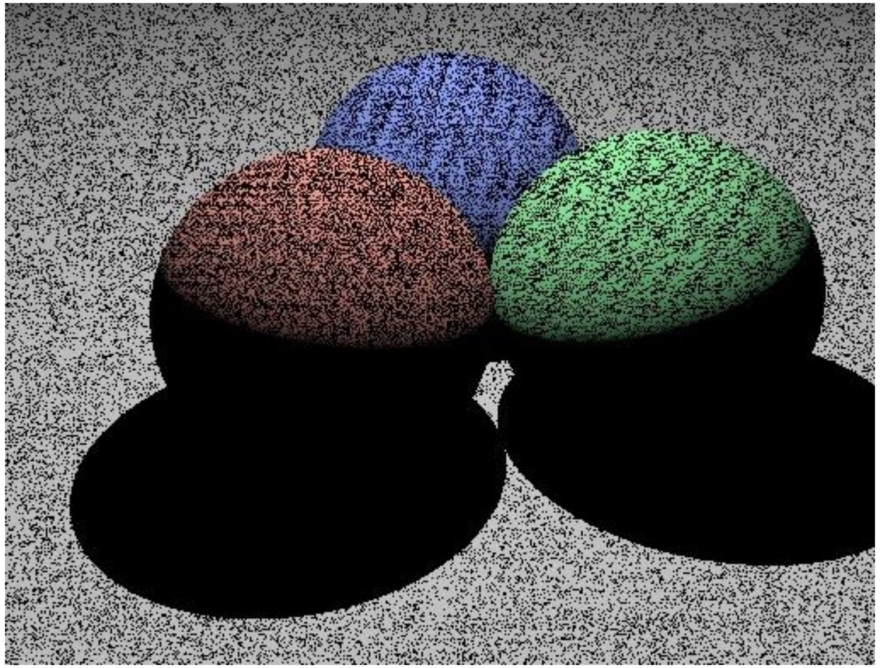
Without shadows



With shadows

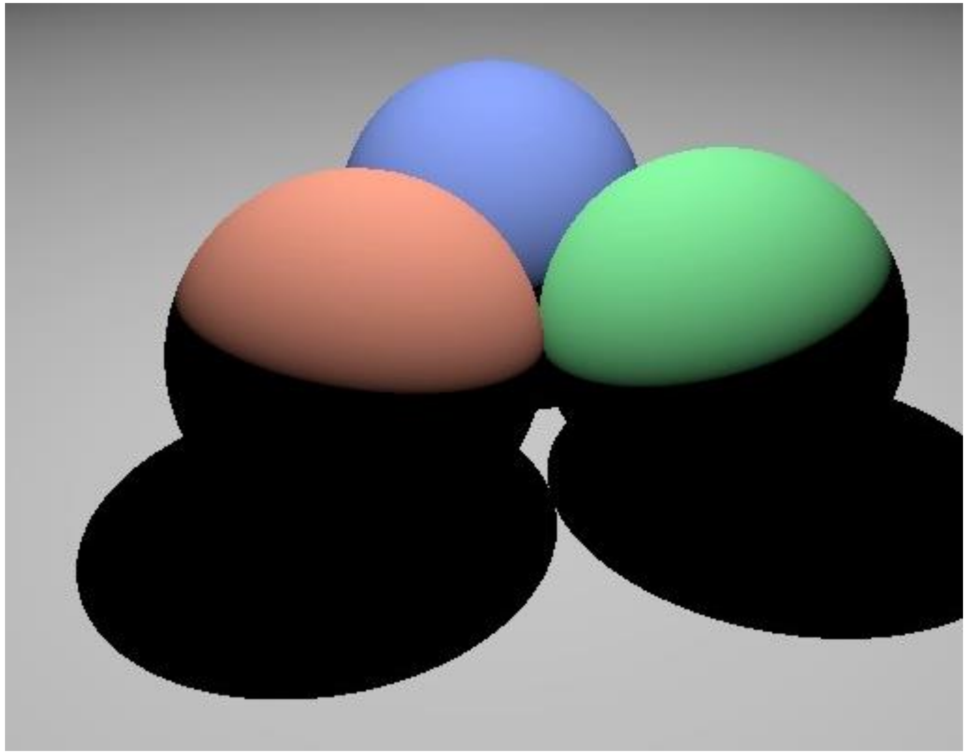
Classic shadow error

What's going on?



Classic shadow error

Start shadow rays just outside surface



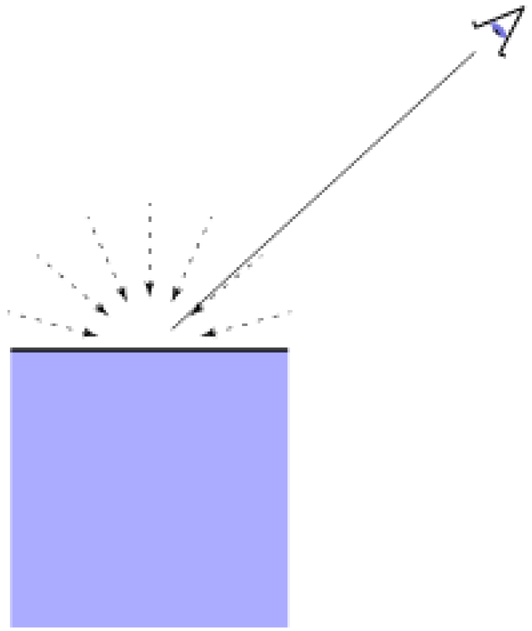
Multiple lights

- Important to fill in black shadows
- Just loop over lights, add contributions
- Ambient shading
  - black shadows are not really right
  - one solution: dim light at camera
  - alternative: add a constant “ambient” color to the shading…

Ambient shading

Shading that does not depend on anything

– add constant color to account for disregarded illumination and fill in black shadows



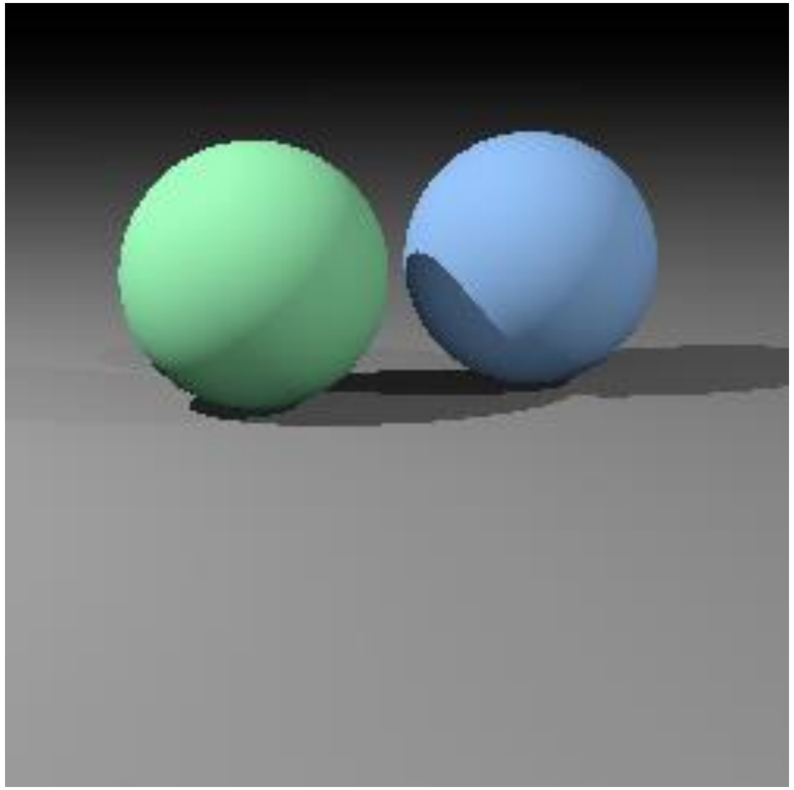
$$L_a = k_a \, I_a$$

ambient coefficient

reflected ambient light

Image with multiple lights

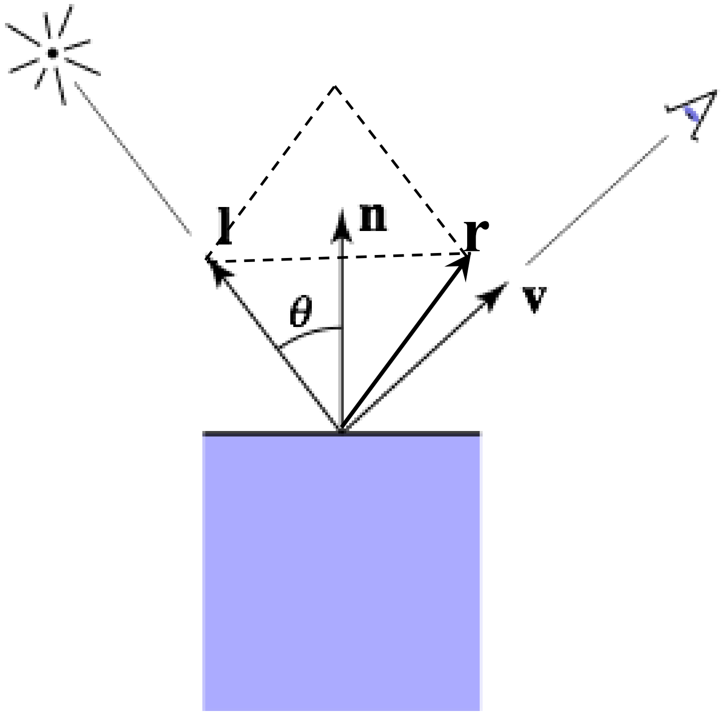
```
shade(ray, lights, point, normal) {
   result = ambient;
   for light in lights {
         l=light.pos-position;
         shadowray=(point+ε*normal,l);
         if  !scene.intersect(result,shadowray)
         {
              it= surface.k*light.intensity*max(0,normal.l);
              result+= surface.color*it;
         }
   }
   return result;
}
```



Mirror reflection

Intensity depends on view direction

– reflects incident light from mirror direction

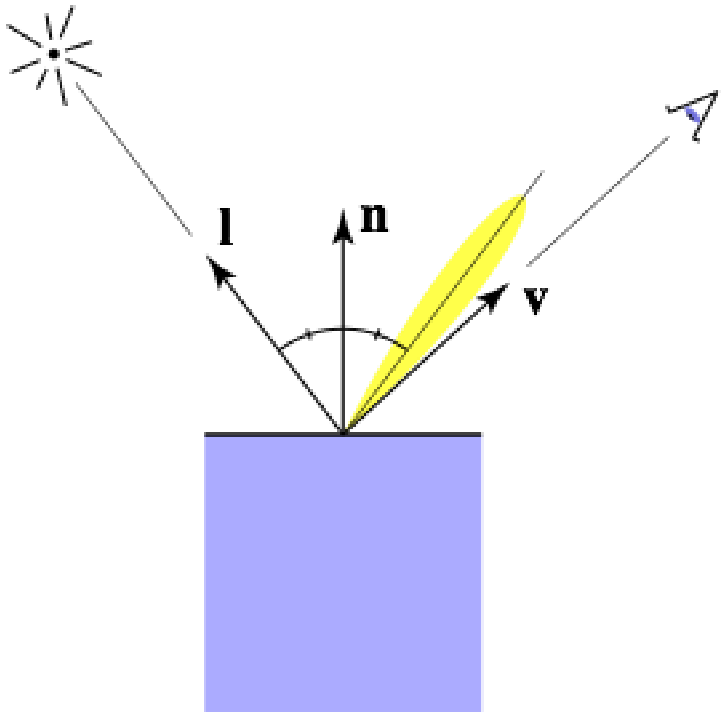


$$\mathbf{r} = 2(\mathbf{n}.\mathbf{l})\mathbf{n} - \mathbf{l}$$

Specular shading (Phong)

Intensity depends on view direction

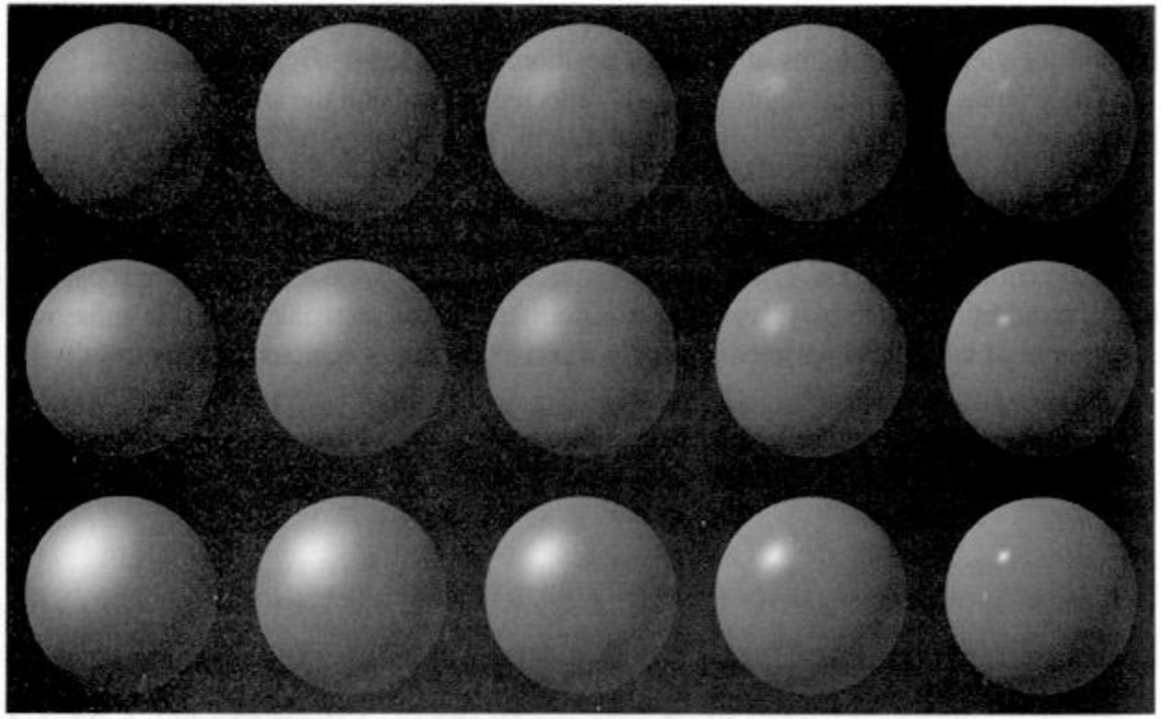
– bright near mirror configuration $k_s * I_s * \boxed{(\boldsymbol{v} \cdot \boldsymbol{r})^{shiny}}$



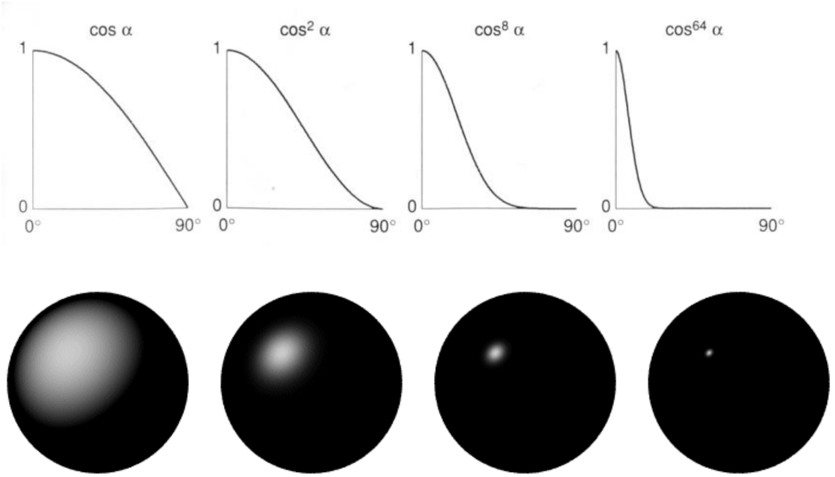
Phong model

Increasing *shiny* narrows the lobe

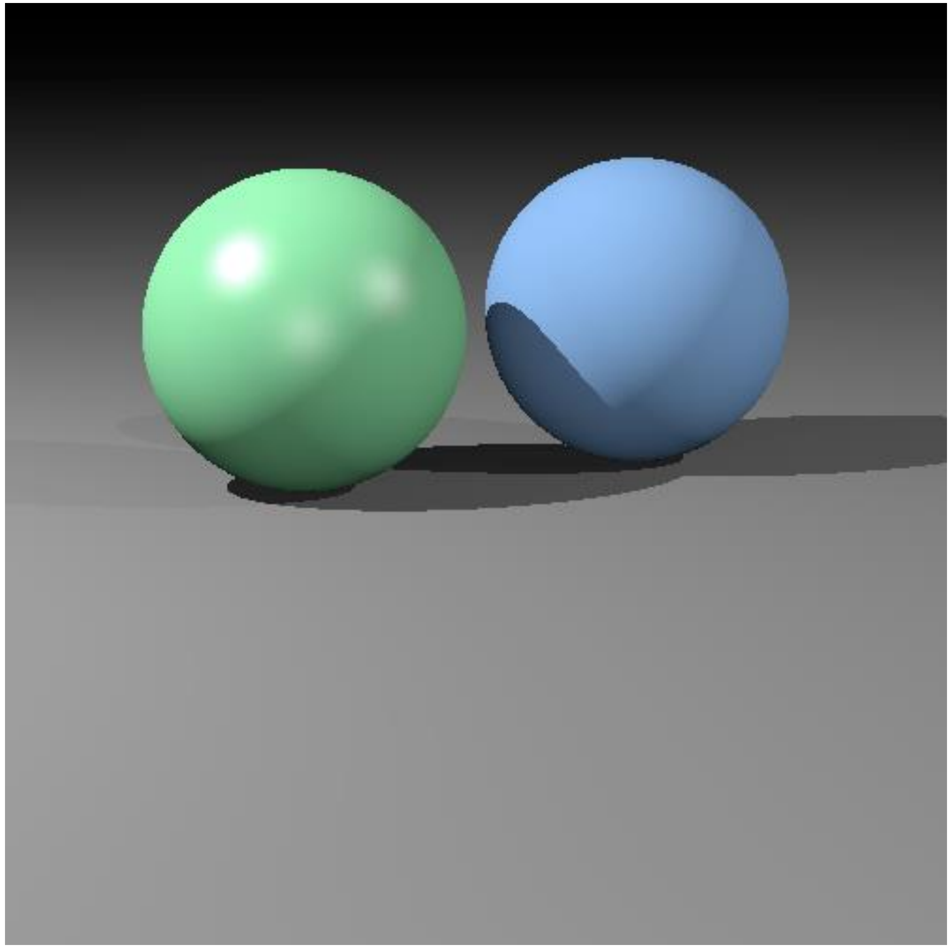
k_s



shiny

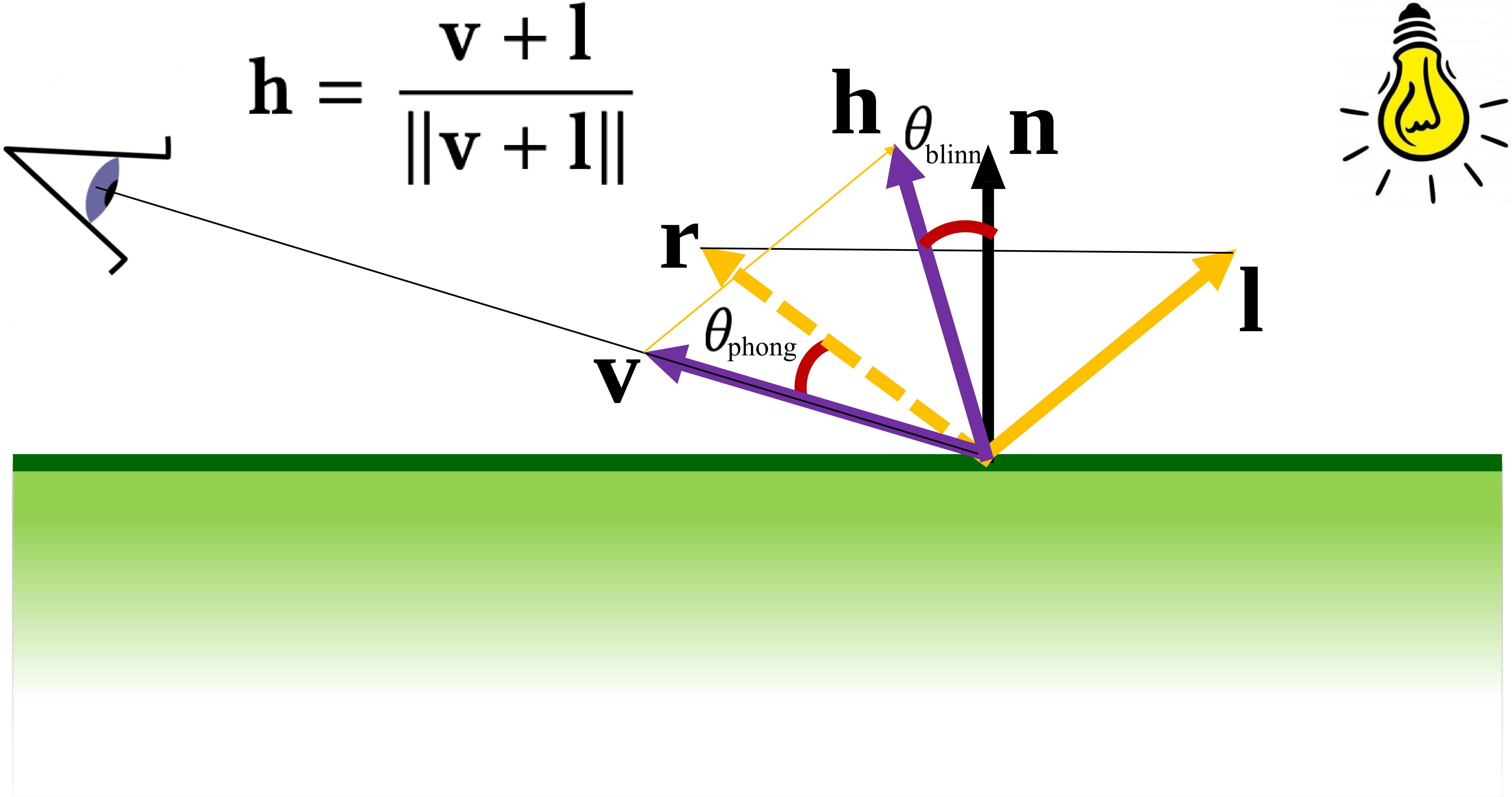


Diffuse + Specular (Phong) shading

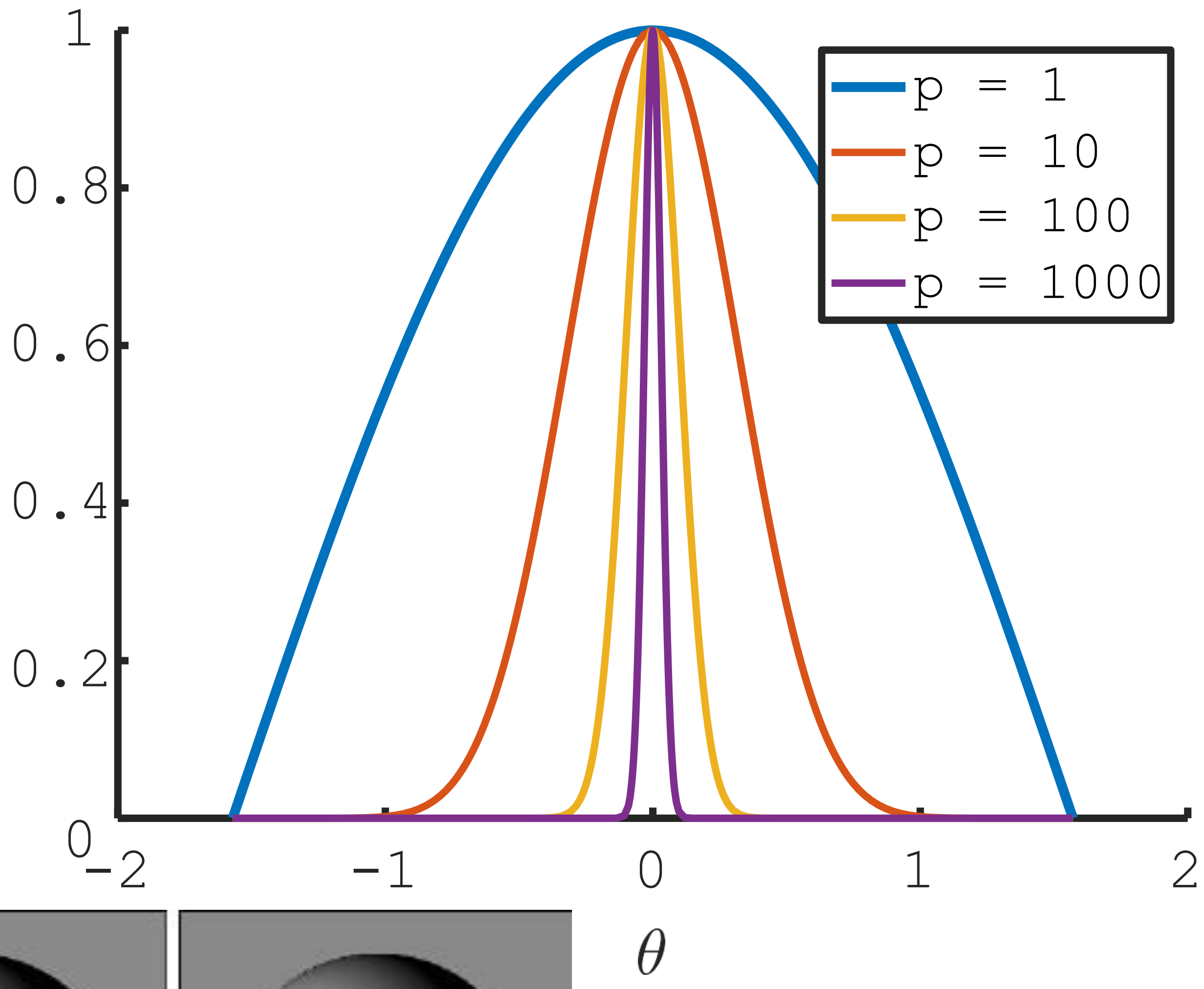


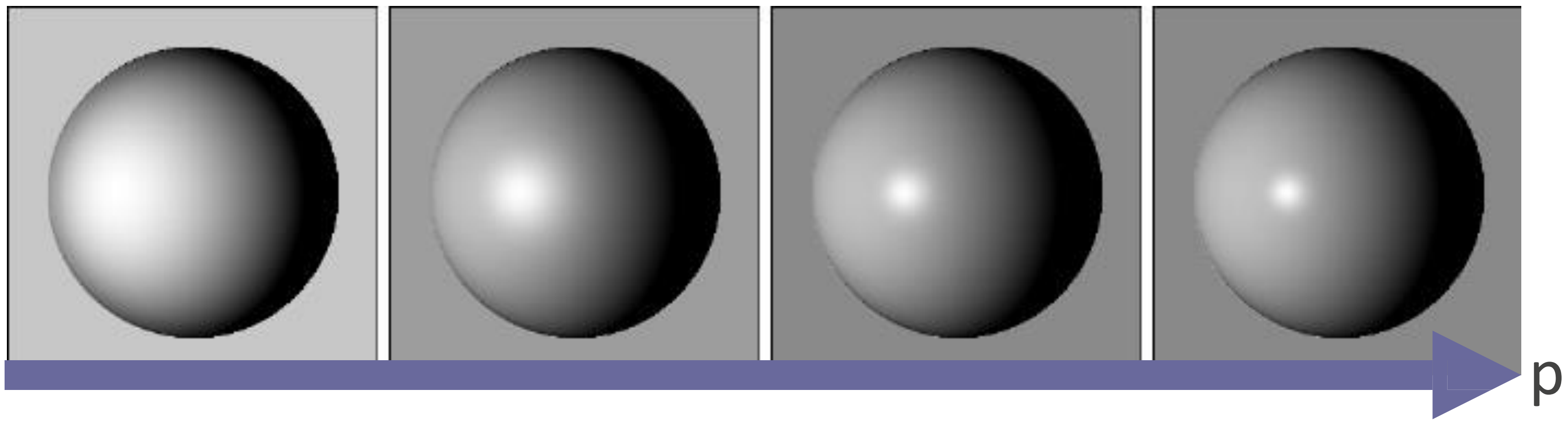
Specular Shading (Blinn)

$$\mathbf{h} = \frac{\mathbf{v} + \mathbf{l}}{\|\mathbf{v} + \mathbf{l}\|}$$

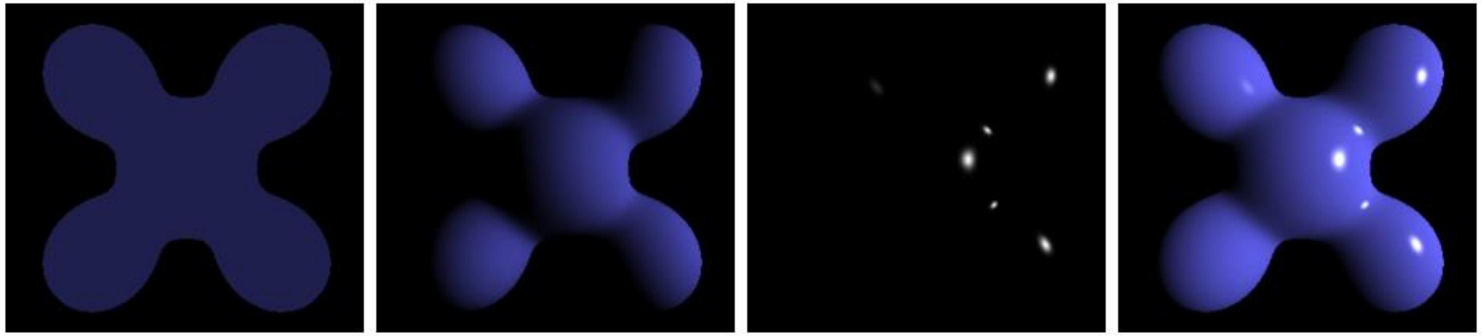


$$L = k_s \, I \, \max(0, \mathbf{n} \cdot \mathbf{h})^p$$





Local Illumination



- Usually include ambient, diffuse, Phong in one model

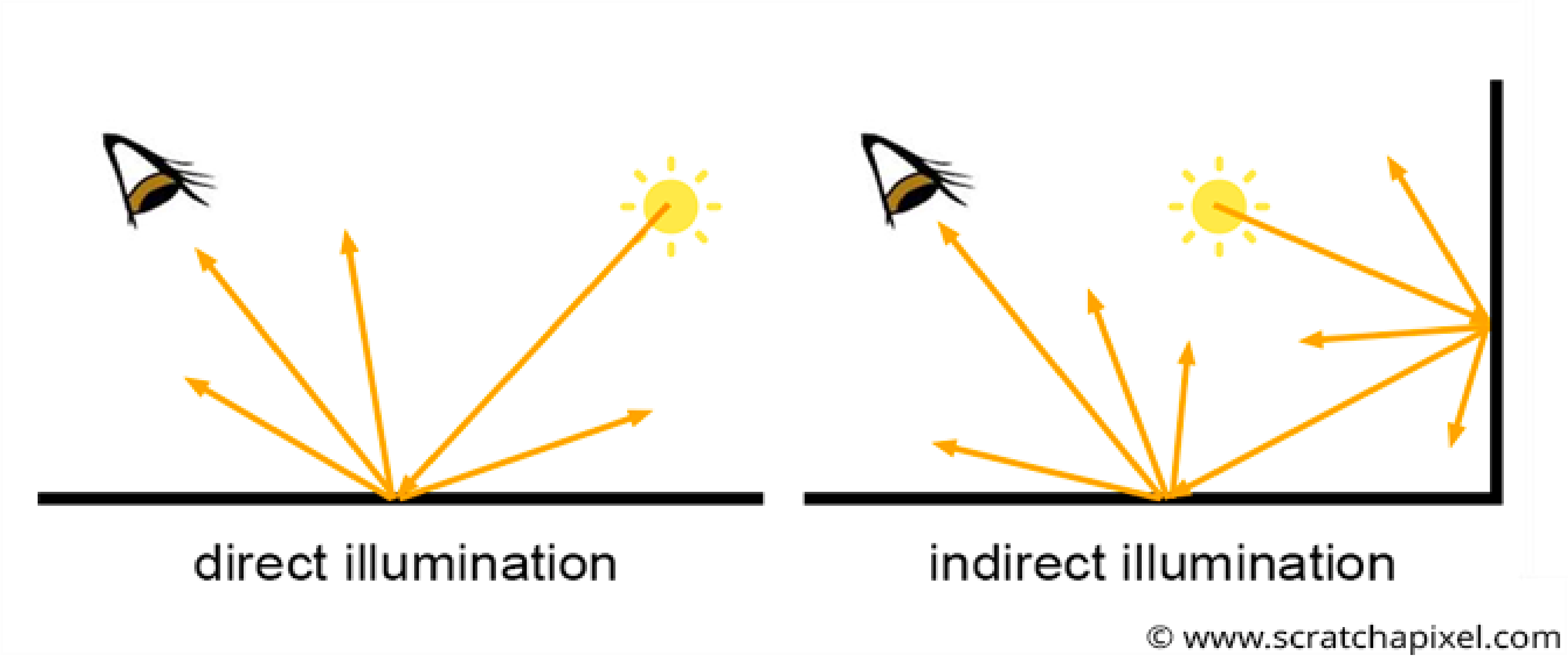
$$
\begin{aligned}
L &= L_a + L_d + L_s \\
&= k_a\, I_a + k_d\,(I/r^2)\max(0, \mathbf{n}\cdot\mathbf{l}) + k_s\,(I/r^2)\max(0, \mathbf{n}\cdot\mathbf{h})^p
\end{aligned}
$$

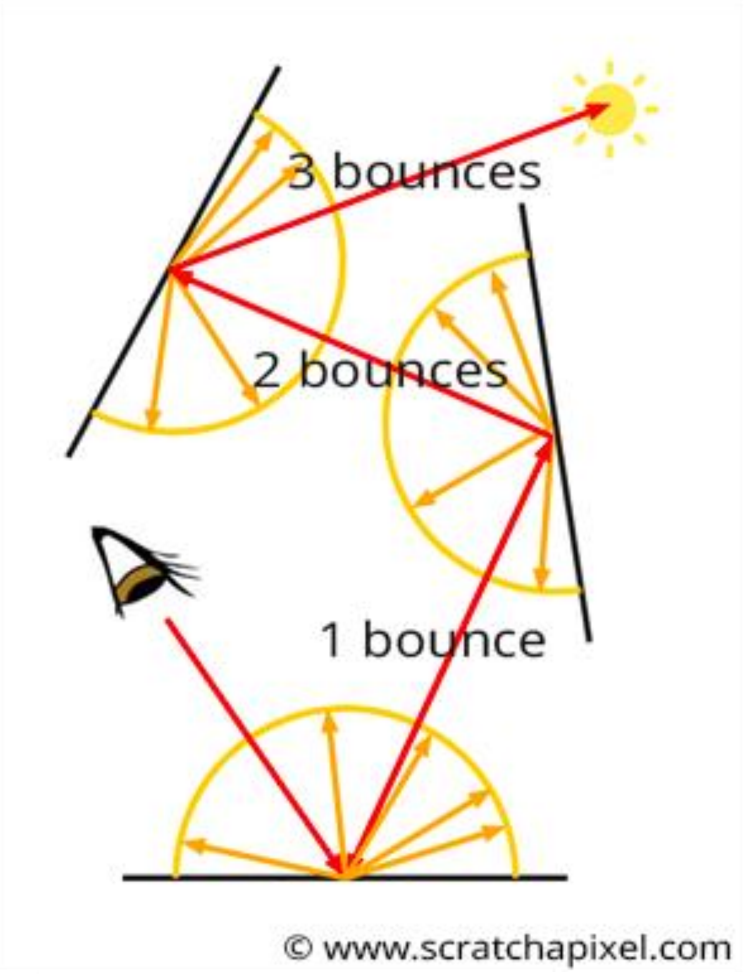
- The final result is the sum over many lights

$$
L = L_a + \sum_{i=1}^{N} \left[(L_d)_i + (L_s)_i\right]
$$

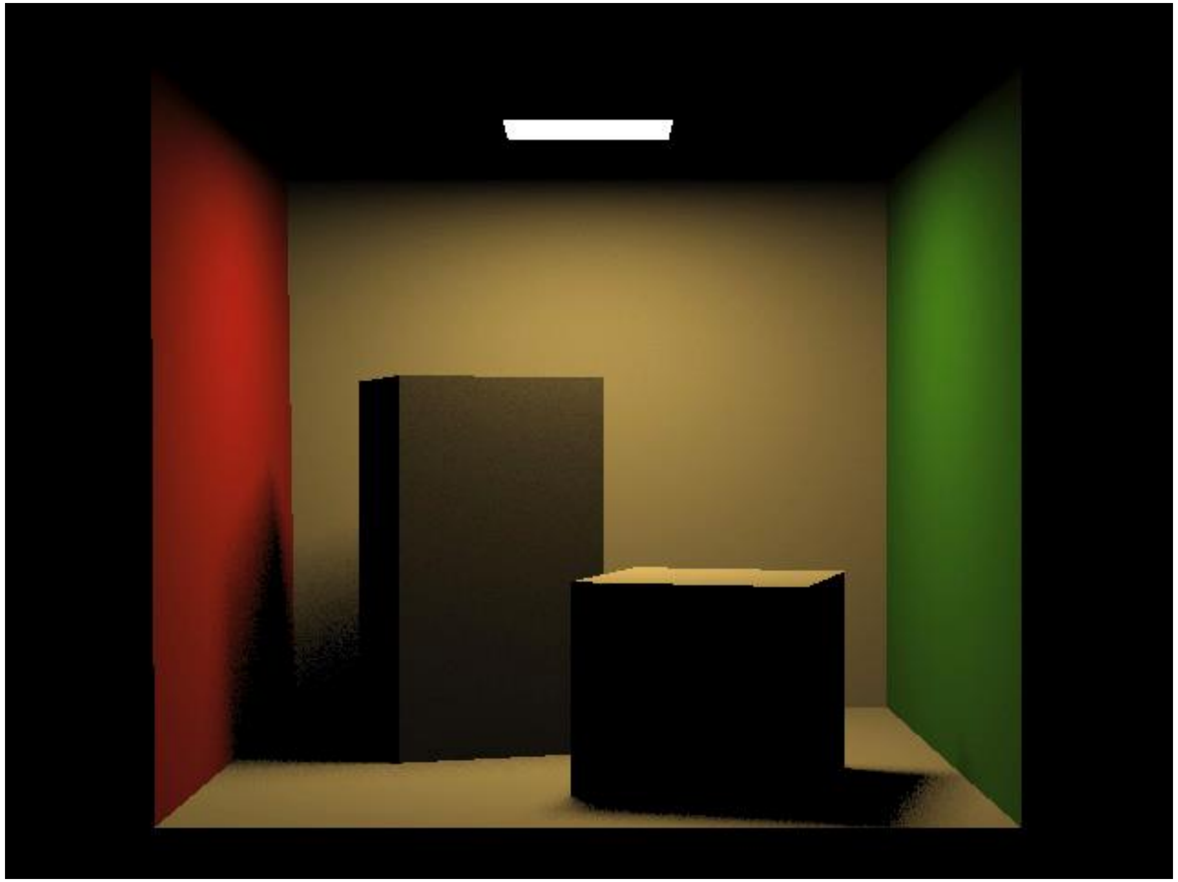
$$
\begin{aligned}
L = k_a\, I_a + \sum_{i=1}^{N} \Big[& k_d\,(I_i/r_i^2)\max(0, \mathbf{n}\cdot\mathbf{l}_i) + \\
& k_s\,(I_i/r_i^2)\max(0, \mathbf{n}\cdot\mathbf{h}_i)^p \Big]
\end{aligned}
$$

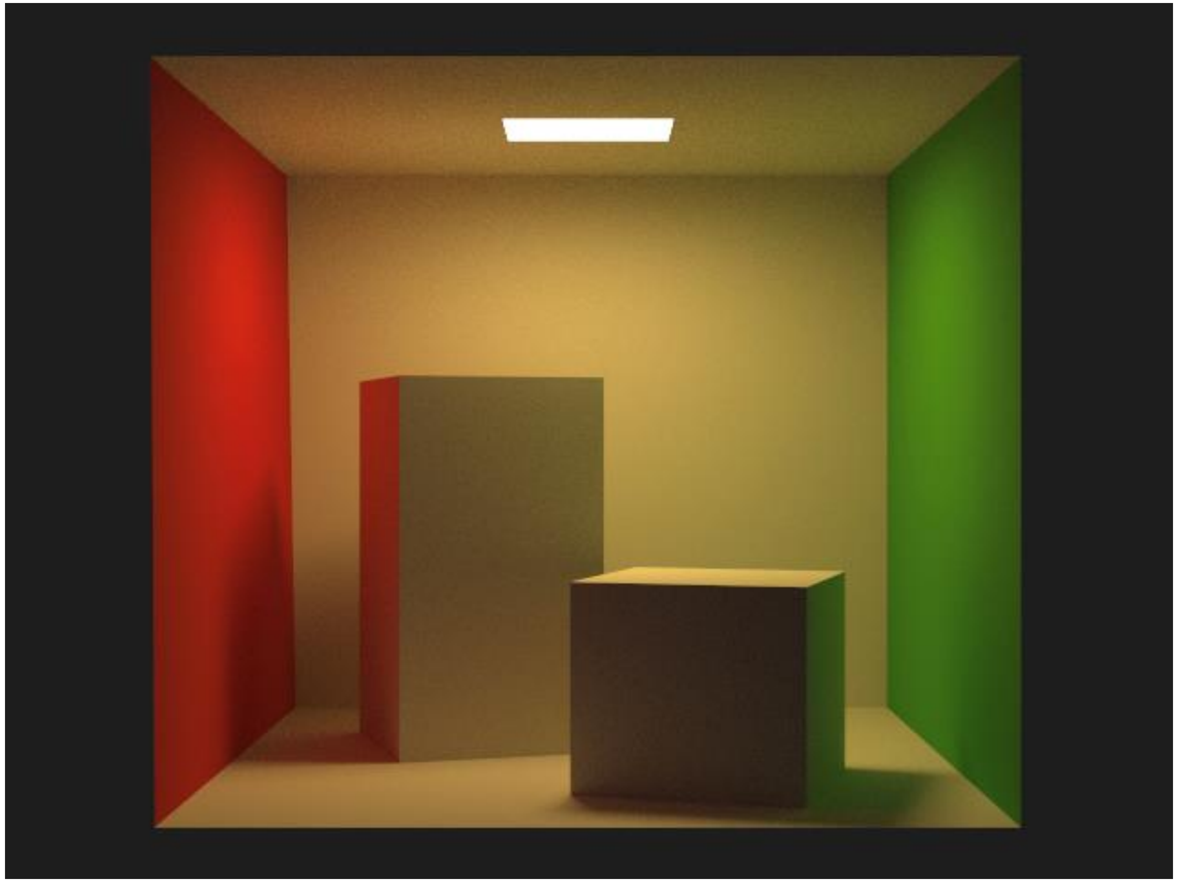
Direct Illumination
…no Global Effects so far





Direct vs. Indirect Illumination





http://www.deluxerender.com/2017/01/the-cornell-box-a-renderers-rite-of-pathage/
https://en.wikipedia.org/wiki/Cornell_box

Local vs. Global Illumination

Local Illumination Models

- e.g. Phong, Blinn.
- Model source from a light reflected once off a surface towards the eye.
- Indirect light is included with an ad hoc “ambient” term which is normally constant across the scene.

Global Illumination Models

- e.g. recursive ray tracing (incomplete model).
- Try to measure light propagation in the scene.
- Model interaction between objects, other objects, and their environment

Path Tracing

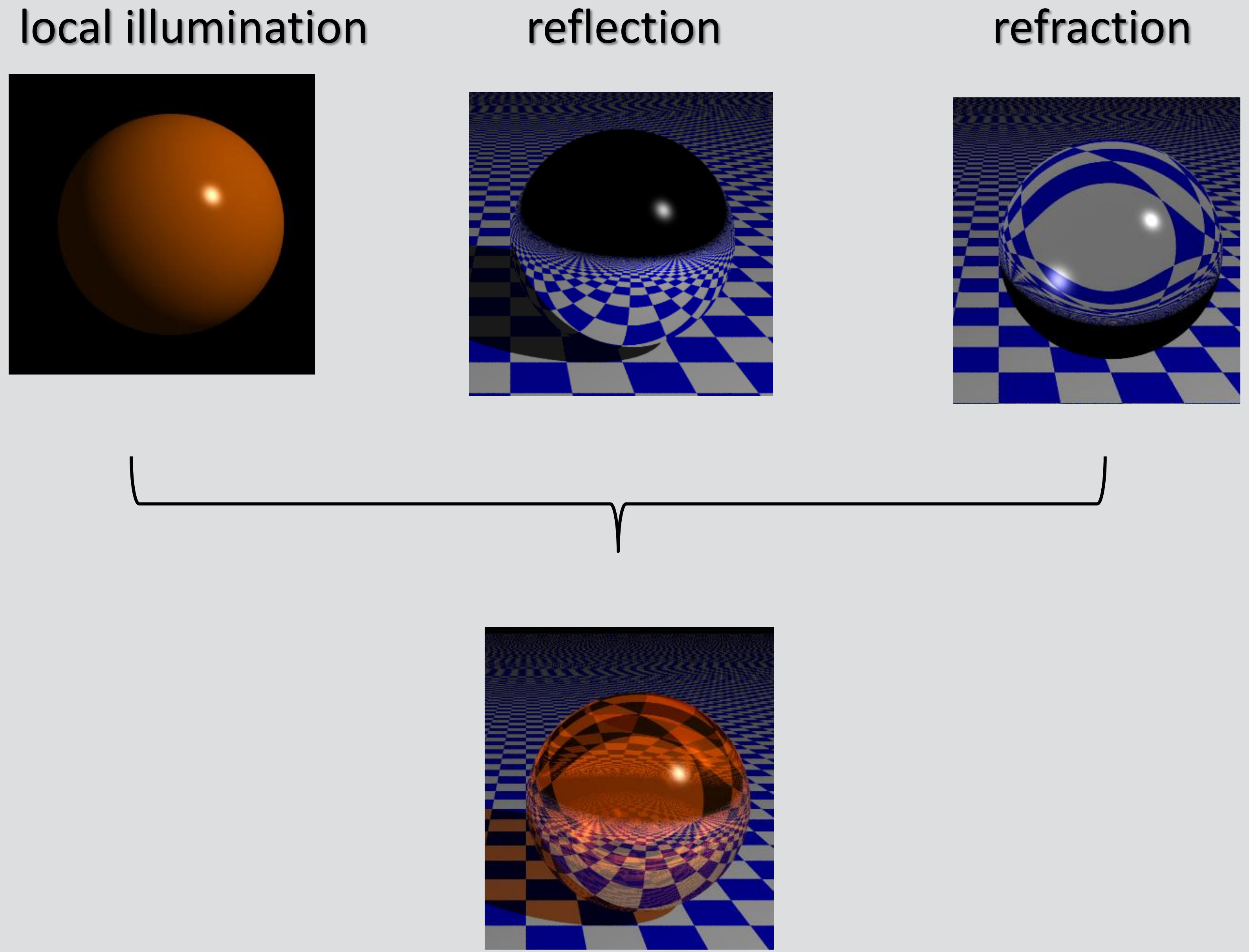
- A ray from a light L can bounce of any number of specular S and diffuse objects D before entering the eye E. The paths from E to L for eg. can be

  E-D-L, E-S-D-D-S-S-D-S-L, E-D-D-S-D-S-L…

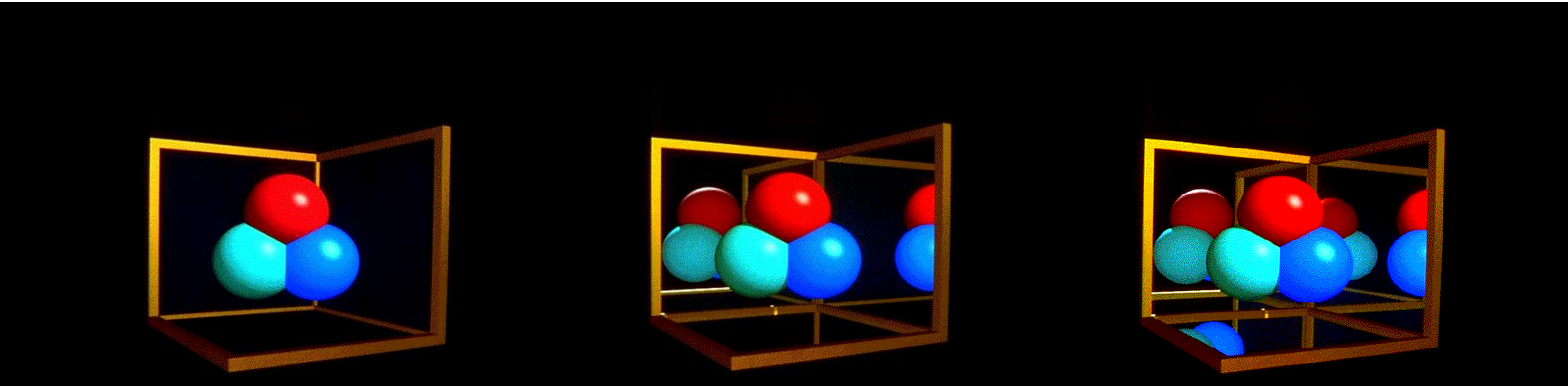
- Rays are infinitely thin
- Don’t disperse

- Ray Tracing model shiny objects exhibiting multiple reflections, i.e. paths of the form

  $E - S^{*} - D^{+} – L$.

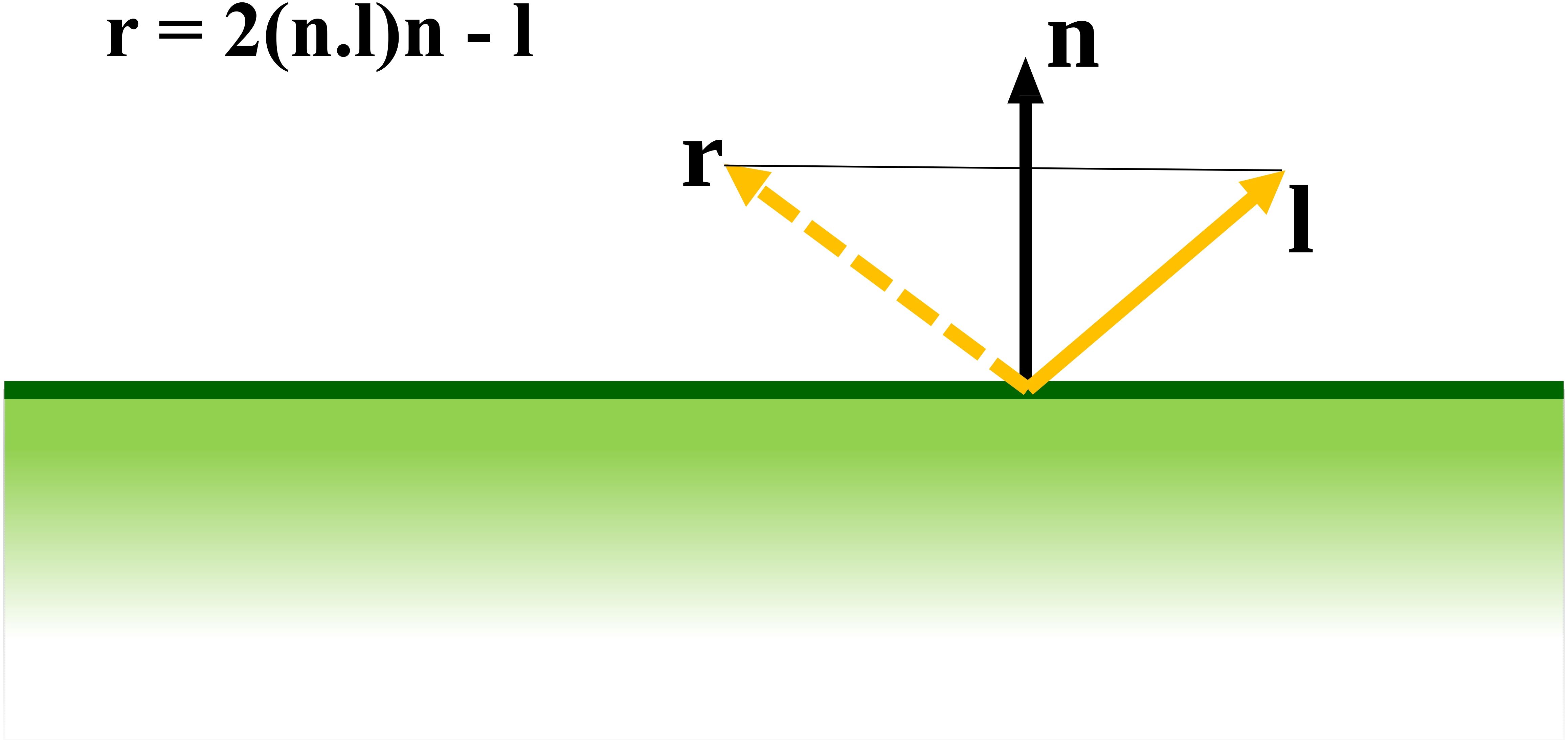

local illumination
reflection
refraction

Ray Tracing recursion



Reminder: reflected ray

$$r = 2(n.l)n - l$$



Ray Tracing

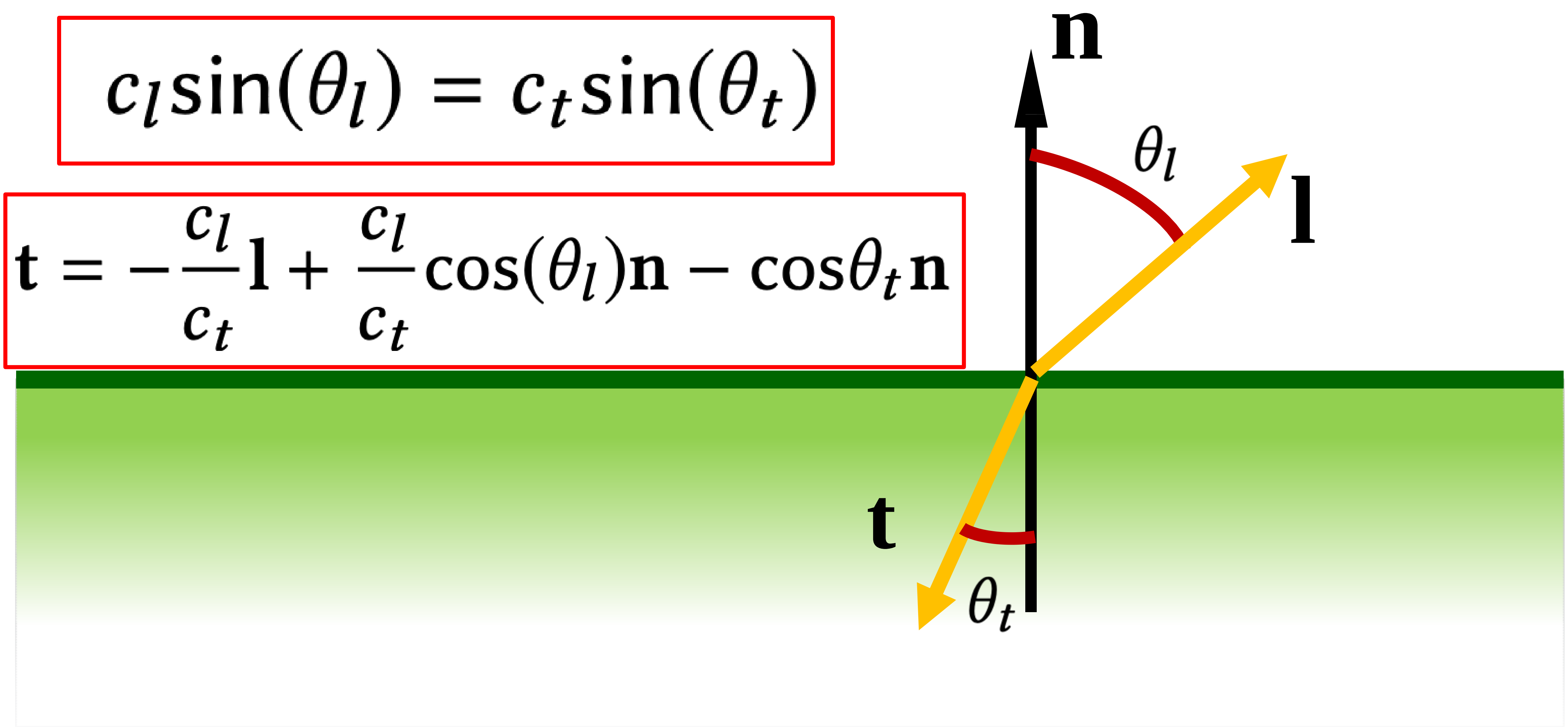
```
for each pixel in the image {
      pixel colour = rayTrace(viewRay, 0)
}
```

```
colour rayTrace(Ray, depth) {
      for each object in the scene {
            if(Intersect ray with object) {
                  colour = shading model
                  if(depth < maxDepth)
                  colour +=rayTrace(reflectedRay,depth+1)
            }
      }
      return colour
}
```

Refraction (Snell's Law)

$$\boxed{c_l \sin(\theta_l) = c_t \sin(\theta_t)}$$

$$\boxed{\mathbf{t} = -\frac{c_l}{c_t}\mathbf{l} + \frac{c_l}{c_t}\cos(\theta_l)\mathbf{n} - \cos\theta_t \mathbf{n}}$$



Refraction (Snell's Law)

$$\boxed{c_l \sin(\theta_l) = c_t \sin(\theta_t)}$$

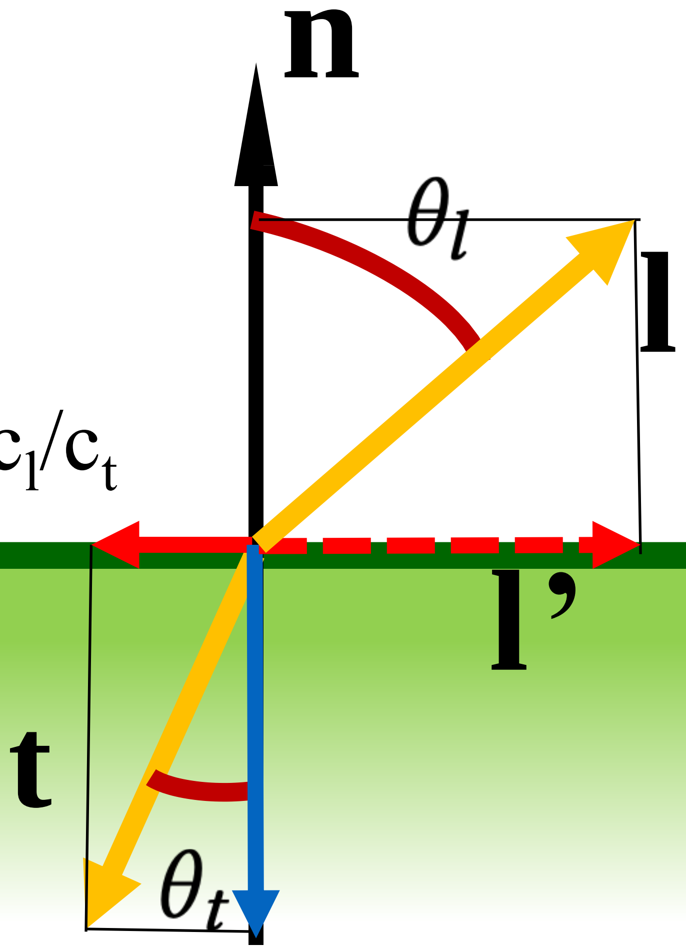
$$\mathbf{t} = \boxed{-\frac{c_l}{c_t}\mathbf{l} + \frac{c_l}{c_t}\cos(\theta_l)\mathbf{n}}\;\boxed{-\cos\theta_t\,\mathbf{n}}$$

$\theta_t = \sin^{-1}(c_l/c_t \sin(\theta_l))$

$\mathbf{l} = \mathbf{l'} + \cos\theta_l \mathbf{n} \Rightarrow \mathbf{-l'} = \mathbf{-l} + \cos\theta_l \mathbf{n}$

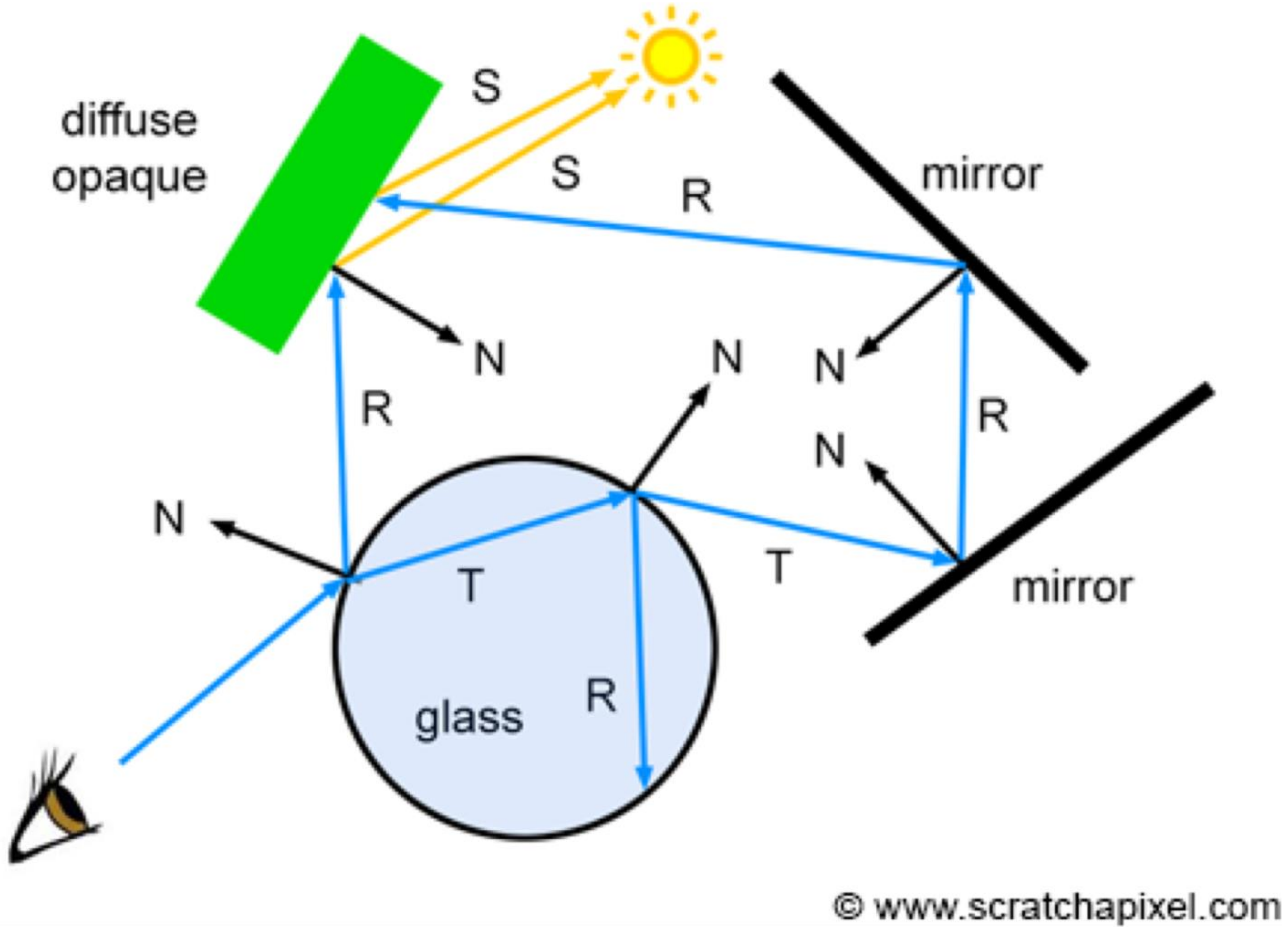
$\mathbf{t'} = (||\mathbf{t'}||/||\mathbf{l'}||)*(\mathbf{-l} + \cos\theta_l \mathbf{n})$

$||\mathbf{t'}|| = \sin\theta_t$, $||\mathbf{l'}|| = \sin\theta_l \Rightarrow ||\mathbf{t'}||/||\mathbf{l'}|| = c_l/c_t$



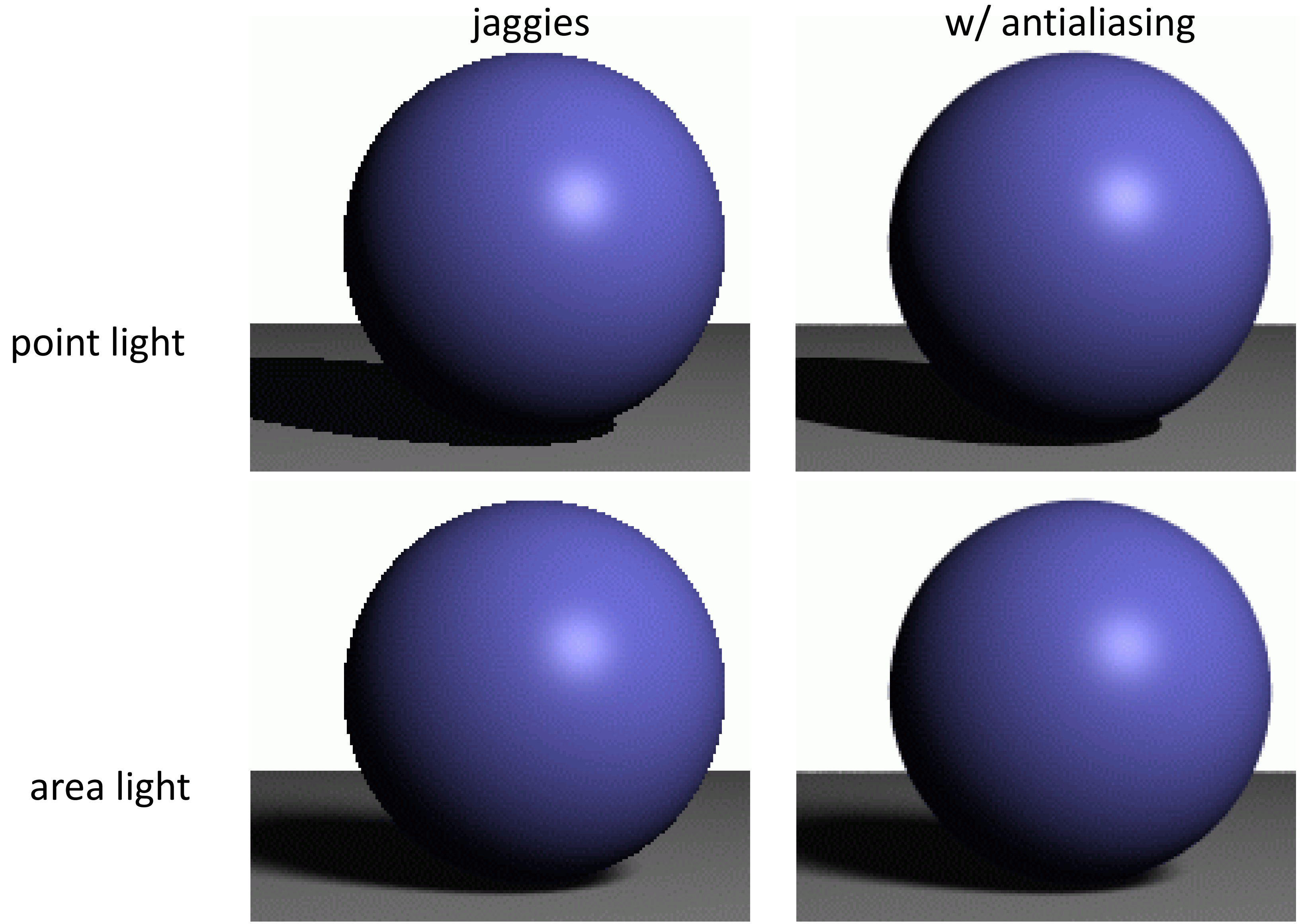
```
colour rayTrace(Ray, depth) {
    for each object in the scene {
        if(Intersect ray with object) {
            colour = shading model
            if(depth < maxDepth) {
                colour +=
                    rayTrace(reflectedRay,depth+1)
                colour +=
                    rayTrace(refractedRay,depth+1)
            }
        }
    }
    return colour
}
```

Ray Spawning



https://www.scratchapixel.com/lessons/3d-basic-rendering/ray-tracing-overview/light-transport-ray-tracing-whitted

Ray Tracing supersampling



Ray Tracing

- Unifies in one framework
  - Hidden surface removal
  - Shadow computation
  - Reflection of light
  - Refraction of light
  - Global **specular** interaction

Assignment #3 tasks

`PointLight::direction` in `src/PointLight.cpp`

Compute the direction to a point light source and its *parametric* distance from a query point.

`DirectionalLight::direction` in `src/DirectionalLight.cpp`

Compute the direction to a direction light source and its *parametric* distance from a query point (infinity).

`src/raycolor.cpp`

Make use of `first_hit.cpp` to shoot a ray into the scene, collect hit information and use this to return a color value.

`src/blinn_phong_shading.cpp`

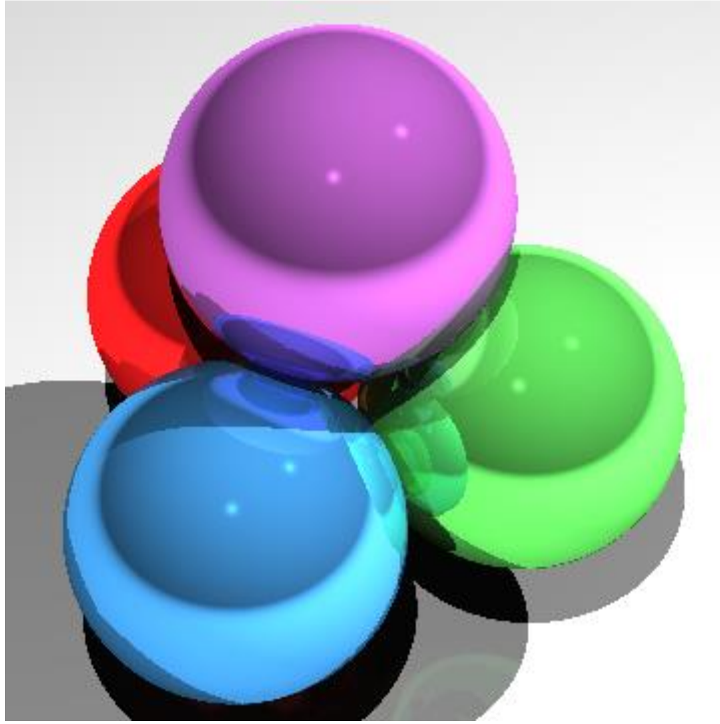
Compute the lit color of a hit object in the scene using Blinn-Phong shading model. This function should also shoot an additional ray to each light source to check for shadows.

`src/reflect.cpp`

Given an "incoming" vector and a normal vector, compute the mirror reflected "outgoing" vector.

`src/creative.json`

Be creative! Design a scene using any of the available Object types (spheres, planes, triangles, triangle soups), Light types (directional, point), Material parameters, colors (materials and/or lights), and don't forget about the camera parameters.

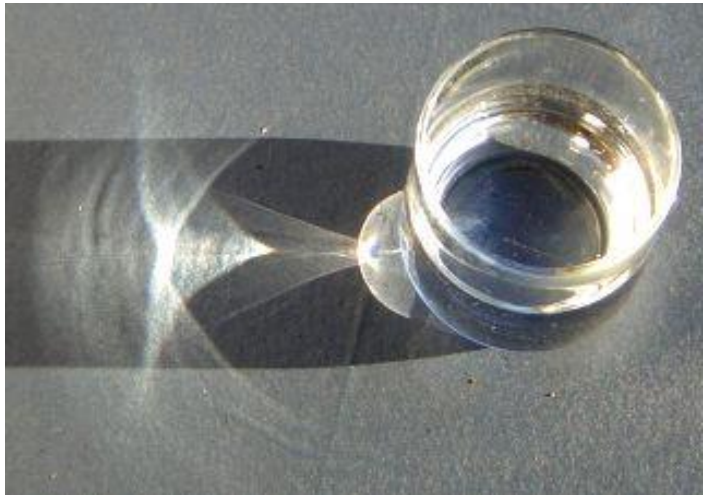


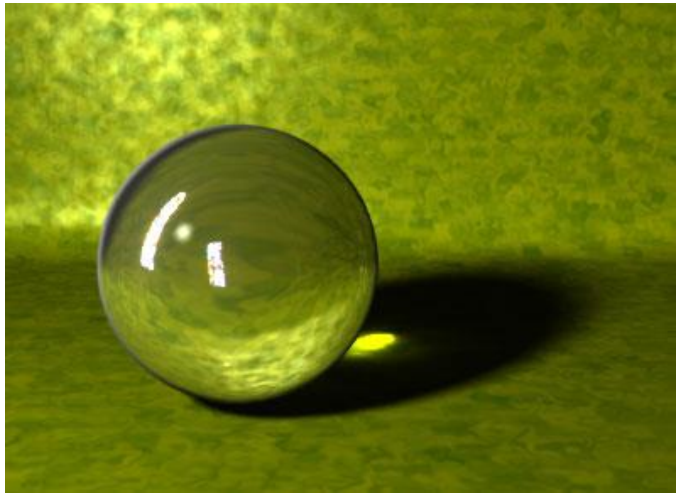
Ray Tracing Deficiencies

- Intersection computation time can be long (solution: **bounding volumes**).
- Recursive algorithm can lead to exponential complexity (solution: stochastic sampling).
- Ignores light transport mechanisms involving diffuse surfaces.

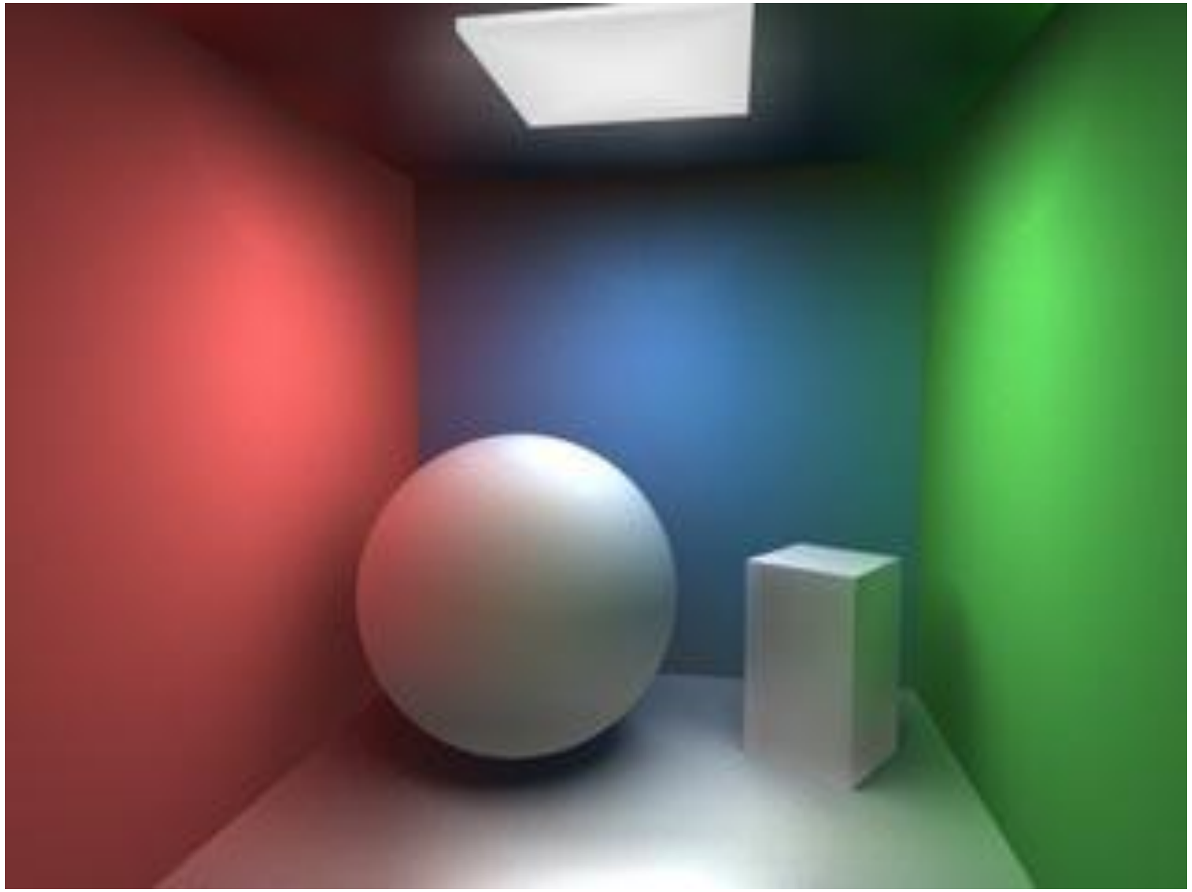
Ray Tracing Improvements: Caustics

- Transport E – S – S – S - D – S – S – S - L
- Trace from the light to the surfaces and then from the eye to the surfaces
- “shower” scene with light and then collect it
- “Where does light go?” vs “Where does light come from?”
- Good for caustics





Radiosity: E – D – D – D - L



The Rendering Equation

$$L_o(x, \vec{w}) = L_e(x, \vec{w}) + \int_\Omega f_r(x, \vec{w}', \vec{w}) L_i(x, \vec{w}')(\vec{w}' \cdot \vec{n}) \mathrm{d}\vec{w}'$$

scarier version found here: https://en.wikipedia.org/wiki/Rendering_equation
research paper found here: https://dl.acm.org/doi/10.1145/15886.15902

The Rendering Equation

$$\boxed{L_o(x, \vec{w})} = \boxed{L_e(x, \vec{w})} + \boxed{\int_\Omega f_r(x, \vec{w}', \vec{w}) L_i(x, \vec{w}')(\vec{w}' \cdot \vec{n}) \mathrm{d}\vec{w}'}$$

outgoing light at position **x** and direction **w**

emitted light at position **x** and direction **w**

and

reflected light at position **x** and direction **w**

The Rendering Equation

$$\boxed{L_o(x, \vec{w})} = \boxed{L_e(x, \vec{w})} + \boxed{\int_\Omega \boxed{f_r(x, \vec{w}', \vec{w})}\boxed{L_i(x, \vec{w}')}(\vec{w}' \cdot \vec{n})\mathrm{d}\vec{w}'}$$

the reflected light at position **x** and direction **w**

is the integral over all possible directions **w'**

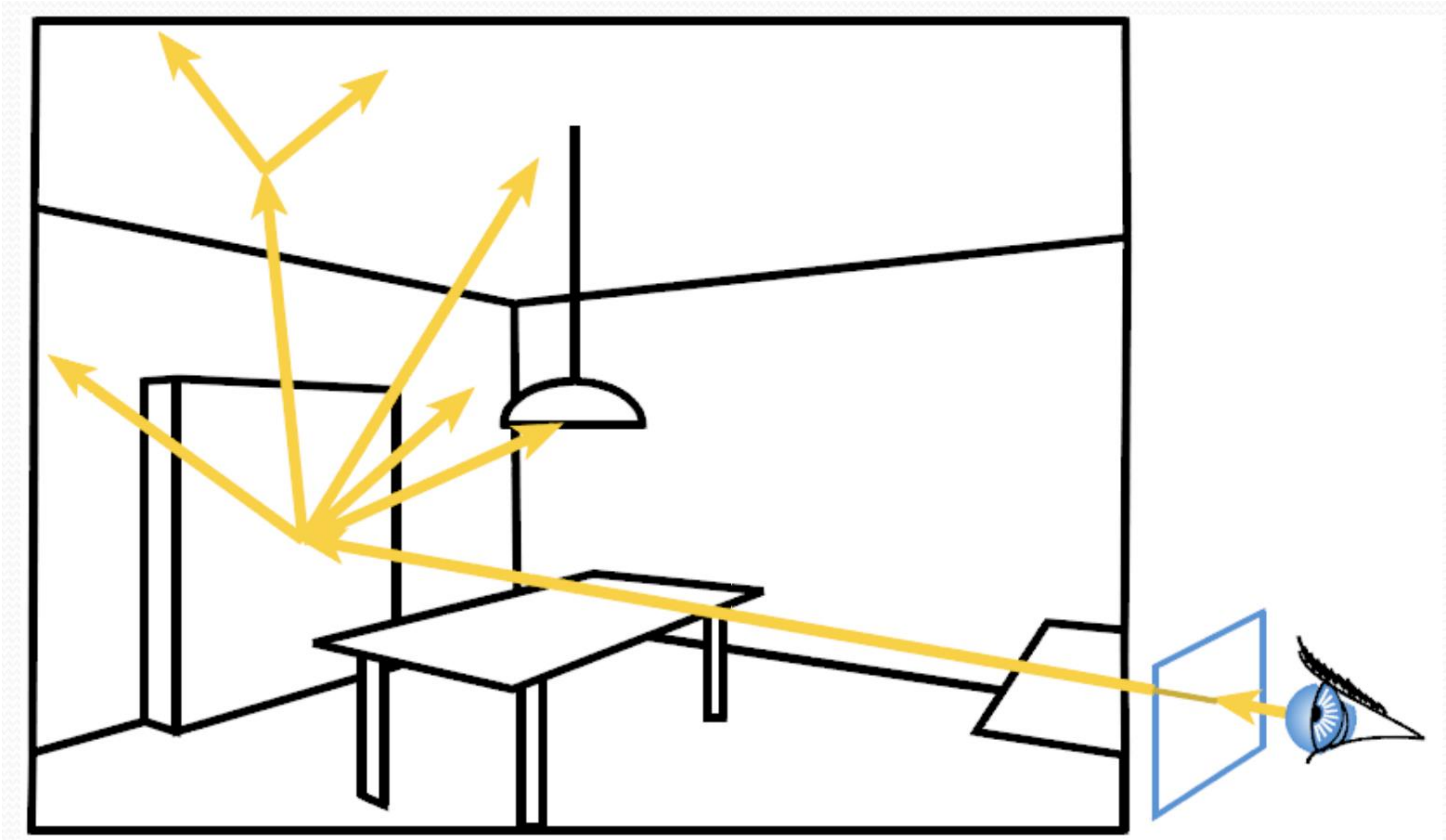
the incoming light from all directions

times

BRDF:
a function describing how light is reflected at an opaque surface

Monte Carlo Methods

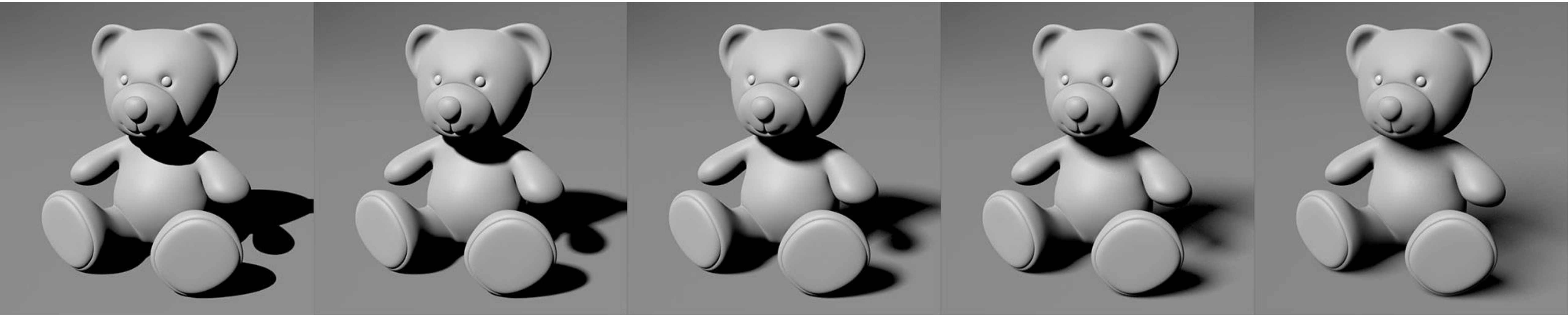
Rely on random sampling to “solve” rendering equation



http://courses.cs.tau.ac.il/Computer-Graphics/10a/lectures/05a-RayTracingAdv.pdf

Area Light

Hard v soft shadows

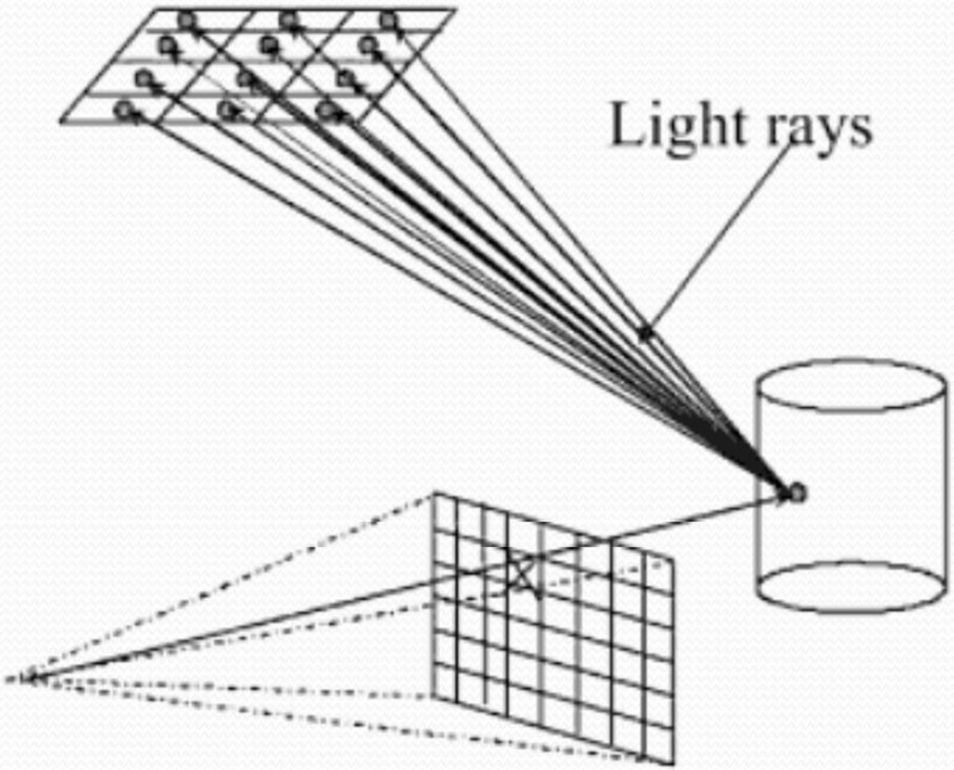


Hard shadow

More realistic soft shadows

Area Light

- Disadvantages of the simple uniform method:
  - Very time consuming
  - If the grid resolution is low, artifacts appear in the shadows.

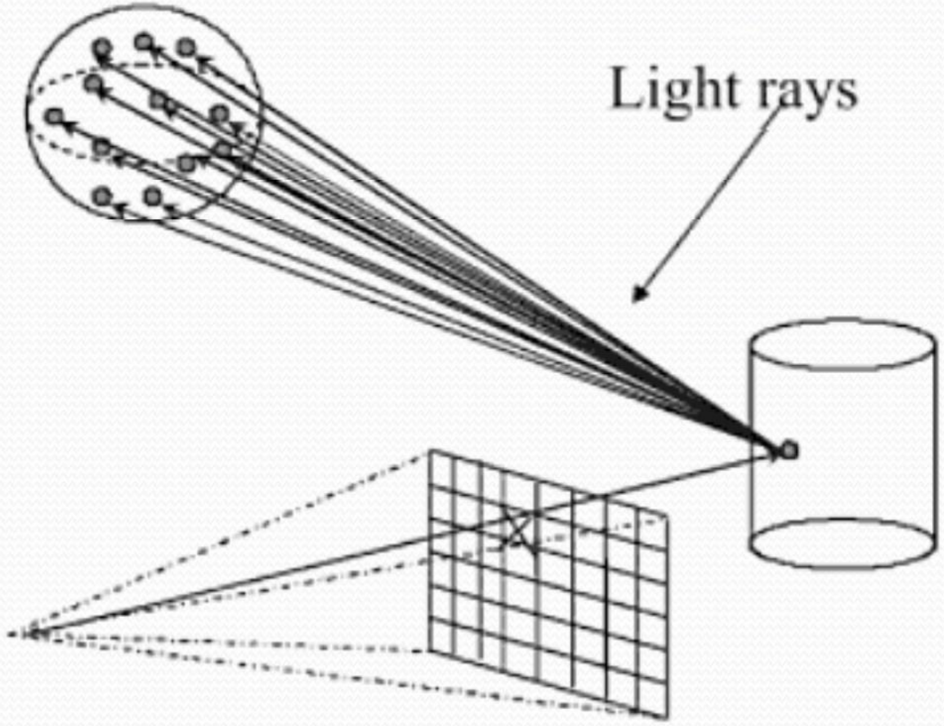


http://courses.cs.tau.ac.il/Computer-Graphics/10a/lectures/05a-RayTracingAdv.pdf

Area Light

Monte-Carlo Area light

- Light is modeled as a sphere
- Highest intensity in the middle. Gradually fade out.
- Shoot n rays to random points in the sphere
- Average their value.



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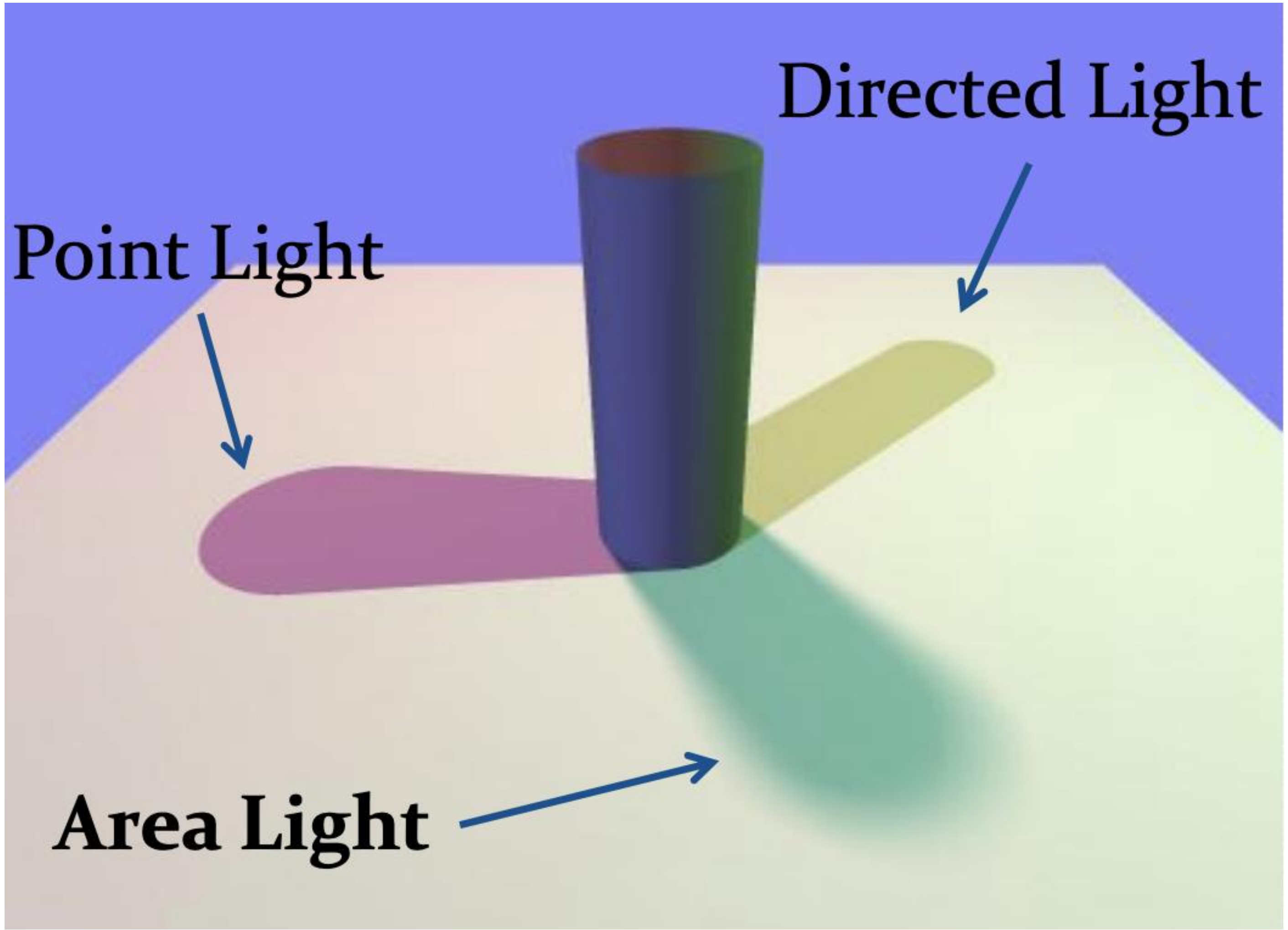
Area Light

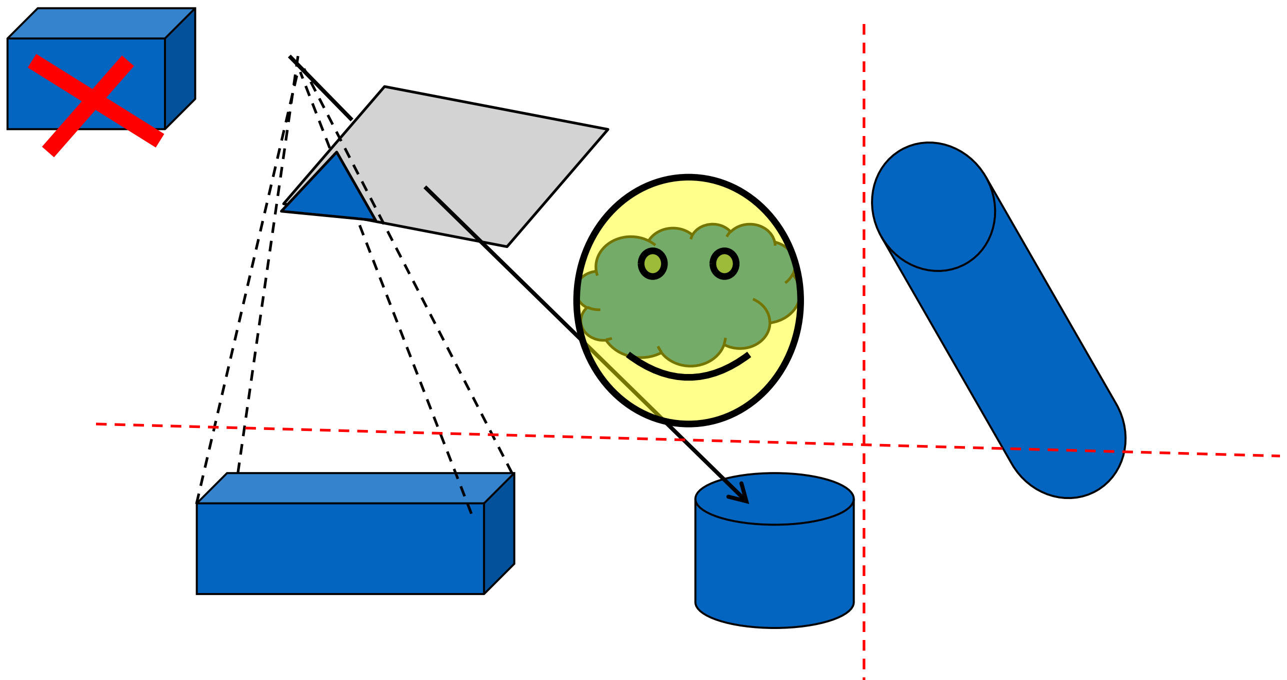


http://courses.cs.tau.ac.il/Computer-Graphics/10a/lectures/05a-RayTracingAdv.pdf

Ray Intersection: Efficiency Considerations

Speed-up the intersection process.

- Ignore object that clearly don't intersect.
- Use proxy geometry.
- Subdivide and structure space hierarchically.
- Project volume onto image to ignore entire sets of rays.



Faster Intersections for Ray Tracing