

Problem_3_2

February 13, 2020

1 Problem_3_2

```
[3]: #!/usr/bin/env python3
# -*- coding: utf-8 -*-
"""
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"""
import h5py
import numpy as np
import matplotlib.pyplot as plt

def LMS(v, z, eta):
    w = np.zeros([np.shape(v)[0], 3])
    err = np.zeros(np.shape(v)[0])
    y = np.zeros(np.shape(v)[0])
    for i in range(1, np.shape(v)[0]):
        y[i - 1] = np.sum(w[i - 1, :] * v[i - 1, :])
        err[i - 1] = z[i - 1] - y[i - 1]
        w[i] = w[i - 1] + eta * err[i - 1] * v[i - 1]

    return w, np.square(err)

model = h5py.File('D:\EE599\HW2\lms_fun_v3.hdf5', 'r')

v_10 = model['matched_10_v'][:]
y_10 = model['matched_10_y'][:]
z_10 = model['matched_10_z'][:]
v_3 = model['matched_3_v'][:]
y_3 = model['matched_3_y'][:]
z_3 = model['matched_3_z'][:]

# using z
# eta = 0.05
```

```

eta = 0.05
w_10 = np.zeros(np.shape(v_10))
err_10 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
w_3 = np.zeros(np.shape(v_10))
err_3 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
for i in range(np.shape(v_10)[0]):
    w_10[i], err_10[i] = LMS(v_10[i], z_10[i], eta)
    w_3[i], err_3[i] = LMS(v_3[i], z_3[i], eta)

w_10_eta_005 = np.average(w_10, axis=0)
err_10_eta_005 = np.average(err_10, axis=0)
w_3_eta_005 = np.average(w_3, axis=0)
err_3_eta_005 = np.average(err_3, axis=0)

print()
print('(b):')

plt.figure()
plt.plot(w_10_eta_005[:, 0])
plt.plot(w_10_eta_005[:, 1])
plt.plot(w_10_eta_005[:, 2])
plt.title('w_10 with eta = 0.05')

plt.figure()
plt.plot(err_10_eta_005)
plt.title('err_10 with eta = 0.05')

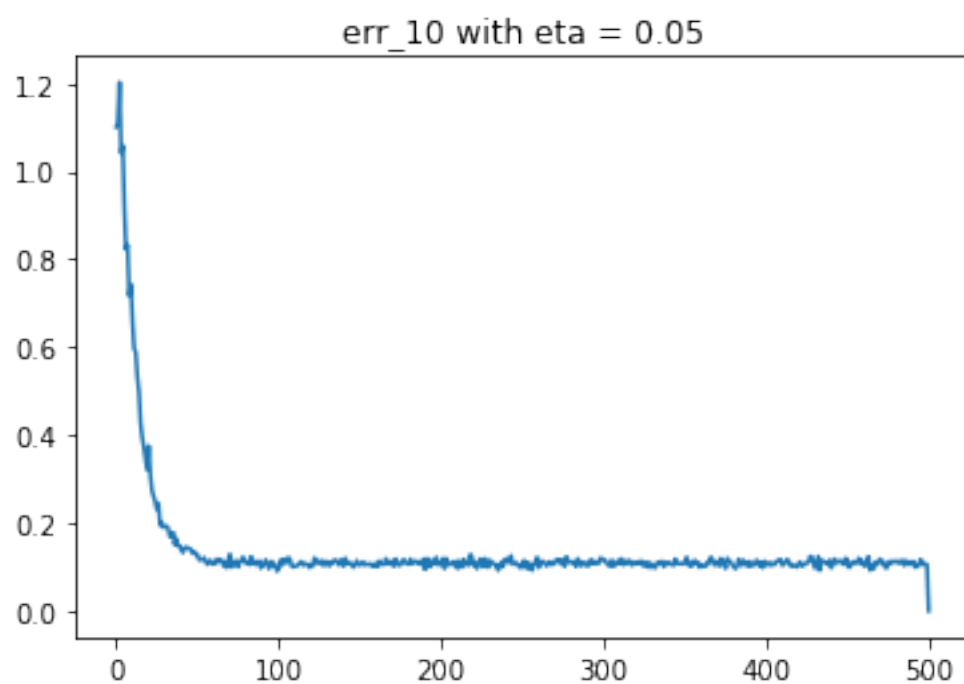
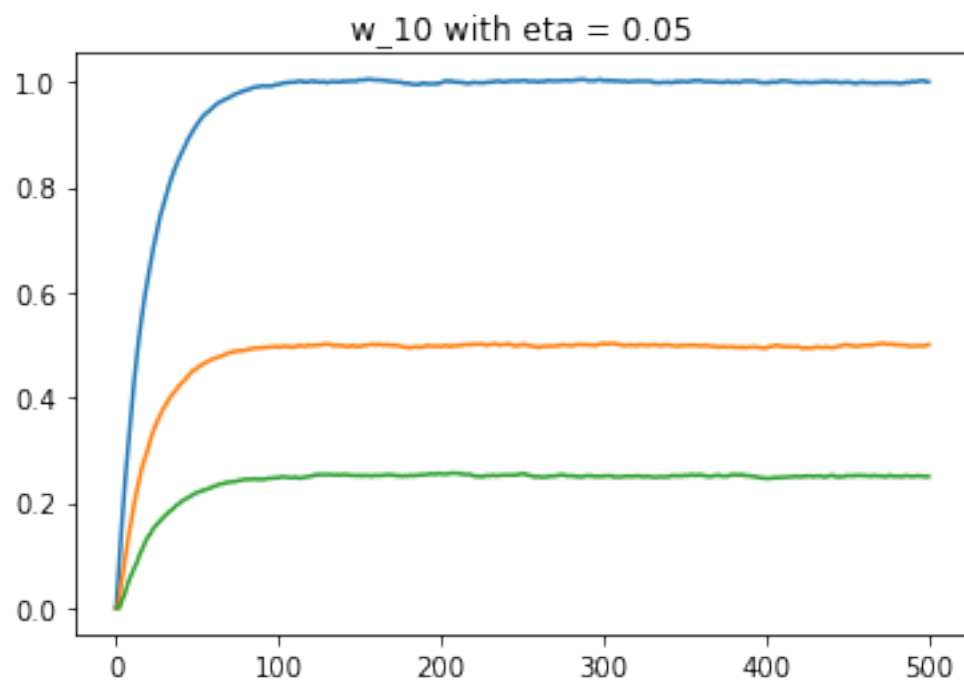
plt.figure()
plt.plot(w_3_eta_005[:, 0])
plt.plot(w_3_eta_005[:, 1])
plt.plot(w_3_eta_005[:, 2])
plt.title('w_3 with eta = 0.05')

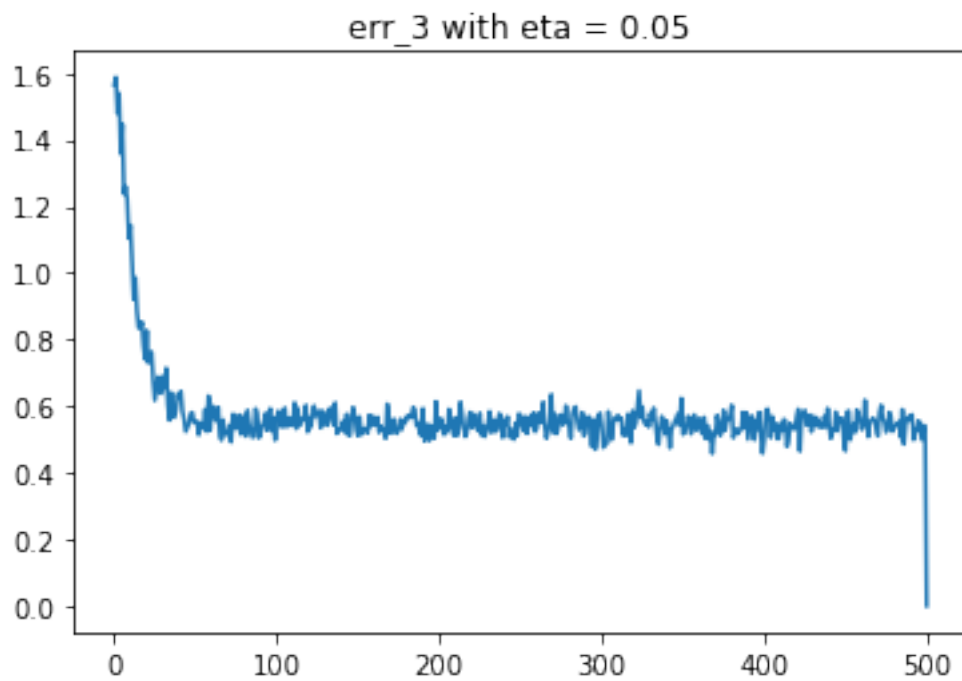
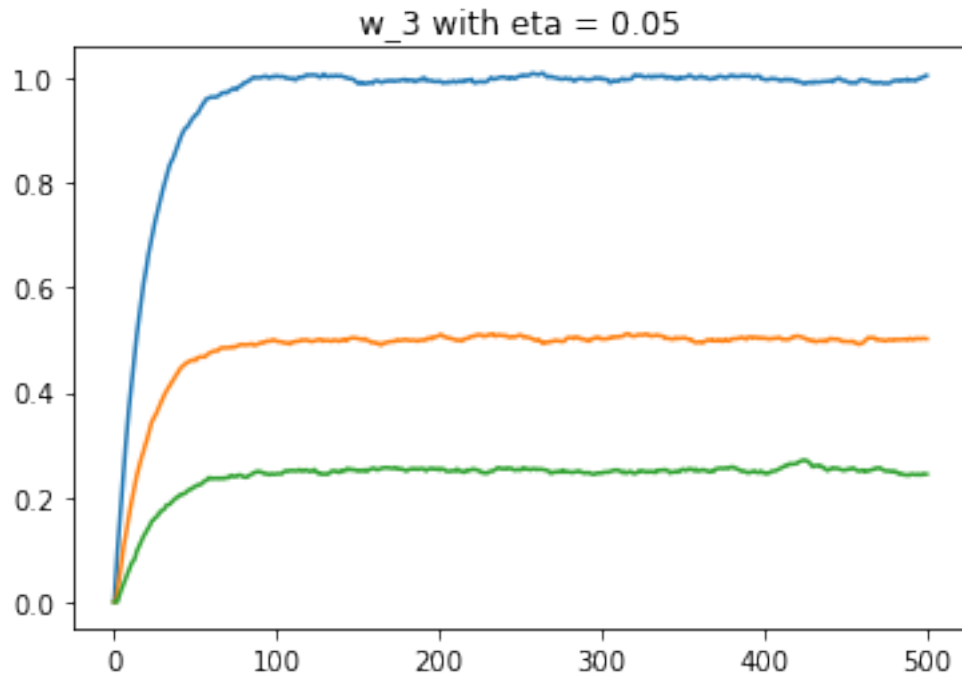
plt.figure()
plt.plot(err_3_eta_005)
plt.title('err_3 with eta = 0.05')

```

(b):

[3]: Text(0.5, 1.0, 'err_3 with eta = 0.05')





```
[4]: # eta = 0.15
```

```

eta = 0.15
w_10 = np.zeros(np.shape(v_10))
err_10 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
w_3 = np.zeros(np.shape(v_10))
err_3 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
for i in range(np.shape(v_10)[0]):
    w_10[i], err_10[i] = LMS(v_10[i], z_10[i], eta)
    w_3[i], err_3[i] = LMS(v_3[i], z_3[i], eta)

w_10_eta_015 = np.average(w_10, axis=0)
err_10_eta_015 = np.average(err_10, axis=0)
w_3_eta_015 = np.average(w_3, axis=0)
err_3_eta_015 = np.average(err_3, axis=0)

plt.figure()
plt.plot(w_10_eta_015[:, 0])
plt.plot(w_10_eta_015[:, 1])
plt.plot(w_10_eta_015[:, 2])
plt.title('w_10 with eta = 0.15')

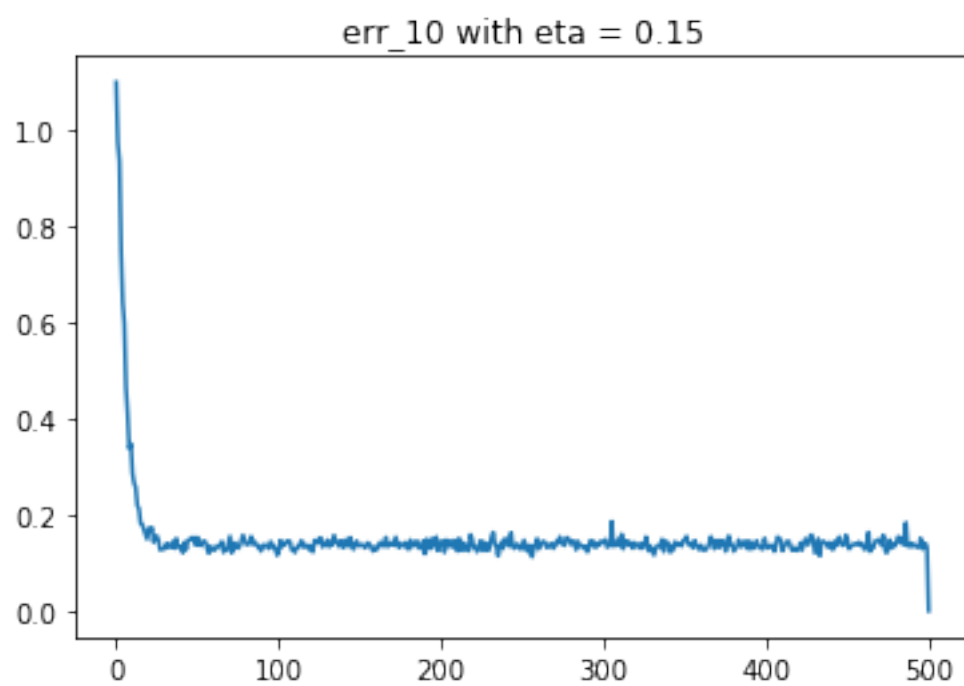
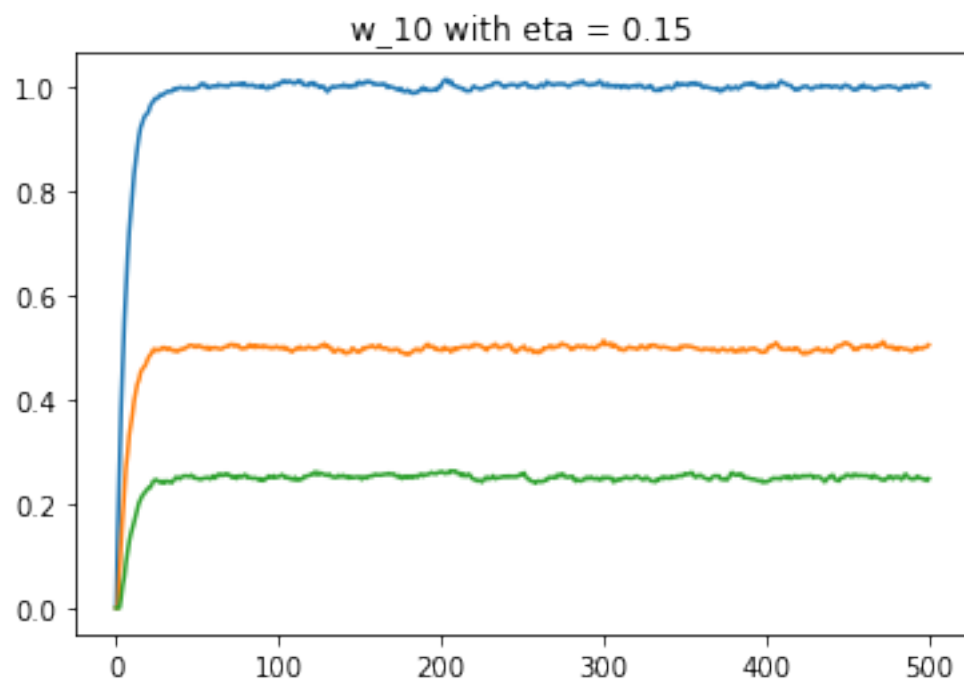
plt.figure()
plt.plot(err_10_eta_015)
plt.title('err_10 with eta = 0.15')

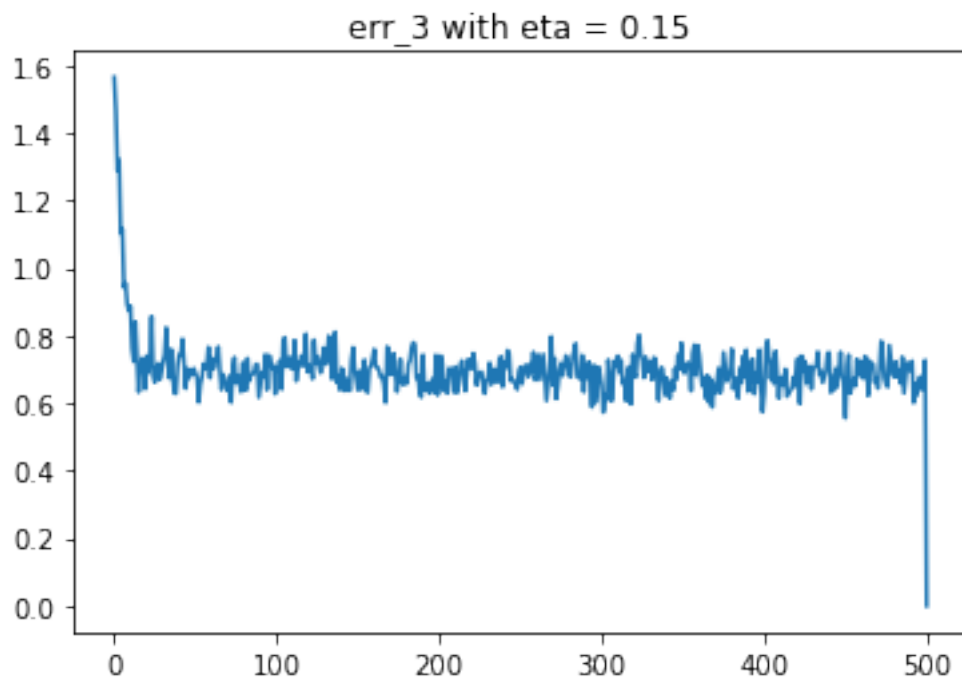
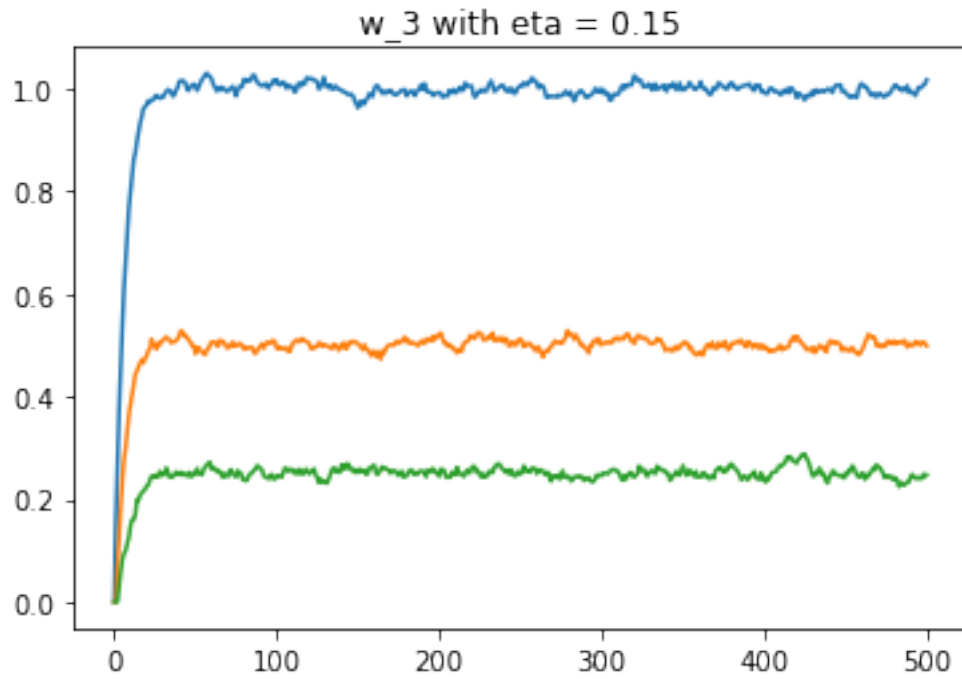
plt.figure()
plt.plot(w_3_eta_015[:, 0])
plt.plot(w_3_eta_015[:, 1])
plt.plot(w_3_eta_015[:, 2])
plt.title('w_3 with eta = 0.15')

plt.figure()
plt.plot(err_3_eta_015)
plt.title('err_3 with eta = 0.15')

```

[4]: Text(0.5, 1.0, 'err_3 with eta = 0.15')





(c)

The MSE when $\eta=0.05$ is about 0.55 when $\text{SNR}=3$ and 0.12 when $\text{SNR}=10$, a little higher than

LMMSE.

The MSE when $\eta=0.15$ is about 0.7 when $\text{SNR}=3$ and 0.18 when $\text{SNR}=10$, much higher than LMMSE in comparison with that when $\eta=0.05$. Besides, they are more noisy than those when $\eta=0.05$

```
[6]: # using y
# eta = 0.05
eta = 0.15
w_10 = np.zeros(np.shape(v_10))
err_10 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
w_3 = np.zeros(np.shape(v_10))
err_3 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
for i in range(np.shape(v_10)[0]):
    w_10[i], err_10[i] = LMS(v_10[i], y_10[i], eta)
    w_3[i], err_3[i] = LMS(v_3[i], y_3[i], eta)

w_10_eta_015 = np.average(w_10, axis=0)
err_10_eta_015 = np.average(err_10, axis=0)
w_3_eta_015 = np.average(w_3, axis=0)
err_3_eta_015 = np.average(err_3, axis=0)

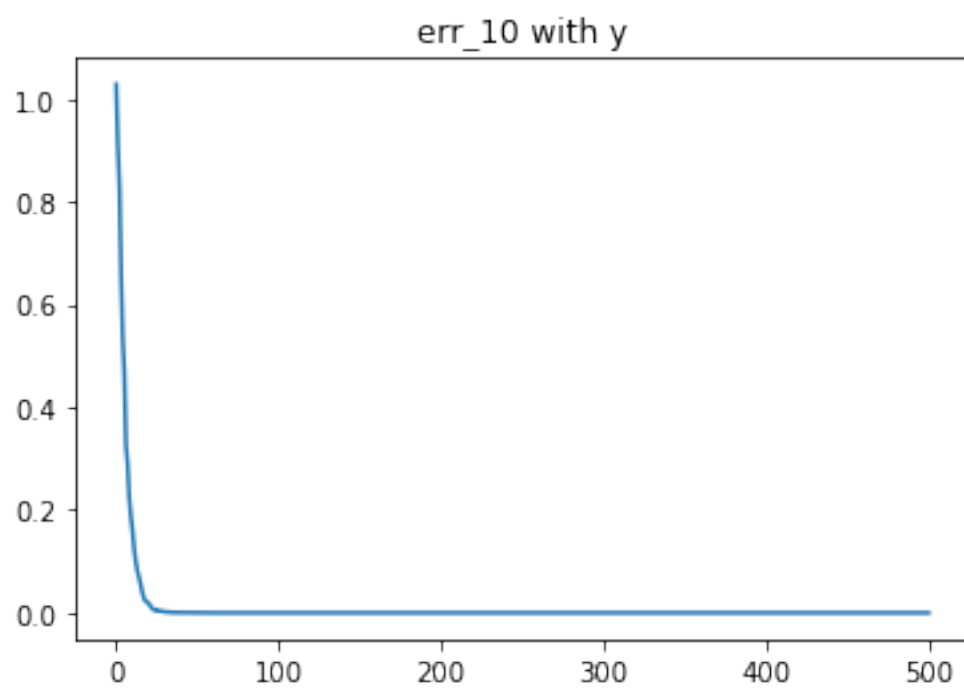
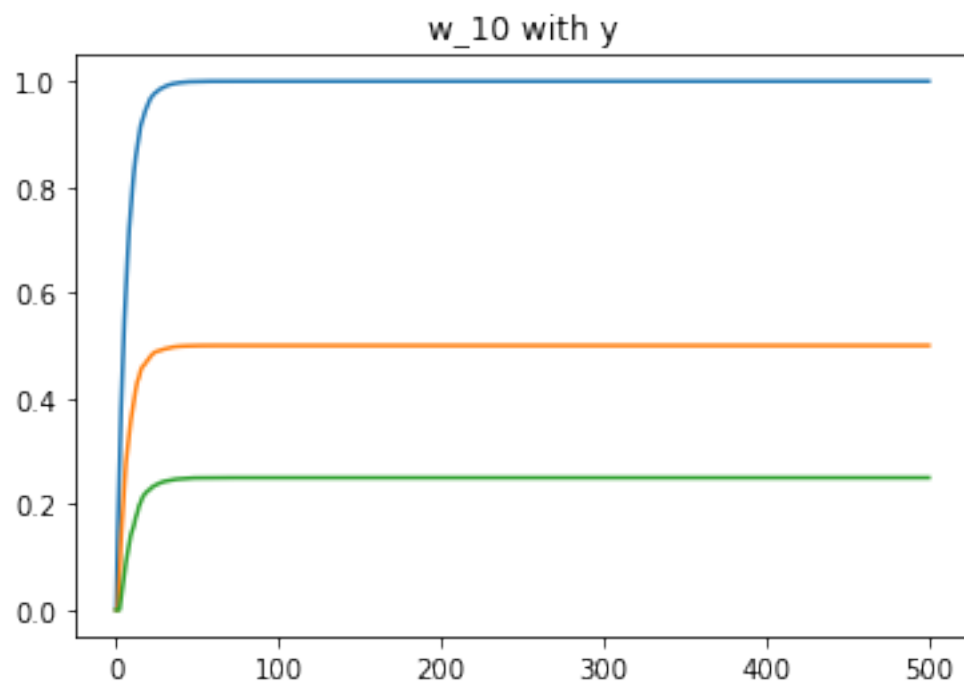
plt.figure()
plt.plot(w_10_eta_015[:, 0])
plt.plot(w_10_eta_015[:, 1])
plt.plot(w_10_eta_015[:, 2])
plt.title('w_10 with y')

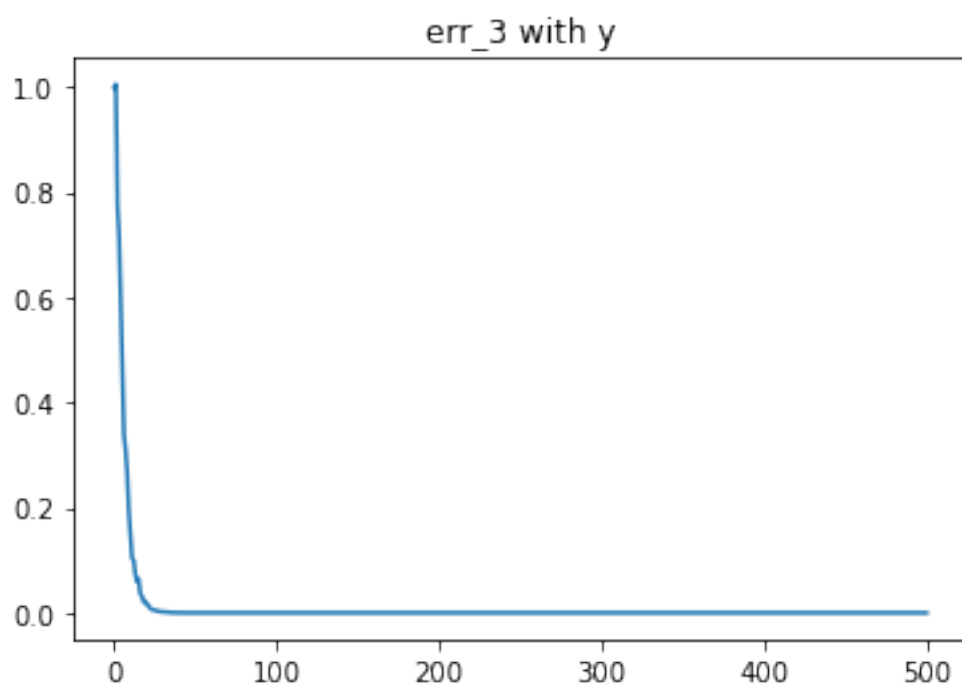
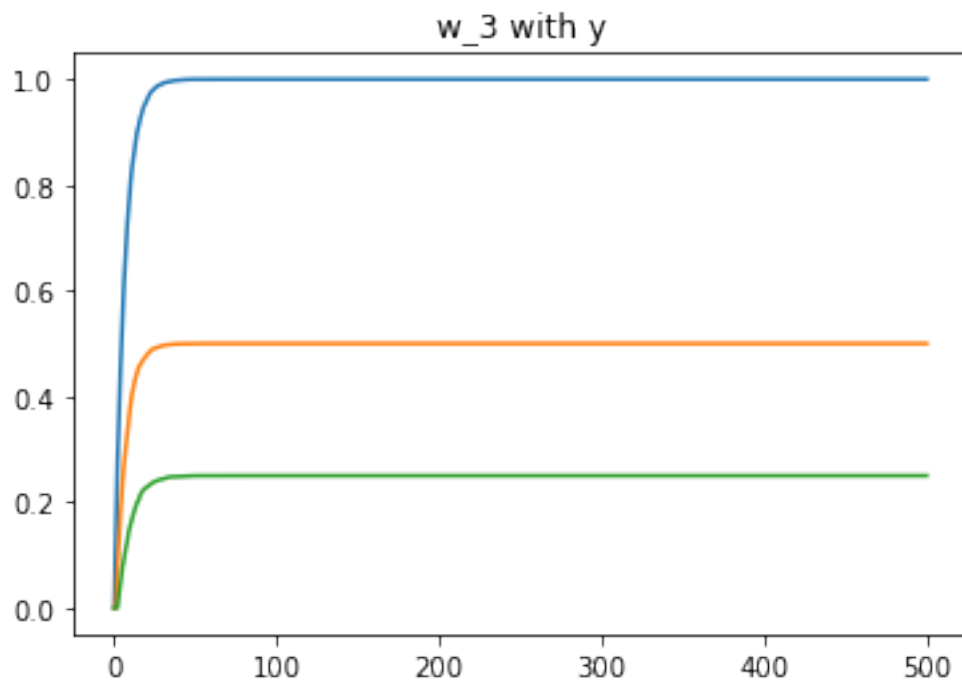
plt.figure()
plt.plot(err_10_eta_015)
plt.title('err_10 with y')

plt.figure()
plt.plot(w_3_eta_015[:, 0])
plt.plot(w_3_eta_015[:, 1])
plt.plot(w_3_eta_015[:, 2])
plt.title('w_3 with y')

plt.figure()
plt.plot(err_3_eta_015)
plt.title('err_3 with y')
```

```
[6]: Text(0.5, 1.0, 'err_3 with y')
```



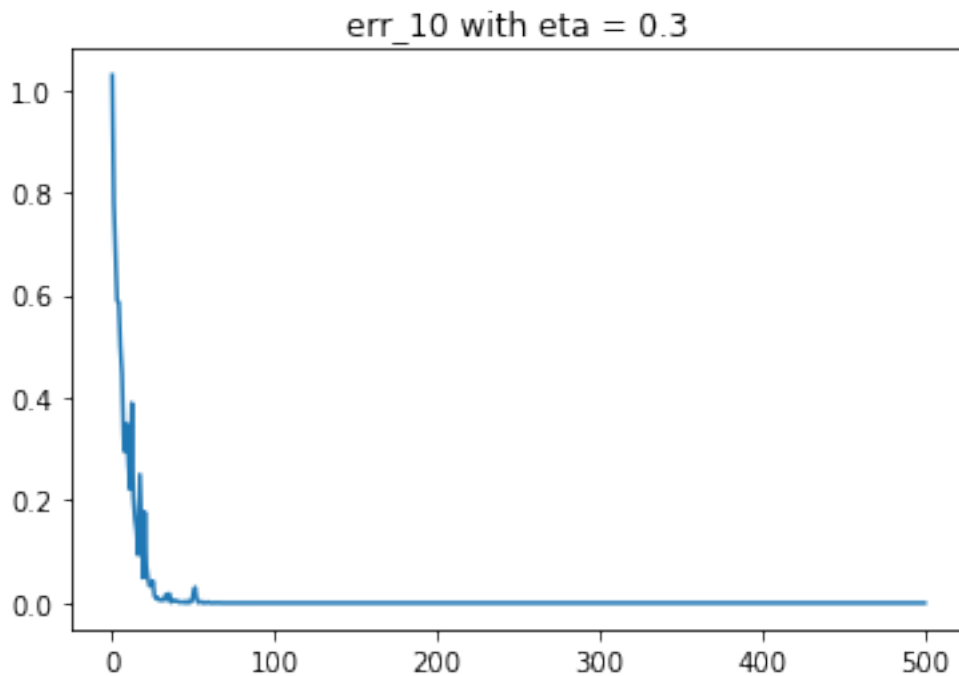
(d)

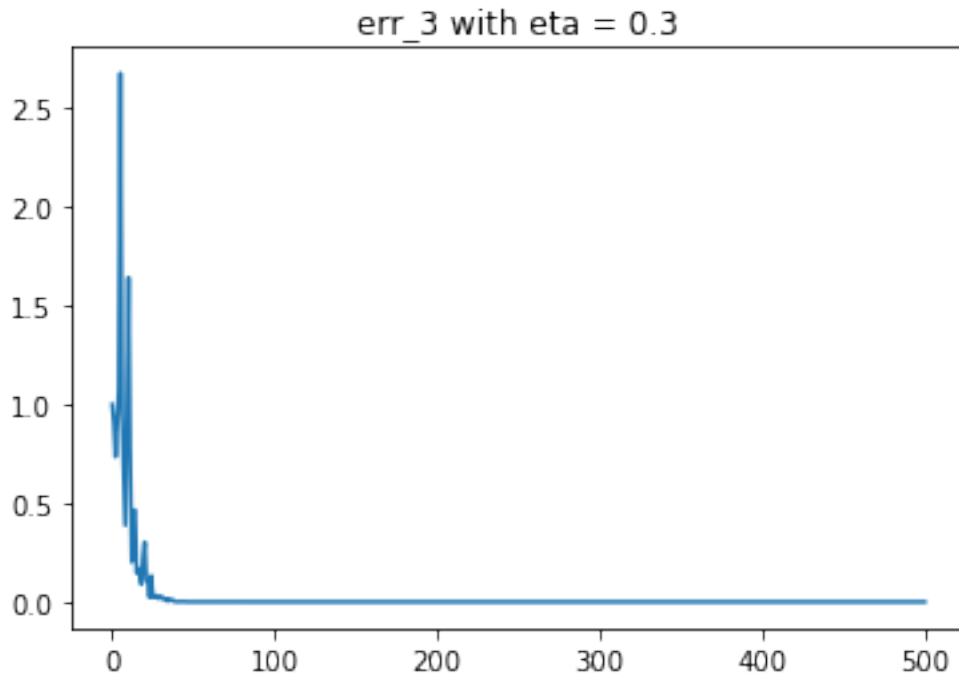
```
[11]: # largest eta
eta = 0.3
w_10 = np.zeros(np.shape(v_10))
err_10 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
w_3 = np.zeros(np.shape(v_10))
err_3 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
for i in range(np.shape(v_10)[0]):
    w_10[i], err_10[i] = LMS(v_10[i], y_10[i], eta)
    w_3[i], err_3[i] = LMS(v_3[i], y_3[i], eta)

w_10_eta_015 = np.average(w_10, axis=0)
err_10_eta_015 = np.average(err_10, axis=0)
w_3_eta_015 = np.average(w_3, axis=0)
err_3_eta_015 = np.average(err_3, axis=0)
plt.figure()
plt.plot(err_10_eta_015)
plt.title('err_10 with eta = 0.3')

plt.figure()
plt.plot(err_3_eta_015)
plt.title('err_3 with eta = 0.3')
```

```
[11]: Text(0.5, 1.0, 'err_3 with eta = 0.3')
```



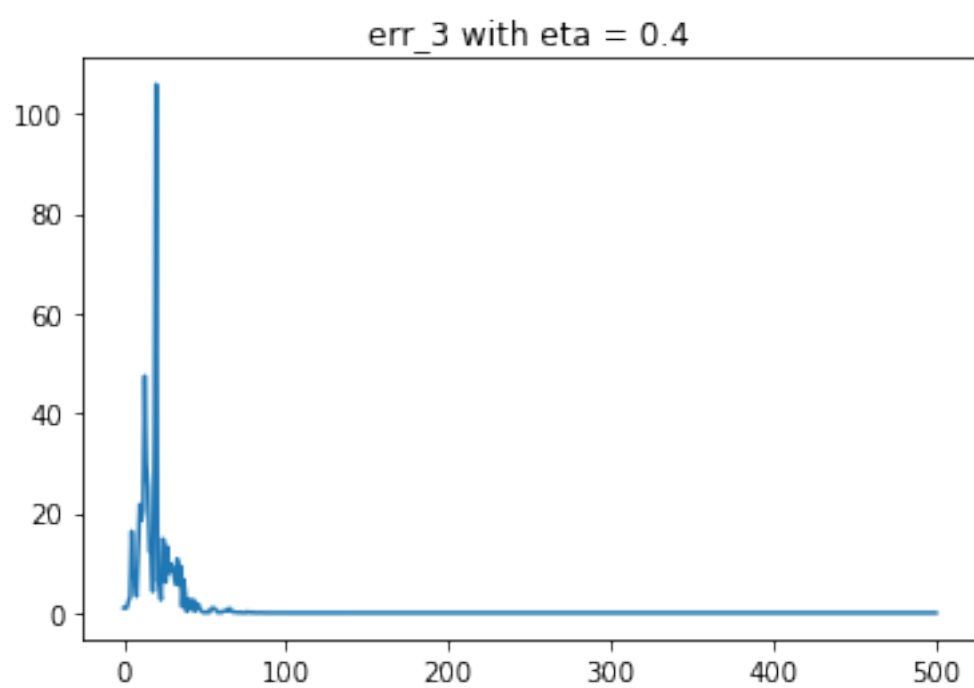
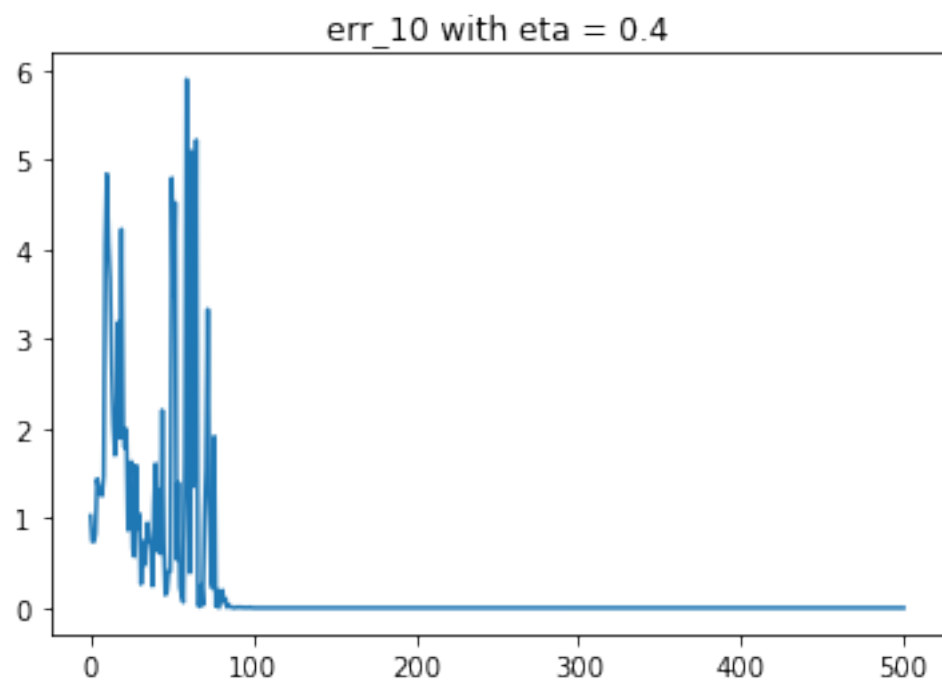


```
[12]: # largest eta
eta = 0.4
w_10 = np.zeros(np.shape(v_10))
err_10 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
w_3 = np.zeros(np.shape(v_10))
err_3 = np.zeros([np.shape(v_10)[0], np.shape(v_10)[1]])
for i in range(np.shape(v_10)[0]):
    w_10[i], err_10[i] = LMS(v_10[i], y_10[i], eta)
    w_3[i], err_3[i] = LMS(v_3[i], y_3[i], eta)

w_10_eta_015 = np.average(w_10, axis=0)
err_10_eta_015 = np.average(err_10, axis=0)
w_3_eta_015 = np.average(w_3, axis=0)
err_3_eta_015 = np.average(err_3, axis=0)
plt.figure()
plt.plot(err_10_eta_015)
plt.title('err_10 with eta = 0.4')

plt.figure()
plt.plot(err_3_eta_015)
plt.title('err_3 with eta = 0.4')
```

```
[12]: Text(0.5, 1.0, 'err_3 with eta = 0.4')
```



from the plots above, the maximum eta is 0.3