Personalized Decision Making for Biopsies in Prostate Cancer Active Surveillance Programs

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Abstract

Background. Low-risk prostate cancer patients enrolled in active surveillance (AS) programs commonly undergo biopsies for examination of cancer progression. Biopsies are conducted as per a fixed and frequent schedule (e.g. annual biopsies), common for all patients. Such schedules may schedule unnecessary biopsies. Since biopsies are burdensome, patients do not always comply with the schedule, which increases the risk of delayed detection of cancer progression.

Objective. Motivated by the world's largest AS program, Prostate Cancer Research International Active Surveillance (PRIAS), our aim is to better balance the number of biopsies (burden) and the delay in detection of cancer progression (benefit). We intend to achieve this by personalizing the decision of conducting biopsies.

Methods. Using joint models for time-to-event and longitudinal data, we jointly model the observed prostate-specific antigen levels, digital rectal examination scores, and the latest biopsy results of a patient at each follow-up visit. This results in a follow-up visit-specific and patient-specific, cumulative risk of cancer progression. When this risk at a visit is above a certain threshold, we schedule a biopsy at that visit. We compare this personalized approach with the currently practiced biopsy schedules via an extensive and realistic simulation study, based on a replica of the patients from the PRIAS program.

Results. In comparison to the currently practiced schedules, the personalized approach saves one to seven burdensome biopsies per patient, depending upon the time of cancer progression of the patient. Despite this reduction in the number of biopsies, the delay in the detection of cancer progression for the personalized approach remains comparable with that of the biopsy schedule of the PRIAS program.

Conclusions. We conclude that the personalized schedules better balance the number of biopsies per detected cancer progression.

Keywords

Active surveillance, biopsy, joint models, personalized medical decisions, prostate cancer

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Introduction

Prostate cancer is the second most frequently diagnosed cancer in men worldwide¹. However, in prostate cancer screening programs, many of the diagnosed tumors are clinically insignificant (over-diagnosed)². To avoid further over-treatment, patients diagnosed with low-grade prostate cancer are commonly advised to join active surveillance (AS) programs. In AS, serious atments such as surgery, chemotherapy are delayed until cancer progresses. Cancer progression is routinely examined via serum prostate-specific antigen (PSA) levels: a protein biomarker, digital rectal examination (DRE) score: a measure of the size and location of the tumor, medical imaging, and biopsies etc.

While larger values for PSA and/or larger score for DRE ay indicate cancer progression, biopsies are the most reliable cancer progression examination technique used in AS. When a patient's biopsy Gleason grading becomes larger than 6 psitive biopsy), AS is stopped and the patient is advised treatment for cancer progression. However, biopsies are invasive, painful, and prone to medical complications 4.5. Hence, they are conducted intermittently until a positive biopsy. Consequently, at the time of a positive biopsy, cancer progression is observed with a delay of an unknown duration. This delay is defined as the difference between the time of the positive biopsy and the unobserved true time of cancer progression. Thus, the decision of conducting a biopsy requires a fine compromise between the burden of biopsy, and the delay in detection of cancer progression.

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In AS, a delay in the detection of cancer progression around twelve to fourteen months is assumed to be unlikely to substantially increase the risk for adverse downstream outcomes 6,7. However, for biopsies, there is little consensus on the time gap between them⁸. Majority of the AS programs focus on minimizing only the delay in detection of cancer progression, by scheduling biopsies annually (most frequent schedule) for all patients. A drawback of annual biopsies, and other fixed/heuristic schedules⁶, is that they ignore the large variation in the time of cancer progression of AS patients. While they may work well for patients who progress early (fast progressing) in AS, but for a large proportion of patients who do not progress until late ow progressing) in AS, many unnecessary burdensome biopsies are scheduled. To mediate the burden between the fast and slow progressing patients, the world's largest AS program, Prostate Cancer Research International Active Surveillance⁹ (see Figure 1), abbreviated as PRIAS, schedules annual biopsies only for patients with a small A doubling time. For everyone else, PRIAS schedules biopsies at following fixed follow-up times: year one, four, seven, and ten, and every five years thereafter. Despite this effort in PRIAS, a patient may get scheduled for four to ten biopsies over a period of ten years. Consequently, patients may not always comply with the biopsy schedul This can lead to the original problem of delayed detection of cancer progression, and reduce the effectiveness of AS.

This article is motivated by the need to better balance the number of biopsies (more are burdensome), and the delay in detection of cancer progression (less is beneficial), than currently practiced schedules (see Figure 2). We intend to achieve this by personalizing the decision of conducting biopsies at follow-up visits. To this end, we utilize the data of the patients of the PRIAS study. Personalized decision making has received much interest in the literature, especially for the screening of various cancers, by exploiting Markov decision process models ^{11–13}. Similar models have also been used for personalizing the pre-diagnosis prostate cancer screening strategy ^{14,15}. However, in post-diagnosis AS programs, to the best of our knowledge, only fixed/heuristic approaches ^{6,7}, or PSA doubling time ³ have been employed for deciding the time of biopsies.

In this work, we make a patient-specific decision of biopsy at a patient's pre-scheduled follow-up visit (logistical considerations) for DRE and PSA

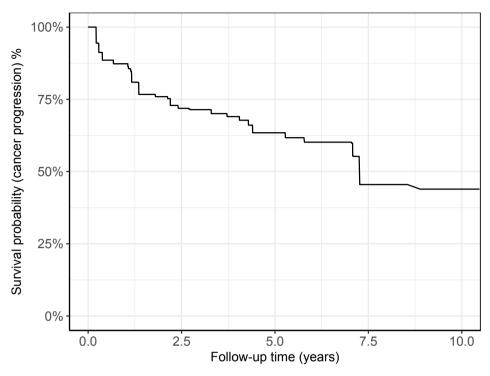


Figure 1. Estimated survival probability of cancer progression in AS for patients in the Prostate Cancer Research International Active Surveillance (PRIAS) dataset. Nearly 50% patients (*slow progressing*) do not progress in the ten year follow-up period. Survival probability is estimated using a nonparametric maximum likelihood estimate of the distribution function for interval censored cancer progression times ¹⁰ observed in PRIAS program.

measurements. In comparison to the work referenced above, we make this decision using the entire history of DRE scores, PSA levels and the estimated rate of change of PSA (PSA velocity), and results of the latest biopsy of a patient up to the latest follow-up visit. We achieve this by utilizing joint models for time-to-event and longitudinal data ^{16,17}. Joint models consist of a longitudinal mixed effects sub-model for periodically measured outcomes such as DRE and PSA, and a relative risk sub-model for modeling the time of cancer progression. The association between these three outcomes, and especially the fact that the DRE and PSA measurements are missing after the detection of cancer progression, is modeled using patient-specific random-effects ¹⁸. By estimating the parameters of the model jointly, we first obtain a full specification of the joint distribution of the time of cancer progression, and DRE and PSA

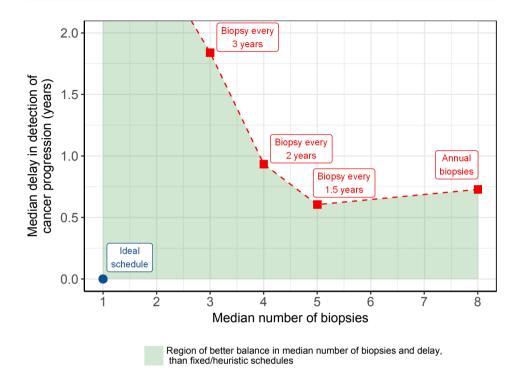


Figure 2. Burden-benefit frontier: Estimated median number of biopsies (more are burdensome), and median delay in detection of cancer progression (less is beneficial), due to various currently practiced fixed/heuristic biopsy schedules (red squares), over a follow-up of ten years. Estimation is based on cancer progression times simulated using the survival probability curve in Figure 1. Using personalized decision making for biopsies, we intend to better balance the number of biopsies and the delay (green region), than currently practiced schedules. An ideal biopsy schedule (blue circle) will schedule only one biopsy, exactly at the true time of cancer progression.

measurements. We then use it at a patient's follow-up visit, to estimate the patient-specific cumulative risk of observing cancer progression at that visit. If that risk is higher than a certain threshold, our method proposes a biopsy at the same follow-up visit. We exploit fixed risk thresholds used in standard clinical settings, as well as we propose a methodology to choose risk thresholds on the basis of their classification accuracy.

We evaluate the personalized risk based biopsy approach, and the currently practiced fixed/heuristic, PRIAS biopsy schedules on the basis of their utility for the patients. That is, the number of biopsies they schedule, and the corresponding delay incurred in the detection of cancer

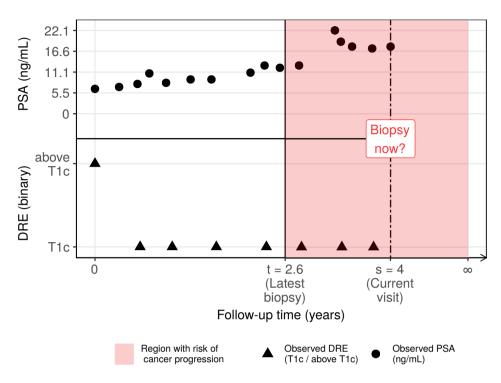


Figure 3. The personalized decision making problem: Available data of a patient j, who had his latest negative biopsy at t=2.6 years. The shaded region shows the time period in which the patient is at risk of cancer progression. His current pre-scheduled follow-up visit for measurement of DRE and PSA is at s=4 years. Using his entire history of DRE $\mathcal{Y}_{dj}(s)$ and PSA $\mathcal{Y}_{pj}(s)$ measurements up to the current visit s, and the time of the latest biopsy t, we intend to make a decision on scheduling a biopsy at the current visit.

progression. To compare the aforementioned schedules on these criteria, we conduct an extensive simulation study. For a realistic comparison, we simulate a replica of the population of the PRIAS patients, using the joint model fitted to the PRIAS dataset.

The rest of the article is structured as follows: The details of the joint modeling framework and biopsy decision making methodology are presented in the Methods section. The details of the simulation study and the corresponding results are presented in Methods and Results sections, respectively.

Methods

Study Population

To develop our methodology we use the data of prostate cancer patients from the world's largest AS study called PRIAS⁹. More than 100 medical centers from 17 countries worldwide contribute to the collection of data. utilizing a common study protocol and a web-based tool, both available at www.prias-project.org. We use the data collected between December 2006 (beginning of the study) and December 2016. It consists of 5270 patients. Cancer progression is observed in 866 patients (see Figure 1). For all patients, PSA measurements (ng/mL) are scheduled every 3 months for the first 2 years and every 6 months thereafter. The DRE measurements (ordinal scale) are scheduled every 6 months. We use the DRE measurements after converting them to a binary scale, namely DRE > T1c and DRE = T1c. A DRE score of T1c 19 indicates a clinically inapparent tumor which is not palpable or visible by imaging. Tumors with DRE > T1c are large enough to be palpable. On average 5 DRE and 9 PSA measurements have been recorded per patient. In order to detect cancer progression, biopsies are scheduled as per the PRIAS protocol (see Introduction).

A Bivariate Joint Model for the Longitudinal PSA, and DRE Measurements, and Time of Cancer Progression

Let T_i^* denote the true cancer progression time of the i-th patient included in PRIAS. Since biopsies are conducted periodically, T_i^* is observed with interval censoring $l_i < T_i^* \le r_i$. When progression is observed for the patient at his latest biopsy time r_i , then l_i denotes the time of the second latest biopsy. Otherwise, l_i denotes the time of the latest biopsy and $r_i = \infty$. Let y_{di} and y_{pi} denote his observed DRE and PSA longitudinal measurements, respectively. The observed data of all n patients is denoted by $\mathcal{D}_n = \{l_i, r_i, y_{di}, y_{ni}; i = 1, \ldots, n\}$.

In our joint model, the patient-specific PSA and DRE measurements over time are modeled using a bivariate generalized linear mixed effects sub-model. The sub-model for DRE is given by (see Panel A, Figure 4):

logit[Pr{
$$y_{di}(t) > \text{T1c}$$
}] = $\beta_{0d} + b_{0di} + (\beta_{1d} + b_{1di})t$
+ $\beta_{2d}(\text{Age}_i - 70) + \beta_{3d}(\text{Age}_i - 70)^2$ (1)

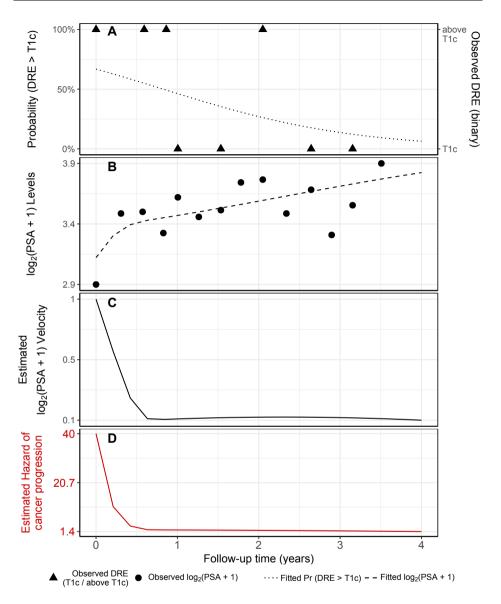


Figure 4. Illustration of the joint model fitted to the PRIAS dataset. Panel A: shows the observed DRE scores and the fitted probability of obtaining DRE > T1c (Equation 1) for . Panel B: shows the observed and fitted $\log_2(\mathsf{PSA}+1)$ levels (Equation 2). Panel C: shows the estimated $\log_2(\mathsf{PSA}+1)$ velocity (velocity cannot be observed directly) over time. The hazard function (Equation 3) shown in Panel D, depends on the fitted log odds of having a DRE > T1c, and the fitted $\log_2(\mathsf{PSA}+1)$ value and velocity.

where, t denotes the follow-up visit time, and Age_i is the age of the i-th patient at the time of inclusion in AS. The fixed effect parameters are denoted by $\{\beta_{0d}, \ldots, \beta_{3d}\}$, and $\{b_{0di}, b_{1di}\}$ are the patient specific random effects. With this definition, we assume that the patient-specific log odds of obtaining a DRE score larger than T1c remain linear over time.

The mixed effects sub-model for PSA is given by (see Panel B, Figure 4):

$$\log_2 \{y_{pi}(t) + 1\} = m_{pi}(t) + \varepsilon_{pi}(t),$$

$$m_{pi}(t) = \beta_{0p} + b_{0pi} + \sum_{k=1}^{4} (\beta_{kp} + b_{kpi}) B_k(t, \mathcal{K})$$

$$+ \beta_{5p} (Age_i - 70) + \beta_{6p} (Age_i - 70)^2, \qquad (2)$$

where, $m_{pi}(t)$ denotes the underlying measurement error free value of $\log_2(\mathrm{PSA}+1)$ transformed 20,21 measurements at time t. We model it non-linearly over time using B-splines 22 . To this end, our B-spline basis function $B_k(t,\mathcal{K})$ has 3 internal knots at $\mathcal{K}=\{0.1,0.7,4\}$ years, and boundary knots at 0 and 5.42 years (95-th percentile of the observed follow-up times). The fixed effect parameters are denoted by $\{\beta_{0p},\ldots,\beta_{6p}\}$, and $\{b_{0pi},\ldots,b_{4pi}\}$ are the patient specific random effects. The error $\varepsilon_{pi}(t)$ is assumed to be t-distributed with three degrees of freedom (see Appendix B.1) and scale σ , and is independent of the random effects.

To account for the correlation between the DRE and PSA measurements of a patient, we link their corresponding random effects. More specifically, the complete vector of random effects $\mathbf{b}_i = (b_{0di}, b_{1di}, b_{0pi}, \dots, b_{4pi})^T$ is assumed to follow a multivariate normal distribution with mean zero and variance-covariance matrix \mathbf{D} .

To model the impact of DRE and PSA measurements on the risk of cancer progression, our joint model uses a relative risk sub-model. More specifically, the hazard of cancer progression $h_i(t)$ at a time t is given by (see Panel D, Figure 4):

$$h_i(t) = h_0(t) \exp\left(\gamma_1(Age_i - 70) + \gamma_2(Age_i - 70)^2 + \alpha_{1d}logit\left[Pr\{y_{di}(t) > T1c\}\right] + \alpha_{1p}m_{pi}(t) + \alpha_{2p}\frac{\partial m_{pi}(t)}{\partial t}\right), \quad (3)$$

where, γ_1,γ_2 are the parameters for the effect of age. The parameter α_{1d} models the impact of log odds of obtaining a DRE > T1c on the hazard of cancer progression. The impact of PSA on the hazard of cancer progression is modeled in two ways: a) the impact of the error free underlying PSA value $m_{pi}(t)$ (see Panel B, Figure 4), and b) the impact of the underlying PSA velocity $\partial m_{pi}(t)/\partial t$ (see Panel C, Figure 4). The corresponding parameters are α_{1p} and α_{2p} , respectively. Lastly, $h_0(t)$ is the baseline hazard at time t, and is modeled flexibly using P-splines ²³. The detailed specification of the baseline hazard $h_0(t)$, and the joint parameter estimation of the two sub-models using the Bayesian approach (R package **JMbayes** ²⁴) are presented in Appendix A of the supplementary material.

Personalized Decisions for Biopsy

Let us assume that a decision of conducting a biopsy is to be made for a new patient j shown in Figure 3, at his current follow-up visit time s. Let $t \leq s$ be the time of his latest negative biopsy. Let $\mathcal{Y}_{dj}(s)$ and $\mathcal{Y}_{pj}(s)$ denote his observed DRE and PSA measurements up to the current visit, respectively. From the observed measurements we want to extract the underlying measurement error free trend of $\log_2(\mathrm{PSA}+1)$ values and velocity, and the log odds of obtaining DRE > T1c. We intend to combine them to inform us when the cancer progression is to be expected (see Figure 5), and to further guide the decision making on whether to conduct a biopsy at the current follow-up visit. The combined information is given by the following posterior predictive distribution $g(T_j^*)$ of his time of cancer progression $T_i^* > t$ (see Appendix A.4 for details):

$$g(T_j^*) = p\{T_j^* \mid T_j^* > t, \mathcal{Y}_{dj}(s), \mathcal{Y}_{pj}(s), \mathcal{D}_n\}.$$
 (4)

The distribution $g(T_j^*)$ is not only patient-specific, but also updates as extra information is recorded at future follow-up visits.

A key ingredient in the decision of conducting a biopsy for patient j at the current follow-up visit time s is the personalized cumulative risk of observing a cancer progression at time s (illustrated in Figure 5). This risk can be derived from the posterior predictive distribution $g(T_j^*)^{25}$, and is given by:

$$R_i(s \mid t) = \Pr\{T_i^* \le s \mid T_i^* > t, \mathcal{Y}_{di}(s), \mathcal{Y}_{pi}(s), \mathcal{D}_n\}, \quad s \ge t.$$
 (5)

A simple and straightforward approach to decide upon conducting a biopsy for patient j at the current follow-up visit would be to do so

if his personalized cumulative risk of cancer progression at the visit is higher than a certain threshold $0 \le \kappa \le 1$. For example, as shown in Panel B of Figure 5, biopsy at a visit may be scheduled if the personalized cumulative risk is higher than 10% (example risk threshold). This decision making process is iterated over the follow-up period, incorporating on each subsequent visit the newly observed data, until a positive biopsy is observed. Subsequently, an entire personalized schedule of biopsies for each patient can be obtained.

The choice of the risk threshold dictates the schedule of biopsies and has to be made on each subsequent follow-up visit of a patient. In this regard, a straightforward approach is choosing a fixed risk threshold, such as 5% or 10% risk, at all follow-up visits. Fixed risk thresholds may be chosen by patients and/or doctors according to how they weigh the relative harms of doing an unnecessary biopsy and a missed cancer progression if the biopsy is not conducted²⁶. Although, the number of unnecessary biopsies a risk threshold may eventually lead to is related to its accuracy of classification between patients whose cancers have progressed and patients without cancer progression. The classification accuracy of a risk threshold also varies over the follow-up period. This motivates an alternative approach, where at each follow-up visit a unique threshold is chosen on the basis of its classification accuracy. More specifically, given the time of latest biopsy t of patient j, and his current visit time s we are interested in a visit-specific biopsy threshold κ , which gives the highest cancer progression detection rate (true positive rate, or TPR) for the period (t, s]. However, we also intend to balance for unnecessary biopsies (high false positive rate), or a low number of correct detections (high false negative rate) when the false positive rate is minimized. An approach to mitigate these issues is to maximize the TPR and positive predictive value (PPV) simultaneously. To this end, we utilize the F_1 score, which is a composite of both TPR and PPV (estimated as in Rizopoulos et al., 2017²⁷), and is defined as:

$$F_{1}(t, s, \kappa) = 2 \frac{\text{TPR}(t, s, \kappa) \text{ PPV}(t, s, \kappa)}{\text{TPR}(t, s, \kappa) + \text{PPV}(t, s, \kappa)},$$

$$\text{TPR}(t, s, \kappa) = \Pr\{R_{j}(s \mid t) > \kappa \mid t < T_{j}^{*} \leq s\},$$

$$\text{PPV}(t, s, \kappa) = \Pr\{t < T_{j}^{*} \leq s \mid R_{j}(s \mid t) > \kappa\}.$$
(6)

The F_1 score ranges between 0 and 1, where a value of 1 signifies perfect TPR and PPV. Since a high F_1 score is desired, the visit-specific threshold $\kappa = \arg\max_{\kappa} F_1(t,s,\kappa)$. The utility on which we evaluate the personalized schedules based on fixed risk threshold at all visits, as well as visit-specific risk threshold using F_1 score, is the total number of biopsies scheduled, and the delay in detection of cancer progression (details in Results).

Simulation Study

Although the personalized decision making approach is motivated by the PRIAS study, it is not possible to evaluate it on the PRIAS dataset. This is because the patients in PRIAS have already had their biopsies as per the PRIAS protocol. In addition, the true time of cancer progression is interval or right censored for all patients, making it impossible to correctly estimate the delay in detection of cancer progression due to a particular schedule. To this end, we conduct an extensive simulation study to find the utility of personalized, PRIAS, and fixed/heuristic schedules. For a realistic comparison, we simulate data from the joint model fitted to the PRIAS dataset. The simulated population has the same ten year follow-up period as the PRIAS study. In addition, the recovered relations between PSA and DRE measurements, and the risk of cancer progression are retained in the simulated population.

From this population, we first sample 500 datasets, each representing a hypothetical AS program with 1000 patients in it. We generate a true cancer progression time for each of the 500×1000 patients, and then sample a set of PSA and DRE measurements at the same follow-up visit times as given in PRIAS protocol. We then split each dataset into a training (750 patients) and a test (250 patients) part, and generate a random and noninformative censoring time for the training patients. We next fit a joint model of the specification given in Equations (1), (2), and (3) to each of the 500 training datasets and obtain MCMC samples from the 500 sets of the posterior distribution of the parameters.

In each of the 500 hypothetical AS programs, we utilize the corresponding fitted joint models to develop cancer progression risk profiles for each of the 500×250 test patients. We make the decision of biopsies for patients at their pre-scheduled follow-up visits for DRE and PSA measurements (see Study Population), on the basis of their

visit and patient-specific estimated cumulative risk of cancer progression. These decisions are made iteratively until a positive biopsy is observed. A recommended gap of one year between consecutive biopsies³ is also maintained. Subsequently, for each patient, an entire personalized schedule of biopsies is obtained.

We evaluate and compare both personalized and currently practiced schedules of biopsies in this in this simulation study. Comparison of the schedules is based on the number of biopsies scheduled and the corresponding delay in detection of cancer progression. We evaluate the following currently practiced fixed/heuristic schedules: biopsy annually, biopsy every one and a half years, biopsy every two years and biopsy every three years. We also evaluate the biopsy schedule of the PRIAS program (see Introduction). For the personalized biopsy schedules, we evaluate schedules based on three fixed risk thresholds: 5%, 10% and 15%, and a personalized schedule where a follow-up visit-specific risk threshold is chosen using F_1 score.

Results

From the joint model fitted to the PRIAS dataset, we found that both $\log_2\{PSA+1\}$ velocity, and log odds of having DRE > T1c were significantly associated with the hazard of cancer progression. For any patient, an increase in $\log_2\{PSA+1\}$ velocity from -0.03 to 0.16 (first and third quartiles of the fitted velocities, respectively) corresponds to a 1.94 fold increase in the hazard of cancer progression. Whereas, an increase in log odds of DRE > T1c from -6.65 to -4.36 (first and third quartiles of the fitted log odds, respectively) corresponds to a 1.40 fold increase in the hazard of cancer progression. Detailed results pertaining to the fitted joint model are presented in Appendix B.

Comparison of Various Approaches for Biopsies

From the simulation study, we obtain the number of biopsies and the delay in detection of cancer progression for each of the 500×250 test patients using different schedules. The corresponding median number of biopsies and delay are shown in Figure 6. The personalized and PRIAS approaches fall in the region of better balance between the number of biopsies and the delay, than fixed/heuristic schedules. We next evaluate these schedules on the basis of both median, and interquartile range (IQR) of the number of

biopsies and delay. For brevity, only the most widely used annual and PRIAS schedules, the proposed personalized approach with fixed risk thresholds of 5% and 10%, and visit-specific threshold chosen using F_1 score are discussed next (see Appendix C for remaining).

Since patients have varying cancer progression speeds, the impact of each schedule also varies with it. In order to highlight these differences, we divide results for three types of patients, as per their time of cancer progression. They are *fast*, *intermediate*, and *slow progressing* patients. Although such a division may be imperfect and can only be done retrospectively in a simulation setting, we do it only for the purpose of illustration. Roughly 50% of the patients did not obtain cancer progression in the ten year follow-up period of the simulation study. We assume these patients to be *slow progressing* patients. We assume *fast progressing* patients are the ones with an initially misdiagnosed state of cancer 28, or high-risk patients who choose AS instead of immediate treatment upon diagnosis. These are roughly 30% of the population, having a cancer progression time less than 3.5 years. We label the remaining 20% patients as *intermediate progressing* patients.

The boxplots in Figure 7, show the variation in the number of biopsies, and the delay in detection of cancer progression, in years (time of positive biopsy - true time of cancer progression) due to various biopsy schedules, for these three types of patients. For *fast progressing* patients (Panel A, Figure 7), we can see that the personalized schedules with fixed 10% risk threshold and visit-specific threshold chosen using F_1 score, reduce one biopsy for 50% of the patients, compared to PRIAS and annual schedule. Despite this, the delay due to personalized schedule with fixed 10% risk threshold (median: 0.7 years, IQR: 0.7 years), and the currently practiced annual (median: 0.6 years, IQR: 0.6 years) and PRIAS schedule (median: 0.7 years, IQR: 0.7 years), is similar.

For *intermediate progressing* patients (Panel A, Figure 7), we can see that the delay due to personalized schedule with fixed 5% risk threshold (median: 0.6 years, IQR: 0.6 years) is comparable to that of annual schedule (median 0.5 years, IQR: 0.5 years). However, it schedules fewer biopsies (median: 6, IQR: 2) than the annual schedule (median: 7, IQR: 3). The delay for PRIAS (median: 0.7 years, IQR: 1 year) and personalized schedule with fixed 10% risk (median: 0.7, IQR: 0.9) is similar, but the personalized approach schedules one less biopsy for 50% (median) of the

patients. Although the approach with visit-specific risk threshold chosen using F_1 score schedules fewer biopsies than the 10% fixed risk approach, but it also has a higher delay.

The patients who are at the most advantage with the personalized schedules are the *slow progressing* patients. These are a total of 50% patients who did not progress during the entire study. Hence, the delay is not available for these patients (Panel C of Figure 7). For all of these patients, annual schedule leads to 10 (unnecessary) biopsies. The PRIAS schedule, schedules a median of 6 biopsies (IQR: 4). In comparison, the biopsies scheduled by the personalized schedules using fixed 10% risk threshold (median: 4, IQR: 2) and visit-specific risk chosen using F_1 score (median: 2, IQR: 2), are much fewer.

Discussion

In this paper, we proposed a methodology for making personalized decisions for biopsies in prostate cancer patients included in active surveillance (AS) programs. Unlike prostate cancer screening programs, AS programs include only the patients diagnosed with low-grade prostate cancer. psies are scheduled iteratively for AS patients, with the goal to detect tancer progression, and subsequently provide medical treatment. In order to detect cancer progression as early as possible, currently, AS programs use frequent schedules of biopsies (e.g. annual biopsies). However, biopsies are burdensome 4,5, and patients do not always comply with them³. This may increase the risk of delay in detection of cancer progression. To address these issues, in this work we developed a methodology to schedule biopsies on the basis of a patient's estimated cumulative risk of cancer progression. Our methodology estimates this personalized risk by combining a patient's entire history of prostatespecific antigen (PSA) levels and digital rectal examination (DRE) scores, and results of the latest biopsy. To this end, we model the aforementioned data and the correlation between them using a joint model for time-toevent and longitudinal data (see Figure 4). Our method schedules a biopsy if the cumulative risk of cancer progression at a follow-up visit is above a risk threshold (see Figure 5).

The proposed personalized method has the following advantages over the currently practiced fixed/heuristic schedules ^{6,8} of biopsies. Firstly, it accounts for variation in cancer progression speeds of patients over time.

In contrast, the fixed/heuristic schedules use a common schedule for all patients, which leads to many unnecessary biopsies in the case of slow progressing (almost 50% of all patients, see Results) patients. Secondly, by providing urologists and patients an estimate of the cumulative risk of cancer progression, a more informed decision of biopsy can be made. The personalized method also has advantages over the in-practice PRIAS schedule of the world's largest AS program PRIAS. In PRIAS, the PSA profiles of patients are modeled linearly over time, which is contrary to observed PSA profiles of the patients (see Figure 6 in Appendix B). Consequently, PRIAS' method of scheduling more biopsies for only the fast progressing patients, may not always correctly identify fast progressing patients. To this end, we assume a non-linear profile for both PSA values and rate of change of PSA values, and utilize the complete observed data (historical PSA and DRE, time of latest biopsy) to obtain the cumulative risk of cancer progression (see Equation 5), which is a finer and easier to understand quantitative measure.

We compared the personalized approach with the in-practice biopsy schedules, by conducting a realistic and extensive simulation study. We evaluated the biopsy schedules on the basis of the number of biopsies they schedule, and the corresponding delay in detection of cancer progression. From the simulation study we found that both the personalized and PRIAS schedules provide much better balance between the number of biopsies and delay in detection of progression, than the fixed/heuristic approaches (see Figure 6). Since, we conducted a simulation study, we are able to retrospectively check the impact of different schedules on patients with different speeds of cancer progression. In this regard, we observed that the commonly used annual schedule puts the highest burden on the slow progressing patients (see Figure 7), by scheduling ten biopsies for each such patient. The PRIAS schedule, despite its effort to identify such patients using PSA doubling time, schedules a minimum of four and a median of six unnecessary biopsies for them. In contrast, the personalized biopsy decision making approach reduces it to a median of two to four biopsies depending upon the choice of the risk threshold.

In this regard, a personalized approach with a 10% risk threshold has a similar delay in detection of cancer progression as PRIAS, and it schedules less biopsies (see Figure 7). While, it may seem attractive for clinical use, but in light of the non-compliance results³, prescribing the same threshold

to all patients may not be suitable. In addition, results pertaining to a fixed risk threshold are valid under the assumption that the same risk threshold is chosen at all follow-up visits even if a patient becomes more/less apprehensive later in AS. For more apprehensive patients, who intend to undergo fewest biopsies, a personalized schedule with risk chosen on the basis of F_1 score may be more suitable. This is because it schedules the least biopsies (median: 2, IQR: 2) among all schedules we tested in the simulation study. However, there is a 40% chance of having a delay more than fourteen months if the patient is not *slow progressing* (unforeseeable). A delay of fourteen months is assumed to be unlikely to increase risk for adverse outcomes 6,7 .

A limitation of our results is that, even if they are based on the world's largest AS program, other AS programs may differ in the patient characteristics⁶. In this regard, a simulation study based on a multi-center cohort is required. Currently, the follow-up of period of our study is ten years. More detailed results, especially for *slow progressing* patients, can be obtained using a cohort having a longer follow-up period. Since Biopsy Gleason grading is susceptible to inter-observer variation²⁹, accounting for it in our model will also be interesting to investigate further. There is also potential for including diagnostic information from magnetic resonance imaging (MRI) in our model. Lastly, considering quality of life measures while discussing utility of each personalized approach may also lead to better decision making. However, given the scarceness of such information in the dataset, including it in the current model may not be feasible.

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Supplemental material

Supplementary material for this article are available after references and figures in this document.

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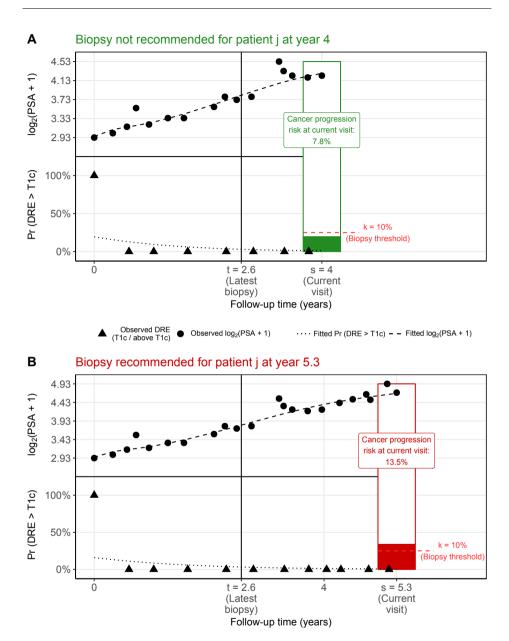


Figure 5. Illustration of personalized decision of biopsy for patient j at two different follow-up visits. Biopsy is recommended if the personalized cumulative risk of cancer progression estimated from the joint model fitted to the observed data of the patient, is higher than the example risk threshold for biopsy ($\kappa=10\%$). **Panel A:** biopsy is not recommended for the patient j at the follow-up visit time s=4 years, because his estimated personalized cumulative risk of cancer progression (7.8%) is less than the threshold. **Panel B:** biopsy is recommended for the patient j at the follow-up visit time s=5.3 years, because his estimated personalized cumulative risk of cancer progression (13.5%) is more than the threshold.

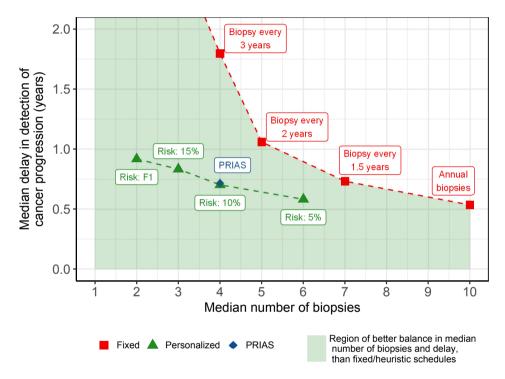


Figure 6. Simulation study results for burden-biopsy frontier: Estimated median number of biopsies, and median delay in detection of cancer progression, due to the currently practiced fixed/heuristic biopsy schedules (red squares) and PRIAS schedule (blue rhombus), and personalized schedules (green triangles), over a follow-up of ten years. The green shaded region depicts the region of better balance in number of biopsies and delay, than the currently practiced fixed/heuristic schedules. Estimation is based on results obtained from the simulation study we conducted.

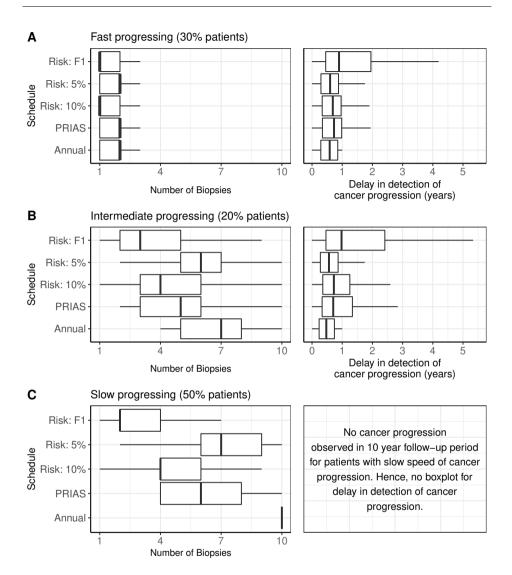


Figure 7. Boxplot showing variation in the number of biopsies, and the delay in detection of cancer progression, in years (time of positive biopsy - true time of cancer progression) for various biopsy schedules. Biopsies are conducted until cancer progression is detected. **Panel A:** results for simulated patients who had a faster speed of cancer progression, with progression times between 0 and 3.5 years. **Panel B:** results for simulated patients who had an intermediate speed of cancer progression, with progression times between 3.5 and 10 years. **Panel C:** results for simulated patients who did not have cancer progression in the ten years of follow-up. **Types of personalized schedules:** Risk: 10% and Risk: 5% approaches, schedule biopsy if the risk of cancer progression at a visit is more than 10% and 5%, respectively. Risk: F1 works similar as previous, except that a visit-specific risk threshold is chosen by maximizing F1 score (see Methods). Annual corresponds to a schedule of yearly biopsies and PRIAS corresponds to biopsies as per PRIAS protocol (see Introduction).

Supplementary Materials for "Personalized Decision Making for Biopsies in Prostate Cancer Active Surveillance Programs"

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Appendix A Bivariate Joint Model for the Longitudinal PSA, and DRE Measurements, and Time to Cancer Progression

In this appendix section, we first provide an introduction to the world's largest active surveillance (AS) program called Prostate Cancer Research International Active Surveillance, abbreviated as PRIAS (Bokhorst et al., 2016), that we use to develop our methodology. We then present an introduction to the joint models for time-to-event and longitudinal data (Rizopoulos, 2012; Tsiatis and Davidian, 2004), that we fit to the PRIAS dataset. Lastly, we present the parameter estimation for our model using the Bayesian approach.

Appendix A.1 PRIAS Dataset

we use the data of prostate cancer patients from the world's largest AS study called PRIAS Bokhorst et al., 2016. More than 100 medical centers from 17 countries worldwide contribute to the collection of data, utilizing a common study protocol and a web-based tool, both available at www.prias-project.org. We use the data collected between December 2006 (beginning of the study) and December 2016. It consists of 5270 patients. Cancer progression is observed in 866 patients. For all patients, PSA measurements (ng/mL) are scheduled every 3 months for the first 2 years and every 6 months thereafter. The DRE measurements (ordinal scale) are scheduled every 6 months. We use the DRE measurements after converting them to a binary scale, namely DRE > T1c and DRE = T1c. A DRE score of T1cSchröder et al., 1992 indicates a clinically inapparent tumor which is not palpable or visible by imaging. Tumors with DRE > T1c are large enough to be palpable. On average 5 DRE and 9 PSA measurements have been recorded per patient. Larger values for

PSA and/or larger score for DRE, may indicate cancer progression. However, it is the occurrence of biopsy Gleason score larger than 6, that is commonly considered as cancer progression. In the PRIAS study, biopsies are scheduled at the following fixed follow-up times (measured since inclusion in AS): year 1, 4, 7, and 10, and every 5 years thereafter. An annual schedule of biopsies is prescribed to those patients who have a PSA doubling time between 0 and 10 years. The PSA doubling time at any point during follow-up is measured as the inverse of the slope of the regression line through the base two logarithm of the observed PSA values.

In Figure 1, we show the survival probability of cancer progression estimated using the cancer progression times observed for the patients from the PRIAS program. Prostate cancer is a slowly progressing disease, which is evident by the large proportion of patients not having a cancer progression by the end of the ten year follow-up period.

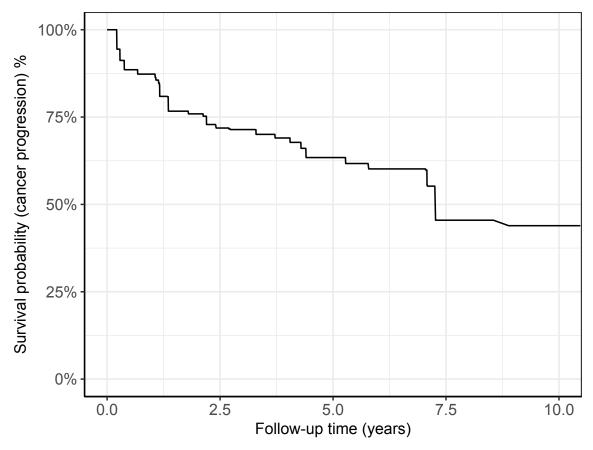


Figure 1: Estimated survival probability of cancer progression in AS: for patients in the Prostate Cancer Research International Active Surveillance (PRIAS) dataset. Nearly 50% patients (*slow progressing*) do not progress in the ten year follow-up period. Estimation is done using a nonparametric maximum likelihood estimate, of the distribution function for interval censored cancer progression times (Turnbull, 1976).

Appendix A.2 Model Definition

Let T_i^* denote the true cancer progression time of the *i*-th patient included in PRIAS. Since biopsies are conducted periodically, T_i^* is observed with interval censoring $l_i < T_i^* \le r_i$. When progression is observed for the patient at his latest biopsy time r_i , then l_i denotes the time of the second latest biopsy. Otherwise, l_i denotes the

time of the latest biopsy and $r_i = \infty$. Let \boldsymbol{y}_{di} and \boldsymbol{y}_{pi} denote his observed DRE and PSA longitudinal measurements, respectively. The observed data of all n patients is denoted by $\mathcal{D}_n = \{l_i, r_i, \boldsymbol{y}_{di}, \boldsymbol{y}_{pi}; i = 1, \dots, n\}$.

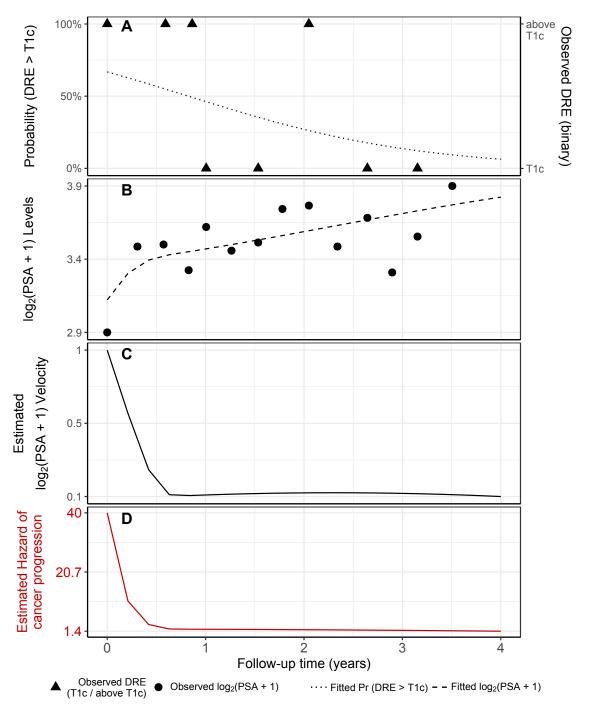


Figure 2: Illustration of the joint model fitted to the PRIAS dataset. Panel A: shows the observed DRE scores and the fitted probability of obtaining DRE > T1c (Equation 1) for . Panel B: shows the observed and fitted $\log_2(PSA+1)$ levels (Equation 2). Panel C: shows the estimated $\log_2(PSA+1)$ velocity (velocity cannot be observed directly) over time. The hazard function (Equation 3) shown in Panel D, depends on the fitted $\log_2(PSA+1)$ value and velocity.

In our joint model, the patient-specific PSA and DRE measurements over time are modeled using a bivariate generalized linear mixed effects sub-model. The sub-

model for DRE is given by (see Panel A, Figure 2):

$$logit[Pr{y_{di}(t) > T1c}] = \beta_{0d} + b_{0di} + (\beta_{1d} + b_{1di})t + \beta_{2d}(Age_i - 70) + \beta_{3d}(Age_i - 70)^2$$
(1)

where, t denotes the follow-up visit time, and Age_i is the age of the i-th patient at the time of inclusion in AS. The fixed effect parameters are denoted by $\{\beta_{0d}, \ldots, \beta_{3d}\}$, and $\{b_{0di}, b_{1di}\}$ are the patient specific random effects. With this definition, we assume that the patient-specific log odds of obtaining a DRE score larger than T1c remain linear over time.

The mixed effects sub-model for PSA is given by (see Panel B, Figure 2):

$$\log_2 \{y_{pi}(t) + 1\} = m_{pi}(t) + \varepsilon_{pi}(t),$$

$$m_{pi}(t) = \beta_{0p} + b_{0pi} + \sum_{k=1}^{4} (\beta_{kp} + b_{kpi}) B_k(t, \mathcal{K})$$

$$+ \beta_{5p} (\text{Age}_i - 70) + \beta_{6p} (\text{Age}_i - 70)^2, \tag{2}$$

where, $m_{pi}(t)$ denotes the underlying measurement error free value of $\log_2(\mathrm{PSA}+1)$ transformed (Lin et al., 2000; Pearson et al., 1994) measurements at time t. We model it non-linearly over time using B-splines (De Boor et al., 1978). To this end, our B-spline basis function $B_k(t,\mathcal{K})$ has 3 internal knots at $\mathcal{K} = \{0.1, 0.7, 4\}$ years, and boundary knots at 0 and 5.42 years (95-th percentile of the observed follow-up times). The fixed effect parameters are denoted by $\{\beta_{0p}, \ldots, \beta_{6p}\}$, and $\{b_{0pi}, \ldots, b_{4pi}\}$ are the patient specific random effects. The error $\varepsilon_{pi}(t)$ is assumed to be t-distributed with three degrees of freedom (see Appendix B.1) and scale σ , and is independent of the random effects.

To account for the correlation between the DRE and PSA measurements of a patient, we link their corresponding random effects. More specifically, the complete vector of random effects $\boldsymbol{b}_i = (b_{0di}, b_{1di}, b_{0pi}, \dots, b_{4pi})^T$ is assumed to follow a multivariate normal distribution with mean zero and variance-covariance matrix \boldsymbol{D} .

To model the impact of DRE and PSA measurements on the risk of cancer progression, our joint model uses a relative risk sub-model. More specifically, the hazard of cancer progression $h_i(t)$ at a time t is given by (see Panel D, Figure 2):

$$h_i(t) = h_0(t) \exp\left(\gamma_1(Age_i - 70) + \gamma_2(Age_i - 70)^2 + \alpha_{1d}logit\left[\Pr\{y_{di}(t) > T1c\}\right] + \alpha_{1p}m_{pi}(t) + \alpha_{2p}\frac{\partial m_{pi}(t)}{\partial t}\right),$$
(3)

where, γ_1, γ_2 are the parameters for the effect of age. The parameter α_{1d} models the impact of log odds of obtaining a DRE > T1c on the hazard of cancer progression. The impact of PSA on the hazard of cancer progression is modeled in two ways: a) the impact of the error free underlying PSA value $m_{pi}(t)$ (see Panel B, Figure 2), and b) the impact of the underlying PSA velocity $\partial m_{pi}(t)/\partial t$ (see Panel C, Figure 2). The corresponding parameters are α_{1p} and α_{2p} , respectively. Lastly, $h_0(t)$ is the baseline hazard at time t, and is modeled flexibly using P-splines (Eilers and Marx, 1996). More specifically:

$$\log h_0(t) = \gamma_{h_0,0} + \sum_{q=1}^{Q} \gamma_{h_0,q} B_q(t, \boldsymbol{v}),$$

where $B_q(t, \mathbf{v})$ denotes the q-th basis function of a B-spline with knots $\mathbf{v} = v_1, \dots, v_Q$ and vector of spline coefficients γ_{h_0} . To avoid choosing the number and position of knots in the spline, a relatively high number of knots (e.g., 15 to 20) are chosen and the corresponding B-spline regression coefficients γ_{h_0} are penalized using a differences penalty (Eilers and Marx, 1996). An example fitted hazard is shown in panel D of Figure 2.

Appendix A.3 Parameter Estimation

We estimate the parameters of the joint model using Markov chain Monte Carlo (MCMC) methods under the Bayesian framework. Let θ denote the vector of all of the parameters of the joint model. The joint model postulates that given the random effects, the time to cancer progression, and the PSA and DRE measurements taken over time are all mutually independent. Under this assumption the posterior distribution of the parameters is given by:

$$p(\boldsymbol{\theta}, \boldsymbol{b} \mid \mathcal{D}_n) \propto \prod_{i=1}^n p(l_i, r_i, \boldsymbol{y}_{di}, \boldsymbol{y}_{pi}, \mid \boldsymbol{b}_i, \boldsymbol{\theta}) p(\boldsymbol{b}_i \mid \boldsymbol{\theta}) p(\boldsymbol{\theta})$$

$$\propto \prod_{i=1}^n p(l_i, r_i \mid \boldsymbol{b}_i, \boldsymbol{\theta}) p(\boldsymbol{y}_{di} \mid \boldsymbol{b}_i, \boldsymbol{\theta}) p(\boldsymbol{y}_{pi} \mid \boldsymbol{b}_i, \boldsymbol{\theta}) p(\boldsymbol{b}_i \mid \boldsymbol{\theta}) p(\boldsymbol{\theta}),$$

$$p(\boldsymbol{b}_i \mid \boldsymbol{\theta}) = \frac{1}{\sqrt{(2\pi)^q \det(\boldsymbol{D})}} \exp(\boldsymbol{b}_i^T \boldsymbol{D}^{-1} \boldsymbol{b}_i),$$

where, the likelihood contribution of the DRE outcome, conditional on the random effects is:

$$p(\boldsymbol{y}_{di} \mid \boldsymbol{b}_i, \boldsymbol{\theta}) = \prod_{k=1}^{n_{di}} \frac{\exp\left[-\operatorname{logit}\left\{\Pr(y_{dik} > \operatorname{T1c})\right\} I(y_{dik} = \operatorname{T1c})\right]}{1 + \exp\left[-\operatorname{logit}\left\{\Pr(y_{dik} > \operatorname{T1c})\right\}\right]},$$

where $I(\cdot)$ is an indicator function which takes the value 1 if the k-th repeated DRE score $y_{dik} = \text{T1c}$, and takes the value 0 otherwise. The likelihood contribution of the PSA outcome, conditional on the random effects is:

$$p(\boldsymbol{y}_{pi} \mid \boldsymbol{b}_i, \boldsymbol{\theta}) = \frac{1}{\left(\sqrt{2\pi\sigma^2}\right)^{n_{pi}}} \exp\bigg(-\frac{\|\boldsymbol{y}_{pi} - \boldsymbol{m}_{pi}\|^2}{\sigma^2}\bigg),$$

The likelihood contribution of the time to cancer progression outcome is given by:

$$p(l_i, r_i \mid \boldsymbol{b}_i, \boldsymbol{\theta}) = \exp\left\{-\int_0^{l_i} h_i(s) ds\right\} - \exp\left\{-\int_0^{r_i} h_i(s) ds\right\}.$$
(4)

The integral in (4) does not have a closed-form solution, and therefore we use a 15-point Gauss-Kronrod quadrature rule to approximate it.

We use independent normal priors with zero mean and variance 100 for the fixed effects $\{\beta_{0d}, \ldots, \beta_{3d}, \beta_{0p}, \ldots, \beta_{6p}\}$, and inverse Gamma prior with shape and rate both equal to 0.01 for the parameter σ^2 . For the variance-covariance matrix \boldsymbol{D} of the random effects we take inverse Wishart prior with an identity scale matrix and degrees of freedom equal to 7 (number of random effects). For the relative risk model's parameters $\{\gamma_1, \gamma_2\}$ and the association parameters $\{\alpha_{1d}, \alpha_{1p}, \alpha_{2p}\}$, we use independent normal priors with zero mean and variance 100.

Appendix A.4 Personalized Posterior Predictive Distribution of Time of Cancer Progression

Let us assume a new patient j, for whom we need to make a personalized biopsy decision. Let his current follow-up visit time be s, latest time of biopsy be $t \leq s$, observed vectors of DRE and PSA measurements be $\mathcal{Y}_{dj}(s)$ and $\mathcal{Y}_{pj}(s)$, respectively. The combined information from the observed data is given by the following posterior predictive distribution $g(T_j^*)$ of his time of cancer progression T_j^* :

$$g(T_j^*) = p\{T_j^* \mid T_j^* > t, \mathcal{Y}_{dj}(s), \mathcal{Y}_{pj}(s), \mathcal{D}_n\}$$

$$= \int \int p\{T_j^* \mid T_j^* > t, \boldsymbol{b}_j, \boldsymbol{\theta}\}$$

$$\times p\{\boldsymbol{b}_j \mid T_j^* > t, \mathcal{Y}_{dj}(s), \mathcal{Y}_{pj}(s), \boldsymbol{\theta}\} p(\boldsymbol{\theta} \mid \mathcal{D}_n) d\boldsymbol{b}_j d\boldsymbol{\theta}.$$

The distribution $g(T_j^*)$ depends on observed data of the patient $\mathcal{Y}_{dj}(s)$ and $\mathcal{Y}_{pj}(s)$, as well information from the PRIAS dataset \mathcal{D}_n via the posterior distribution of random effects \boldsymbol{b}_j and posterior distribution of the vector of all parameters $\boldsymbol{\theta}$, respectively.

The distribution can be estimated as detailed in Rizopoulos, Molenberghs, and Lesaffre (2017). However, majority of the prostate cancer patients do not progress in the ten year follow-up period of PRIAS (see Figure 1). Consequently, the personalized density function of cancer progression $g(T_j^*)$ can only be estimated for time points falling within the ten year follow-up.

Appendix B Parameter Estimates from the Joint Model Fitted to the PRIAS Dataset

We fit a joint model to the PRIAS dataset using the R package **JMbayes** (Rizopoulos, 2016). The corresponding posterior parameter estimates are shown in Table 2 (longitudinal sub-model for DRE outcome), Table 3 (longitudinal sub-model for PSA outcome) and Table 4 (relative risk sub-model). The parameter estimates for the variance-covariance matrix \boldsymbol{D} from the longitudinal sub-model are shown in the following Table 1:

Table 1: Estimated variance-covariance matrix \mathbf{D} of the random effects $\mathbf{b} = (b_{0d}, b_{1d}, b_{0p}, b_{1p}, b_{2p}, b_{3p}, b_{4p})$ (see Appendix A.2) from the joint model fitted to the PRIAS dataset. The variances of the random effects are highlighted along the diagonal of the variance-covariance matrix.

Random Effects	b_{0d}	b_{1d}	b_{0p}	b_{1p}	b_{2p}	b_{3p}	$\overline{b_{4p}}$
b_{0d}	7.55	-0.56	-0.18	0.08	0.084	0.003	-0.019
b_{1d}	-0.564	1.379	0.081	0.119	0.165	0.266	0.219
$\overline{b_{0p}}$	-0.182	0.081	0.208	0.031	0.034	0.068	0.014
b_{1p}	0.075	0.119	0.031	0.224	0.109	0.158	0.088
b_{2p}	0.084	0.165	0.034	0.109	0.293	0.324	0.238
b_{3p}	0.003	0.266	0.068	0.158	0.324	0.480	0.312
b_{4p}	-0.019	0.219	0.014	0.088	0.238	0.312	0.290

For the DRE mixed effects sub-model (see Equation 1) parameter estimates, in Table 2 we can see that the age of the patient trivially affects the baseline log odds of obtaining a DRE score larger than T1c. In Figure 3 we present the marginal evolution of log odds of obtaining a DRE larger than T1c, and the corresponding marginal probability, over a period of 10 years for a hypothetical AS patient who is included in AS at the age of 70 years. In addition, we present plots of observed DRE versus fitted probabilities of obtaining a DRE score larger than T1c, for nine randomly selected patients in Figure 4.

Table 2: Estimated mean and 95% credible interval for the parameters of the longitudinal sub-model (see Equation 1) for the DRE outcome.

Variable	Mean	Std. Dev	2.5%	97.5%	P
(Intercept)	-4.017	0.136	-4.270	-3.763	< 0.001
(Age - 70)	0.058	0.009	0.041	0.075	< 0.001
$(Age - 70)^2$	-0.001	0.001	-0.003	0.000	0.076
${\bf visit Time Years}$	-0.604	0.095	-0.794	-0.437	< 0.001

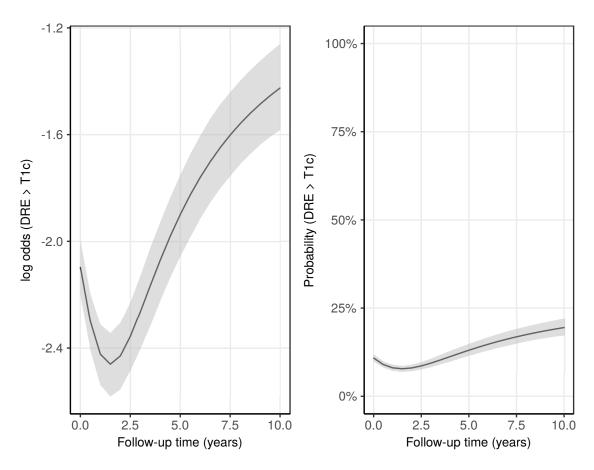


Figure 3: Fitted marginal evolution of the log odds of obtaining a DRE larger than T1c, and the corresponding marginal probability, with 95% credible interval. These results are for a hypothetical AS patient who is included in AS at the age of 70 years.

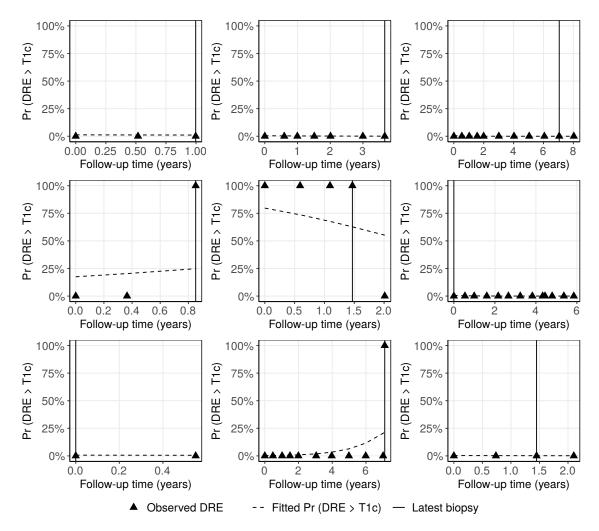


Figure 4: Observed DRE versus fitted probabilities of obtaining a DRE score larger than T1c, for nine randomly selected PRIAS patients. The fitted profiles utilize information from the observed DRE scores, PSA levels, and time of the latest biopsy. Observed DRE scores plotted against 0% probability are equal to T1c. Observed DRE scores plotted against 100% probability are larger than T1c.

For the PSA mixed effects sub-model parameter estimates (see Equation 2), in Table 3 we can see that the age of the patient trivially affects the baseline $\log_2(\text{PSA}+1)$ level. Since the longitudinal evolution of $\log_2(\text{PSA}+1)$ levels is modeled with non-linear terms, the interpretation of the coefficients corresponding to time is not straightforward. In lieu of the interpretation, in Figure 5 we present the fitted marginal evolution of $\log_2(\text{PSA}+1)$ over a period of 10 years for a hypothetical patient who is included in AS at the age of 70 years. In addition, we present plots of observed versus fitted PSA profiles for nine randomly selected patients in Figure 6.

Table 3: Estimated mean and 95% credible interval for the parameters of the longitudinal sub-model (see Equation 2) for the PSA outcome.

Variable	Mean	Std. Dev	2.5%	97.5%	P
(Intercept)	2.701	0.008	2.686	2.716	< 0.001
(Age - 70)	0.003	0.001	0.001	0.005	< 0.001
$(Age - 70)^2$	-4.7×10^{-4}	9.8×10^{-5}	-6.6×10^{-4}	-2.7×10^{-4}	< 0.001
Spline: $[0.00, 0.10]$ years	0.054	0.009	0.037	0.073	< 0.001
Spline: $[0.10, 0.70]$ years	0.177	0.012	0.151	0.200	< 0.001
Spline: [0.70, 4.00] years	0.194	0.016	0.161	0.225	< 0.001
Spline: $[4.00, 5.42]$ years	0.341	0.015	0.312	0.371	< 0.001
σ	0.137	0.001	0.135	0.138	

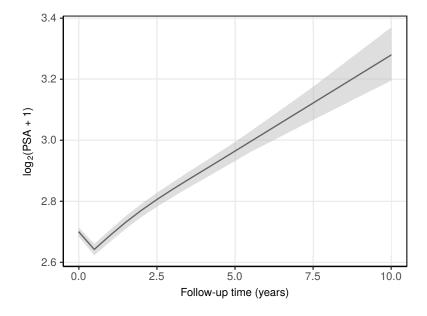


Figure 5: Fitted marginal evolution of $\log_2(\mathrm{PSA}+1)$ levels over a period of 10 years with 95% credible interval, for a hypothetical patient who is included in AS at the age of 70 years.

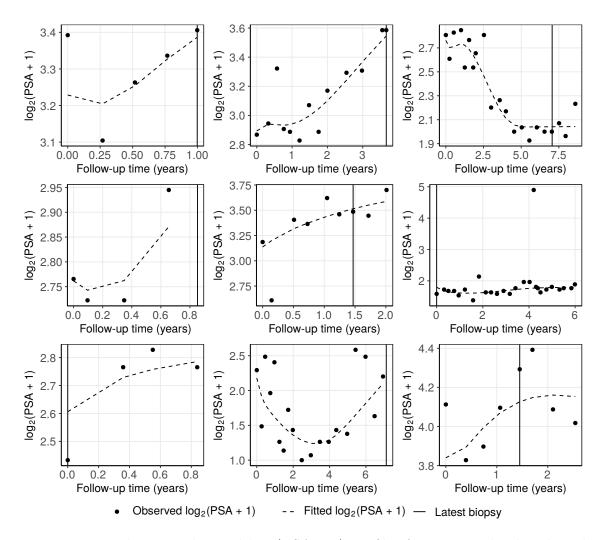


Figure 6: Fitted versus observed $log_2(PSA + 1)$ profiles for nine randomly selected PRIAS patients. The fitted profiles utilize information from the observed PSA levels, DRE scores, and time of the latest biopsy.

For the relative risk sub-model (see Equation 3), the parameter estimates in Table 4 show that both $\log_2\{PSA + 1\}$ velocity, and the log odds of having DRE > T1c were significantly associated with the hazard of cancer progression.

Table 4: Estimated mean and 95% credible interval for the parameters of the relative risk sub-model (see Equation 3) of the joint model fitted to the PRIAS dataset.

Variable	Mean	Std. Dev	2.5%	97.5%	P
(Age - 70)	0.012	0.006	0.000	0.022	0.045
$(Age - 70)^2$	-0.001	0.001	-0.002	0.000	0.095
$logit\{Pr(DRE > T1c)\}$	0.147	0.017	0.115	0.183	< 0.001
Fitted $\log_2(PSA + 1)$ value	0.104	0.078	-0.044	0.256	0.193
Fitted $\log_2(PSA + 1)$ velocity	3.396	0.564	2.376	4.475	< 0.001

It is important to note that since age, $\log_2\{PSA+1\}$ value and velocity, and $\log_2\{PSA+1\}$ value and velocity and $\log_2\{PSA+1\}$ value

Table 5: Hazard (of cancer progression) ratio and 95% credible interval (CI), for an increase in the variables of relative risk sub-model, from their first quartile (Q_1) to their third quartile (Q_3). Except for age, quartiles for all other variables are based on their fitted values obtained from the joint model fitted to the PRIAS dataset.

Variable	Q_1	Q_3	Hazard ratio [95% CI]
Age	65	75	1.129 [1.002, 1.251]
$logit{Pr(DRE > T1c)}$	-6.650	-4.356	1.402 [1.301, 1.521]
$\log_2(PSA + 1)$ value	2.336	3.053	1.079 [0.969, 1.201]
$\log_2(\mathrm{PSA} + 1)$ velocity	-0.032	0.161	1.938 [1.582, 2.372]

Appendix B.1 Assumption of t-distributed (df=3) Error Terms

With regards to the choice of the distribution for the error term ε_p for the PSA measurements (see Equation 2), we attempted fitting multiple joint models differing in error distribution, namely t-distribution with three, and four degrees of freedom, and a normal distribution for the error term. However, the model assumption for the error term were best met by the model with t-distribution having three degrees of freedom. The quantile-quantile plot of subject-specific residuals for the corresponding model in Panel A of Figure 7, shows that the assumption of t-distributed (df=3) errors is reasonably met by the fitted model.

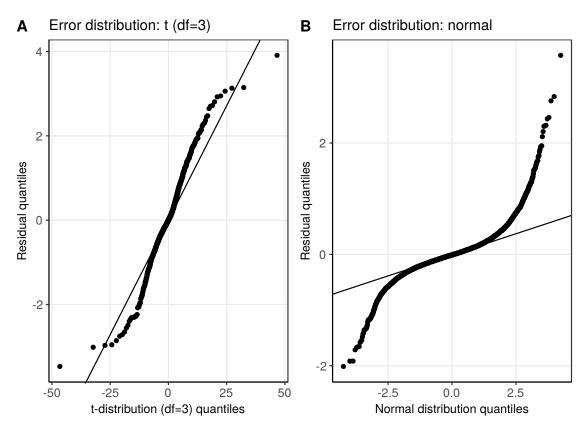


Figure 7: Quantile-quantile plot of subject-specific residuals from the joint models fitted to the PRIAS dataset. **Panel A**: model assuming a t-distribution (df=3) for the error term ε_p . **Panel B**: model assuming a normal distribution for the error term ε_p .

Appendix B.2 Predictive Performance of the Joint Model Fitted to the PRIAS dataset

We evaluate the predictive performance of our model using two measures: the area under the receiver operating characteristic curve (AUC), and the prediction error. Given the longitudinal nature of the data at hand, in a joint model time dependent AUC and prediction errors are more relevant. More specifically, given the time of latest biopsy t, and history of DRE and PSA measurements up to time s, we are interested in a medically relevant time frame (t, s], within which the occurrence of cancer progression is of interest. In the case of prostate cancer, at any point in time it is of interest to identify patients who may have obtained cancer progression in the last one year (s - t = 1). Using data of the patients from the PRIAS study, we calculate the AUC and prediction error (see Rizopoulos, Molenberghs, and Lesaffre (2017) for estimation) at the following s: year one, year two, year three, year four, and year five (95-percentile of observed cancer progression times) of follow-up in AS. The resulting AUC, and prediction are presented in Table 6.

Table 6: Area under the receiver operating characteristic curves (AUC), and prediction error, with 95% confidence interval in brackets.

Follow-up year	AUC	Prediction Error
1	0.651 [0.633, 0.663]	0.055 [0.052, 0.059]
2	0.621 [0.610, 0.640]	0.144 [0.140, 0.148]
3	0.748 [0.728, 0.770]	0.076 [0.075, 0.078]
4	0.710 [0.691, 0.736]	0.076 [0.072, 0.079]
5	0.592 [0.577, 0.614]	0.107 [0.103, 0.112]

Appendix C Full Results of the Simulation Study

In the simulation study, we evaluate the following in-practice fixed/heuristic approaches (Inoue et al., 2018; Loeb et al., 2014) for biopsies: biopsy every year, biopsy every one and a half years, biopsy every two years and biopsy every three years. For the personalized biopsy approach we evaluate three fixed risk thresholds: 5%, 10% and 15%, and a risk threshold chosen using F_1 score. Lastly, we also evaluate the PRIAS schedule of biopsies. We compare all the aforementioned schedules on two criteria, namely the number of biopsies they schedule and the corresponding delay in detection of cancer progression, in years (time of positive biopsy - true time of cancer progression). The corresponding results, using 500×250 test patients are presented in Table 7.

Table 7: Simulation study results for all patients: Estimated first, second (median), and third quartiles for number of biopsies $(Q_1^{nb}, Q_2^{nb}, Q_3^{nb})$ and for the delay in detection of cancer progression $(Q_1^{\text{delay}}, Q_2^{\text{delay}}, Q_3^{\text{delay}})$, in years, for various biopsy schedules. The delay is equal to the difference between the time of the positive biopsy and the unobserved true time of progression. The results in the table are obtained from test patients of our simulation study.

In-practice schedules	Q ₁ nb	Q_2^{nb}	Q_3^{nb}	Q_1^{delay}	Q_2^{delay}	Q_3^{delay}	
Every year (annual)	3	10	10	0.3	0.5	0.8	
Every 1.5 years	2	7	7	0.4	0.7	1.1	
Every 2 years	2	5	5	0.6	1.1	1.5	
Every 3 years	1	4	4	1.1	1.8	2.3	
PRIAS	2	4	6	0.3	0.7	1.0	
Personalized approach	Personalized approach						
Risk threshold: 5%	2	6	8	0.3	0.6	0.9	
Risk threshold: 10%	2	4	5	0.3	0.7	1.0	
Risk threshold: 15%	2	3	4	0.4	0.8	1.4	
Risk using F_1 score	1	2	3	0.5	0.9	2.2	

Since patients have varying cancer progression speeds, the impact of each schedule also varies with it. In order to highlight these differences we divide results for three types of patients, as per their time of cancer progression. They are fast, intermediate, and slow progressing patients. Although such a division may be imperfect and can only be done retrospectively in a simulation setting, we do it only for the purpose of illustration. We assume that the slow progressing patients, are the 50% of the total population, having a cancer progression time after the ten year follow-up period of the study (see Figure 1). We assume fast progressing patients, are the patients with an initially misdiagnosed state of cancer (Cooperberg et al., 2011), or high risk patients who choose AS instead of immediate treatment. These are roughly 30% of the population, having a cancer progression time less than 3.5 years. We label the remaining 20% patients as intermediate progressing patients. Table 8, Table 9, and Table 10 show the results for the fast, intermediate, and slow progressing patients, respectively.

Table 8: Simulation study results for fast progressing patients (30% of all patients): Estimated first, second (median), and third quartiles for number of biopsies (Q_1^{nb} , Q_2^{nb} , Q_3^{nb}) and for the delay in detection of cancer progression (Q_1^{delay} , Q_2^{delay} , Q_3^{delay}), in years, for various biopsy schedules. The delay is equal to the difference between the time of the positive biopsy and the unobserved true time of progression. The results in the table are obtained from the fast progressing test patients of our simulation study.

In-practice schedules	Q_1^{nb}	Q_2^{nb}	Q_3^{nb}	Q_1^{delay}	Q_2^{delay}	Q_3^{delay}
Every year (annual)	1	2	2	0.3	0.6	0.9
Every 1.5 years	1	1	2	0.4	0.8	1.2
Every 2 years	1	1	1	0.7	1.1	1.5
Every 3 years	1	1	1	1.5	2.0	2.5
PRIAS	1	2	2	0.3	0.7	1.0
Personalized approach	1					
Risk threshold: 5%	1	2	2	0.3	0.6	0.9
Risk threshold: 10%	1	1	2	0.3	0.7	1.0
Risk threshold: 15%	1	1	2	0.4	0.8	1.2
Risk using F_1 score	1	1	2	0.5	0.9	2.0

Table 9: Simulation study results for intermediate progressing patients (20% of all patients): Estimated first, second (median), and third quartiles for number of biopsies (Q_1^{nb} , Q_2^{nb} , Q_3^{nb}) and for the delay in detection of cancer progression (Q_1^{delay} , Q_2^{delay} , Q_3^{delay}), in years, for various biopsy schedules. The delay is equal to the difference between the time of the positive biopsy and the unobserved true time of progression. The results in the table are obtained from the intermediate progressing test patients of our simulation study.

In-practice schedules	Q ₁ nb	Q_2^{nb}	Q ₃ ^{nb}	Q_1^{delay}	Q_2^{delay}	Q_3^{delay}
Every year (annual)	5	7	8	0.2	0.5	0.7
Every 1.5 years	4	5	6	0.3	0.7	1.0
Every 2 years	3	4	4	0.4	1.0	1.5
Every 3 years	2	3	3	0.6	1.3	2.0
PRIAS	3	5	6	0.3	0.7	1.3
Personalized approach	1					
Risk threshold: 5%	5	6	7	0.3	0.6	0.9
Risk threshold: 10%	3	4	6	0.4	0.7	1.3
Risk threshold: 15%	3	3	5	0.4	0.8	1.7
Risk using F_1 score	2	3	5	0.5	1.0	2.4

Table 10: Simulation study results for slow progressing patients (50% of all patients): Estimated first, second (median), and third quartiles for number of biopsies (Q_1^{nb} , Q_2^{nb} , Q_3^{nb}) and for the delay in detection of cancer progression (Q_1^{delay} , Q_2^{delay} , Q_3^{delay}), in years, for various biopsy schedules. The delay is equal to the difference between the time of the positive biopsy and the unobserved true time of progression. The results in the table are obtained from the slow progressing test patients of our simulation study. Since no cancer progression is observed in the ten year follow-up period for these patients, delay cannot be estimated, and hence is not reported.

In-practice schedules	Q_1^{nb}	Q_2^{nb}	Q_3^{nb}	Q_1^{delay}	Q_2^{delay}	Q_3^{delay}
Every year (annual)	10	10	10			
Every 1.5 years	7	7	7			
Every 2 years	5	5	5			
Every 3 years	4	4	4			
PRIAS	4	6	8			
Personalized approach	1					
Risk threshold: 5%	6	7	9			
Risk threshold: 10%	4	4	6			
Risk threshold: 15%	2	3	4			
Risk using F_1 score	2	2	4			

Appendix D Source Code

The R code for fitting the joint model to the PRIAS dataset, and for the simulation study, along with sample dataset, and instructions for running the code are available with this paper at the following link:

https://github.com/anirudhtomer/prias/tree/master/src/decision_analytic

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