

# Personalized Biopsy Schedules Based on Risk of Gleason Upgrading for Low-Risk Prostate Cancer Active Surveillance Patients\*

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## Abstract

**Objective:** To develop a model and methodology for predicting the risk of Gleason *upgrading* in prostate cancer active surveillance (AS) patients, and using the predicted risks to create risk-based *personalized* biopsy schedules as an alternative to one-size-fits-all schedules (e.g., annually). Furthermore,

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to assist patients and doctors in making shared decisions of biopsy schedules, by providing them quantitative estimates of the *burden* and *benefit* of opting for personalized versus any other schedule in AS. Last, to externally validate our model and implement it along with personalized schedules in a ready to use web-application.

**Materials and Methods:** Repeat prostate-specific antigen (PSA) measurements, timing and results of previous biopsies, and age at baseline from the world’s largest AS study, Prostate Cancer Research International Active Surveillance or PRIAS (7813 patients, 1134 experienced upgrading). We fitted a Bayesian joint model for time-to-event and longitudinal data to this dataset. We then validated our model externally in the largest six AS cohorts of the Movember Foundation’s Global Action Plan (GAP3) database ( $> 20,000$  patients, 27 centers worldwide). Using the model predicted upgrading-risks, we scheduled biopsies whenever a patient’s upgrading-risk was above a certain threshold. To assist patients/doctors in choice of this threshold, and to compare the resulting personalized schedule with currently practiced schedules, along with the timing and the total number of biopsies (burden) planned, for each schedule we provided them the time delay expected in detecting upgrading (shorter is better).

**Results:** The cause-specific cumulative upgrading-risk at year five of follow-up was 35% in PRIAS, and at most 50% in GAP3 cohorts. In the PRIAS based model, PSA velocity was a stronger predictor of upgrading (Hazard Ratio: 2.47, 95%CI: 1.93–2.99) than PSA value (Hazard Ratio: 0.99,

95%CI: 0.89–1.11). Our model had a moderate area under the receiver operating characteristic curve (0.6–0.7) in validation cohorts. The prediction error was moderate (0.1–0.2) in validation cohorts where the impact of PSA value and velocity on upgrading-risk was similar to PRIAS, but large (0.2–0.3) otherwise. Our model required recalibration of baseline upgrading-risk in validation cohorts. We implemented the validated models and the methodology for personalized schedules in a web-application (<http://tiny.cc/biopsy>).

**Conclusions:** We successfully developed and validated a model for predicting upgrading-risk, and providing risk-based personalized biopsy decisions, in prostate cancer AS. Personalized prostate biopsies are a novel alternative to fixed one-size-fits-all schedules that may help to reduce unnecessary prostate biopsies while maintaining cancer control. The model and schedules made available via a web-application enable shared decision making of biopsy schedules by comparing fixed and personalized schedules on total biopsies and expected time delay in detecting upgrading.

**Keywords:** Active Surveillance, Biopsies, Personalized Medicine, Prostate Cancer, Shared Decision Making.

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## 1. Introduction

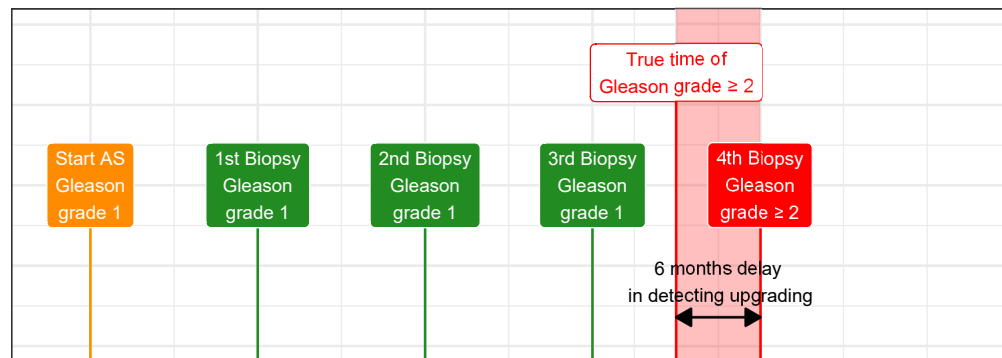
Patients with low- and very low-risk screening-detected localized prostate cancer are recommended active surveillance (AS) usually, instead of immediate radical treatment [1]. In AS, cancer progression is monitored routinely via prostate-specific antigen (PSA), digital rectal examination (DRE), repeat

6 biopsies, and recently, magnetic resonance imaging (MRI). Among these, the  
 7 strongest indicator of cancer-related outcomes is the biopsy Gleason grade  
 8 group [2]. When it increases from group 1 (Gleason 3+3) to 2 (Gleason 3+4)  
 9 or higher, it is called *upgrading* [3]. Upgrading is an important endpoint in  
 10 AS upon which patients are commonly advised curative treatment [4].

11 Biopsies in AS are always conducted with a time gap between them.  
 12 Consequently, upgrading is always detected with a time delay (Figure 1)  
 13 that cannot be measured directly. In this regard, to detect upgrading timely,  
 14 many patients are prescribed fixed and frequent biopsies, most often annu-  
 15 ally [5]. However, such one-size-fits-all schedules lead to unnecessary biopsies  
 16 in slow/non-progressing patients. Biopsies are invasive, may be painful, and  
 17 are prone to medical complications such as bleeding and septicemia[6]. Thus,  
 18 biopsy burden and patient non-compliance to frequent biopsies [7] have raised  
 19 concerns regarding the optimal biopsy schedule [8, 9] in AS.

20 Except for the confirmatory biopsy at year one of AS [7], opinions and  
 21 practice regarding the timing of remaining biopsies lack agreement [10]. Some  
 22 AS programs utilize patients' observed PSA, DRE, previous biopsy Gleason  
 23 grade, and lately, MRI results to decide biopsies [11, 4, 10]. In contrast,  
 24 others discourage schedules based on clinical data and MRI results [12, 5],  
 25 and instead support periodical one-size-fits-all biopsy schedules. Further-  
 26 more, some suggest replacing frequent periodical schedules with infrequent  
 27 ones (e.g., biennially) [8, 13]. Each of these approaches has limitations. For  
 28 example, one-size-fits-all schedules can lead to many unnecessary biopsies  
 29 because of differences in baseline *upgrading-risk* across cohorts [8]. Whereas,  
 30 since observed clinical data has measurement error (e.g., PSA fluctuations),

### A Biopsy every year



### B Biopsy every 2 years

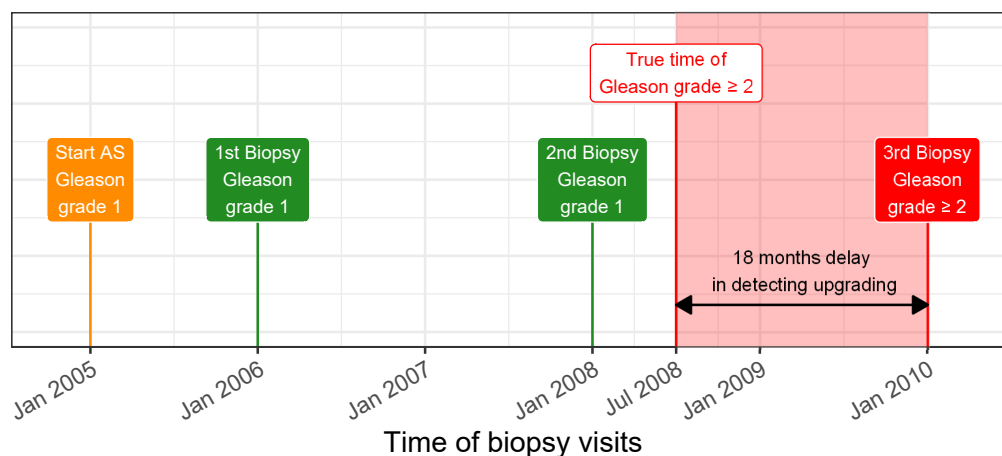
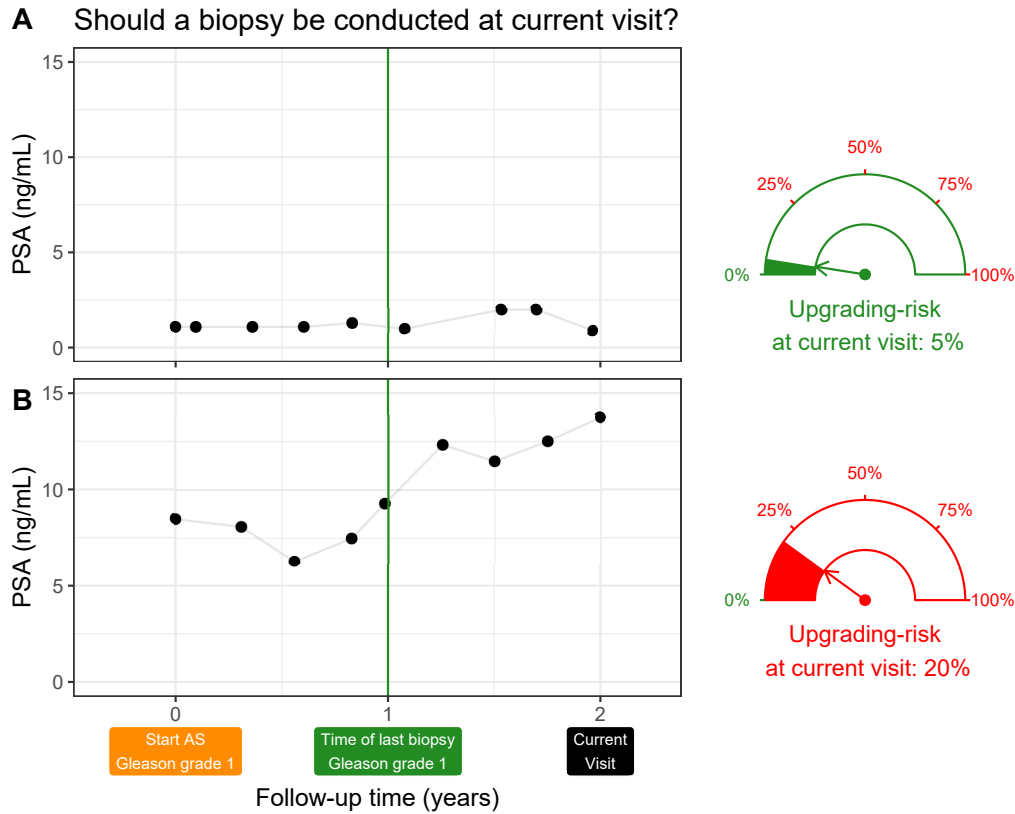


Figure 1: **Trade-off between the timing and number of biopsies (burden) and time delay in detecting Gleason upgrading (shorter is better):** The true time of Gleason upgrading (increase in Gleason grade group from group 1 to 2 or higher) for the patient in this figure is July 2008. When biopsies are scheduled annually (**Panel A**), upgrading is detected in January 2009 with a time delay of six months, and a total of four biopsies are scheduled. When biopsies are scheduled biennially (**Panel B**), upgrading is detected in January 2010 with a time delay of 18 months, and a total of three biopsies are scheduled. Since biopsies are conducted periodically, the time of upgrading is observed as an interval. For example, between Jan 2008–Jan 2009 in **Panel A** and between Jan 2008–Jan 2010 in **Panel B**. The phrase ‘Gleason grade group’ is shortened to ‘Gleason grade’ for brevity.

31 a flaw of using it directly is that it may lead to poor decisions. Also, deci-  
 32 sions based on clinical data typically rely only on the latest data point and  
 33 ignore previous repeated measurements. A novel alternative that counters  
 34 these drawbacks is first processing patient data via a statistical model, and  
 35 subsequently using model predicted upgrading-risks to create *personalized*  
 36 biopsy schedules [10] (Figure 2). While, upgrading-risk calculators are not  
 37 new [14, 15, 16, 17], not all are personalized either. Besides, they do not  
 38 specify how risk predictions can be exploited to create a schedule.

39 This work is motivated by the problem of scheduling biopsies in AS. We  
 40 have two goals. First, we want to assist practitioners in using clinical data  
 41 in biopsy decisions in a statistically sound manner. To this end, we plan to  
 42 develop a robust, generalizable statistical model that provides reliable indi-  
 43 vidual upgrading-risk in AS. Subsequently, we will employ these predictions  
 44 to derive risk-based personalized biopsy schedules. Our second goal is to  
 45 enable shared decision making of biopsy schedules. We intend to achieve this  
 46 by allowing patients and doctors to compare the *burden* and *benefit* (Fig-  
 47 ure 1) of opting for personalized schedules versus periodical schedules versus  
 48 schedules based on clinical data. Specifically, we propose timing and number  
 49 of planned biopsies (more/frequent are burdensome), and the expected time  
 50 delay in detecting upgrading (shorter is beneficial) for any given schedule.  
 51 While fulfilling our goals, we want to capture the maximum possible informa-  
 52 tion from the available data. Hence, we will use all repeated measurements  
 53 of patients, previous biopsy results, baseline characteristics, and keep our  
 54 model flexible to accommodate novel biomarkers in the future. To fit this  
 55 model, we will utilize data of the world’s largest AS study, Prostate Cancer



**Figure 2: Motivation for upgrading-risk based personalized biopsy decisions:** To utilize patients' complete longitudinal data and results from previous biopsies in making biopsy decisions. For this purpose, we first process data using a statistical model and then utilize the patient-specific predictions for risk of Gleason upgrading to schedule biopsies. For example, Patient A (**Panel A**) and B (**Panel B**) had their latest biopsy at year one of follow-up (green vertical line). Patient A's prostate-specific antigen (PSA) profile remained stable until his current visit at year two, whereas patient B's profile has shown a rise. Consequently, patient B's upgrading-risk at the current visit (year two) is higher than that of patient A. This makes patient B a more suitable candidate for biopsy than Patient A. Risk estimates in this figure are only illustrative.

Research International Active Surveillance (PRIAS). To evaluate our model, we will externally validate it in the largest six AS cohorts from the Movember Foundation’s Global Action Plan (GAP3) database [18]. Last, we aim to implement the validated model and methodology in a web-application.

## 2. Patients and Methods

### 2.1. Study Cohort

For developing a statistical model to predict upgrading-risk, we used the world’s largest AS dataset, Prostate Cancer International Active Surveillance or PRIAS [4], dated April 2019 (Table 1). In PRIAS, biopsies were scheduled at year one, four, seven, ten, and additional yearly biopsies were scheduled when PSA doubling time was between zero and ten years. We selected all 7813 patients who had Gleason grade group 1 at inclusion in AS. Our primary event of interest is an increase in this Gleason grade group observed upon repeat biopsy, called *upgrading* (1134 patients). Upgrading is a trigger for treatment advice in PRIAS. Also, 2250 patients were provided treatment based on their PSA, the number of biopsy cores with cancer, or anxiety/other reasons. However, our reasons for focusing solely on upgrading are that upgrading is strongly associated with cancer-related outcomes, and other treatment triggers vary between cohorts [10].

For externally validating our model’s predictions, we selected the following largest (by the number of repeated measurements) six cohorts from Movember Foundation’s GAP3 database [18] version 3.1, covering nearly 73% of the GAP3 patients: the University of Toronto AS (Toronto), Johns Hopkins AS (Hopkins), Memorial Sloan Kettering Cancer Center AS (MSKCC),



King’s College London AS (KCL), Michigan Urological Surgery Improvement Collaborative AS (MUSIC), and University of California San Francisco AS (UCSF, version 3.2). Only patients with a Gleason grade group 1 at the time of inclusion in these cohorts were selected. Summary statistics are presented in Supplementary A.2.

*Choice of predictors:* In our model, we used all repeated PSA measurements, the timing of the previous biopsy and Gleason grade, and age at inclusion in AS. Other predictors such as prostate volume, MRI results can also be important. MRI is utilized already for targeting biopsies, but regarding its use in deciding the time of biopsies, there are arguments both for and against it [11, 12, 19]. MRI is still a recent addition in most AS protocols. Consequently, repeated MRI data is very sparsely available in both PRIAS and GAP3 databases to make a stable prediction model. Prostate volume data is also sparsely available, especially in validation cohorts. Based on these reasons, we did not include them in our model. However, the model we propose next is extendable to include MRI and other novel biomarkers in the future.

## 2.2. Statistical Model

Modeling an AS dataset such as PRIAS, posed certain challenges. First, PSA was measured longitudinally, and over follow-up time, it did not always increase linearly. Also, PSA was available only until a patient observed upgrading. Hence, we need to accommodate the within-patient correlation for PSA, the association between the Gleason grades and PSA profiles of a patient, and handle missing PSA measurements after a patient experienced upgrading. Second, since the PRIAS biopsy schedule uses PSA, a patient’s

Table 1: **Summary of the PRIAS dataset as of April 2019.** The primary event of interest is upgrading, that is, increase in Gleason grade group from group 1 [2] to 2 or higher. IQR: interquartile range, PSA: prostate-specific antigen. Study protocol URL: <https://www.prias-project.org>

Characteristic	Value
Total patients	7813
Upgrading (primary event)	1134
Treatment	2250
Watchful waiting	334
Loss to follow-up	249
Death (unrelated to prostate cancer)	95
Death (related to prostate cancer)	2
Median age at diagnosis (years)	66 (IQR: 61–71)
Median maximum follow-up per patient (years)	1.8 (IQR: 0.9–4.0)
Total PSA measurements	67578
Median number of PSA measurements per patient	6 (IQR: 4–12)
Median PSA value (ng/mL)	5.7 (IQR: 4.1–7.7)
Total biopsies	15686
Median number of biopsies per patient	2 (IQR: 1–2)

104 observed time of upgrading was also dependent on their PSA. Thus, the effect  
 105 of PSA on the upgrading-risk need to be adjusted for the effect of PSA on  
 106 the biopsy schedule. Third, many patients obtained treatment and watchful  
 107 waiting before observing upgrading. Since we considered events other than  
 108 upgrading as censoring, the model needs to account for patients' reasons for  
 109 treatment or watchful waiting (e.g., age, treatment based on observed data).  
 110 A model that handles these challenges in a statistically sound manner is the  
 111 joint model for time-to-event and longitudinal data [20, 14, 21].

112 Our joint model consisted of two sub-models. Namely, a linear mixed-  
 113 effects sub-model [22] for longitudinally measured PSA (log-transformed),  
 114 and a relative-risk sub-model (similar to the Cox model) for the interval-  
 115 censored time of upgrading. Patient age was used in both sub-models. Re-  
 116 sults and timing of the previous negative biopsies were used only in the risk  
 117 sub-model. To account for PSA fluctuations [23], we assumed t-distributed  
 118 PSA measurement errors. The correlation between PSA measurements of the  
 119 same patient was established using patient-specific random-effects. We fitted  
 120 a unique curve to the PSA measurements of each patient (Panel A, Figure 3).  
 121 Subsequently, we calculated the mathematical derivative of the patient's fit-  
 122 ted PSA profile (Equation 2, Supplementary A), to obtain his follow-up time  
 123 specific instantaneous PSA velocity (Panel B, Figure 3). This instantaneous  
 124 velocity is a stronger predictor of upgrading than the widely used average  
 125 PSA velocity [24]. We modeled the impact of PSA on upgrading-risk by em-  
 126 ploying fitted PSA value and instantaneous velocity as predictors in the risk  
 127 sub-model (Panel C, Figure 3). We adjusted the effect of PSA on upgrading-  
 128 risk for the PSA dependent PRIAS biopsy schedule by estimating parameters

129 using a full likelihood method (proof in Supplementary A). This approach  
 130 also accommodates watchful waiting and treatment protocols that are also  
 131 based on patient data. Specifically, the parameters of our two sub-models  
 132 were estimated jointly under the Bayesian paradigm (Supplementary A) us-  
 133 ing the R package **JMbayes** [25].

### 134 2.3. Risk Prediction and Model Validation

135 Our model provides predictions for upgrading-risk over the entire future  
 136 follow-up period of a patient (Panel C, Figure 3). However, we recommend  
 137 using predictions only after year one. This is because most AS programs rec-  
 138 ommend a confirmatory biopsy at year one, especially to detect patients who  
 139 may be misdiagnosed as low-grade at inclusion in AS. The model also au-  
 140 tomatically updates risk-predictions over follow-up as more patient data be-  
 141 comes available (Figure 5, Supplementary B). We validated our model inter-  
 142 nally in the PRIAS cohort, and externally in the largest six GAP3 database  
 143 cohorts. We employed calibration plots [26, 27] and follow-up *time-dependent*  
 144 mean absolute risk prediction error or MAPE [28] to graphically and quan-  
 145 titatively evaluate our model’s risk prediction accuracy, respectively. We  
 146 assessed our model’s ability to discriminate between patients who experi-  
 147 ence/do not experience upgrading via the time-dependent area under the  
 148 receiver operating characteristic curve or AUC [28].

149 The aforementioned *time-dependent* AUC and MAPE [28] are temporal  
 150 extensions of their standard versions [27] in a longitudinal setting. Specif-  
 151 ically, at every six months of follow-up, we calculated a unique AUC and  
 152 MAPE for predicting upgrading-risk in the subsequent one year (Supplemen-  
 153 tary B.1). For emulating a realistic situation, we calculated the AUC and

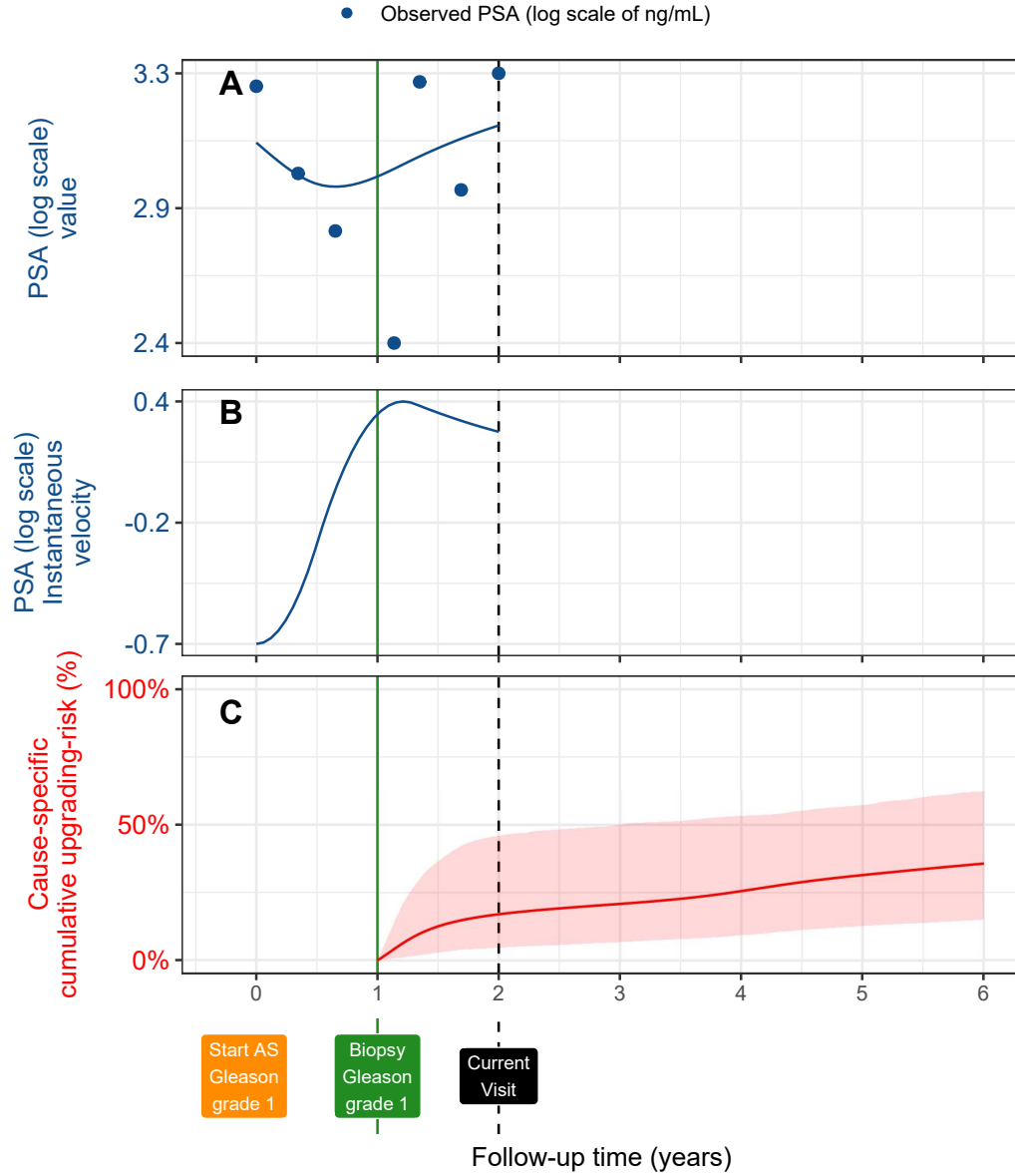


Figure 3: **Illustration of the joint model on a real PRIAS patient.** **Panel A:** Observed PSA (blue dots) and fitted PSA (solid blue line), log-transformed from ng/mL. **Panel B:** Estimated instantaneous velocity of PSA (log-transformed). **Panel C:** Predicted cause-specific cumulative upgrading-risk (95% credible interval shaded). Upgrading is defined as an increase in the Gleason grade group from group 1 [2] to 2 or higher. This upgrading-risk is calculated starting from the time of the latest negative biopsy (vertical green line at year one of follow-up). The joint model estimated it by combining the fitted PSA (log scale) value and instantaneous velocity, and time of the latest negative biopsy. Black dashed line at year two denotes the time of current visit.

MAPE at each follow-up using only the validation data available until that follow-up. Last, to resolve any potential model miscalibration in validation cohorts, we aimed to recalibrate our model’s baseline hazard of upgrading (Supplementary B.1), individually for each cohort.

### 3. Results

The cause-specific cumulative upgrading-risk at year five of follow-up was 35% in PRIAS and at most 50% in validation cohorts (Panel B, Figure 4). In the fitted PRIAS model, the adjusted hazard ratio (aHR) of upgrading for an increase in patient age from 61 to 71 years (25-th to 75-th percentile) was 1.45 (95%CI: 1.30–1.63). For an increase in fitted PSA value from 2.36 to 3.07 (25-th to 75-th percentile, log scale), the aHR was 0.99 (95%CI: 0.89–1.11). The strongest predictor of upgrading-risk was instantaneous PSA velocity, with an increase from -0.09 to 0.31 (25-th to 75-th percentile), giving an aHR of 2.47 (95%CI: 1.93–2.99). The aHR for PSA value and velocity was different in each GAP3 cohort (Supplementary Table 8).

The time-dependent AUC, calibration plot, and time-dependent MAPE of our model are shown in Figure 4, and Supplementary Figure 8. In all cohorts, time-dependent AUC was moderate (0.6 to 0.7) over the whole follow-up period. Time-dependent MAPE was moderate (0.1 to 0.2) in those cohorts where the impact of PSA on upgrading-risk was similar to PRIAS (e.g., Hopkins cohort, Supplementary Table 8), and large (0.2 to 0.3) otherwise. Our model was miscalibrated for validation cohorts (Panel B, Figure 4). Recalibrating the baseline hazard of upgrading in validation cohorts resolved this issue (Supplementary Figure 6). We compared risk predictions from the

178 recalibrated models, with predictions from separately fitted cohort-specific  
 179 joint models (Supplementary Figure 7). The difference in predictions was  
 180 lowest in the Johns Hopkins cohort (impact of PSA on upgrading-risk sim-  
 181 ilar to PRIAS). Comprehensive results are in Supplementary A.3 and Sup-  
 182 plementary B.

### 183 *3.1. Personalized Biopsy Schedules*

184 We employed the PRIAS based fitted model to create personalized biopsy  
 185 schedules for real PRIAS patients. Particularly, first using the model and pa-  
 186 tient’s observed data, we predicted his cumulative upgrading-risk (Figure 5)  
 187 on all of his future follow-up visits (biannually in PRIAS). Subsequently,  
 188 we planned biopsies on those future visits where his conditional cumulative  
 189 upgrading-risk was more than a certain threshold (see Supplementary C for  
 190 mathematical details). The choice of this threshold dictates the timing of  
 191 biopsies in a risk-based personalized schedule. For example, personalized  
 192 schedules based on 5% and 10% risk thresholds are shown in Figure 5, and  
 193 in Supplementary Figure 10–12.

194 To facilitate the choice of a risk-threshold, and for comparing the conse-  
 195 quences of opting for a risk-based schedule versus any other schedule (e.g.,  
 196 annual, PRIAS), we predict expected time delay in detecting upgrading for  
 197 following a schedule. We are able to predict this delay for any schedule. For  
 198 example, in Panel C of Figure 5, the annual schedule has the least expected  
 199 delay. In contrast, a personalized schedule based on a 10% risk threshold has  
 200 a slightly larger expected delay, but it also schedules much fewer biopsies.  
 201 An important aspect of this delay is that it is personalized as well. That is,  
 202 even if two different patients are prescribed the same biopsy schedule, their

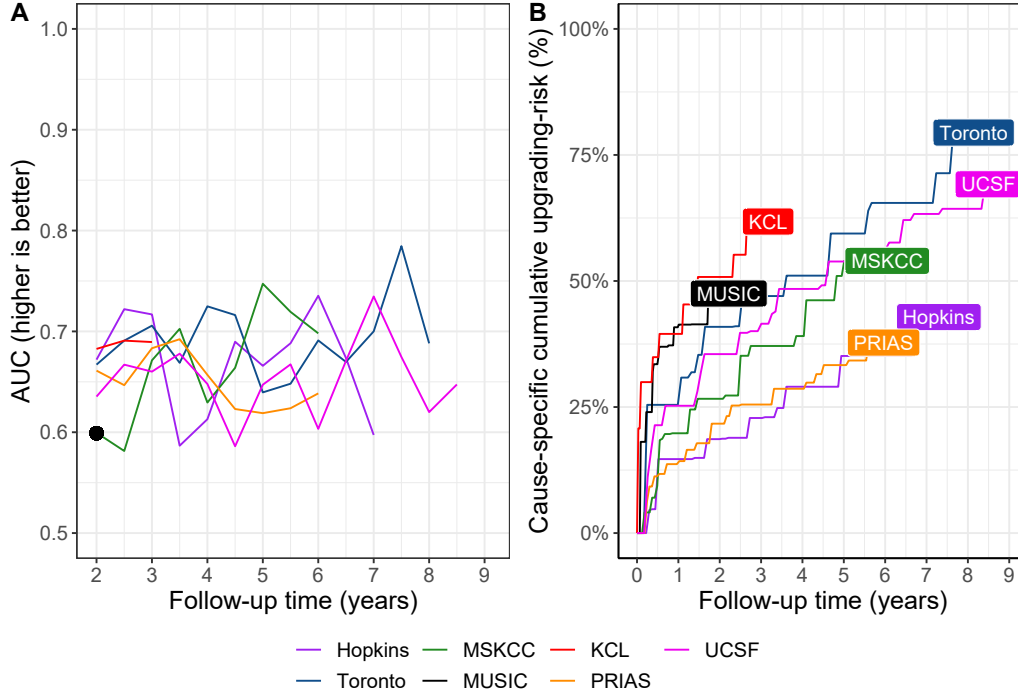


Figure 4: **Model Validation Results.** **Panel A:** time-dependent area under the receiver operating characteristic curve or AUC (measure of discrimination). AUC at year one is not shown because we do not intend to replace the confirmatory biopsy at year one. **Panel B:** calibration-at-large indicates model miscalibration. This is because solid lines depicting the non-parametric estimate of the cause-specific cumulative upgrading-risk [29], and dashed lines showing the average cause-specific cumulative upgrading-risk obtained using the joint model fitted to the PRIAS dataset, are not overlapping. Recalibrating the baseline hazard of upgrading resolved this issue (Supplementary Figure 6). Full names of Cohorts are *PRIAS*: Prostate Cancer International Active Surveillance, *Toronto*: University of Toronto Active Surveillance, *Hopkins*: Johns Hopkins Active Surveillance, *MSKCC*: Memorial Sloan Kettering Cancer Center Active Surveillance, *KCL*: King's College London Active Surveillance, *MUSIC*: Michigan Urological Surgery Improvement Collaborative Active Surveillance, *UCSF*: University of California San Francisco AS.



203 expected delays will be different. This is because delay is estimated using all  
 204 available clinical data of the patient (see Supplementary C). While the timing  
 205 and the total number of planned biopsies denote the burden of a schedule, a  
 206 shorter expected time delay in detecting upgrading can be a benefit. These  
 207 two, along with other measures such as a patient’s comorbidities, anxiety,  
 208 etc., can help to make an informed biopsy decision.

### 209 *3.2. Web-Application*

210 We implemented the PRIAS based model, recalibrated models for GAP3  
 211 cohorts, and personalized schedules in a user-friendly web-application [https://emcbiostatistics.shinyapps.io/prias\\_biopsy\\_recommender/](https://emcbiostatistics.shinyapps.io/prias_biopsy_recommender/). This  
 212 application works on both desktop and mobile devices. Patient data can be  
 213 entered in Microsoft Excel format. The maximum follow-up time up to which  
 214 predictions can be obtained depends on each cohort (Supplementary Table 9).  
 215 The web-application supports personalized, annual, and PRIAS schedules.  
 216 For personalized schedules, users can control the choice of risk-threshold.  
 217 The web-application also compares the resulting risk-based schedule’s tim-  
 218 ing of biopsies, and expected time delay in detecting upgrading, with annual  
 219 and PRIAS schedules, to enable sharing biopsy decision making.

## 221 **4. Discussion**

222 We successfully developed and externally validated a statistical model for  
 223 predicting upgrading-risk [3] in prostate cancer AS, and providing risk-based  
 224 personalized biopsy decisions. Our work has four novel features over earlier  
 225 risk calculators [14, 15]. First, our model was fitted to the world’s largest  
 226 AS dataset PRIAS and externally validated in the largest six cohorts of the

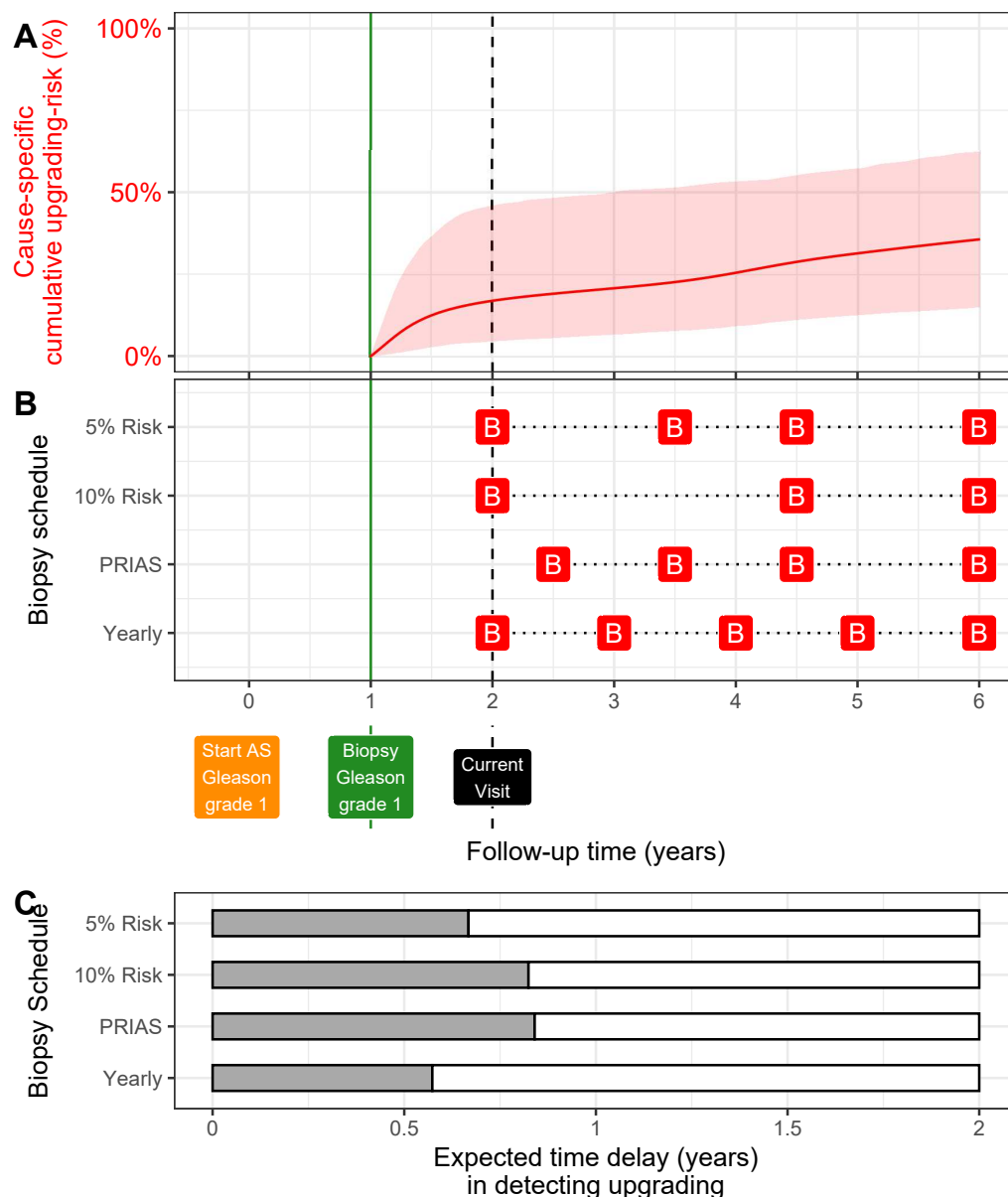


Figure 5: **Illustration of personalized and fixed schedules of biopsies for patient from Figure 3.** **Panel A:** Predicted cumulative upgrading-risk (95% credible interval shaded). **Panel B:** Different biopsy schedules with a red 'B' indicating a future biopsy. Risk: 5% and Risk: 10% are personalized schedules in which a biopsy is planned whenever the conditional cause-specific cumulative upgrading-risk is above 5% or 10% risk, respectively. Green vertical line at year one is the time of the latest negative biopsy. Black dashed line at year two denotes the time of the current visit. **Panel C:** Expected time delay in detecting upgrading (years) if patient progresses before year six. A compulsory biopsy was scheduled at year six (maximum biopsy scheduling time in PRIAS, Supplementary C) in all schedules for a meaningful comparison between them.

227 Movember Foundation’s GAP3 database [18]. Second, the model predicts a  
 228 patient’s current and future upgrading-risk in a personalized manner. Third,  
 229 using the predicted risks, we created personalized biopsy schedules. We also  
 230 calculated the expected time delay in detecting upgrading (less is benefi-  
 231 cial) for following any schedule. Thus, patients/doctors can compare sched-  
 232 ules before making a choice. Fourth, we implemented our methodology in a  
 233 user-friendly web-application ([https://emcbiostatistics.shinyapps.io/  
 234 prias\\_biopsy\\_recommender/](https://emcbiostatistics.shinyapps.io/prias_biopsy_recommender/)) for both PRIAS and validated cohorts.

235 Our model and methods can be useful for numerous patients from PRIAS  
 236 and the validated GAP3 cohorts (nearly 73% of all GAP3 patients). The  
 237 model utilizes all repeated PSA measurements, results of previous biopsies,  
 238 and baseline characteristics of a patient. We could not include MRI and  
 239 PSA volume because of sparsely available data in both PRIAS and GAP3  
 240 databases. But, our model is extendable to include them in the near fu-  
 241 ture. The current discrimination ability of our model, exhibited by the *time-*  
 242 *dependent* AUC, was between 0.6 and 0.7 over-follow. While this is moderate,  
 243 it is also so because unlike the standard AUC [27] the time-dependent AUC  
 244 is more conservative as it utilizes only the validation data available until the  
 245 time at which it is calculated. The same holds for the time-dependent MAPE  
 246 (mean absolute prediction error). Although, MAPE varied much more be-  
 247 tween cohorts than AUC. In cohorts where the effect size for the impact of  
 248 PSA value and velocity on upgrading-risk was similar to that for PRIAS  
 249 (e.g., Hopkins cohort), MAPE was moderate. Otherwise, MAPE was large  
 250 (e.g., KCL and MUSIC cohorts). We required recalibration of our model’s  
 251 baseline hazard of upgrading for all validation cohorts.

252 The clinical implications of our work are as follows. First, the cause-  
 253 specific cumulative upgrading-risk at year five of follow-up was at most 50%  
 254 in all cohorts (Panel B, Figure 4). That is, many patients may not re-  
 255 quire some of the biopsies planned in the first five years of AS. Given the  
 256 non-compliance and burden of frequent biopsies [7], the availability of our  
 257 methodology as a web-application may encourage patients/doctors to con-  
 258 sider upgrading-risk based personalized schedules instead. An additional ad-  
 259 vantage of personalized schedules is that they update as more patient data  
 260 becomes available over follow-up. We have shown via a simulation study [30]  
 261 that personalized schedules plan, on average, six fewer biopsies compared to  
 262 annual schedule and two fewer biopsies than the PRIAS schedule in slow/non-  
 263 progressing AS patients, while maintaining almost the same time delay in  
 264 detecting upgrading as PRIAS schedule. Personalized schedules with dif-  
 265 ferent risk thresholds indeed have different performance. In this regard, to  
 266 assist patients/doctors in choosing between fixed schedules and personalized  
 267 schedules based on different risk thresholds, the web-application provides a  
 268 patient-specific estimate of the expected time delay in detecting upgrading,  
 269 for both personalized and fixed schedules. We hope that this will objectively  
 270 address patient apprehensions regarding adverse outcomes in AS. Last, we  
 271 note that our web-application should only be used to decide biopsies after  
 272 the compulsory confirmatory biopsy at year one of follow-up.

273 This work has certain limitations. Predictions for upgrading-risk and per-  
 274 sonalized schedules are available only for a currently limited, cohort-specific,  
 275 follow-up period (Supplementary Table 9). This problem can be mitigated  
 276 by refitting the model with new follow-up data in the future. Recently, some

cohorts started utilizing MRI to explore the possibility of targeting visible lesions by biopsy. Presently, the GAP3 database has limited MRI follow-up data available. As more such data becomes available, the current model can be extended to include MRI based predictors. We scheduled biopsies using cause-specific cumulative upgrading-risk, which ignores competing events such as treatment based on the number of positive biopsy cores. Employing a competing-risk model may lead to improved personalized schedules. Upgrading is susceptible to inter-observer variation too. Models which account for this variation [14, 31] will be interesting to investigate further. Even with an enhanced risk prediction model, the methodology for personalized scheduling and calculation of expected time delay (Supplementary C) need not change. Last, our web-application only allows uploading patient data in Microsoft Excel format. Connecting it with patient databases can increase usability.

## 5. Conclusions

We successfully developed a statistical model and methodology for predicting upgrading-risk, and providing risk-based personalized biopsy decisions, in prostate cancer AS. We externally validated our model, covering nearly 73% patients from the Movember Foundations' GAP3 database. The model made available via a user-friendly web-application ([https://emcbiostatistics.shinyapps.io/prias\\_biopsy\\_recommender/](https://emcbiostatistics.shinyapps.io/prias_biopsy_recommender/)) enables shared decision making of biopsy schedules by comparing fixed and personalized schedules on total biopsies and expected time delay in detecting upgrading. Novel biomarkers and MRI data can be added as predictors in the model to

improve predictions in the future. Recalibration of baseline upgrading-risk is advised for cohorts not validated in this work.

### Author Contributions

Anirudh Tomer had full access to all the data in the study and takes responsibility for the integrity of the data and the accuracy of the data analysis.

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### 335 **Conflicts of Interest**

336 The authors do not report any conflict of interest, and have nothing to  
 337 disclose.

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