$\mathcal{O}$ after lower-pass