Law of double negation:  $\neg \neg P$  LEQV P

De Morgan's laws:  $\neg (P \land Q) \quad \texttt{LEQV} \quad \neg P \lor \neg Q$ 

 $\neg (P \lor Q)$  LEQV  $\neg P \land \neg Q$ 

Commutative laws:  $P \wedge Q$  LEQV  $Q \wedge P$ 

 $P \lor Q$  LEQV  $Q \lor P$ 

Associative laws:  $P \wedge (Q \wedge R)$  LEQV  $(P \wedge Q) \wedge R$ 

 $P \lor (Q \lor R)$  Lequ  $(P \lor Q) \lor R$ 

Distributive laws:  $P \wedge (Q \vee R)$  LEQV  $(P \wedge Q) \vee (P \wedge R)$ 

 $P \lor (Q \land R)$  LEQV  $(P \lor Q) \land (P \lor R)$ 

Identity laws:  $P \wedge (Q \vee \neg Q)$  LEQV P

 $P \lor (Q \land \neg Q)$  LEQV P

Idempotency laws:  $P \wedge P$  Lequer P

 $P \lor P$  LEQV P

ightarrow law: P 
ightarrow Q Lequ  $\neg P \lor Q$ 

 $\leftrightarrow$  law:  $P \leftrightarrow Q$  LEQV  $P \land Q \lor \neg P \land \neg Q$ 

Duality of quantifiers:

I.  $\neg \mathbf{Q} x \ F \text{ leqv } \overline{\mathbf{Q}} x \ \neg F$ 

Factoring quantifiers:

IIa.  $E \wedge \mathbf{Q}x$  F LEQV  $\mathbf{Q}x$   $(E \wedge F)$ , if x is not free in E

IIb.  $E \vee \mathbf{Q}x$  F LEQV  $\mathbf{Q}x$   $(E \vee F)$ , if x is not free in E

IIc.  $\mathbf{Q}x \ E \wedge F$  LEQV  $\mathbf{Q}x \ (E \wedge F)$ , if x is not free in F

IId.  $\mathbf{Q}x \ E \lor F \ \text{LEQV} \ \mathbf{Q}x \ (E \lor F)$ , if x is not free in F

He.  $\mathbf{Q}x \ E \to F$  Lequer  $\overline{\mathbf{Q}}x \ (E \to F)$ , if x is not free in F

IIf.  $E \to \mathbf{Q}x$  F LEQV  $\mathbf{Q}x$   $(E \to F)$ , if x is not free in E

Renaming of quantified variables:

III.  $\mathbf{Q}x \ F \ \text{LEQV} \ \mathbf{Q}y \ F_y^x$ , if y does not occur in F