

No.

for $D(q)$.Date $\dot{q}_T: \dot{q}$ for all 6 joints. J_{iv} : first half of Jacobian for joint i J_{iw} : second half of Jacobian for joint i but this is just $[J_{iv}, 0, 0, 0, 0, 0]$ this $\begin{bmatrix} \dot{q}_i \\ \vdots \end{bmatrix}$ will just be \dot{q}_T and will be fine

$$\dot{q} = J_{iv} \cdot \dot{q}_i \Rightarrow \dot{q}_i = J_{iv}^{-1} \dot{q} \quad \omega_i = J_{iw} \dot{q}_i$$

$$\omega = J_{iw} \cdot \dot{q} \quad \dot{q}_i = J_{iv}^{-1} \begin{bmatrix} \dot{q}_1 \\ \vdots \\ \dot{q}_n \end{bmatrix} \quad \omega_2 = J_2 \omega \begin{bmatrix} \dot{q}_1 \\ \vdots \\ \dot{q}_n \end{bmatrix}$$

total kinetic energy \rightarrow number of joints

DOF for 6 joints total

$$T = \sum_{i=1}^n \left[\frac{1}{2} m_i \dot{q}_i^T \dot{q}_i + \frac{1}{2} \omega_i^T J_{oi} \omega_i \right]$$

aside:

$$J_{oi} = J_{oi} - m[(c_i - b_i)x]^2$$

$$= \sum_{i=1}^n \left[\frac{1}{2} m_i \dot{q}_i^T J_{iv}^T J_{iv} \dot{q}_i + \frac{1}{2} \dot{q}_i^T J_{iw}^T J_{oi} J_{iw} \dot{q}_i \right]$$

$$\text{since: } T = \frac{1}{2} \dot{q}_T^T D(q) \dot{q}_T$$

$$D(q) = \sum_{i=1}^n \left[m_i \cdot J_{iv}^T J_{iv} + J_{iw}^T J_{oi} J_{iw} \right]$$

For J_{oi} at each joint:

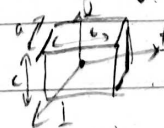
$$I_z = \frac{1}{2} m r^2$$

$$I_x = I_y = \frac{1}{12} m (3r^2 + h^2)$$

$$J_{oi} = \begin{bmatrix} I_x & 0 & 0 \\ 0 & I_y & 0 \\ 0 & 0 & I_z \end{bmatrix}$$

use relation matrix to get J_{oi}
and use H-S formula
to get J_{oi}

For Rectangular Solid:



$$I_1 = \int_{-\frac{a}{2}}^{\frac{a}{2}} \int_{-\frac{b}{2}}^{\frac{b}{2}} \int_{-\frac{c}{2}}^{\frac{c}{2}} (k^2 + j^2) \rho(x, y, z) dx dy dz$$

$$= \frac{m}{abc} \iiint (k^2 + j^2) dx dy dz$$

$$= \frac{m}{3} \cdot \left(3(k^2 + j^2) + \frac{c^2 + b^2}{4} \right)$$

$$I_2 = \frac{m}{3} \cdot \left(3(j^2 + k^2) + \frac{a^2 + b^2}{4} \right)$$

$$I_k = \frac{m}{3} \cdot \left(3(i^2 + j^2) + \frac{b^2 + c^2}{4} \right)$$

$$J_{oi} = \begin{bmatrix} I_i & 0 \\ 0 & I_k \end{bmatrix}$$

 c_i - center of mass

For $C(q, \dot{q})$:

First need to get: V (potential energy)

$$V_i = g^T \cdot r_{ci} m_i$$

coordinate
of centre of gravity.

$$g = \begin{bmatrix} 0 \\ 0 \\ 9.81 \end{bmatrix}$$

$$V_T = \sum_{i=0}^N g^T r_{ci} m_i$$

$$L = T - V$$

$$\tau_i = \frac{d}{dt} \frac{\partial L}{\partial \dot{\theta}_i} - \frac{\partial L}{\partial \theta_i}$$

$C(q, \dot{q})\dot{q}$ = terms in τ_i that contains $\dot{\theta}_i$ and not on $\ddot{\theta}$ or g
 $G(q)$ = terms in τ_i that contains g .

$$M(q) = J_{motor} + D(q),$$

$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} + B\dot{q} + G(q) = u$$

dynamic friction $f = I_{no-load} \cdot \frac{\text{Torque constant}(k_t)}{\text{Speed no-load}}$

$$\ddot{q} = m^{-1}(q) \cdot (u - G(q) - B\dot{q} - C(q, \dot{q})\dot{q})$$