

1. probability of event A occurs given event B

$$P(A|B) = \frac{P(AB)}{P(B)}$$

Similarity,

$$P(B|A) = \frac{P(AB)}{P(A)}$$

Combine both formula

$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

Bayes theorem is a method for calculating conditional probabilities or the likelihood of one event occurring if another has previously occurred.

A condition probability can lead to more accurate outcomes cause using condition probability means more data we have.

2. if the two tests are independent, the posterior probabilities for cancer and  $\neg$  cancer are the same.

$$P(\text{cancer}) = 0.008 \quad P(\neg \text{cancer}) = 0.992$$

$$P(+ | \text{cancer}) = 0.98 \quad P(- | \text{cancer}) = 0.02$$

$$P(+ | \neg \text{cancer}) = 0.03 \quad P(- | \neg \text{cancer}) = 0.97$$

$$h(\text{cancer})_{\max} = P(+ | \text{cancer}) P(\text{cancer}) = 0.98 \times 0.08 = 0.078$$

$$h(\neg \text{cancer})_{\max} = P(+ | \neg \text{cancer}) P(\neg \text{cancer}) = 0.03 \times 0.992 = 0.0298$$

The step is warranted as Bayes theorem states that the posterior probabilities are just  $P(+)$ ,

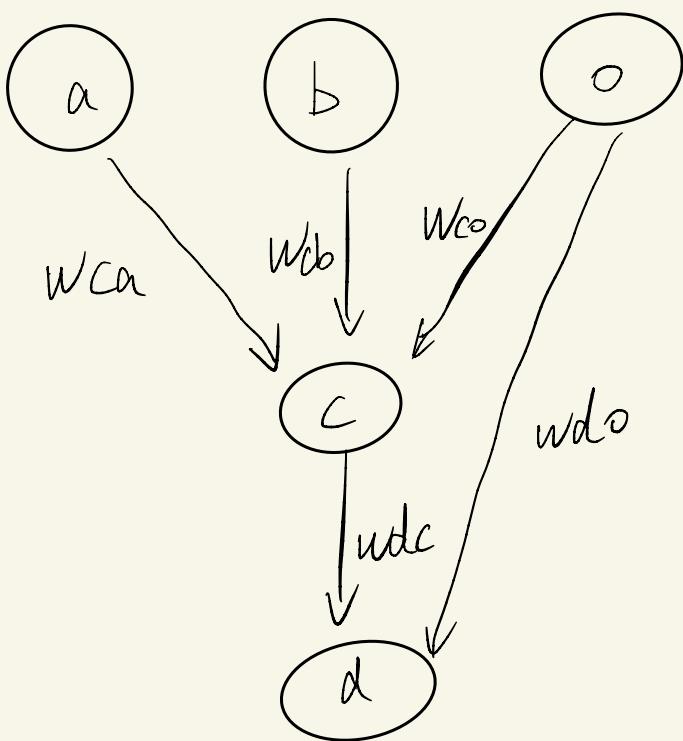
3.

$$P(\text{yes}) P(\text{sun} | \text{yes}) P(\text{cool} | \text{yes}) P(\text{high} | \text{yes}) P(\text{strong} | \text{yes}) \\ = \frac{8}{12} \cdot \frac{2}{8} \cdot \frac{3}{8} \cdot \frac{3}{8} \cdot \frac{3}{8} = 0.00879$$

$$P(\text{no}) P(\text{sun} | \text{no}) P(\text{cool} | \text{no}) P(\text{high} | \text{no}) P(\text{strong} | \text{no}) \\ = \frac{4}{12} \cdot \frac{3}{4} \cdot \frac{1}{4} \cdot \frac{3}{4} \cdot \frac{2}{4} = 0.0234$$

predict result is no

4.



as activation function  $\sigma(y) = \frac{1}{1+e^{-y}}$      $\sigma'(y) = (1-\sigma(y))\sigma(y)$

training 1:

$$o_c = \sigma(0.1 \cdot 1 + 0.1 \cdot 0 + 0.1 \cdot 1) = \sigma(0.2) = 0.55$$

$$o_d = \sigma(0.1 \cdot 0.55 + 0.1 \cdot 1) = \sigma(0.55) = 0.54$$

$$\delta_d = o_d(1-o_d)(d-o_d) = 0.54 \cdot (1-0.54) \cdot (1-0.54) = 0.115$$

$$\delta'_c = o_c(1-o_c)(w_{dc} \times \delta_d) = 0.55(1-0.55) \cdot 0.1 \cdot 0.115 = 0.0028$$

$$w_{ca} = w_{ca} + \delta_{ca} = 0.1 + 0.0085 = 0.10085$$

$$w_{co} = w_{co} + \delta_{co} = 0.1 + 0.0085 = 0.10085$$

$$w_{do} = w_{do} + \delta_{do} = 0.1 + 0.034 = 0.134$$

$$w_{dc} = w_{dc} + \delta_{dc} = 0.1 + 0.019 = 0.119$$

$$w_{cb} = w_{cb} + \delta_{cb} = 0.1 + 0 = 0.1$$

training 2:

$$o_c = \sigma(0.10085 \cdot 1 + 0.10085 \cdot 0 + 0.1 \cdot 1) = \sigma(0.20085) = 0.55$$

$$o_d = \sigma(0.119 \cdot 0.55 + 0.134 \cdot 1) = \sigma(0.1996) = 0.5497$$

$$D'd = 0.5497 \cdot (-0.5497) (-0.5497) = -0.1361$$

$$D'C = 0.55 \cdot (-0.55) : 0.119 \cdot (-0.1361) = -0.0004$$

as before

$$W_{Ca} = 0.10085$$

$$W_{Co} = 0.1016$$

$$W_{Do} = 0.1242$$

$$W_{Dc} = 0.1134$$

$$W_{Cb} = 0.0988$$