AKLT model, $|\psi_n\rangle=(Q^\dagger)^N|G\rangle$, and then calculate the correlation matrix $\mathcal M$ of using pure range-3 operator basis. The resulting kernal $Ker(\mathcal{M})$, Aarray and the corresponding values of ξ_{α} . Alamvals, of the first scar state $|\psi_1\rangle$ are then saved to be use in degeneracy. jl for recursive calculations; Moreover, we numerically check to make sure $\operatorname{Ker}(\mathcal{M})$ of $|\psi_1\rangle$ remains the same for different L.

corrMat.jl: this program uses the MPO x MPS method to calculate the n-pairing states in the

degeneracy. jl: an implementation of the recursive method in section III of the supplementary material that determines the ground state dengeracy of a projector Hamiltonian recursively.

EE.jl: use the MPO x MPS method to calculate the n-pairing states, calculate the entanglement

entropies of all n-pairing states and then get the largest value of EE.

./plots/AKLT.py: plots Fig. 2 in the paper.