



CHAPTER 9 OPTION MARKETS

Derivatives Securities
Junho Park



Chapter Outline

- Option positions. 옵션 포지션의 종류
- Terminology. 용어
- Adjustment in stock dividends. 주식 배당시 조정
- Option-like securities. 성질이 비슷한 증권들

Types of Options

옵션이란? 권리를 매매하는 것

- There are two basic types of options:
 - A **call option** gives the holder of the option the right to buy an asset by the expiration date for the exercise price.
 - A **put option** gives the holder of the option the right to sell an asset by the expiration date for the exercise price.
- Options can be categorized by the timing of exercise:
 - **American options** can be exercised at any time up to maturity. ↳ 옵션 만기일 전에 행사가능
 - **European options** can be exercised only on the maturity. ↳ 옵션 만기일에만 행사가능 (한국 옵션)

Option Positions

- There are four types of option positions:
 - A long position in a call option.
 - A long position in a put option.
 - A short position in a call option.
 - A short position in a put option.

주가변화에 따른 수익 패턴

	롱	숏
콜	상승시 수익	고정 프리미엄
풋	하락시 수익	고정 프리미엄

Long Call

* 옵션 프리미엄을 고려하지 않았음에 주의하자!

- The payoff from a long position in a European call option is

$$\max(S_T - K, 0)$$

만기일의 주가 ■ S_T is the final price of the underlying asset on maturity.

행사가격 ■ K is the strike price.

Example: Long Call

- Suppose that:
 - An investor buys a European call option.
 - The strike price of the option is \$100.
 - The size of contract is 100 shares per contract.
 - The price of the option is \$5 per share.
 - The expiration date of the option is in 4 months.
 - The stock price becomes \$115 after 4 months.

콜옵션 구매

행사가격 K 는 \$100

1 계약당 100주

옵션의 가격: 주당 \$5

만기: 4개월 후

만기시 주가: \$115

S_T

Example: Long Call

- The initial investment is

$$5 \times 100 = \$500$$

- The investor exercises the option by paying

$$100 \times 100 = \$10,000$$

- The investor sells the shares and receives

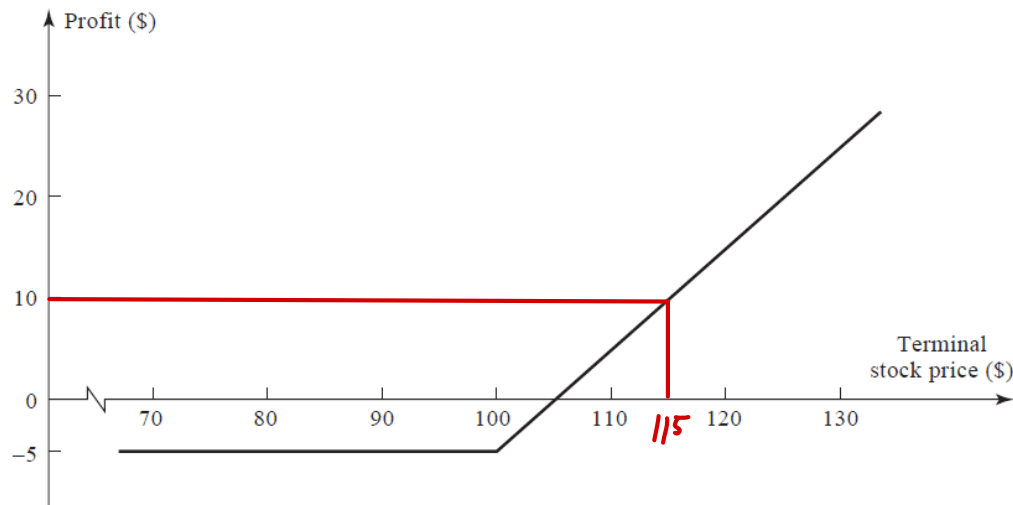
$$115 \times 100 = \$11,500$$

Example: Long Call

- The net gain of the investor is

$$\underset{S_T}{11,500} - \underset{K}{10,000} - \underset{\text{Premium}}{500} = \$1,000$$

Figure 9.1 Profit from buying a European call option on one share of a stock. Option price = \$5; strike price = \$100.



Short Call

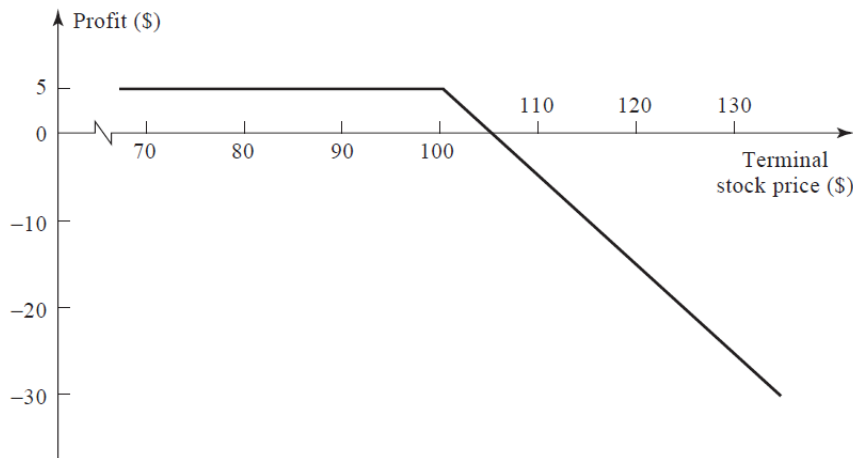
살 수 있는 권리를 파는 것

- The payoff from a short position in a European call option is

* Max함수의 마이너스는 Min으로 변환 가능

$$-\max(S_T - K, 0) = \min(K - S_T, 0) \leftarrow \text{이 식은 프리미엄을 고려하지 않은 것에 주의하자}$$

Figure 9.3 Profit from writing a European call option on one share of a stock. Option price = \$5; strike price = \$100.



← 그래프는 옵션 프리미엄만큼 y축으로 수평이동 했다

Long Put 팔 권리를 사는 것

- The payoff from a long position in a European put option is

$$\max(K - S_T, 0)$$

- S_T is the final price of the underlying asset on maturity.
- K is the strike price.

* 주가가 하락하면 이익을 보는 공매도의 패턴을 생각해보자!

Example: Long Put

- Suppose that:
 - An investor buys a European put option.
 - The strike price of the option is \$70.
 - The size of contract is 100 shares per contract.
 - The price of the option is \$7 per share.
 - The expiration date of the option is in 4 months.
 - The stock price becomes \$55 after 4 months.

풋옵션 구매

행사가격 K는 \$70

1 계약당 100주

옵션의 가격: 주당 \$7

만기: 4개월 후

만기시 주가: \$55

Example: Long Put

- The initial investment is

옵션 프리미엄 지불

$$7 \times 100 = \$700$$

- The investor buys the shares by paying

4개월뒤 가격이 떨어진 주식 100주 구매

$$55 \times 100 = \$5,500$$

- The investor exercises the option and receives

옵션 행사(행사 가격 K= 70으로 팔)

$$70 \times 100 = \$7,000$$

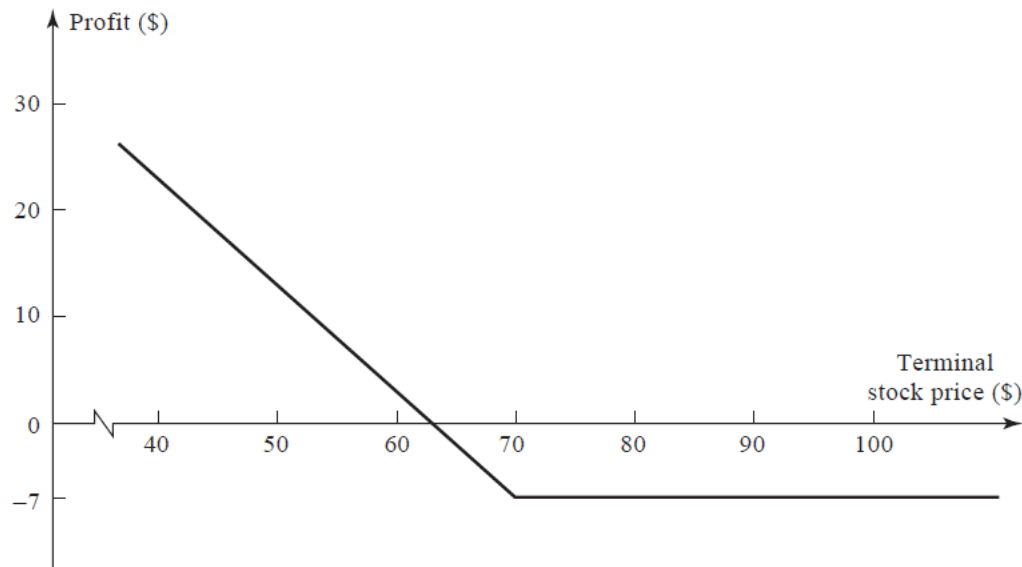
Example: Long Put

- The net gain of the investor is

$$7,000 - 5,500 - 700 = \$800$$

K S_T 옵션가격

Figure 9.2 Profit from buying a European put option on one share of a stock. Option price = \$7; strike price = \$70.



Short Put

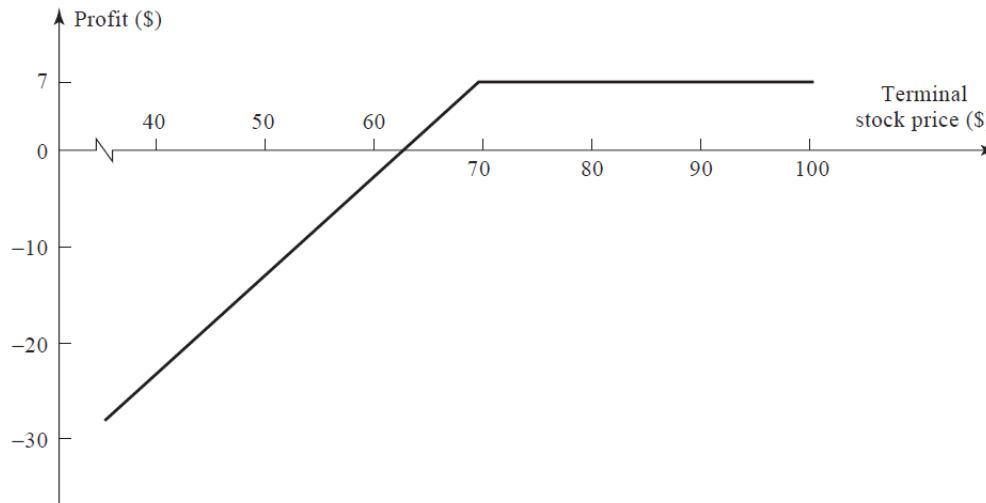
일반투자자: 숏 잘 안함

기관: 헷징과 옵션프리미엄 -> 숏 유인 존재 -> 시장조성자 역할

- The payoff from a short position in a European put option is

$$-\max(K - S_T, 0) = \min(S_T - K, 0)$$

Figure 9.4 Profit from writing a European put option on one share of a stock. Option price = \$7; strike price = \$70.

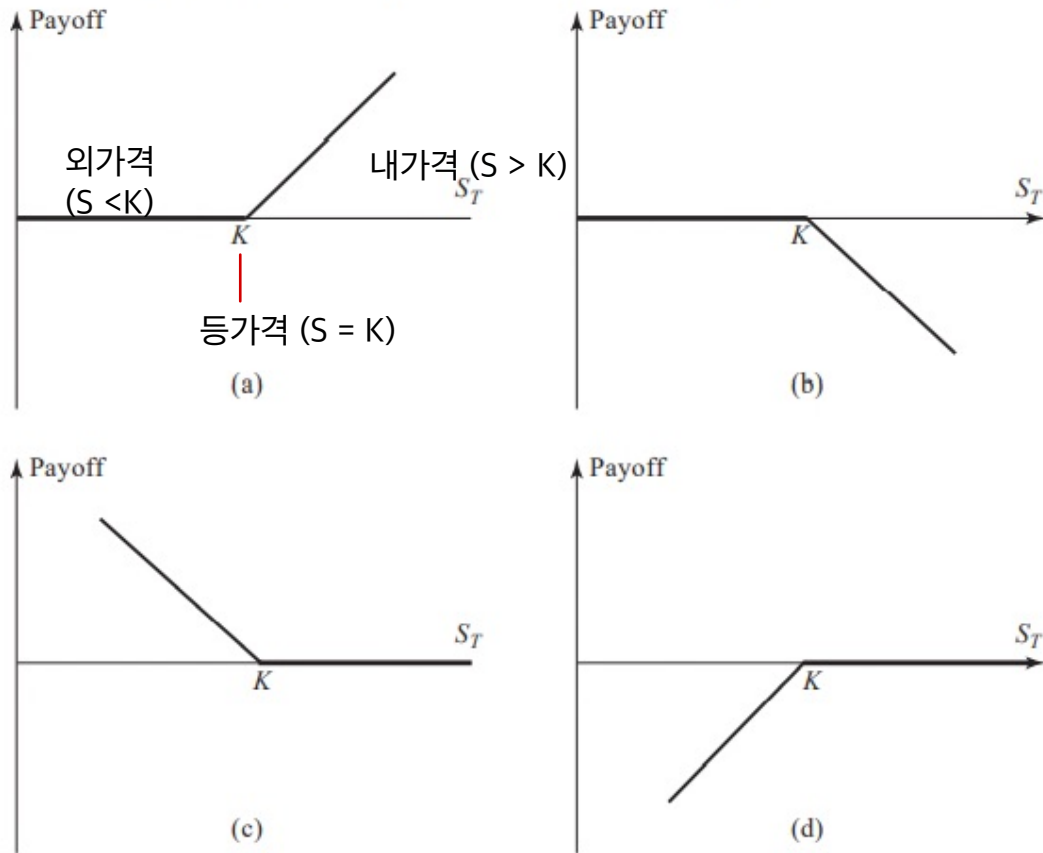


Terminology

S = 현재의 주가
 K = 행사가격

- An option is **in the money** if its current payoff is positive. 내가격
 - A call option is in the money if $S > K$.
 - A put option is in the money if $S < K$.
- An option is **at the money** if its current payoff is zero. That is, an option is at the money if $S = K$. 등가격
- An option is **out of the money** if its current payoff is negative. 외가격
 - A call option is out of money if $S < K$.
 - A put option is out of money if $S > K$.

Figure 10.5 Payoffs from positions in European options: (a) long call; (b) short call; (c) long put; (d) short put. Strike price = K ; price of asset at maturity = S_T .



Intrinsic Value

옵션의 내재가치

- The **intrinsic value** of an option is the maximum of zero and the value the option would have if it were exercised immediately.

- The intrinsic value of a call option is

$$\max(S - K, 0)$$

- The intrinsic value of a put option is

$$\max(K - S, 0)$$

- The intrinsic value of an in-the-money option is positive.

내재가치는 내가격에서만 존재
외가격에서 내재가치는 0

Time Value

아메리칸은 만기 전에 행사가능 = 시간가치

- An American option has **time value** when it is better for the holder of the option to wait rather than exercise it immediately.
 - There is time value when it is possible to have better payoffs in the future.
- The total value of an American option is the sum of its intrinsic value and its time value.

아메리칸 옵션 = 내재가치 + 시간가치

KOSPI200	413.86 ▲ 0.97 0.23%
선 물	413.25 ▲ 1.30 0.32%
상한가	17.70 하한가 0.01
이론가	0.79 역사적변동 22.84
과리도	-0.29 과리율 -36.71
내재변동성	20.38 델타 10.2411
감마	1.0898 베가 0.1281
세타	-0.1339 로 0.0125
내재가치	0 시간가치 0.50
최종거래일	2021/04/08 잔존일 11 9
상장최고	+19.25 -97.40% 2021/01/25
상장최저	0.39 +28.21% 2021/03/25

투자자별		프로그램매매		
KP200	▼	◎금액(억) ○수량 ○차트 ◎텍스트		
전체		개인	외국인	기관계
거	6,146	1,167	4,911	
코	712	232	416	
KP선	3,821	3,157	237	
KP콜	9	7	13	
KP풋	9	15	5	
	413.71	413.86	413.86	

콜옵션				풋옵션			
거래량	대비	현재가	행사가	현재가	대비	거래량	
25,153 ▼	0.06	0.31	440.00	30.30 ▲	1.95	3	
13,739 ▼	0.06	0.39	437.50	28.80	0	0	
29,374 ▼	0.07	0.50	435.00	22.70 ▼	0.95	8	
27,139 ▼	0.07	0.64	432.50	22.60 ▲	0.80	1	
44,739 ▼	0.08	0.84	430.00	18.40 ▼	0.65	9	
34,290 ▼	0.07	1.11	427.50	18.75 ▲	1.95	2	
47,509 ▼	0.01	1.47	425.00	13.95 ▼	0.75	25	
35,098 ▼	0.01	1.95	422.50	11.90 ▼	0.60	97	
41,436 ▲	0.02	2.58	420.00	9.41 ▼	1.14	194	
18,081 ▲	0.14	3.39	417.50	7.67 ▼	1.25	1,714	
17,030 ▲	0.20	4.40	415.00	6.14 ▼	1.18	2,930	
8,121 ▲	0.30	5.66	412.50	4.97 ▼	1.01	4,769	
5,115 ▲	0.44	7.15	410.00	3.94 ▼	0.89	7,755	
1,300 ▲	0.66	8.90	407.50	3.11 ▼	0.78	8,566	

KOSPI200	413.84 ▲ 0.95 0.23%
선 물	413.25 ▲ 1.30 0.32%
상한가	38.60 하한가 0.01
이론가	9.81 역사적변동 22.84
과리도	-0.89 과리율 -9.28
내재변동성	19.37 델타 64.7239
감마	2.2671 베가 0.2665
세타	-0.2819 로 0.0776
내재가치	6.34 시간가치 2.56
최종거래일	2021/04/08 잔존일 11 9
상장최고	+20.00 -55.50% 2021/03/02
상장최저	2.50 +256.00% 2020/12/07

투자자별		프로그램매매		
KP200	▼	◎금액(억) ○수량 ○차트 ◎텍스트		
전체		개인	외국인	기관계
거	6,146	1,167	4,911	
코	712	232	416	
KP선	3,792	3,144	220	
KP콜	9	7	13	
KP풋	8	15	5	
	413.84	414.01	413.84	

콜옵션				풋옵션			
거래량	대비	현재가	행사가	현재가	대비	거래량	
25,153 ▼	0.06	0.31	440.00	30.30 ▲	1.95	3	
13,740 ▼	0.06	0.39	437.50	28.80	0	0	
29,376 ▼	0.07	0.50	435.00	22.70 ▼	0.95	8	
27,147 ▼	0.07	0.64	432.50	22.60 ▲	0.80	1	
44,786 ▼	0.08	0.84	430.00	18.40 ▼	0.65	9	
34,301 ▼	0.07	1.11	427.50	18.75 ▲	1.95	2	
47,522 ▼	0.02	1.46	425.00	13.95 ▼	0.75	25	
35,102 ▼	0.02	1.94	422.50	11.90 ▼	0.60	97	
41,494 ▲	0.01	2.57	420.00	9.37 ▼	1.18	196	
18,095 ▲	0.13	3.38	417.50	7.69 ▼	1.23	1,717	
17,035 ▲	0.20	4.40	415.00	6.14 ▼	1.18	2,930	
8,132 ▲	0.29	5.65	412.50	4.95 ▼	1.03	4,771	
5,124 ▲	0.43	7.14	410.00	3.94 ▼	0.89	7,756	
1,300 ▲	0.66	8.90	407.50	3.13 ▼	0.76	8,568	
246 ▲	0.75	10.75	405.00	2.49 ▼	0.64	29,091	
107 ▲	0.35	12.10	402.50	1.98 ▼	0.55	22,626	
74 ▲	0.75	14.70	400.00	1.58 ▼	0.45	42,047	
11 ▲	0.50	16.65	397.50	1.27 ▼	0.40	32,993	
31 ▲	0.75	18.95	395.00	1.02 ▼	0.32	39,573	
2	0	19.80	392.50	0.82 ▼	0.28	25,400	
10 ▼	1.85	21.10	390.00	0.67 ▼	0.20	35,147	
1 ▼	2.00	23.20	387.50	0.54 ▼	0.17	20,002	▼

Underlying Assets

- The underlying assets of the options which are traded in exchanges are:
 - Stocks.
 - Foreign currency.
 - Stock indices.
 - Futures.

Dividends and Stock Splits

<-> 장외시장은 합의해서 보호 받을 수 있음

- Exchange-traded options are not adjusted for cash dividends.
현금배당 조정 X
- However, they are adjusted for stock dividends and stock splits.
주식분할, 주식배당 조정
 - Strike price and the number of shares changes.
- Usually, if there is a n-for-m stock split,
n 대 m 액면분할
ex) 테슬라 5대1 액면분할
 - The changed strike price is mK/n .
 - The changed number of shares is nN/m .

Example: Stock Dividends

- Suppose that:
 - There is a call option already issued.
 - The strike price of the option is \$30 per share.
 - The number of shares per option is 100 shares.
 - A company announces 2-for-1 stock split.

콜옵션 발행

행사가 $K=30$

옵션 한 계약당 100주

2대1 액면분할 발표

Example: Stock Dividends

- Note that stock split and stock dividends do not change the fundamental of the company.
- Suppose that the stock price before stock split was \$40 per share.
- Then, the intrinsic value of the call option was

$$100 \times (40 - 30) = \$1,000$$

Example: Stock Dividends

- Now the changed stock price due to the stock split is

$$\frac{40}{2} = \$20$$

- If there were no change in strike price, the intrinsic value would be zero.
- Therefore, it is reasonable to adjust the terms of the call option.

Example: Stock Dividends

- To guarantee the same condition in which the option is at-the-money, the modified strike price is

$$\frac{30}{2} = \$15$$

- To guarantee the same intrinsic value, the modified number of shares covered by the option is

$$N = \frac{1,000}{20 - 15} = 200$$

Example: Stock Dividends

- Suppose that:
 - There is a put option.
 - The number of shares covered by the option is 100 shares.
 - The strike price of the option is \$15 per share.
 - There is a 25% stock dividend.

풋옵션의 경우

옵션당 100주 커버

행사가 $K = 15$

25퍼 비율 주식배당을 한다고 가정하면?

Example: Stock Dividends

- This stock dividend is equivalent to a 5-for-4 stock split.
- Therefore, the changed strike price is

$$\frac{4}{5} \times 15 = \$12$$

- The changed number of shares is

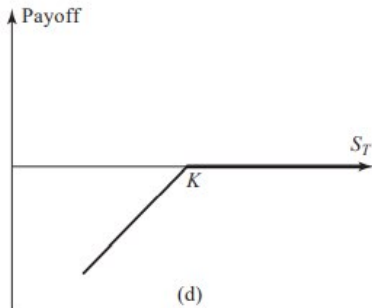
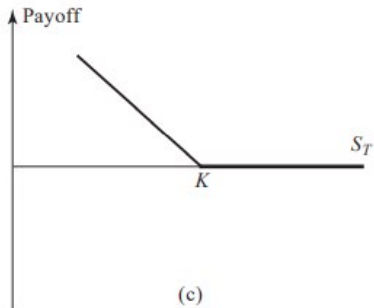
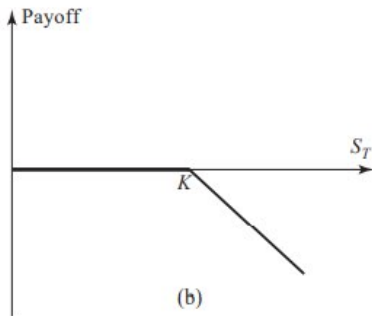
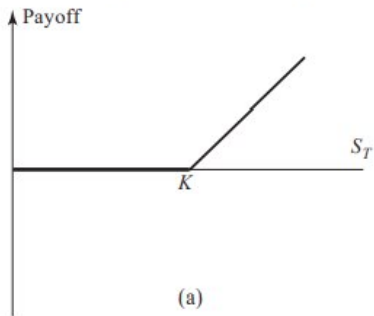
$$\frac{5}{4} \times 100 = 125$$

Margins

일반 주식, 옵션 롱 포지션 -> 현금으로 구매 -> 마진(증거금) 요구 x
공매도, 옵션 숏 포지션 -> 하방 열려있음 -> 증거금 요구

- A long position in a call option or a put option is made by paying the option price fully in cash.
 - Options already contain substantial leverage.
- A short position in an option is required to maintain sufficient amount of margin account.
 - The level of maintenance margin is determined by the volatility of the underlying asset.

Figure 10.5 Payoffs from positions in European options: (a) long call; (b) short call; (c) long put; (d) short put. Strike price = K ; price of asset at maturity = S_T .



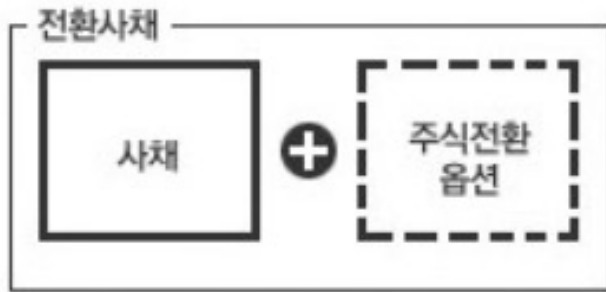
Option-like Securities

성질이 옵션과 비슷한 증권들

- There are some securities which are not exchange-traded options but have similar characteristics of options:
 - Convertible bonds. 전환사채
 - Warrants. Bond with warrants : 신주인수권부 사채
 - Employee stock options. 스탁옵션

Convertible Bonds & Warrants

- **Convertible bonds**, or **convertibles**, are bonds issued by a company which can be converted into equity in some specific conditions.
- **Warrants** are options issued by a company at the time of a bond issue.
 - The company issues call warrants on its own stock and then attaches them to the bond issued.
 - This kind of issued bonds are often referred as **bonds with warrants**, or BW.
- When convertibles or warrants are exercised, new shares are issued.



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전환가액, 신주인수가액 사전에 설정

신주인수옵션은 따로 매매 가능

옵션행사 시 단기적으로는 주가에 부정적

Employee Stock Options

- **Employee stock options** are call options issued to employees by their company to motivate them to act in the best interest of the shareholders.
 - Usually issued to executives.
 - Generally, they are non-transferrable.
 - When ESOs are exercised, the company issue new shares.
 - They are now less attractive than used to be.

90년도까지는 활발히 쓰임

but...

1. 규제문제
2. 주식회석
3. 효과에 대한 의문 때문에
점점 줄어드는 추세