

# Anti-Aging Scheduling in Single-Server Queues: A Systematic and Comparative Study

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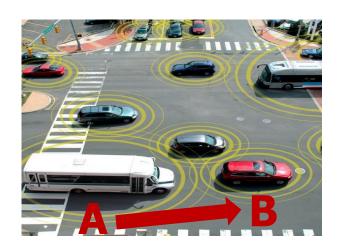
Joint work with

**Liang Huang** (Zhejiang University of Technology), **Bin Li** (University of Rhode Island) and **Bo Ji** (Temple University)

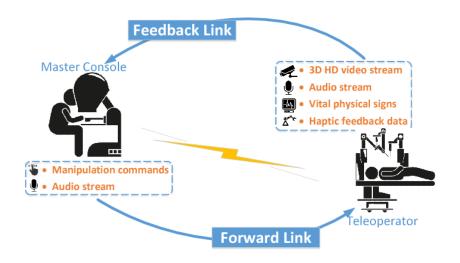
### Freshness Matters



- Real-time services are ubiquitous
  - Intelligent transportation systems & vehicular networks
  - Sensor networks (for environment/health monitoring), wireless channel feedback, news feeds, weather updates, fare aggregating, etc.



(a) Intelligent vehicular networks

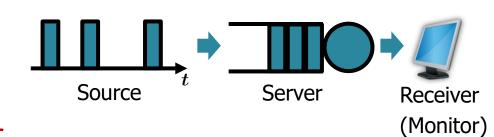


(b) Sensor networks



- A simple abstract model
  - Source/Server/Receiver (Monitor)
  - Performance of interest:

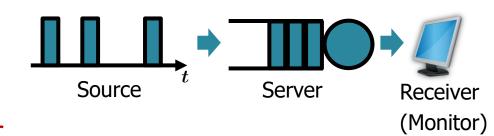
freshness of update at the monitor





the

- A simple abstract model
  - Source/Server/Receiver (Monitor)
  - Performance of interest: freshness of update at the monitor



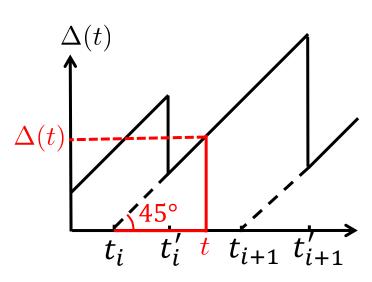
the time elapsed

since generation

- Definition
  - At time t, the **Age-of-information (AoI)**  $\Delta(t)$  is the "age" of the "youngest" update that was delivered to the receiver before time t
  - If update i is generated at  $t_i$  and delivered at  $t'_i$

$$\Delta(t) = t - \max\{t_i : t_i' \le t\}$$

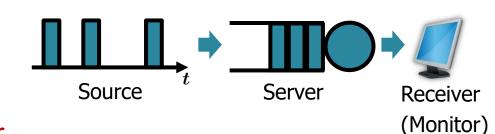
 AoI grows linearly and drops upon new update delivered





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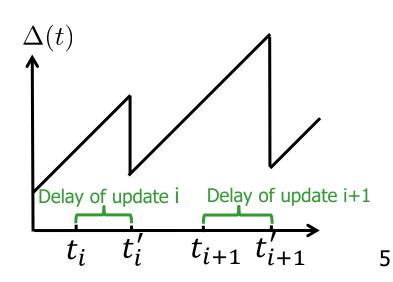
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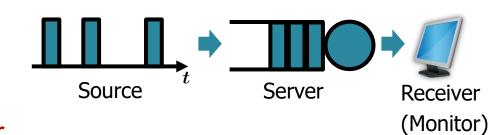




the

latest

- A simple abstract model
  - Source/Server/Receiver (Monitor)
  - Performance of interest:
     freshness of update at the monitor



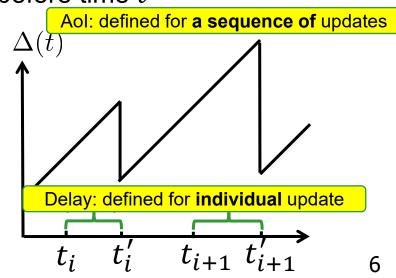
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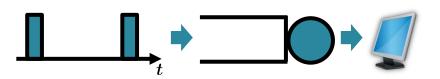
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 AoI grows linearly and drops upon new update delivered



## Aol vs. Delay

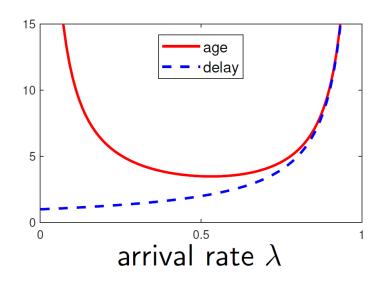






- Low arrival rate
  - Empty buffer → low delay
  - Infrequent updates → large interarrival time & high AoI

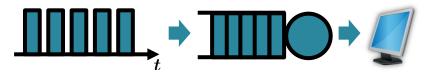
- Large arrival rate
  - Full buffer → high delay
  - Become stale while waiting→ high AoI



## Aol vs. Delay





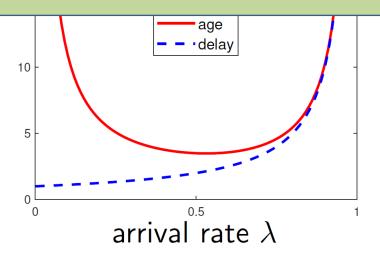


Low arrival rate

Large arrival rate

In M/M/1 FCFS queues: [Kaul et al.,12]

- AoI first decreases, then increases with arrival rate
- Delay increases with arrival rate



#### Anlys Delay

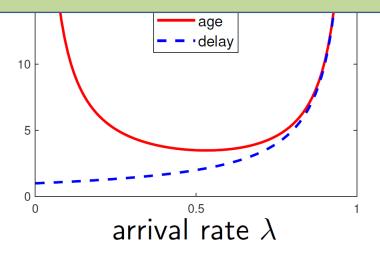


#### Aol depends on both

- Queueing delay (how fast to deliver)
- Inter-arrival time (how often to generate)

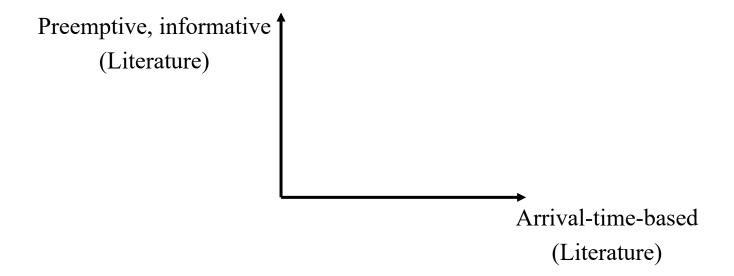
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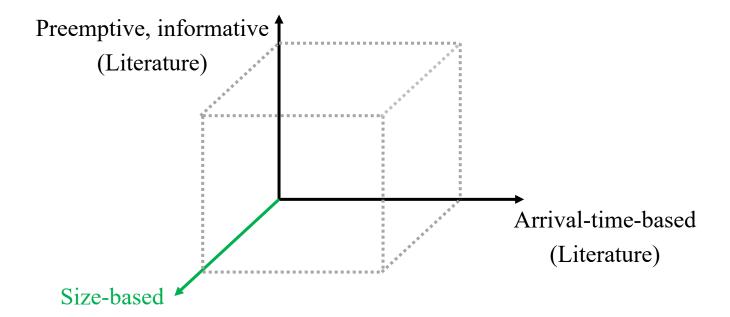


Motivation & Position



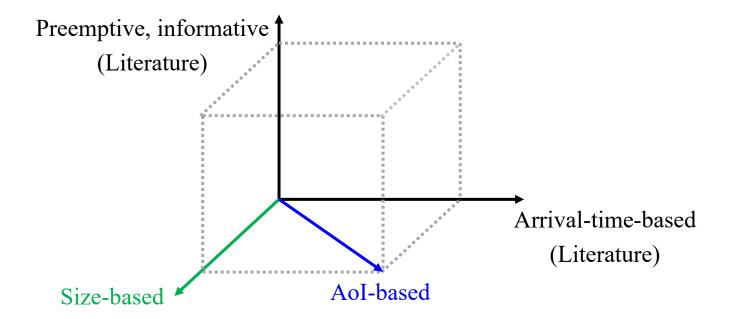


#### Motivation & Position



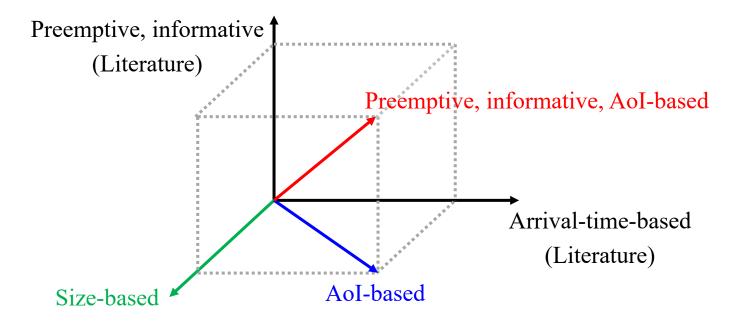


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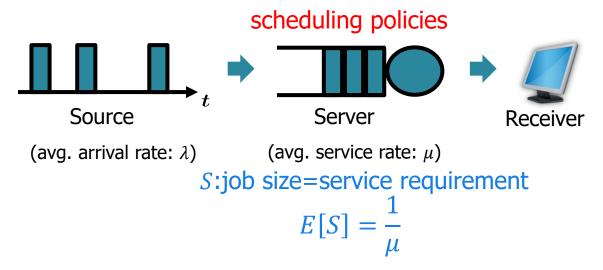


#### Contributions

- Investigate the impact of scheduling policies on the AoI performance
- Summarize useful guidelines for the design of AoI-efficient policies
- Equivalence between some size-based and AoI-based policies

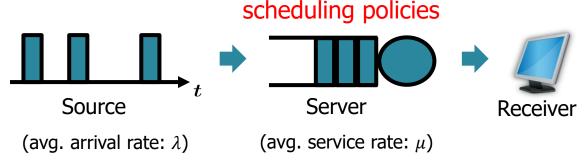


System model: G/G/1





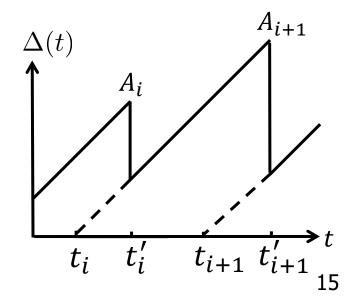
System model: G/G/1



S:job size=service requirement

$$E[S] = \frac{1}{\mu}$$

- Performance metrics
  - Time Average AoI:  $\Delta = \lim_{t \to \infty} \frac{1}{t} \int_0^t \Delta(\tau) d\tau$
  - Average Peak AoI (PAoI):  $E[A] = \frac{1}{N} \sum_{i=0}^{N} A_i$

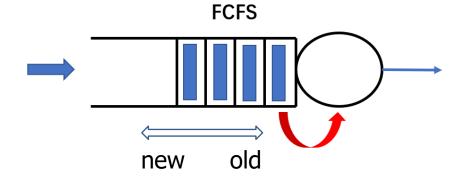




	Non-preemptive	Preemptive
Blind to Size	FCFS (First-Come-First-Served) LCFS (Last-Come-First-Served) RANDOM (Random-Order-Service)	PS (Processor-Sharing) LCFS_P
Uses Size	SJF (Shortest-Job-First)	SJF_P SRPT (Shortest-Remaining- Processing-Time)

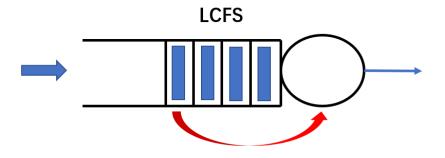


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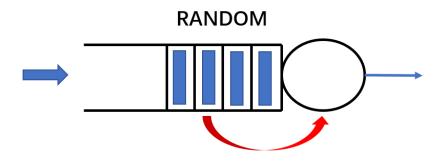


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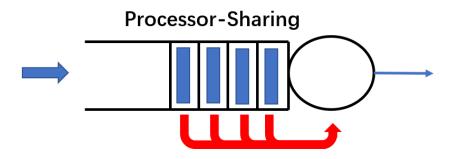


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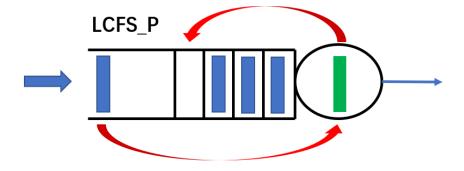


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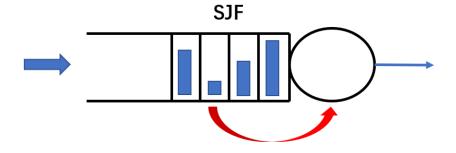


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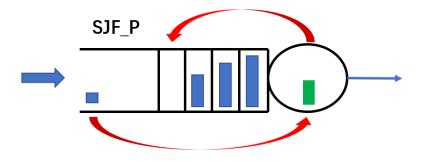


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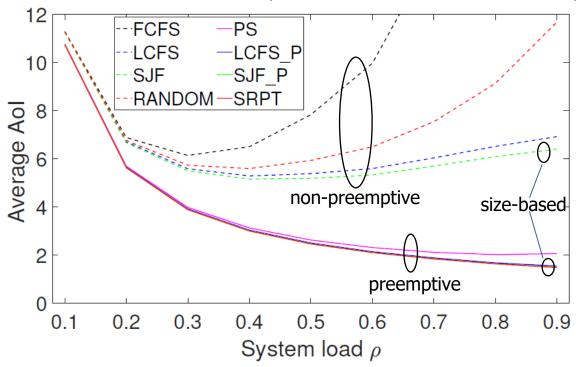


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Average AoI performance (with update size info.)

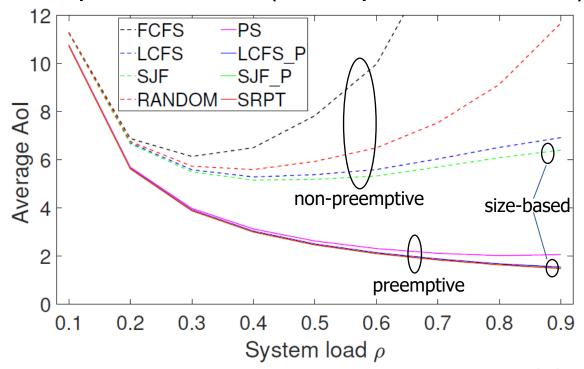


Weibull: 
$$\mu = 1$$
 and  $C^2 = \frac{\text{Var}(S)}{\text{E}[S]^2} = 10$ 

Observation 1: Size-based policies > Non-size-based policies



Average AoI performance (with update size info.)



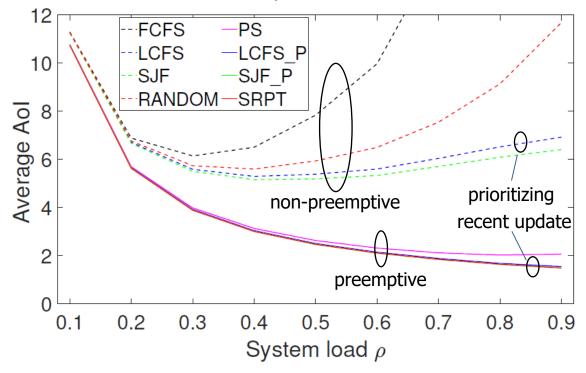
Weibull: 
$$\mu = 1$$
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Guideline 1: Prioritizing updates with small size

## Arrival-time-based Policies



Average AoI performance (without update size info.)

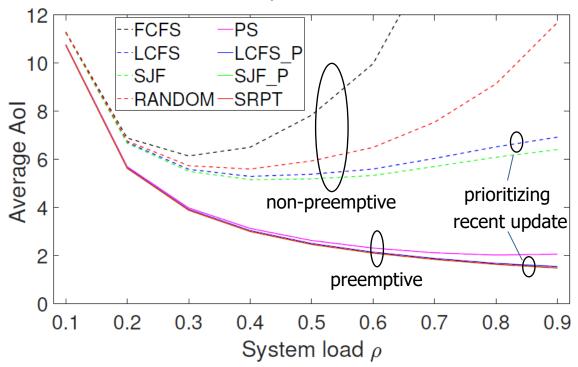


Weibull:  $\mu = 1$  and  $C^2 = 10$ 

## Arrival-time-based Policies



Average AoI performance (without update size info.)



Weibull:  $\mu = 1$  and  $C^2 = 10$ 

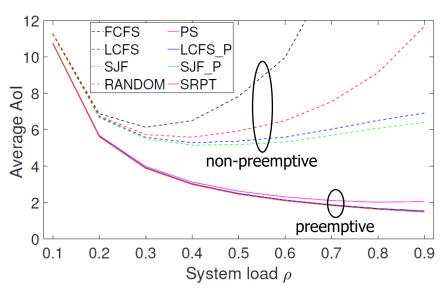
#### **Guideline 2: Prioritizing recent updates**

[Kaul et al., 2012; Costa et al., 2016]

# Preemptive Policies



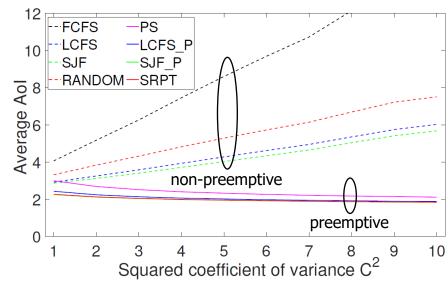
#### Average AoI performance (with service preemption)



Weibull:  $\mu = 1$  and  $C^2 = 10$ 

**Observation 3:** 

Preemptive>Non-preemption



Weibull:  $\mu = 1$  and  $\rho = 0.7$ 

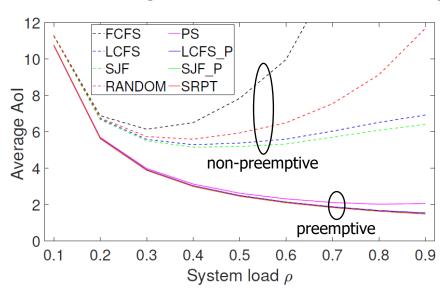
**Observation 4:** 

Preemptive policies are less sensitive to update size variability

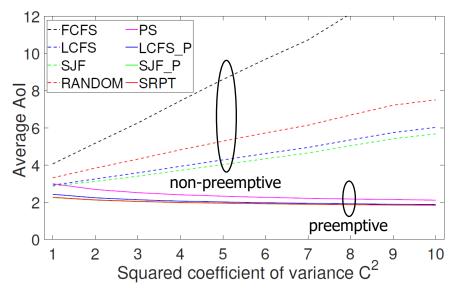
# **Preemptive Policies**



Average AoI performance (with service preemption)



Weibull:  $\mu = 1$  and  $C^2 = 10$ 



Weibull:  $\mu = 1$  and  $\rho = 0.7$ 

#### **Guideline 3: Allowing service preemption**

[Kaul et al., 2012; Bedeway et al., 2016; Najm et al., 2018]

## **Current Guidelines**



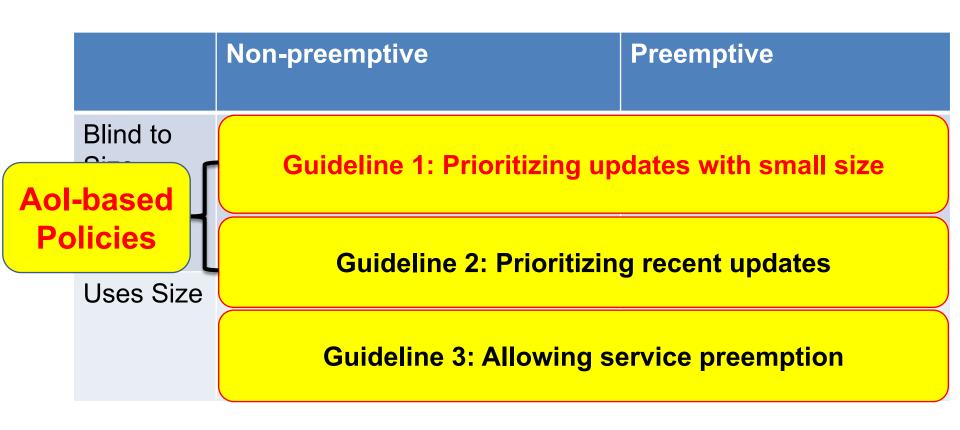
Summary of guidelines

	Non-preemptive	Preemptive
Blind to Size	Guideline 1: Prioritizing updates with small size	
Uses Size	Guideline 2: Prioritizin	ng recent updates
	Guideline 3: Allowing service preemption	

### **Current Guidelines**



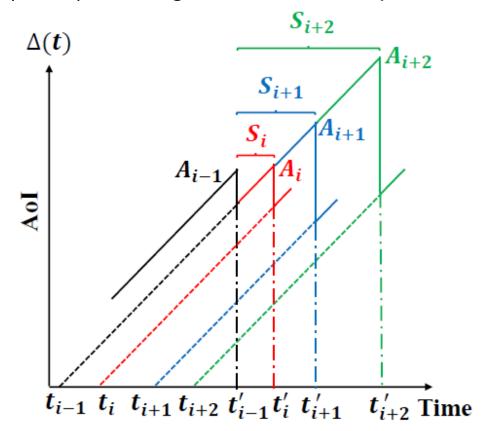
Summary of guidelines



### **Aol-based Policies**



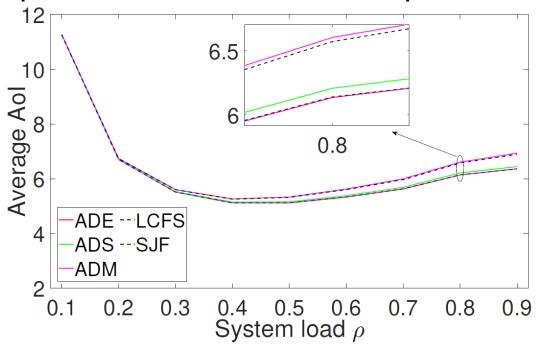
- Aol-based policies
  - AoI-Drop-Earliest (ADE): make next AoI drop the earliest
  - Aol-Drop-to-Smallest (ADS): making the next Aol drop to the smallest
  - AoI-Drop-Most (ADM): making the next AoI drop most



### **Aol-based Policies**



Aol-based policies vs. non-Aol-based policies

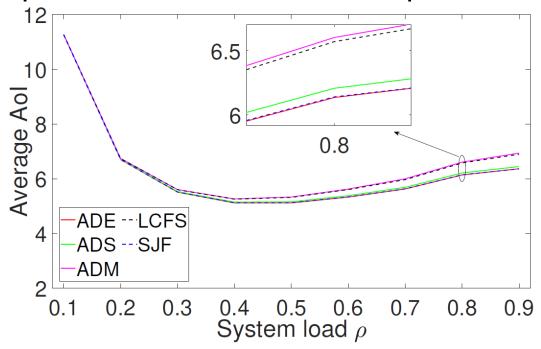


Weibull:  $\mu = 1$  and  $C^2 = 10$ 

#### **Aol-based Policies**



Aol-based policies vs. non-Aol-based policies



Weibull:  $\mu = 1$  and  $C^2 = 10$ 

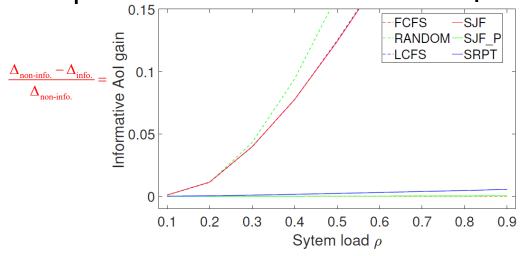
Guideline 4: Aol-based policies can further improve the Aol performance



- Informative policies
  - Informative policies only serve informative updates (can make Aol drop)
  - Almost all introduced policies have "informative" version



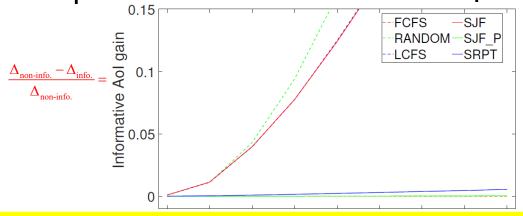
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- Informative policies vs. Non-informative policies



Weibull:  $\mu = 1$  and  $C^2 = 10$ 



- Informative policies
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- Informative policies vs. Non-informative policies

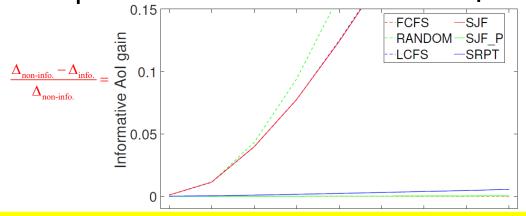


#### **Guideline 5: Prioritizing informative updates**

[Costa et al., 2014; Pappas et al., 2015]



- Informative policies
  - Informative policies only serve informative updates (can make AoI drop)
  - Almost all introduced policies have "informative" version
- Informative policies vs. Non-informative policies



#### **Guideline 5: Prioritizing informative updates**

[Costa et al., 2014; Pappas et al., 2015]

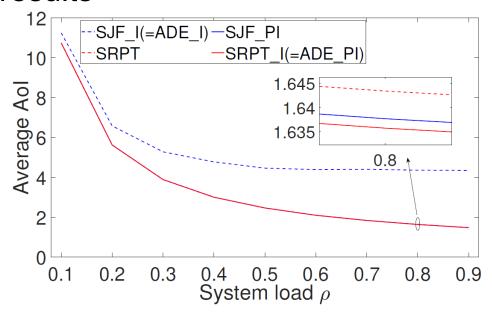
Theoretical result

Proposition 1: In the G/M/1 queueing system, the AoI under LCFS\_I is stochastically smaller than that under LCFS.

# Preemptive, Informative, Aol-based Policies



Simulation results



Weibull:  $\mu = 1$  and  $C^2 = 10$ 

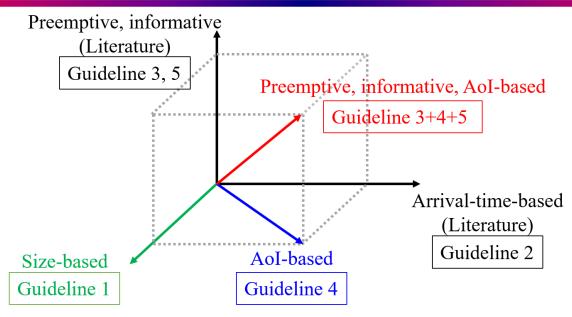
Sample path equivalence results

Proposition 2: SRPT\_I is equivalent to ADE\_PI.

Proposition 3: SJF\_I is equivalent to ADE\_I.

### Conclusion





- Design Aol-efficient scheduling policies
  - Prioritizing small updates, allowing service preemption, prioritizing informative updates
- Equivalence between some size-based and AoI-based policies
  - SRPT\_I = ADE\_PI; SJF\_I=ADE\_I
- Delay-efficient 

  Aol-efficient (for exogenous source)
  - High load: delay dominates
     Low load: interarrival dominates

## **Future Work**



- Pursue more theoretical results
  - Does any informative policy always outperform its non-informative counterpart?
  - Can we derive the closed-form formulas of the average Aol/PAol for the Aol-efficient scheduling policies (such as SRPT)?
- Apply to more complex network
  - Does our guidelines hold for multi-server queues?
  - What's the performance of our policies/guidelines in a more complex network (e.g., multi-hop networks)?



Thank