LINE: Performance and Reliability Analysis Engine

User manual

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## **Chapter 1**

## Introduction

#### 1.1 What is LINE?

LINE is a MATLAB toolbox for performance and reliability analysis of complex systems based on queueing theory and stochastic modeling. Systems may either represent software applications, business processes, computer networks, or else. LINE transforms a high-level system model into one or more stochastic models, typically extended queueing networks, that are subsequently analyzed using either numerical algorithms or simulation. A key feature of LINE is that the engine decouples the model description from the solvers used for its solution. The engine acts as a bridge between model and solvers, implementing model-to-model transformations that automatically translate the model specification into the input format or data structure accepted by the target solver.

#### 1.1.1 Supported models

Target models include extended queueing networks, both open and closed, and layered queueing networks. Wrappers are integrated in LINE to solve a model via an external solver such as JMT and LQNS/LQSIM. LINE also features several native model solvers written in MATLAB and based on

- Continuous-time Markov chains (CTMC)
- Fluid ordinary differential equations (FLUID)
- Matrix analytic methods (MAM)
- Normalizing constant analysis (NC)
- Approximate mean-value analysis (AMVA)

Currently, LINE is able to load and analyze models specified in the following languages and formats:

- LINE modeling language. This is a MATLAB-based object-oriented language designed to closely resemble the abstractions available in the Java Modelling Tools (JMT) queueing network simulator<sup>1</sup>. Among the benefit of this language is the possibility to transform back-and-forth LINE models into JMT simulation models. Such models can be easily inspected within MATLAB, or using the JSIMgraph and JSIMwiz tools within JMT.
- Layered queueing network models (LQNS XML format). LINE is able to solve a sub-class of LQN models, provided that they are specified using the XML metamodel of the LQNS solver<sup>2</sup>.

<sup>1</sup>http://jmt.sf.net

<sup>&</sup>lt;sup>2</sup>https://github.com/layeredqueuing/

- *JMT simulation models (JSIMg, JSIMw formats)*. LINE is able to import and solve queueing network model specified using JMT.
- Performance Model Interchange Format (PMIF XML format). LINE is able to import and solve closed queueing network model specified using PMIF v1.0.

This document contains installation and usage instructions for the features in version 2.0.0-BETA1.

#### 1.2 LINE distributions

LINE 2.0.0-BETA1 can be downloaded from:

https://github.com/line-solver/line/releases

Contrary to earlier versions, LINE 2.0.0-BETA1 is released only as a MATLAB binary (compiled .p files). The distribution has been tested on MATLAB R2018a. If you are interested to obtain a JAR or executable distribution for one of the operating systems supported by the MATLAB Compiler Runtime (MCR), please contact the maintainer.

#### 1.3 References

To cite LINE, we recommend to reference:

• J. F. Pérez and G. Casale. "LINE: Evaluating Software Applications in Unreliable Environments", in *IEEE Transactions on Reliability*, 2017.

The following papers discuss recent applications of LINE:

- C. Li and G. Casale. "Performance-Aware Refactoring of Cloud-based Big Data Applications", in Proceedings of 10th IEEE/ACM International Conference on Utility and Cloud Computing, 2017. This paper uses LINE to model stream processing systems
- D. J. Dubois, G. Casale. "OptiSpot: minimizing application deployment cost using spot cloud resources", in *Cluster Computing*, Volume 19, Issue 2, pages 893-909, 2016. This paper uses LINE to determine bidding costs in spot VMs
- R. Osman, J. F. Pérez, and G. Casale. "Quantifying the Impact of Replication on the Quality-of-Service in Cloud Databases'. Proceedings of the IEEE International Conference on Software Quality, Reliability and Security (QRS), 286-297, 2016. This paper uses LINE to model the Amazon RDS database
- C. Müller, P. Rygielski, S. Spinner, and S. Kounev. Enabling Fluid Analysis for Queueing Petri Nets via Model Transformation, Electr. Notes Theor. Comput. Sci, 327, 71–91, 2016. *This paper uses LINE to analyze Descartes models used in software engineering*
- J. F. Pérez and G. Casale. "Assessing SLA compliance from Palladio component models," in Proceedings of the 2nd Workshop on Management of resources and services in Cloud and Sky computing (MICAS), IEEE Press, 2013. This paper uses LINE to analyze Palladio component models used in software engineering

## **1.4 Installing** LINE

This is the quickest way to getting started with LINE

- 1. Download the latest release from https://github.com/line-solver/line/releases
- 2. Unzip the file in the chosen installation folder.
- 3. Start MATLAB and change the active directory to the installation folder. Then add all LINE folders to the path

```
addpath (genpath (pwd))
```

4. Run the LINE demonstrators using

allExamples

#### 1.5 Contact

For bugs or feature requests, please use: https://github.com/line-solver/line/issues

Project coordinator and maintainer: Giuliano Casale, Dept. of Computing, Imperial College London.

### 1.6 Copyright and license

Copyright Imperial College London (2012-Present). LINE 2.0.0-BETA1 is freeware, but closed-source, and released under the 3-clause BSD license.

## 1.7 Acknowledgement

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## Chapter 2

## **Network models**

LINE can map a system description into one of two main types of stochastic models: Network and LayeredNetwork models, each specified by a corresponding MATLAB class. Networks are extended queueing networks with open or closed classes of jobs, while a LayeredNetwork consists of layers, each corresponding to a queueing network, which interact through synchronous and asynchronous calls. Technical background on these models can be found in books such as [1, 2] or in tutorials [3, 4].

Throughout this chapter, we discuss the specification of Network models. Instead, we point to Chapter 4 for LayeredNetwork models. It is important to keep in mind that not all of the model features described in the present chapter are supported by all LINE solvers. However, upon invoking a solver, LINE automatically detects if the supplied model can be analyzed by the solver. If this is not possible, an empty result set will be returned. We point to Chapter 3 for tables summarizing the features supported by each solver.

### 2.1 Network object definition

#### 2.1.1 Creating a network of resources

A queueing network model can be easily described using the LINE modelling language, which decouples network specification from its solution. To get started, we can create our first queueing network model, called 'myModel', as follows

```
model = Network('myModel');
```

The returned object of the Network class offers methods to instantiate and manage resource nodes (stations, routers, delays, ...) visited by jobs of several types (classes).

A *node* is a resource in the network that can be visited by a job. If jobs are allowed to spend time in the node during the visit to the system, the node is said to be a *station*. For example, a first-come first-served queue is a station, while a sink or class-switching router are nodes. Stations are instances of the Station class and its descendants. In particular, the QueueingStation class specifies a queueing system from its name and scheduling strategy, e.g.

```
node{1} = QueueingStation(model, 'Queue1', SchedStrategy.FCFS);
```

Valid scheduling strategies are specified within the SchedStrategy static class and include:

• First-come first-served (SchedStrategy.FCFS)

- Infinite-server (SchedStrategy.INF)
- Processor-sharing (SchedStrategy.PS)
- Discriminatory processor-sharing (SchedStrategy.DPS)
- Generalized processor-sharing (SchedStrategy.GPS)
- Shortest expected processing time (SchedStrategy.SEPT)
- Shortest job first (SchedStrategy.SJF)
- Head-of-line priority (SchedStrategy.HOL)

Infinite-server stations may be instantiated as either stations with the SchedStrategy. INF strategy or using the following specialized constructor

```
node{2} = DelayStation(model, 'ThinkTime');
```

If a strategy requires class weights, these can be specified directly as an argument to the setService method, which is discussed later in Section 2.1.5, or using the setStrategyPar method.

#### 2.1.2 Service classes

Jobs travel within the network placing service demands at the stations. Jobs in *open classes* arrive from the external world and, upon completing the visit, leave the network. Jobs in *closed classes* start within the network and are forbidden to ever leave it, perpetually cycling among nodes. The demand placed by a job at a station depends on the current class of the job.

The constructor for an open class only requires the class name and the creation of special nodes called Source and Sink

```
jobclass{1} = OpenClass(model, 'Class1');
node{3} = Source(model, 'Source');
node{4} = Sink(model, 'Sink');
```

Sources are special stations holding an infinite pool of jobs, representing the external world. Sinks are nodes that route a departing job back into this infinite pool. A network can include at most a single Source and a single Sink. LINE does not require to associate these nodes explicitly with the open classes, as this is done automatically. However, the LINE language requires to explicitly create these nodes as the routing topology needs to specify the entry and exit points of jobs.

To create a closed class, we need instead to indicate the number of jobs initially in the class (e.g., 5 jobs) and the *reference station* (e.g., node {1}):

```
jobclass{2} = ClosedClass(model, 'Class2', 5, node{1});
```

If the network includes only closed classes, there is no need to instantiate Source and Sink.

#### Reference station

As discussed later, each closed class r belongs to one and only one chain. A chain defines the set of reachable classes for a job that starts in a given class and over time switches class according to a probabilistic strategy, as described later in Section 2.1.3. The reference station is a node used to calculate performance indexes of the closed chains. For example, the system throughput for a chain is defined as sum of the arrival rates at the reference station for all classes in that chain. If there is

no class switching, each chain contain a single class, thus the per-chain and per-class performance indexes are identical.

#### Class priorities

If a class has a priority, with 0 representing the highest priority, this can be specified as an additional argument in both OpenClass and ClosedClass, e.g.,

```
jobclass{2} = ClosedClass(model, 'Class2', 5, node{1}, 0);
```

### 2.1.3 Routing policies

Jobs travel between nodes according to the network topology and a routing policy. The function addLink can be used to specify that two nodes are connected

```
model.addLink(node{1}, node{1}); %self-loop
model.addLink(node{1}, node{2});
```

Typically, a queueing network will use a probabilistic routing policy. If two nodes are connected, it is possible to specify the routing probability of jobs between the jobs for each class, e.g.,

```
node{1}.setProbRouting(jobclass{1}, node{1}, 0.6)
node{1}.setProbRouting(jobclass{1}, node{2}, 0.4)
```

However, the simplest way to specify a large routing topology is to define the routing probability matrix for each class, followed by a method call to the linkNetwork method.

For example, consider a network with two classes and four nodes where: (i) class one visits node 1, then one at random between nodes 2,3, and 4, and finally cycles back to node 1; (ii) class two cycles among stations 1 to 4 in a sequence. We can instantiate this routing topology as follows:

```
P{1} = zeros(4); P{1}(1,2:4) = [1/3, 1/3, 1/3]; P{1}(2:4,1) = 1.0; % class 1 P{2} = circul(4); % class 2 visits stations in order model.linkNetwork(P);
```

It is important to note that the routing matrix in the example is specified between *nodes*, instead than between stations, which means that elements such as the Source and the Sink are explicitly considered in the routing matrix.

The numbering of classes and nodes corresponds to the order in which these elements are instantiated in the model. The <code>getClassIndex</code> and <code>getNodeIndex</code> methods return the numeric index associated to a node name, e.g., <code>model.getNodeIndex('Delay')</code>. Class and node names in a network need to be unique and can be fully listed calling on the model object the <code>getClassNames</code> and <code>getNodeNames</code> methods.

#### **Class switching**

In LINE, jobs can switch class while they travel between stations (including self-loops on the same station). This feature can be used to model queueing properties such as re-entrant lines, whereby a job visiting a station a second time may require a different average demand than at the first visit. Jobs in open classes can only switch to another open class. Similarly, jobs in closed classes can only switch to a closed class. Thus, class switching from open to closed classes (or vice-versa) is forbidden. The

policy to describe the class switching process is integrated in the specification of the routing between stations

In models with class switching, a routing matrix is required for each possible pair of source and target classes. For example, assume that in the previous example a job in class 1 can switch into class 2 after departing node 4, remaining there forever. We can specify this routing policy as follows:

```
P = cellzeros(2,4); % 2 classes, 4 stations
% switching probabilities from class 1 to class 2
P{1,2}(4,1) = 1.0; % routing from station 4 to 1
% routing probabilities for class 1 (no switching)
P{1,1}(1,2:4) = [1/3, 1/3, 1/3]; P{1,1}(2:3,1) = 1.0;
% routing probabilities for class 2 (no switching)
P{2,2} = circul(4); % class 2 visits stations in order
model.linkNetwork(P);
```

where  $P\{r, s\}$  is the routing matrix for jobs switching from class r to s, i.e.,  $P\{r, s\}$  (i, j) is the probability that a job in class r departs node i routing into node j as a job of class s.

LINE assumes that a job switches class an instant *before* leaving a station, so that the throughput of the station is already accounting for the new class of the job.

Depending on the specified probabilities, a job will be able to switch class among a subset of the available classes. Each subset is called a *chain*. Chains are determined as the weakly connected components of the routing probability matrix of the network, when this is seen as an undirected graph. The function model.getChains produces a list of chains for a model and of their member classes.

#### Routing probabilities for source and sink nodes

In the presence of open classes, and in mixed models with both open and closed classes, one needs only to specify the routing probabilities *out* of the source. The probabilities out of the sink can all be set to zero for all classes and destinations (including self-loops). The solver will take care of adjusting these inputs to create a valid routing table.

#### Tandem and cyclic topologies

Tandem networks are open queueing networks with a serial topology. LINE provides functions that ease the definition of tandem networks of stations with exponential service times. For example, we can rapidly instantiate a tandem network consisting of stations with PS and INF scheduling as follows

```
A = [10,20]; % A(r) - arrival rate of class r
D = [11,12; 21,22]; % D(i,r) - class-r demand at station i (PS)
Z = [91,92; 93,94]; % Z(i,r) - class-r demand at station i (INF)
modelPsInf = Network.tandemPsInf(A,D,Z)
```

The above snippet instantiates an open network with two queueing stations (PS), two delay stations (INF), and exponential distributions with the given inter-arrival rates and mean service times. The Network.tandemPs, Network.tandemFcfs, and Network.tandemFcfsInf methods provide static constructors for networks with other combinations of scheduling policies, namely only PS, only FCFS, or FCFS and INF.

A tandem network with closed classes is instead called a cyclic network. Similar to tandem networks, LINE offers a set of static constructors: Network.cyclicPs, Network.cyclicPsInf, Network.cyclicFcfs, and Network.cyclicFcfsInf. These methods only require to replace

the arrival rate vector A by a vector N specifying the job populations for each of the closed classes, e.g.,

```
N = [10,20]; % N(r) - closed population in class r
modelPsInf = Network.cyclicPsInf(N,D,Z)
```

#### 2.1.4 Finite buffers

The station methods setBufferCapacity and setBufferChainCapacity are used to place constraints on the number of jobs, total or for each chain, that can reside within a station. Note that LINE does not allow one to specify buffer constraints at the level of individual classes, unless chains contain a single class, in which case setBufferChainCapacity is sufficient for the purpose.

For example,

```
example_closedModel_3
node{2}.setBufferChainCapacity([1,1])
model.refreshBuffer()
```

creates an example model with two chains and three classes (specified in example\_closedModel\_3.m) and requires the second station to accept a maximum of one job in each chain. Note that if we were to ask for a higher capacity, such as setBufferChainCapacity([1,7]), which exceeds the total job population in chain 2, LINE would have automatically reduced the value 7 to the chain 2 job population (2). This automatic correction ensures that methods that analyze the state space of the model do not generate unreachable states.

The refreshBuffer method updates the buffer parameterizations, performing appropriate sanity checks. Since example\_closedModel\_3 has already invoked a solver prior to our changes, the requested modifications are materially applied by LINE to the network only after calling an appropriate refresh method, see Section 2.4. If the buffer capacity changes were made before the first solver invocation on the model, then there would not be need for a refreshBuffer call, since the internal representation of the Network object used by the solvers is still to be created.

#### 2.1.5 Service and inter-arrival time processes

A number of statistical distributions are available to specify job service times at the stations and interarrival times from the Source station. The class MarkovianDistribution offers distributions that are analytically tractable, which are defined upon certain absorbing Markov chains consisting of one or more states (*phases*) that are called phase-type distributions. They include as special case the following distributions supported in LINE, along with their respective constructors:

- Exponential distribution:  $Exp(\lambda)$ , where  $\lambda$  is the rate of the exponential
- n-phase Erlang distribution: Erlang $(\alpha, n)$ , where  $\alpha$  is the rate of each of the n exponential phases
- 2-phase hyper-exponential distribution: HyperExp $(p, \lambda_1, \lambda_2)$ , that returns an exponential with rate  $\lambda_1$  with probability p, and an exponential with rate  $\lambda_2$  otherwise.
- 2-phase Coxian distribution:  $Cox2(\mu_1, \mu_2, \phi_1)$ , which assigns rates  $\mu_1$  and  $\mu_2$  to the two rates, and completion probability from phase 1 equal to  $\phi_1$  (the probability from phase 2 is  $\phi_2 = 1.0$ ).

For example, given mean  $\mu = 0.2$  and squared coefficient of variation SCV=10, where SCV=variance/ $\mu^2$ , we can assign to a node a 2-phase Coxian service time distribution with these moments as

```
node{1}.setService(jobclass{2}, Cox2.fitMoments(0.2,10));
```

Inter-arrival time distributions can be instantiated in a similar way, using setArrival instead of setService on the Source node. For example, if the Source is node 3 we may assign the inter-arrival times of class 2 to be exponential with mean 0.1 as follows

```
node{3}.setArrival(jobclass{2}, Exp.fitMoments(0.1));
```

where we have used a single parameter in fitMoments since the exponential distribution does not allow to choose the SCV.

Non-Markovian distributions are also available, but typically they restrict the available network analysis techniques to simulation. They include the following distributions:

- Deterministic distribution:  $Det(\mu)$  assigns probability 1.0 to the value  $\mu$ .
- Uniform distribution: Uniform (a, b) assigns uniform probability 1/(b-a) to the interval [a, b].
- Gamma distribution:  $Gamma(\alpha, k)$  assigns a gamma density with shape  $\alpha$  and scale k.
- Pareto distribution:  $Pareto(\alpha, k)$  assigns a Pareto density with shape  $\alpha$  and scale k.

Lastly, we discuss two special distributions. The <code>Disabled</code> distribution can be used to explicitly forbid a class to receive service at a station. This may be useful in models with sparse routing matrices, both to ensure an efficient model solution and to debug the model specification. Performance metrics for disabled classes will be set to <code>NaN</code>.

Conversely, the Immediate class can be used to specify instantaneous service (zero service time). Typically, LINE solvers will replace zero service times with small positive values ( $\varepsilon = 10^{-7}$ ).

#### Fitting a distribution

The fitMoments method is available for all distributions that inherit from the Markovian Distribution class. This method provides exact or approximate matching of the requested moments, depending on the theoretical constraints imposed by the distribution. For example, an Erlang distribution with SCV=0.75 does not exist, because in a n-phase Erlang it must be SCV=1/n. In a case like this, Erlang.fitMoments(1,0.75) will return the closest approximation, e.g., a 2-phase Erlang (SCV=0.5) with unit mean. The Erlang distribution also offer a method fitMeanAndOrder( $\mu$ , n), which instantiates a n-phase Erlang with given mean  $\mu$ .

In distributions that are uniquely determined by more than two moments, fitMoments chooses a particular assignment of the residual degrees of freedom other than mean and SCV. For example, HyperExp depends on three parameters, therefore it is insufficient to specify mean and SCV to identify the distribution. Thus, HyperExp.fitMoments automatically chooses to return a probability of selecting phase 1 equal to 0.99, as this spends the degree of freedom corresponding to the (unspecified) third moment of the distribution. Compared to other choices, this particular assignment corresponds to an higher probability mass in the tail of the distribution.

#### Inspecting and sampling a distribution

To verify that the fitted distribution has the expected mean and SCV it is possible to use the getMean and getSCV methods, e.g.,

```
>> dist = Exp(1);
>> dist.getMean
```

```
ans =
    1
>> dist.getSCV
ans =
    1
```

Moreover, the sample method can be used to generate values from the obtained distribution, e.g. we can generate 3 samples as

The evalCDF and evalCDFInterval methods return the cumulative distribution function at the specified point or within a range, e.g.,

```
>> dist.evalCDFInterval(2,5)
ans =
    0.1286
>> dist.evalCDF(5)-dist.evalCDF(2)
ans =
    0.1286
```

For more advanced uses, the distributions of the MarkovianDistribution class also offer the possibility to obtain the standard  $(D_0,D_1)$  representation used in the theory of Markovian arrival processes by means of the <code>getMarkovianRepresentation</code> method. The result will be a cell array where element k+1 corresponds to matrix  $D_k$ .

#### **Temporal dependent processes**

It is sometimes useful to specify the statistical properties of a *time series* of service or inter-arrival times, as in the case of systems with short- and long-range dependent workloads. When the model is stochastic, we refer to these as situations where one specifies a *process*, as opposed to only specifying the *distribution* of the service or inter-arrival times. In LINE processes inherit from the PointProcess class, and include the 2-state Markov-modulated Poisson process (MMPP2) and empirical traces read from files (Trace).

In particular, LINE assumes that empirical traces are supplied as text files (ASCII), formatted as a column of numbers. Once specified, the Trace object can be used as any other distribution. This means that it is possible to run a simulation of the model with the specified trace. However, analytical solvers will require tractable distributions from the MarkovianDistribution class.

#### **Scheduling parameters**

Upon setting service distributions at a station, one may also specify scheduling parameters such as weights as additional arguments to the setService method. For example, if the node implements discriminatory processor sharing (SchedStrategy.DPS), the command

```
node{1}.setService(jobclass{2}, Cox2.fitMoments(0.2,10), 5.0);
```

assigns a weight 5.0 to jobs in class 2. The default weight of a class is 1.0.

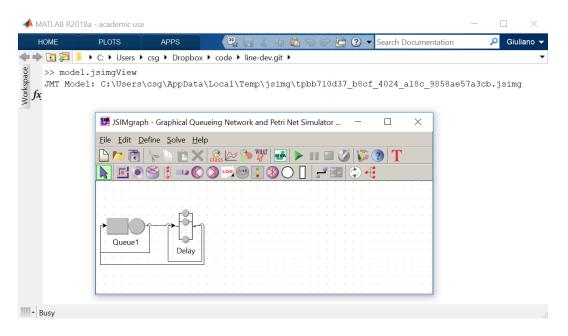


Figure 2.1: Network.jsimgView method

### 2.1.6 Debugging and visualization

JSIMgraph is the graphical simulation environment of the JMT suite. LINE can export models to this environment for visualization purposes using the command

```
model.jsimgView
```

An example is shown in Figure 2.1. Using a related function, <code>jsimwView</code>, it is also possible to export the model to the JSIMwiz environment, which offers a wizard-based interface.

Another way to debug a LINE model is to transforming it into a MATLAB graph object, e.g.

```
G = model.getGraph();
plot(G,'EdgeLabel',G.Edges.Weight,'Layout','Layered')
```

plots a graph of the queueing network topology. Furthermore, the graph properties concisely summarize the key features of the network

```
>> G.Nodes
ans =
  2x5 table
                                                          ClosedClass1
      Name
                       Type
                                        Sched
                                                  Jobs
    'Delay'
                 'DelayStation'
                                        'inf'
                                                   5
                                                                1
    'Queue1'
                 'QueueingStation'
                                        'ps'
                                                   0
                                                                2
>> G.Edges
ans =
  3x4 table
          EndNodes
                              Weight
                                         Rate
                                                      Class
                               0.7
                                                  'ClosedClass1'
    'Delay'
                 'Delay'
                                           1
                 'Queue1'
                                                  'ClosedClass1'
    'Delay'
                               0.3
                                           1
```

```
'Queuel' 'Delay' 1 0.5 'ClosedClass1'
```

Here, Edge. Weight is the routing probability between the nodes, whereas Edge. Rate is the service rate of the source node.

#### 2.1.7 Model import and export

LINE offers a number of scripts to import external models into Network object instances that can be analyzed through its solvers. The available scripts are as follows:

- JMT2LINE imports a JMT simulation model (.jsimg or .jsimw file) instance.
- PMIF2LINE imports a XML file containing a PMIF 1.0 model.

Both scripts require in input the filename and desired model name, and return a single output, e.g.,

```
qn = PMIF2LINE([pwd,'\\examples\\data\\PMIF\\pmif_example_closed.xml'],'Mod1')
```

where qn is an instance of the Network class.

Network object can be saved in binary .mat files using MATLAB's standard save command. However, it is also possible to export a textual script that will dynamically recreate the same <code>Network</code> object. For example,

```
example_closedModel_1; LINE2SCRIPT(model, 'script.m')
```

creates a new file script.m with code

```
model = Network('model');
node{1} = DelayStation(model, 'Delay');
node{2} = QueueingStation(model, 'Queuel', SchedStrategy.PS);
node{2}.setNumServers(1);
jobclass{1} = ClosedClass(model, 'ClosedClass1', 5, node{1}, 0);
node{1}.setService(jobclass{1}, Cox2.fitMoments(1.000000,1.000000));
node{2}.setService(jobclass{1}, Cox2.fitMoments(2.000000,1.000000));
myP = cell(1);
myP{1,1} = [0.7 0.3;1 0];
model.linkNetwork(myP);
```

that is equivalent to the model specified in example\_closedModel\_1.m.

## 2.2 Defining network states

In some analyses it is important to specify the state of the network, for example to assign the initial position of the jobs in a transient analysis. We thus discuss the native support in LINE for state modeling.

#### 2.2.1 Station states

We begin by explaining how to specify a state  $s_0$ . State modelling is supported only for stations with scheduling policies that depend on the number of jobs running or waiting at the node. For example, it is not supported for shortest job first (SchedStrategy.SJF) scheduling, in which state depends on the service time samples for the jobs.

Suppose that the network has R classes and that service distributions are phase-type, i.e., that they inherit from MarkovianDistribution. Let  $K_r$  be the number of phases for the service distribution in class r at a given station. Then, we define three types of state variables:

- $c_j$ : class of the job waiting in position  $j \le b$  of the buffer, out of the b currently occupied positions. If b = 0, then the state vector is indicated with a single empty element  $c_1 = 0$ .
- $n_r$ : total number of jobs of class r in the station
- $s_{rk}$ : total number of jobs of class r running in phase k in the server

Here, by phase we mean the number of states of a distribution of class MarkovianDistribution. If the distribution is not Markovian, then there is a single phase. With these definitions, Table 2.1 illustrates how to specify in LINE a valid state for a station depending on its scheduling policy. States

rable 2.1. State descriptors for warkovian scheduling policies						
Strategy	Station state					
FCFS, HOL, LCFS	$[c_b, c_{b-1}, \dots, c_1, s_{11}, \dots, s_{1K_1}, s_{21}, \dots, s_{2K_2}, \dots, s_{R1}, \dots, s_{RK_R}]$					
SEPT, RAND	$[n_1, n_2, \dots, n_R, s_{11}, \dots, s_{1K_1}, s_{21}, \dots, s_{2K_2}, \dots, s_{R1}, \dots, s_{RK_R}]$					
PS, DPS, GPS, INF	$[s_{11},\ldots,s_{1K_1},s_{21},\ldots,s_{2K_2},\ldots,s_{R1},\ldots,s_{RK_R}]$					

Table 2.1: State descriptors for Markovian scheduling policies

can be manually specified or enumerated automatically through LINE. Library functions for handling states are as follows:

- State from Marginal: enumerates all states that have the same marginal state  $[n_1, n_2, \dots, n_R]$ .
- State.fromMarginalAndRunning: restricts the output of State.fromMarginal to states with given number of running jobs, irrespectively of the service phase in which they currently run.
- State.fromMarginalAndStarted: restricts the output of State.fromMarginal to states with given number of running jobs, all assumed to be in service phase k=1.
- State.fromMarginalBounds: similar to State.fromMarginal, but produces valid states between given minimum and maximum of resident jobs.
- State.toMarginal: extracts statistics from a state, such as the total number of jobs in a given class that are running at the station in a certain phase.

Note that if a function call returns an empty state ([]), this should be interpreted as an indication that no valid state exists that meets the required criteria. Often, this is because the state supplied in input is invalid.

#### **Example**

We consider the example network in example\_closedModel\_4.m. We look at the state of station 3, which is a multi-server FCFS station. There are 4 classes all having exponential service times except class 2 that has Erlang-2 service times. We are interested to states with 2 running jobs in class 1 and 1 in class 2, and with 2 jobs, respectively of classes 3 and 4, waiting in the buffer. We can automatically generate this state space, which we store in the space variable, as:

```
>> example_closedModel_4;

>> space = State.fromMarginalAndRunning(model,3,[2,1,1,1],[2,1,0,0])

space =

4  3  2  1  0  0  0

4  3  2  0  1  0  0
```

```
3 4 2 1 0 0 0
3 4 2 0 1 0 0
```

Here, each row of space corresponds to a valid state. The argument [2,1,1,1,1] gives the number of jobs in the node for the 4 classes, while [2,1,0,0] gives the number of running jobs in each class. This station has four valid states, differing on whether the class-2 job runs in the first or in the second phase of the Erlang-2 and on the relative position of the jobs of class 3 and 4 in the waiting buffer.

To obtain states where the jobs have just started running, we can instead use

If we instead remove the specification of the running jobs, we can use State.fromMarginal to generate all possible combinations of states depending on the class and phase of the running jobs. In the example, this returns a space of 20 possible states.

```
>> space = stateFromMarginal(model, 3, [2, 1, 1, 1], [2, 1, 0, 0])
space =
      4
              3
                      2
                             1
                                     0
                                             0
                                                     0
      4
              3
                      2
                             0
                                     1
                                             0
                                                     0
      4
              2
                      2.
                             0
                                     0
                                             1
                                                     0
      4
                                     0
                                                     0
              1
                      1
                             1
                                             1
                                                     0
      4
                             0
                                     1
                                             1
              1
                      1
      3
              4
                      2
                                     0
                                             0
                                                     0
                             1
      3
              4
                      2
                             0
                                     1
                                             Ω
                                                     0
      3
              2
                      2
                             0
                                     0
                                             0
                                                     1
      3
                                             0
                                     0
      3
                             0
                                     1
                                             0
                                                     1
      2
              4
                      2
                             0
                                     0
                                             1
                                                     0
      2
              3
                      2
                             0
                                     0
                                             0
                                                     1
      2
              1
                      1
                             0
                                     0
                                             1
                                                     1
                                     0
                                             1
                                                     0
      1
              4
                      1
                             1
      1
              4
                             0
                                     1
                                             1
                                                     0
                      1
      1
              3
                      1
                             1
                                     0
                                             0
                                                     1
              3
                             0
                                     1
                                             0
      1
                      1
                                                     1
      1
              2
                      1
                             0
                                     0
                                             1
                                                     1
      1
              1
                      0
                             1
                                     0
                                             1
                                                     1
                                     1
```

#### Assigning a state to a station

Given a single or multiple states, it is possible to assign the initial state to a station using the setState method on that station's object. To cope with multiple states, LINE offers the possibility to specify a prior probability on the initial states, so that if multiple states have a non-zero prior, then the solver will need to analyze the network from all those states and weight the results according to the prior probabilities. The default prior value assigned probability 1.0 to the *first* specified state. The station methods setStatePrior and getStatePrior can be used to check and change the prior probabilities for the supplied initial states.

#### 2.2.2 Network states

A collection of states that are valid for each station is not necessarily valid for the network as a whole. For example, if the sum of jobs of a closed class exceeds the population of the class, then the network state would be invalid. To identify these situations, LINE requires to specify the initial state of a network using methods supplied by the Network class. These methods are initFromMarginal, initFromMarginalAndRunning, and initFromMarginalAndStarted. They require a matrix with elements  $\mathbf{n}(i,r)$  specifying the total number of resident class-r jobs at node i and the latter two require a matrix  $\mathbf{s}(i,r)$  with the number of running (or started) class-r jobs at node i. The user can also manually verify if the supplied network state is going to be valid using State.IsValid.

It is also possible to request LINE to automatically identify a valid initial state, which is done using the initDefault method available in the Network class. This is going to select a state where:

- no jobs in open classes are present in the network;
- jobs in closed classes all start at their reference stations;
- the server of reference stations are occupied in order of class id, i.e., jobs in the firstly created class are assigned to the server in phase 1, then spare servers are allocated to the second class in phase 1, and so forth;
- if the scheduling policy requires it, jobs are ordered in the buffer by class, with the firstly created class at the head and the lastly created class at the tail of the buffer.

#### 2.2.3 Station response time distribution

SolverFluid supports the computation of response time distributions for individual classes through the getCdfRespT method. The method returns the response time distribution for every station and class. For example, the following code plots the cumulative distribution function at steady-state for class 1 jobs when they visit station 2:

```
solver = SolverFluid(model);
FC = solver.getCdfRespT();
plot(FC{2,1}(:,2),FC{2,1}(:,1)); xlabel('t'); ylabel('Pr(RespT<t)');</pre>
```

#### 2.2.4 System average performance

LINE also allows users to analyze models for end-to-end performance indexes such a system throughput or system response time. However, in models with class switching the notion of system-wide metrics can be ambiguous. For example, consider a job that enters the network in one class and departs the network in another class. In this situation one may attribute system response time to either the arriving class or the departing one, or attempt to partition it proportionally to the time spent by the job within each class. In general, the right semantics depends on the aim of the study.

LINE tackles this issue by supporting only the computation of system performance indexes *by chain*, instead than by class. In this way, since a job switching from a class to another remains by definition in the same chain, there is no ambiguity in attributing the system metrics to the chain. The solver methods <code>getAvgSysByChain</code> and <code>getAvgSysByChainTable</code> return system response time and system throughput per chain as observed: (i) upon arrival to the sink, for open classes; (ii) upon arrival to the reference station, for closed classes.

In some cases, it is possible that a chain visits multiple times the reference station before the job completes. This also affects the definition of the system averages, since in some applications one may

want to avoid counting each visit as a completion of the visit to the system. In such cases, LINE allows to specify which classes of the chain can complete at the reference station. For example, in the code below we require that a job visits reference station 1 twice, in classes 1 and 2, but completes at the reference station only when arriving in class 2. Therefore, the system response time will be counted between successive passages in class 2.

```
jobclass{1} = ClosedClass(model, 'ClosedClass1', 1, node{1}, 0);
jobclass{2} = ClosedClass(model, 'ClosedClass2', 0, node{1}, 0);

jobclass{1}.completes = false;

P = cell(2); % 2-classes model
P{1,1} = [0,1; 0,0]; % routing within class 1 (no switching)
P{1,2} = [0,0; 1,0]; % routing from class 1 into class 2
P{2,1} = [0,0; 1,0]; % routing within class 2 (no switching)
P{2,2} = [0,1; 0,0]; % routing from class 2 into class 2

model.linkNetwork(P);
```

Note that LINE does not allow a chain to complete at heterogeneous stations, therefore the completes property of a class always refers to the reference station for the chain.

## 2.3 Transient analysis

So far, we have seen how to compute steady-state average performance indexes, which are given by

$$E[n] = \lim_{t \to +\infty} E[n(t)]$$

where n(t) is an arbitrary performance index, e.g., the queue-length of a given class at time t.

We now consider instead the computation of the quantity  $E[n(t)|s_0]$ , which is the *transient average* of the performance index, conditional on a given initial system state  $s_0$ . Compared to n(t), this quantity averages the system state at time t across all possible evolutions of the system from state  $s_0$  during the t time units, weighted by their probability. In other words, we observe all possible stochastic evolutions of the system from state  $s_0$  for t time units, recording the final values of n(t) in each trajectory, and finally average the recorded values at time t to obtain  $E[n(t)|s_0]$ .

#### 2.3.1 Computing transient averages

At present, LINE supports only transient computation of queue-lengths, throughputs and utilizations using the CTMC and FLUID solvers. Transient response times are not currently supported, as they do not always obey Little's law.

The computation of transient metrics proceeds similarly to the steady-state case. We first obtain the handles for transient averages:

```
[Qt,Ut,Tt] = model.getTransientHandlers();
```

After solving the model, we will be able to retrieve both steady-state and transient averages as follows

```
[QNt,UNt,TNt] = solver{s}.getTransientAvg(Qt,Ut,Tt)
plot(QNt{1,1}(:,2), QNt{1,1}(:,1))
```

The transient average queue-length at node i for class r is stored within QNt  $\{i, r\}$ .

Note that the above code does not show how to specify a maximum time t for the output time series. This can be done using the timespan field of the options, as described later in Chapter 3.

#### 2.3.2 First passage times into stations

When the model is in a transient, the average state seen upon arrival to a station changes over time. That is, in a transient, successive visits by a job may experience different response time distributions. To avoid ambiguities, the notion of response time distribution is best replaced in transient by the one of *first passage time*, i.e., the distribution of the time to complete the *first visit* to the station under consideration. The method <code>getCdfFirstPassT</code> provides this distribution, assuming as initial state the one specified for the model, e.g., using <code>setState</code> or <code>initDefault</code>. This method is available only in <code>SolverFluid</code> and has a similar syntax as <code>getCdfRespT</code>.

## 2.4 Sensitivity analysis and numerical optimization

Frequently, performance and reliability analysis requires to change one or more model parameters to see the sensitivity of the results or to optimize some goal function. In order to do this efficiently, we discuss the internal representation of the Network objects used within the LINE solvers. By applying changes directly to this internal representation it is possible to considerably speed-up the sequential evaluation of several models.

#### 2.4.1 Internal representation

For efficiency reasons, once a user requests to solve a Network, LINE calls internally generates a static representation of the network using the generateQN method, and then passes this object to the chosen solver to parameterize the analysis.

The main representation used within LINE is the QNCoxCS class, which describes an extended multiclass queueing network with class-switching and Coxian service times. The representation can be obtained as follows

```
myQN = model.getQN()
```

Table 2.2 presents the properties of the QNCoxCS class.

#### 2.4.2 Fast parameter update

Successive invocations of getQN will return a cached copy of the QN representation, unless the user has called model.refresh() or model.reset() in-between the invocations. The refresh method regenerates the internal representation, while reset destroys it, together with all other representations and cached results stored in the Network object. In the case of reset, the internal data structure will be regenerated at the next refresh or getQN call.

The performance cost of updating the representation can be significant, as some of the structure array field require a dedicated algorithm to compute. For example, finding the chains in the model requires an analysis of the weakly connected components of the network routing matrix. For this reason, the Network class provides several methods to selectively refresh only part of the QN representation, once the modification has been applied to the objects (e.g., stations, classes, ...) used to define the network. These methods are as follows:

Table 2.2: QNCoxCS class properties

Field	Type	Description
$\mathtt{bufsz}(i)$	integer	Total buffer size at station $i$
bufszclass(i,r)	integer	Maximum buffer size used by class $r$ at station $i$
$\mathtt{chains}(c,r)$	logical	true if class $r$ is in chain $c$ , or false otherwise
$\texttt{classname}\{r\}$	string	Name of class $r$
${\tt classprio}(r)$	integer	Priority of class $r$ (0 = highest priority)
$\operatorname{mu}\{i,r\}(k)$	double	Coxian service or arrival rate in phase $k$ for class $r$ at station $i$
nchains	integer	Number of chains in the network
nchainjobs(c)	integer	Number of jobs in chain $c$
nclasses	integer	Number of classes in the network
nclosedjobs	integer	Total number of jobs in closed classes
njobs(r)	integer	Number of jobs in class $r$ (Inf for open classes)
nnodes	integer	Number of nodes in the network
nservers(i)	integer	Number of servers in station $i$
nstations	integer	Number of stations in the network
$\mathtt{phi}\{i,r\}(k)$	double	Coxian completion probability in phase $k$ for class $r$ at station $i$
phases(i,r)	integer	Number of phases for service process of class $r$ at station $i$
rates(i,r)	double	Service rate of class $r$ at station $i$ (or arrival rate if $i$ is a Source)
refstat(r)	integer	Index of reference station for class $r$
$rt(idx_{ir}, idx_{js})$	double	Routing probability from station $i$ to $j$ , switching class from $r$ to
		$s$ where, e.g., $idx_{ir}=(i-1)*{ t myQN}$ . ${ t nclasses}+r.$
$\mathrm{sched}\{i\}$	cell	Scheduling strategy at station $i$ (e.g., SchedStrategy.PS)
$\verb schedparam (i,r)$	double	Parameter for class $r$ strategy at station $i$
$ exttt{schedid}(i)$	integer	Scheduling strategy id at station $i$ (e.g., SchedStrategy.ID_PS)
scv(i,r)	double	Squared coefficient of variation of class $r$ service times at station
		i (or inter-arrival times if station $i$ is a Source)
$space\{t\}$	integer	The $t$ -th state in the state space (or a portion thereof). This field is
	vector	initially empty and assigned by the solver during execution.
state	integer	Initial state of the model. This field is initially empty and assigned
	vector	by the solver during execution.
${\tt stationname}\{i\}$	string	Name of station i
$   \text{visits}\{c\}(i,r)  $	double	Number of visits that a chain $c$ job pays at node $i$ in class $r$

- refreshArrival: this method should be called after updating the inter-arrival distribution at a Source.
- refreshBuffer: this method should be called after changing buffer capacities, as it updates the bufsz and bufszclass fields.
- refreshChains: this method should be used after changing the routing topology, as it refreshes the rt, chains, nchains, nchainjobs, and visits fields.
- refreshPriorities: this method updates class priorities by refreshing the classprio field.
- refreshScheduling: updates the sched, schedid, and schedparam fields.
- refreshService: updates the mu, phi, phases, rates and scv fields.

For example, suppose we wish to update the service time distribution for class-1 at node 1 to be exponential with unit rate. This can be done efficiently as follows:

```
node{1}.setService(jobclass{1}, Exp(1.0));
model.refreshService;
```

#### 2.4.3 Saving a network object before a change

The Network object, and its inner objects that describe the network elements, are always passed by reference. The copy method should be used to clone LINE objects, for example before modifying a parameter for a sensitivity analysis. This method recursively clones all objects in the model, therefore creating an independent copy of the network. For example, consider the following code

```
modelByRef = model; modelByRef.setName('myModel1');
modelByCopy = model.copy; modelByCopy.setName('myModel2');
```

Using the getName method it is then possible to verify that model has now name 'myModell', since the first assignment was by reference. Conversely, modelByCopy.setName did not affect the original model since this is a clone of the original network.

Last revision: July 29, 2018

## Chapter 3

## **Network solvers**

#### 3.1 Overview

Solvers analyze objects of class Network to return average, transient, distributions, or state probability metrics.

#### Available solvers

The following Network solvers are available within LINE 2.0.0-BETA1:

- AMVA: This is a solver based on approximate mean-value analysis (AMVA). This solver is typically the fastest and offers very good accuracy in a number of situations, in particular models where stations have a single-server. This solver is implemented by the SolverAMVA class.
- CTMC: This is a solver that returns the exact values of the performance metrics by explicit generation of the continuous-time Markov chain (CTMC) underpinning the model. As the CTMC typically incurs state-space explosion, this solver can successfully analyze only small models. The CTMC solver is the only method offered within LINE that can return an exact solution on all Markovian models, all other solvers are either approximate or are simulators. This solver is implemented by the SolverCTMC class.
- FLUID: This solver analyzes the model by means of an approximate fluid model, leveraging a representation of the queueing network as a system of ordinary differential equations (ODEs). The fluid model is approximate, but if the servers are all PS or INF, it can be shown to become exact in the limit where the number of users and the number of servers in each node grow to infinity [5,6]. This solver is implemented by the SolverFluid class.
- JMT: This is a solver that uses a model-to-model transformation to export the LINE representation into a JMT simulation model [7]. This solver can analyze also non-Markovian models, in particular those involving deterministic or Pareto distributions, or empirical traces. This solver is implemented by the SolverJMT class.
- MAM: This is a matrix-analytic method solver, which relies on quasi-birth death (QBD) processes to analyze open queueing systems. This solver is implemented by the SolverMAM class.
- NC: This solver uses a combination of methods based on the normalizing constant of state probability to solve a model. The underpinning algorithm are particularly useful to compute marginal and joint state probabilities in queueing network models. This solver is implemented by the SolverNC class.

• SSA: This is a discrete-event simulation based on the CTMC representation of the model. It is fully implemented in MATLAB language and thus offer lower speed than JMT, but the model execution can be easily parallelized using MATLAB's *spmd* construct. This solver is implemented by the SolverSSA class.

### 3.2 Solver features and options

#### **Scheduling strategies**

Table 3.1 shows the supported scheduling strategies within LINE queueing stations. Each strategy belongs to a policy class: preemptive resume (SchedPolicy.PR), non-preemptive (SchedPolicy.NP), non-preemptive priority (SchedPolicy.NPPrio).

			1 1		$\mathcal{C}$	$\mathcal{C}$		
				Networl	k Solve	r		
Strategy	<b>Policy Class</b>	AMVA	CTMC	FLUID	JMT	MAM	NC	SSA
FCFS	NP	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	~	<b>✓</b>	<b>✓</b>
INF	NP	<b>✓</b>	~	<b>✓</b>	~		<b>✓</b>	<b>✓</b>
RAND	NP	<b>✓</b>	<b>✓</b>		<b>✓</b>		<b>✓</b>	~
SEPT	NP		~		~			<b>✓</b>
SJF	NP				<b>✓</b>			
HOL	NPPrio		~		~			~
PS	PR	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>		<b>✓</b>	~
DPS	PR	~	~	<b>✓</b>	<b>✓</b>			~
GPS	PR		~		<b>✓</b>			<b>✓</b>

Table 3.1: Solver support for scheduling strategies

### **Statistical distributions**

Table 3.2 summarizes the current level of support for arrival and service distributions within each solver. Trace represents an empirical trace read from a file, which will be either replayed as-is by the JMT solver, or fitted automatically to a Cox by the other solvers. Note that JMT requires that the last row of the trace must be a number, *not* an empty row.

#### **Solver options**

Solver-specific default options can be obtained by the defaultOptions static method of the corresponding class, e.g.,

SolverJMT.defaultOptions

Unspecified entries indicate that the option is not available. Options are as follows:

• cutoff (integer  $\geq$  1) requires to ignore states where stations have more than the specified number of jobs. This is a mandatory option to analyze open classes using the CTMC solver.

			Networl	k Solve	r		
Distribution	AMVA	CTMC	FLUID	JMT	MAM	NC	SSA
Cox2	~	~	<b>✓</b>	<b>✓</b>	~	<b>✓</b>	<b>✓</b>
Exp	<b>✓</b>						
Erlang	<b>/</b>	<b>/</b>	<b>✓</b>	<b>/</b>	<b>~</b>	<b>/</b>	<
HyperExp	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>~</b>	<b>✓</b>	<b>✓</b>
Disabled	~	~	<b>✓</b>	~	~	<b>✓</b>	<b>✓</b>
Det				<b>/</b>			
Gamma				~			
Pareto				<b>/</b>			
Trace				<b>/</b>			
Uniform				<b>/</b>			

Table 3.2: Solver support for statistical distributions

- force (logical) requires the solver to proceed with analyzing the model. This bypasses checks and therefore can result in the solver either failing or requiring an excessive amount of resources from the system.
- iter\_max (integer  $\geq 1$ ) controls the maximum number of iterations that a solver can use, where applicable. If iter\_max=n, this option forces the FLUID solver to compute the ODEs over the timespan  $t \in [0, 10n/\mu^{\min}]$ , where  $\mu^{\min}$  is the slowest service rate in the model. For the AMVA solver this option instead regulates the number of successive substitutions allowed in the fixed-point iteration.
- iter\_tol (double) controls the numerical tolerance used to convergence of iterative methods. In the FLUID solver this option regulates both the absolute and relative tolerance of the ODE solver.
- init\_sol (solver dependent) re-initializes iterative solvers with the given configuration of the solution variables. In the case of AMVA, this is a matrix where element (i,j) is the mean queue-length at station i in class j. In the case of FLUID, this is a model-dependent vector with the values of all the variables used within the ODE system that underpins the fluid approximation.
- keep (logical) determines if the model-to-model transformations store on file their intermediate outputs. In particular, if verbose > 1 then the location of the .jsimg models sent to JMT will be printed on screen.
- method (solver dependent) enables to configure the internal algorithms used by a given solver.
- samples (integer  $\geq 1$ ) controls the number of samples collected for each performance index by simulation-based solvers. JMT requires a minimum number of samples of  $5 \cdot 10^3$  samples.
- seed (integer  $\geq 1$ ) controls the seed used by the pseudo-random number generators. For example, simulation-based solvers will give identical results across invocations only if called with the same seed.
- stiff (logical) requires the solver to use a stiff ODE solver.
- timestamp (real interval) requires the transient solver to produce a solution in the spec-

ified temporal range. If the value is set to [Inf, Inf] the solver will only return a steady-state solution. In the case of the FLUID solver and in simulation, [Inf, Inf] has the same computational cost of [0, Inf] therefore the latter is used as default.

• verbose controls the verbosity level of the solver. Supported levels are 0 for silent, 1 for standard verbosity, 2 for debugging.

#### 3.3 Network solvers

#### 3.3.1 SolverAMVA class

The solver is based on the Bard-Schweitzer AMVA. Non-exponential service times in FCFS nodes are treated using a diffusion approximation [8]. Multi-server FCFS is dealt with using a slight modification of the Rolia-Sevcik method [9]. DPS queues are analyzed with a time-scale separation method, so that for an incoming job of class r and weight  $w_r$ , classes with weight  $w_s \geq 5w_r$  are replaced by high-priority classes that are analyzed using the standard AMVA priority approximation. Conversely the remaining classes are treated by weighting the queue-length seen upon arrival in class  $s \neq r$  by the correction factor  $w_s/w_r$ .

#### 3.3.2 SolverCTMC class

The SolverCTMC class solves the model by first generating the infinitesimal generator of the Network and then calling an appropriate solver. Steady-state analysis is carried out by solving the global balance equations defined by the infinitesimal generator. If the keep option is set to true, the solver will save the infinitesimal generator in a temporary file and its location will be shown to the user.

Transient analysis is carried out by numerically solving Kolmogorov's forward equations using MATLAB's ODE solvers. The range of integration is controlled by the timespan option and the ODE solver by the stiff option.

The CTMC solver heuristically limits the solution to models with no more than 6000 states. The force option needs to be set to true to bypass this control. In models with infinite states, such as networks with open classes, the <code>cutoff</code> option should be used to specify the maximum number of jobs that is allowed in any station.

#### 3.3.3 SolverFluid class

This solver is based on the system of fluid ordinary differential equations for INF-PS queueing networks presented in [10].

The fluid ODEs are normally solved with the 'NonNegative' ODE solver option enabled. Four types of ODE solvers are used: fast or accurate, the former only if options.iter\_tol>  $10^{-3}$ , and stiff or non-stiff, depending on the value of options.stiff. The default options for the solver are stored in the following static methods:

- Solver.accurateStiffOdeSolver, set to MATLAB's ode15s.
- Solver.accurateOdeSolver, set to ode45.
- Solver.fastStiffOdeSolver, set to ode23s.
- Solver.fastOdeSolver, set to ode23.

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ODE variables corresponding to an infinite number of jobs, as in the job pool of a source station, or to jobs in a disabled class are not included in the solution vector. These rules apply also to the options.init\_sol vector.

The solution of models with FCFS stations maps these stations into corresponding PS stations where the service rates across classes are set identical to each other with a service distribution given by a mixture of the service processes of the service classes. The mixture weights are determined iteratively by solving a sequence of PS models until convergence. Upon initializing FCFS queues, jobs in the buffer are all initialized in the first phase of the service.

#### 3.3.4 Solver, IMT class

The class is a wrapper for the JMT simulation and consists of a model-to-model transformation from the Network data structure into the JMT's input XML format (.jsimg) and a corresponding parser for JMT's results. In the transformation, artificial nodes will be automatically added to the routing table to represent class-switching nodes used in the simulator to specify the switching rules. One such class-switching node is defined for every ordered pair of stations (i,j) such that jobs change class in transit from i to j.

Upon invocation, the JMT JAR archive will be searched in the MATLAB path and if unavailable automatically downloaded.

#### 3.3.5 SolverMAM class

This is a basic solver for some Markovian open queueing systems that can be analyzed using matrix analytic methods. The solver at the moment is a basic wrapper for the BU tools library for matrix-analytic methods [11]. At present, it is not possible to solve a queueing network model using SolverMAM.

#### 3.3.6 SolverSSA class

SolverSSA is a basic stochastic simulator for continuous-time Markov chains. It reuses some of the methods that underpin SolverCTMC to generate the network state space and subsequently simulates the state dynamics by probabilistically choosing one among the possible events that can incur in the system, according to the state spaces of each of node in the network. For efficiency reasons, states are tracked at the level of individual stations, and hashed. The state space is not generated upfront, but rather stored during the simulation, starting from the initial state. If the initialization of a station generates multiple possible initial states, SSA initializes the model using the first state found. The list of initial states for each station can be obtained using the getInitState methods of the Network class.

#### 3.4 Solver maintenance

The following best practices can be helpful in maintaining the LINE installation:

- To install a new release of JMT, it is necessary to delete the JMT.jar file under '\solvers\JMT'. This forces LINE to download the latest version of the JMT executable.
- Periodically running the jmtCleanTempDir script can help removing temporary by-products of the JMT solver. This is strongly encouraged under repeated uses of the keep=1 option, as this stores on disk the temporary models sent to JMT.

## **Chapter 4**

# Layered network models

In this chapter, we present the definition of the LayeredNetwork class, which encodes the support in LINE for layered queueing networks. These models are extended queueing networks where servers, in order to process jobs, can issue synchronous and asynchronous calls among each other. The topology of call dependencies makes it possible to partition the model into a set of layers, each consisting of a subset of the resources. We point to [12] and to the LQNS user manual for an introduction [13].

## 4.1 LayeredNetwork object definition

#### 4.1.1 Creating a layered network topology

A layered queueing network consists of four types of elements: processors, tasks, entries and activities. An entry is a class of service specified through a finite sequence of activities, and hosted by a task running on a (physical) processor. A task is typically a software queue that models access to the capacity of the underpinning processor. Activities model either service demands required at the underpinning processor, or calls to entries exposed by some remote tasks.

To create our first layered network, we instantiate a new model as

```
model = LayeredNetwork('myLayeredModel');
```

We now proceed to instantiate the static topology of processors, tasks and entries:

```
P1 = Processor(model, 'P1', 1, SchedStrategy.PS);
P2 = Processor(model, 'P2', 1, SchedStrategy.PS);
T1 = Task(model, 'T1', 5, SchedStrategy.REF).on(P1);
T2 = Task(model, 'T2', 1, SchedStrategy.INF).on(P2);
E1 = Entry(model, 'E1').on(T1);
E2 = Entry(model, 'E2').on(T2);
```

Here, the on method specifies the associations between the elements, e.g., task T1 runs on processor P1, and accepts calls to entry E1. Furthermore, the multiplicity of T1 is 5, meaning that up to 5 calls can be simultaneously served by this element (i.e., 5 is the number of servers in the underpinning queueing system for T1). Note that both processors and tasks can be associated to the standard LINE scheduling strategies, with the exception that SchedStrategy.REF should be used to denote the reference task, which has a similar meaning to the reference node in the Network object.

#### 4.1.2 Describing service times of entries

The service demands placed by an entry on the underpinning processor is described in terms of execution of one or more activities. Although in tools such as LQNS activities can be associated to either entries or tasks, LINE supports only the more general of the two options, i.e., the definition of activities of the level of tasks. In this case:

- Every task defines a collection of activities.
- Every entry needs to specify an initial activity where the execution of the entry starts (the activity is said to be "bound to the entry") and a final activity, which upon completion terminates the execution of the entry.

For example, we can associate an activity to each entry as follows:

```
A1 = Activity(model, 'A1', Exp(1.0)).on(T1).boundTo(E1).synchCall(E2,3.5);
A2 = Activity(model, 'A2', Exp(2.0)).on(T2).boundTo(E2).repliesTo(E2);
```

Here, A1 is a task activity for T1, acts as initial activity for E1, consumes an exponential distributed time on the processor underpinning T1, and requires on average 3.5 synchronous calls to E2 to complete. Each call to entry E2 is served by the activity A2, with a service time on the processor underneath T2 given by an exponential distribution with rate  $\lambda=2.0$ .

At present, LINE 2.0.0-BETA1 supports only synchronous calls. Support for asynchronous calls is available in older versions, e.g. LINE 1.0.0. Extension of LINE 2.0.0-BETA1 to asynchronous calls

#### **Activity graphs**

Often, it is useful to structure the sequence of activities carried out by an entry in a graph. Currently, LINE supports this feature only for activities places in series. For example, we may replace the specification of the activities underpinning a call to E2 as

```
A20 = Activity(model, 'A20', Exp(1.0)).on(T2).boundTo(E2);
A21 = Activity(model, 'A21', Erlang.fitMeanAndOrder(1.0,2)).on(T2);
A22 = Activity(model, 'A22', Exp(1.0)).on(T2).repliesTo(E2);
T2.addPrecedence(ActivityPrecedence.Serial(A20, A21, A22));
```

such that a call to E2 serially executes A20, A21, and A22 prior to replying. Here, A21 is chosen to be an Erlang distribution with given mean (1.0) and number of phases (2).

#### 4.1.3 Debugging and visualization

The structure of a LayeredNetwork object can be graphically visualized as follows

```
plot(model)
```

An example of the result is shown in Figure 4.1. The figure shows two processors (P1 and P2), two tasks (T1 and T2), and three entries (E1, E2, and E3) with their associated activities. Both dependencies and calls are both shown as directed arcs, with the edge weight on call arcs corresponding to the average number of calls to the target entry. For example, A1 calls E3 on average 2.0 times. As in the case of the Network class, the getGraph method can be called to inspect the structure of the object.

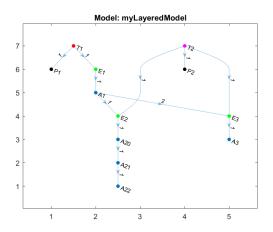


Figure 4.1: LayeredNetwork.plot method

### 4.2 Decomposition into layers

Layers are a form of decomposition where the influence of resources not explicitly represented in that layer is taken into account through an artificial delay station, placed in a closed loop to the resources [9]. This artificial delay is used to model the inter-arrival time between calls from resources that belong to other layers.

#### 4.2.1 Running a decomposition

The current version of LINE adopts SRVN-type layering [13], whereby a layer corresponds to one and only one resource, either a processor or a task. The only exception are reference tasks, which can only appear as clients to their processors. The <code>getLayers</code> method returns a cell array consisting of the <code>Network</code> objects corresponding to each layer

```
layers = model.getLayers()
```

Within each layer, classes are used to model the time a job spends in a given activity or call, with synchronous calls being modeled by classed with label including an arrow, e.g., 'AS1=>E3' is a closed class used represent synchronous calls from activity AS1 to entry E3. Artificial delays and reference nodes are modelled as a delay station named 'Clients', whereas the task or processor assigned to the layer is modelled as the other node in the layer.

#### 4.2.2 Initialization and update

In general, the parameters of a layer will depend on the steady-state solution of an other layer, causing a cyclic dependence that can be broken only after the model is analyzed by a solver. In order to assign parameters within each layer prior to its solution, the LayeredNetwork class uses the initDefault method, which sets the value of the artificial delay to simple operational analysis bounds [2].

The layer parameterization depends on a subset of performance indexes stored in a param structure array within the LayeredNetwork class. After initialization, it is possible to update the layer parameterization for example as follows

```
layers = model.getLayers();
for l=1:model.getNumberOfLayers()
    AvgTableByLayer{l} = SolverAMVA(layers{l}).getAvgTable;
end
model.updateParam(AvgTableByLayer);
model.refreshLayers;
```

Here, the refreshParam method updates the param structure array from a cell array of steady-state solutions for the Network objects in each layer. Subsequently, the refreshLayers method enacts the new parameterization across the Network objects in each layer.

### 4.3 Steady-state analysis

LINE offers two solvers for the solution of a LayeredNetwork model consisting in its own native solver (LN) and a wrapper (LQNS) to the LQNS solver [13]. The latter requires a distribution of LQNS to be available on the operating system command line.

The solution methods available for LayeredNetwork models are similar to those for Network objects. For example, the getAvgTable can be used to obtain a full set of mean performance indexes for the model, e.g.,

	е				
Node	NodeType	QLen	Util	RespT	Tput
'P1'	'Processor'	NaN	0.071429	NaN	NaN
'T1'	'Task'	0.28571	0.071429	NaN	0.071429
'E1'	'Entry'	0.28571	0.071429	4	0.071429
'A1'	'Activity'	0.28571	0.071429	4	0.071429
'P2'	'Processor'	NaN	0.21429	NaN	NaN
'T2'	'Task'	0.21429	0.21429	NaN	0.21429
'E2'	'Entry'	0.21429	0.21429	1	0.21429
'A2'	'Activity'	0.21429	0.21429	1	0.21429

Note that in the above table, some performance indexes are marked as NaN because they are not defined in a layered queueing network. Further, compared to the getAvgTable method in Network objects, LayeredNetwork do not have an explicit differentiation between stations and classes, since in a layer a task may either act as a server station or a client class.

The main challenge in solving layered queueing networks through analytical methods is that the parameterization of the artificial delays depends on the steady-state performance of the other layers, thus causing a cyclic dependence between input parameters and solutions across the layers. Depending on the solver in use, such issue can be addressed in a different way, but in general a decomposition into layers will remain parametric on a set of response times, throughputs and utilizations.

This issue can be resolved through solvers that, starting from an initial guess, cyclically analyze the layers and update their artificial delays on the basis of the results of these analyses. Both LN and LQNS implement this solution method. Normally, after a number of iterations the model converges to a steady-state solution, where the parameterization of the artificial delays does not change after additional iterations.

#### 4.3.1 SolverLQNS class

The LQNS wrapper operates by first transforming the specification into a valid LQNS XML file. Subsequently, LQNS calls the solver and parses the results from disks in order to present them to the user in the appropriate LINE tables or vectors. The options.method can be used to configure the LQNS execution as follows:

- options.method='std' or 'lqns': LQNS analytical solver with default settings.
- options.method='exact': the solver will execute the standard LQNS analytical solver with the exact MVA method.
- options.method='srvn': LQNS analytical solver with SRVN layering.
- options.method='srvnexact': the solver will execute the standard LQNS analytical solver with SRVN layering and the exact MVA method.
- options.method='lqsim': LQSIM simulator, with simulation length specified via the samples field (i.e., with parameter -A options.samples, 0.95).

Upon invocation, the lqns or lqsim commands will be searched for in the system path. If they are unavailable, the termination of SolverLQNS will interrupt.

#### 4.3.2 SolverLN class

The native LN solver iteratively applies the updates described in Section 4.2.2 until convergence of the steady-state measures. Since updates are parametric on the solution of each layer, LN can apply any of the Network solvers described in Chapter 3 to the analysis of individual layers, as illustrated in the following example for the AMVA solver

```
options = SolverLN.defaultOptions;
amvaopt = SolverAMVA.defaultOptions;
SolverLN(model, @(layer) SolverAMVA(layer, amvaopt), options).getAvgTable
```

Options parameters may also be omitted. The LN method converges when the maximum relative change of mean response times across layers from the last iteration is less than options.iter tol.

## 4.4 Model import and export

A LayeredNetwork can be easily read from, or written to, a XML file in the LQNS meta-model format. The read operation can be done using a static method of the LayeredNetwork class, i.e.,

```
model = LayeredNetwork.parseXML(filename)
```

Conversely, the write operation is invoked directly on the model object

```
model.writeXML(filename)
```

In both examples, filename is a string including both file name and its path.

## Chapter 5

## **Random environments**

Systems modeled with LINE can be described as operating in an environment whose state affects the way the system operates. The distinguish the states of the environment from the ones of the system within it, we shall refer to the former as the environment *stages*. In particular, LINE 2.0.0-BETA1 supports the definition of a class of random environments subject to three assumptions:

- The stage of the environment evolves independently of the state of the system.
- The dynamics of the environment stage can be described by a continuous-time Markov chain.
- The topology of the system is independent of the environment stage.

The above definitions are in particular appropriate to describe systems whose input parameters change with the environment stage. For example, an environment with two stages, normal load and peak load, may differ for the number of servers that are configured in a server station, i.e., the user may add servers during peak load. Upon a stage change in the environment, the model parameters will instantaneously change, but the state reached during the previous stage will be used to initialize the system in the new stage.

Although in a number of cases the system performance may be similar to a weighted combination of the average performance in each stage, this is not true in general, especially if the system dynamic (e.g., the rate at which jobs are served) and the environment dynamic happen at similar timescales [14].

## 5.1 Environment object definition

#### **5.1.1** Specifying the environment transitions

To specify an environment, it is sufficient to define a cell array with entries describing the distribution of time before the environment jumps to a given target state. For example

```
env{1,1} = Exp(0);
env{1,2} = Exp(1);
env{2,1} = Exp(1);
env{2,2} = Exp(0);
```

describes an environment consisting of two stage, where the time before a transition to the other stage is exponential with unit rate. If we were to set instead

```
env{2,2} = Erlang.fitMeanAndOrder(1,2);
```

this would cause a race condition between two distributions in stage two: the exponential transition back to stage 1, and the Erlang-2 distributed transition with unit rate that remains in stage 2. The latter means that periodically the system will be re-initialized in stage 2, meaning that jobs in execution at a server are required all to restart execution.

In LINE, an environment is internally described by a Markov renewal process (MRP) with transition times belonging to the MarkovianDistribution class. A MRP is similar to a Markov chain, but state transitions are not restricted to be exponential. Although the time spent in each state of the MRP is not exponential, the MRP can be easily transformed into an equivalent continuous-time Markov chain (CTMC) to enable analysis, a task that LINE performs automatically. In the example above, the underpinning CTMC will therefore consider the distribution of the minimum between the exponential and the Erlang-2 distribution, in order to decide the next stage transition.

State space explosion may occur in the definition of an environment if the user specifies a large number of non-exponential transition. For example, a race condition among n Erlang-2 distribution translates at the level of the CTMC into a state space with  $2^n$  states. In such situations, it is recommended to replace some of the distributions with exponential ones.

#### **5.1.2** Specifying the system models

LINE places loose assumptions in the way the system should be described in each stage. It is just expected that the user supplies a model object, either a Network or a LayeredNetwork, in each stage, and that a transient analysis method is available in the chosen solver, a requirement fulfilled for example by SolverFluid.

However, we note that the model definition can be somewhat simplified if the user describes the system model in a separate MATLAB function, accepting the stage-specific parameters in input to the function. This enables reuse of the system topology across stages, while creating independent model objects. An example of this specification style is given in <code>example\_randomEnvironment\_1.m</code> under LINE's example folder.

## 5.2 Steady-state analysis

The analysis of a system in a random environment is carried out in LINE using the blending method [14], which is an iterative algorithm leveraging the transient solution of the model. In essence, the model looks at the *average* state of the system at the instant of each stage transition, and upon restarting the system in the new stage re-initializes it from this average value. This algorithm is implemented in LINE by the SolverEnv class, which is described next.

#### 5.2.1 SolverEnv class

The SolverEnv class applies the blending algorithm by iteratively carrying out a transient analysis of each system model in each environment stage, and probabilistically weighting the solution to extract the steady-state behavior of the system.

As in the transient analysis of Network objects, LINE does not supply a method to obtain mean response times, since Little's law does not hold in the transient regime. To obtain the mean queuelength, utilization and throughput of the system one can call as usual the getAvg method on the SolverEnv object, e.g.,

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models = {model1, model2, model3, model4};

```
envSolver = SolverEnv(models, env, @SolverFluid,options);
[QN,UN,TN] = envSolver.getAvg()
```

Note that as model complexity grows, the number of iterations required by the blending algorithm to converge may grow large. In such cases, the  $options.iter_max$  option may be used to bound the maximum analysis time.

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# Appendix A

# **Examples**

In this appendix, we summarize the features exercised in the LINE scripts under the examples folder.

Table A.1: Examples

Example	Problem
example_cdfRespT_1	Station response time distribution in a single-class single-job closed network
example_cdfRespT_2	Station response time distribution in a multi-chain network
example_cdfRespT_3	Station response time distribution under increasing job populations
example_cdfRespT_4	Simulation-based station response time distribution analysis
example_closedModel_1	Solving a single-class exponential closed queueing network
example_closedModel_2	Solving a closed queueing network with a multi-class FCFS station
example_closedModel_3	Solving exactly a multi-chain product-form closed queueing network
example_closedModel_4	Local state space generation for a station in a closed network
example_closedModel_5	1-line solution of a cyclic network of PS and INF stations
example_feasibility_1	Automatic detection of solvers that cannot analyze the model
example_initState_1	Specifying an initial state using prior probabilities.
example_initState_2	
example_initState_3	
example_layeredModel_1	Analyze a layered network specified in a LQNS XML file
example_layeredModel_2	Specifying and solving a basic layered network
example_layeredModel_3	
example_layeredModel_4	
example_mixedModel_1	Solving a queueing network model with both closed and open classes
example_openModel_1	Solving a queueing network model with open classes
example_openModel_2	Compactly specifying a tandem network of PS and INF stations
example_randomEnvironment_1	Solving a model in a 2-stage random environment
example_randomEnvironment_2	Solving a model in a 4-stage random environment
example_stateProbabilities_1	Computing marginal state probabilities
example_stateProbabilities_2	Computing marginal state probabilities
example_syntax_1	Use of performance indexes handles
example_syntax_2	Update and refresh of service times
example_scheduling_1	Parameterization of a discriminatory processor sharing (DPS) station