

# Prior distribution study

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## Set up

Seed = 2021;

The number of sampling times is 1000;

## Parameters

Prior distribution  $\theta \sim \text{Beta}(\alpha, \beta)$ ,  $Y \sim \text{Bin}(100, \theta)$ ;

### Scenario 1:

$\alpha = 1, \beta = 1$

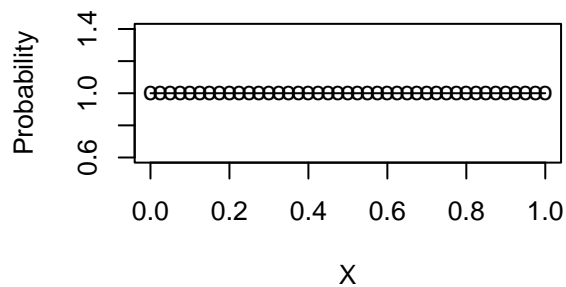
- Mean and Variance of Beta(1,1)

```
## [1] "mean = 0.5"
```

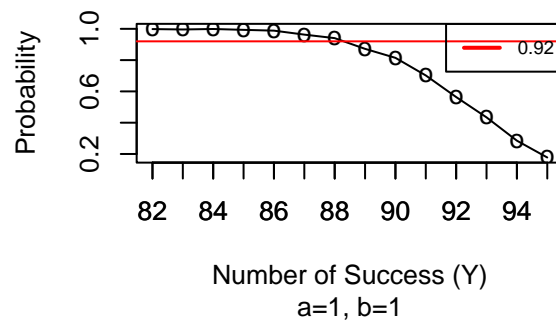
```
## [1] "variance = 0.0833333333333333"
```

- Posterior plot for number of success from 82 to 95

**Pdf of Beta(1,1)**



**Posterior distribution of theta**



- Threshold value

```
## [1] "P|Y=88: 0.9405"
```

```
## [1] "P|Y=89: 0.872"
```

### Scenario 2:

$\alpha = 0.9, \beta = 0.1$

- Mean and Variance of Beta(0.9,0.1)

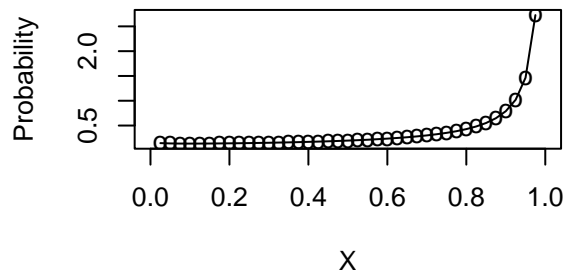
```
## [1] "mean = 0.9"
```

```
## [1] "variance = 0.045"
```

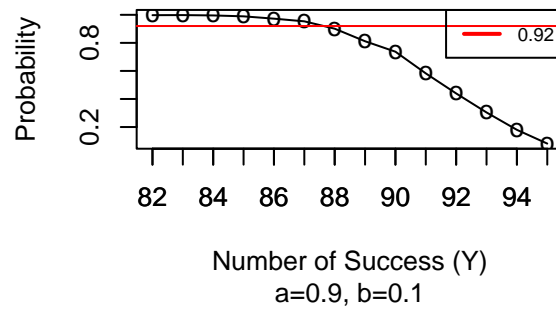
Mean is 0.9, and variance is relatively high.

- Posterior plot for number of success from 82 to 95

**Pdf of Beta(0.9,0.1)**



**Posterior distribution of theta**



- Threshold value

```
## [1] "P|Y=87: 0.9535"
```

```
## [1] "P|Y=88: 0.901"
```

### Scenario 3:

$\alpha = 9, \beta = 1$

- Mean and Variance of Beta(9,1)

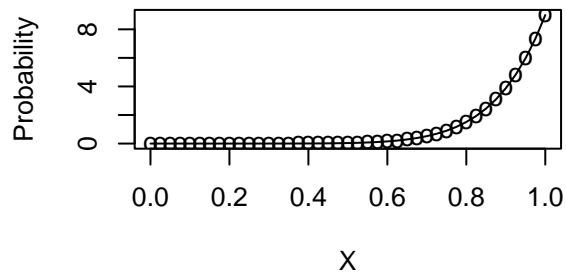
```
## [1] "mean = 0.9"
```

```
## [1] "variance = 0.00818181818181818"
```

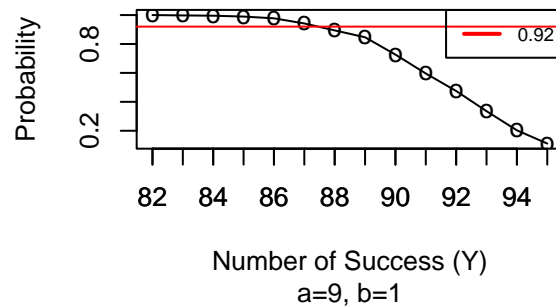
Mean is 0.9, and variance is relatively medium.

- Posterior plot for number of success from 82 to 95

**Pdf of Beta(9,1)**



**Posterior distribution of theta**



- Threshold value

```
## [1] "P|Y=87: 0.942"
```

```
## [1] "P|Y=88: 0.894"
```

#### Scenario 4:

$$\alpha = 90, \beta = 10$$

- Mean and Variance of Beta(90,10)

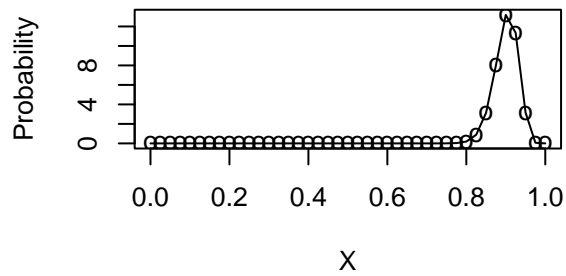
```
## [1] "mean = 0.9"
```

```
## [1] "variance = 0.000891089108910891"
```

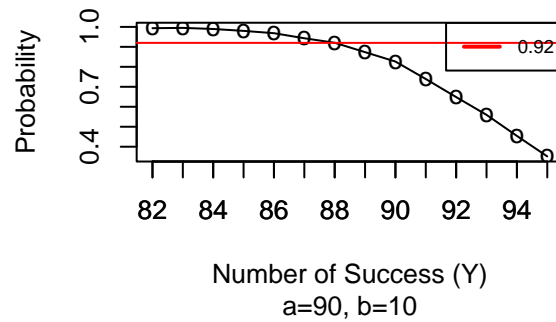
Mean is 0.9, and variance is way lower.

- Posterior plot for number of success from 82 to 95

**Pdf of Beta(90,10)**



**Posterior distribution of theta**



- Threshold value

```
## [1] "P|Y=88: 0.9205"
```

```
## [1] "P|Y=89: 0.8735"
```