

# A predictive probability design for phase II cancer clinical trials

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**Background** Two- or three-stage designs are commonly used in phase II cancer clinical trials. These designs possess good frequentist properties and allow early termination of the trial when the interim data indicate that the experimental regimen is inefficacious. The rigid study design, however, can be difficult to follow exactly because the response has to be evaluated at prespecified fixed number of patients.

**Purpose** Our goal is to develop an efficient and flexible design that possesses desirable statistical properties.

**Methods** A flexible design based on Bayesian predictive probability and the minimax criterion is constructed. A three-dimensional search algorithm is implemented to determine the design parameters.

**Results** The new design controls type I and type II error rates, and allows continuous monitoring of the trial outcome. Consequently, under the null hypothesis when the experimental treatment is not efficacious, the design is more efficient in stopping the trial earlier, which results in a smaller expected sample size. Exact computation and simulation studies demonstrate that the predictive probability design possesses good operating characteristics.

**Limitations** The predictive probability design is more computationally intensive than two- or three-stage designs. Similar to all designs with early stopping due to futility, the resulting estimate of treatment efficacy may be biased.

**Conclusions** The predictive probability design is efficient and remains robust in controlling type I and type II error rates when the trial conduct deviates from the original design. It is more adaptable than traditional multi-stage designs in evaluating the study outcome, hence, it is easier to implement. S-PLUS/R programs are provided to assist the study design. *Clinical Trials* 2008; 5: 93–106. <http://ctj.sagepub.com>

## Introduction

Phase II studies play a pivotal role in drug development. The main purpose for phase II clinical trials is to determine whether a new treatment demonstrates sufficient efficacy to warrant further investigation. It helps to screen out inefficacious agents and avoid sending them to large phase III trials. [1,2] A commonly used primary endpoint in phase II cancer clinical trials is the clinical response to a treatment, which is a binary endpoint defined as the patient achieving complete or partial response within a predefined

treatment course. In the early phase II development of new drugs, most trials are open label, single-arm studies, while late phase II trials tend to be multi-arm, randomized studies. Overviews of statistical methods for phase II trials can be found in the work of Thall and Simon [3], Kramar *et al.* [4], Mariani and Marubini [5], and Lee and Feng [6].

In this paper, we focus on the one arm phase II trials with binary endpoints. Multi-stage designs are often implemented in such settings to increase the study efficiency by allowing early termination if the treatment is deemed inefficacious. The first phase II design proposed for cancer research is a two-stage

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procedure by Gehan [7]. With that design, if no responses are observed in the first stage, the new treatment is abandoned. Otherwise, additional patients are enrolled in the second stage to provide a better estimation of the response rate. The commonly used Simon's designs [8] are also two-stage designs. Simon's designs allow early stopping due to futility, i.e., when lack of efficacy is observed. If the experimental treatment works well, more patients are treated in the second stage, which also allows better estimation of the response rate and toxicity of the new treatment, before launching a phase III trial. Under the null hypothesis, the optimal two-stage design minimizes the expected sample size, while the minimax design minimizes the maximum sample size. Both designs are subject to the constraints of type I and type II error rates. Many other multi-stage designs with different objectives and optimization criteria can be found in the literature [9–12]. Jung *et al.* [13] devised a graphical method for searching all design parameters to attain certain admissible two-stage designs with good design characteristics. They later generalized the method and identified a family of admissible designs using a Bayesian decision-theoretic criterion [14].

Multi-stage designs possess better statistical properties than single-stage designs by utilizing the information gained in the interim data. Furthermore, three-stage designs are generally more efficient than two-stage designs because the additional interim look at the data allows for earlier decision to stop the trial if convincing evidence to support the null or alternative hypothesis is found. These designs, however, are more difficult to conduct because of the rigid requirement of examining the outcome at the specified sample size in each fixed stage. The strict sample size guideline in each stage is particularly difficult to adhere to in multi-center trials due to the complexity of coordinating patient accrual and follow-up across multiple sites. Temporarily halting the study accrual can also stall the momentum of the trial and lower the enthusiasm for investigators to participate in the trial. In addition, when the actual conduct deviates from the original design, the stopping boundaries are left undefined and the planned statistical properties no longer hold. Many authors have recognized this problem and have offered solutions. Green and Dahlberg [15] examined the performance of planned versus attained designs and gave an empirical solution by adapting the stopping rules to achieve desirable statistical properties when the actual sample size deviates from the planned one. Herndon proposed a hybrid design by blending the one-stage and two-stage designs, which allows uninterrupted accrual between the stages [16]. Chen and Ng [17] gave

a collection of two-stage designs with a range of sample sizes in the first and second stages to construct optimal flexible designs.

Another limitation of the fixed design is that even after an extra long series of failures is observed, there is no formal mechanism to stop the trial before the predetermined sample size is reached. Furthermore, investigators often need to decide whether to continue or to terminate a trial at certain interim points, not always at the time points initially planned, due to slow accrual or other practical considerations [18]. This lack of design flexibility exposes a fundamental limitation of all frequentist-based methods because statistical inference is made by computing the probability of observing certain data conditioned on a particular design and the sampling plan. When there is a disparity between the proposed design and the actual trial conduct, which is more a norm than an exception in clinical trials, adjustments must be made in all statistical inferences. All these reasons support the need for more flexible designs.

Bayesian methods, on the other hand, offer a different approach for designing and monitoring clinical trials by computing the probability of parameters given data. Based on the likelihood principle, all information pertinent to the parameters is contained in the data and is not constrained by the design. Bayesian methods are particularly appealing in clinical trial design because, inherently, they allow for flexibility in trial conduct and impart the ability to examine interim data, update the posterior probability of parameters, and make sensible decisions accordingly. Bayesian methods can also incorporate relevant information, both internal and external to the trial, for decision making [19,20]. Several Bayesian phase II designs have been proposed in the literature. Sylvester proposed a decision theoretical approach by minimizing the expected loss to determine an optimal Bayesian design [21]. Thall and Simon developed a design with continuous monitoring until achieving a high posterior probability that either a drug is promising or not promising, or until reaching the maximum sample size [22,23]. Also based on the posterior probability, Heitjan [24] advocated the use of 'persuasion probability' as a consistent criterion for determining whether the drug is promising or not. Tan and Machin [25] constructed Bayesian two-stage designs, which mimic the frequentist alternatives, by calibrating design parameters based on the posterior probability approach. Similar approaches based on informative priors or mixtures of informative priors have also been reported [26,27].

Applying the concept of predictive probability, we take the proper Bayesian approach in the sense that we apply the full likelihood approach, but

without specifying the loss function, as in the decision theoretical approach. Hence, we do not compute the Bayes risk [28]. One advantage of the predictive probability approach is that it closely mimics the clinical decision making process. Predictive probability is obtained by calculating the probability of a positive conclusion (rejecting the null hypothesis) should the trial be conducted to the maximum planned sample size given the interim observed data. In this framework, the chance that the trial will show a conclusive result at the end of the study, given the current information, is evaluated. Then, the decision to continue or to stop the trial can be made according to the strength of the predictive probability. Several adaptations of predictive probability approaches for interim monitoring of clinical trials have been discussed [29–31, 32–34, 35–39]. Notably, Choi *et al.* [29] calculated predictive probability in making an early decision in a large sample two-arm trial where the outcome is the proportion of successes, using normal approximation under a large sample assumption. Spiegelhalter *et al.* [31] suggested that the predictive power, derived by averaging the conditional power based on current data over the current belief about the unknown parameters, should be used to detect significant differences between treatments. As for trial design, Herson [36] first proposed the predictive probability approach for designing phase II clinical trials with dichotomous outcomes. The proposed maximum sample size and critical region are originated from a frequentist one-stage design. The choice of the cutoff values for the predictive probability is somewhat arbitrary and does not guarantee the type I and type II error rates.

Under the predictive probability framework, our approach searches for the design parameters within the given constraints such that both the size and power of the test can be guaranteed. In the section ‘Methods for Simon’s two-stage design and predictive probability design’, we give an overview of Simon’s two-stage design and define the proposed predictive probability approach in a Bayesian setting. Exact computation and a searching procedure have been developed to facilitate the predictive probability design. In section ‘Comparison between predictive probability approach and Simon’s two-stage design’, we investigate the property of the predictive probability approach and compare its performance with Simon’s two-stage design through several examples. In ‘Properties of the predictive probability approach’, section we describe the simulation studies for evaluating the robustness of the design when trial conduct deviates from the originally proposed design and when the trial is stopped prematurely. The estimation bias and the comparison between

the predictive probability versus the posterior probability approaches are also given. We provide a discussion in the final section.

## Methods for Simon’s two-stage design and predictive probability design

Under the hypothesis testing framework, a phase IIA clinical trial is designed to test

$$H_0: p \leq p_0$$

$$H_1: p \geq p_1$$

where  $p_0$  represents a prespecified response rate of the standard treatment and  $p_1$  represents a target response rate of a new treatment. A study is designed such that

$$P(\text{Accept New Treatment} | H_0) \leq \alpha$$

$$\text{and } P(\text{Reject New Treatment} | H_1) \leq \beta$$

where  $\alpha$  and  $\beta$  are type I and type II error rates, respectively. Given  $p_0, p_1$ , the maximum number of patients, number of stages, cohort size at each stage, acceptance region and rejection region at each stage, the type I and type II error rates, the probability of early termination (PET) of the trial and the expected sample size ( $E(N)$ ) under  $H_0$  can be calculated by applying the recursive formulas of Schultz *et al.* [38]. A desirable design is one with operating characteristics that satisfy the constraints of the type I and type II error rates, with a high probability of early termination and a small expected sample size under  $H_0$ . Note that we define the acceptance region as the outcome space leading to the acceptance of the new treatment (i.e., reject the null hypothesis) and, the rejection region as the outcome space leading to the rejection of the agent (i.e., fail to reject the null hypothesis).

### Simon’s two-stage designs

The algorithm for implementing Simon’s two-stage designs is as follows:

Stage I: Enroll  $n_1$  patients. Stop the trial and reject the new treatment (stop for futility) if the number of observed responses,  $x_1$ , is  $r_1$  or less. Otherwise, continue to stage II.

Stage II: Enroll  $(N_{\max} - n_1)$  patients to reach a total of  $N_{\max}$  patients. Reject the new treatment if the number of responses is  $r$  or less. Otherwise, consider that the new treatment warrants further development.

Based on these decision rules, PET and  $E(N)$  under  $H_0$  can be calculated:

$PET(p_0) = \text{Prob}(\text{Early Termination} | H_0) = \text{Prob}(X_1 \leq r_1 | H_0)$ , where  $X_1$  is the number of responses in  $n_1$  ( $n_1 < N_{\max}$ ) patients from the first stage, and  $X_1$  follows a binomial distribution with  $X_1 \sim \text{binomial}(n_1, p_0)$ ,

$$E(N | p_0) = n_1 + [1 - PET(p_0)] \times (N_{\max} - n_1).$$

Among all designs that satisfy the constraint of the type I and type II error rates, Simon's optimal two-stage design is obtained when  $E(N | p_0)$  is the smallest. On the other hand, the minimax design is defined when the maximum sample size is the smallest.

### Predictive probability approach in a Bayesian setting

In the Bayesian approach, we assume that the prior distribution of the response rate  $\pi(p)$  follows a beta distribution,  $\text{beta}(a_0, b_0)$ . It represents the investigator's previous knowledge or belief of the efficacy of the new regimen. The quantity  $a_0/(a_0 + b_0)$  reflects the prior mean while size of  $a_0 + b_0$  indicates how informative the prior is. The quantities  $a_0$  and  $b_0$  can be considered as the number of response and the number of nonresponses, respectively. Thus,  $a_0 + b_0$  can be considered as a measure of the amount of information contained in the prior. The larger the value of  $a_0 + b_0$ , the more informative the prior and the stronger the belief it contains. We set a maximum accrual of patients to  $N_{\max}$ . We assume the number of responses in the current  $n$  ( $n \leq N_{\max}$ ) patients,  $X$ , follows a binomial distribution,  $\text{binomial}(n, p)$ , and the likelihood function for the observed data  $x$  is

$$L_x(p) \propto p^x \times (1 - p)^{n-x}.$$

Consequently, the posterior distribution of the response rate follows a beta distribution

$$P|x \sim \text{beta}(a_0 + x, b_0 + n - x).$$

Thus, the number of responses in the potential  $m = N_{\max} - n$  future patients,  $Y$ , follows a beta-binomial distribution,  $\text{beta-binomial}(m, a_0 + x, b_0 + n - x)$ .

When  $Y = i$ , we denote the posterior probability of  $P$  as  $f(p | X = x, Y = i)$ , where  $P | X = x, Y = i \sim \text{beta}(a_0 + x + i, b_0 + N_{\max} - x - i)$ .

From here on, the observed response  $X = x$  will be abbreviated as  $x$ . To calculate the predictive probability, we further define

$$B_i = \text{Prob}(P > p_0 | x, Y = i),$$

where  $P$  follows a beta distribution.  $B_i$  measures the probability that the response rate is larger than  $p_0$  given  $x$  responses in  $n$  patients in the current data and  $i$  responses in  $m$  future patients. Comparing  $B_i$  to a threshold value  $\theta_T$  yields an indicator  $I_i$  for considering that the treatment is efficacious at the end of the trial given the current data and the potential outcome of  $Y = i$  (see Table 1, Panel A for a schematic representation).

We define

### Predictive Probability (PP)

$$\begin{aligned} &= \sum_{i=0}^m \{ \text{Prob}(Y = i | x) \\ &\quad \times I(\text{Prob}(P > p_0 | x, Y = i) > \theta_T) \} \\ &= \sum_{i=0}^m \{ \text{Prob}(Y = i | x) \times I(B_i > \theta_T) \} \\ &= \sum_{i=0}^m \{ \text{Prob}(Y = i | x) \times I_i \} \end{aligned}$$

where  $\text{Prob}(Y = i | x)$  is the probability of observing  $i$  responses in  $m$  patients given current data  $x$ , where  $Y$  follows a beta-binomial distribution. The weighted sum of indicator  $I_i$  over  $Y$  yields the predictive probability (PP) of concluding a positive result by the end of the trial based on the cumulative information in the current stage. A high PP means that the treatment is likely to be efficacious by the end of the study, given the current data, whereas a low PP suggests that the treatment may not have sufficient activity. Therefore, PP can be used to determine whether the trial should be stopped early due to efficacy/futility or continued because the current data are not yet conclusive. The decision rules can be constructed as follows:

If  $PP < \theta_L$ , then stop the trial and reject the alternative hypothesis;

If  $PP > \theta_U$ , then stop the trial and reject the null hypothesis;

Otherwise continue to the next stage until reaching  $N_{\max}$  patients.

Typically, we choose  $\theta_L$  as a small positive number and  $\theta_U$  as a large positive constant, both between 0 and 1 (inclusive).  $PP < \theta_L$  indicates that it is unlikely the response rate will be larger than  $p_0$  at the end of the trial given the current information. When this happens, we may as well stop the trial and reject the alternative hypothesis at that point. On the other hand, when  $PP > \theta_U$ , the current data suggest that, if the same trend continues, we will have a high probability to conclude that the treatment is efficacious at the end of the study. This result, then, provides evidence to stop the trial early due to efficacy. By choosing  $\theta_L > 0$  and

**Table 1** Bayesian predictive probability approach: a schema and an example

Panel A: Schema			
$Y=i$	$\text{Prob}(Y=i x)$	$B_i = \text{Prob}(P > p_0   x, Y=i)$	$I_i(B_i > \theta_T)$
0	$\text{Prob}(Y=0 x)$	$B_0 = \text{Prob}(P > p_0   p, f(p x, Y=0))$	0
1	$\text{Prob}(Y=1 x)$	$B_1 = \text{Prob}(P > p_0   p, f(p x, Y=1))$	0
...	...	...	...
$m-1$	$\text{Prob}(Y=m-1 x)$	$B_{m-1} = \text{Prob}(P > p_0   p, f(p x, Y=m-1))$	1
$m$	$\text{Prob}(Y=m x)$	$B_m = \text{Prob}(P > p_0   p, f(p x, Y=m))$	1
Panel B: Example: $N_{\max} = 40$ , $x = 16$ , $n = 23$ , prior distribution of $P \sim \text{beta}(0.6, 0.4)$			
$Y=i$	$\text{Prob}(Y=i x)$	$B_i = \text{Prob}(P > 60\%   x, Y=i)$	$I_i(B_i > 0.90)$
0	0.0000	0.0059	0
1	0.0000	0.0138	0
2	0.0001	0.0296	0
3	0.0006	0.0581	0
4	0.0021	0.1049	0
5	0.0058	0.1743	0
6	0.0135	0.2679	0
7	0.0276	0.3822	0
8	0.0497	0.5085	0
9	0.0794	0.6349	0
10	0.1129	0.7489	0
11	0.1426	0.8415	0
12	0.1587	0.9089	1
13	0.1532	0.9528	1
14	0.1246	0.9781	1
15	0.0811	0.9910	1
16	0.0381	0.9968	1
17	0.0099	0.9990	1

$\theta_U < 1.0$ , the trial can terminate early due to either futility or efficacy. For phase IIA trials, we prefer to choose  $\theta_L > 0$  and  $\theta_U = 1.0$  to allow early stopping due to futility, but not due to efficacy.

For example (Table 1, Panel B), in a phase II trial, an investigator plans to enroll a maximum of  $N_{\max} = 40$  patients into the study. At a given time,  $x = 16$  responses are observed in  $n = 23$  patients. What is  $P(\text{response rate} > 60\%)$ ? Assuming a prior distribution of response rate ( $p$ ) as  $\text{beta}(0.6, 0.4)$  and with the number of responses in future  $m = 17$  patients,  $Y$  follows a beta-binomial distribution,  $\text{beta-binomial}(17, 16.6, 7.4)$ . At each possible value of  $Y = i$ , the posterior probability of  $P$  follows a beta distribution,  $P|x, Y=i \sim \text{beta}(16.6 + i, 24.4 - i)$ . In this example, we set  $\theta_T = 0.90$ . As it can be seen, when  $Y$  is in the range from 0 to 11, the resulting  $P(\text{response rate} > 60\%)$  ranges from 0.0059 to 0.8415. Hence, we will conclude  $H_0$  for  $Y \leq 11$ . On the other hand, when  $Y$  goes from 12 to 17, the resulting  $P(\text{response rate} > 60\%)$  ranges from 0.9089 to 0.9990. Therefore, we will conclude  $H_1$  for  $Y \geq 12$ . The predictive probability is then the weighted average (weighted by the probability of the realization of each  $Y$ ) of the indicator of a positive trial should the current trend continue and the trial

be conducted until the end of the study. The calculation yields  $PP = 0.5656$ . If we choose  $\theta_L = 0.10$ , the trial will not be stopped because  $PP$  is greater than  $\theta_L$ .

#### Designing a trial using the PP approach: Search $N_{\max}$ , $\theta_L$ , $\theta_T$ , and $\theta_U$ for the PP design to satisfy the constraints of the type I and type II error rates

Given  $p_0, p_1$ , the prior distribution of response rate  $\pi(p)$  and the cohort size for interim monitoring, we search the design parameters, including the maximum sample size  $N_{\max}$ ,  $\theta_L$ ,  $\theta_T$ , and  $\theta_U$ , to yield a design satisfying the type I and type II error rates constraints simultaneously. As mentioned earlier, we choose  $\theta_U = 1.0$  because if the treatment is working, there is little reason to stop the trial early – enrolling more patients to the active treatment is good. Treating more patients until the maximum sample size is reached (usually, less than 100) can also increase the precision in estimating the response rate. Given  $N_{\max}$ , the question is, ‘Are there values of  $\theta_L$  and  $\theta_T$  that yield desirable design properties?’ By searching over all possible values of



$\theta_L$  and  $\theta_T$ , our goal is to identify the combinations of  $\theta_L$  and  $\theta_T$  to yield the desirable power within the constraint of the specified type I error rates. There may exist ranges of  $\theta_L$  and  $\theta_T$  that satisfy the constraints. By varying  $N_{\max}$  from small to large, the design with the smallest  $N_{\max}$  that controls both type I and type II error rates at the nominal level is the one we choose. This idea is similar to finding the minimax design, i.e., minimizing the maximum sample size.

The framework of this PP method allows the investigator to monitor the trial continuously or by any cohort size. We choose to start computing PP and making interim decisions after the first 10 patients have been treated and evaluated for their response status. Although the choice of treating a minimum of 10 patients is somewhat arbitrary, a minimum number of patients is required to provide sufficient information in order to obtain a good estimate of the treatment efficacy and avoid making premature decisions based on spurious results from a small number of patients. After 10 patients, we calculate PP continuously (i.e., with cohort size of 1) to monitor the treatment efficacy. If PP is low, the data indicate that the treatment may not be efficacious. A sufficiently low PP (e.g.,  $PP < \theta_L$ ) suggests that the trial could be stopped early due to lack of efficacy. Note that PP can be computed for any cohort size and at any interim time. A trial can be stopped anytime due to excessive toxicity, however.

### Comparison between predictive probability approach and Simon's two-stage design

The comparison between the PP design and Simon's two-stage design is performed by examining the design's operating characteristics, such as the type I error rate, power,  $PET(p_0)$  and  $E(N|p_0)$ . The concept of designing trials using the PP approach is illustrated in the following examples.

#### Example 1: A lung cancer trial

The primary objective of this study is to assess the efficacy of a combination therapy as front-line treatment in patients with advanced nonsmall cell lung cancer. The study involves the combination of a vascular endothelial growth factor antibody plus an epidermal growth factor receptor tyrosine kinase inhibitor. The primary endpoint is the clinical response rate (i.e., rate of complete response and partial response combined) to the new regimen.

The current standard treatment yields a response rate of approximately 20% ( $p_0$ ). The target response rate of the new regimen is 40% ( $p_1$ ). With the constraint of both type I and type II error rates  $\leq 0.1$ , Simon's optimal two-stage design yields  $n_1 = 17$ ,  $r_1 = 3$ ,  $N_{\max} = 37$ ,  $r = 10$ ,  $PET(p_0) = 0.55$  and  $E(N|p_0) = 26.02$  with  $\alpha = 0.095$  and  $\beta = 0.097$ . The corresponding minimax design yields  $n_1 = 19$ ,  $r_1 = 3$ ,  $N_{\max} = 36$ ,  $r = 10$ ,  $PET(p_0) = 0.46$  and  $E(N|p_0) = 28.26$  with  $\alpha = 0.086$  and  $\beta = 0.098$ .

Taking the PP approach, we assume that the response rate  $P$  has a prior distribution of  $\text{beta}(0.2, 0.8)$ . The trial is monitored continuously after evaluating the responses of the first 10 patients. For each  $N_{\max}$  between 25 and 50, we search the  $\theta_L$  and  $\theta_T$  space to generate designs that have both type I and type II error rates under 0.10. listed in Table 2 are some of the results in the order of the maximum sample size,  $N_{\max}$ . Among all the designs, the design with  $N_{\max} = 36$  (boldfaced type) is the design with the smallest  $N_{\max}$  that has both type I and type II error rates controlled under 0.1.

Based on this setting,  $\theta_L$  and  $\theta_T$  are determined to be 0.001 and [0.852, 0.922], respectively. The corresponding rejection region (in number of response/ $n$ ) is 0/10, 1/17, 2/21, 3/24, 4/27, 5/29, 6/31, 7/33, 8/34, 9/35, and 10/36. The trial will be stopped and the treatment is considered ineffective when the number of responses first falls into the rejection region. Based on these boundaries, if the true response rate is 20%, the probability of accepting the treatment is 0.088. On the other hand, if the true response rate is 40%, the probability of accepting the treatment is 0.906. The probability of stopping the trial early is 0.86 and the expected sample size is 27.67 when the true response rate is 20%. Compared to Simon's minimax two-stage design, the trial is monitored more frequently in the PP design, which also has a larger probability of early termination and a smaller expected sample size in the null case. Both designs have the same maximum sample size with controlled type I and type II error rates.

#### Example 2: A tongue cancer trial

The primary objective of a second study is to assess the efficacy of induction chemotherapy (with paclitaxel, ifosfamide, and carboplatin) followed by radiation in treating young patients with prior untreated squamous cell carcinoma of the tongue. Previous results show that radiation alone gives a response rate of 60% ( $p_0$ ). With induction chemotherapy plus radiation, the target response rate is set at 80% ( $p_1$ ). Under the constraint of a type I error rate  $\leq 0.05$  and a type II error rate  $\leq 0.20$ ,

**Table 2** Operating characteristics of Simon's two-stage designs and the PP design with type I and type II error rates  $\leq 0.10$ , prior for  $p = \text{beta}(0.2, 0.8)$ ,  $p_0 = 0.2$ ,  $p_1 = 0.4$ 

Simon's minimax/optimal 2-stage						
	$r_1/n_1$	$r/N_{\max}$	PET ( $p_0$ )	$E(N p_0)$	$\alpha$	$\beta$
Minimax	3/19	10/36	0.46	28.26	0.086	0.098
Optimal	3/17	10/37	0.55	26.02	0.095	0.097
Predictive probability						
$\theta_L$	$\theta_T$	$r/N_{\max}$	PET ( $p_0$ )	$E(N p_0)$	$\alpha$	$\beta$
<b>0.001</b>	<b>[0.852, 0.922]*</b>	<b>10/36</b>	<b>0.86</b>	<b>27.67</b>	<b>0.088</b>	<b>0.094</b>
0.011	[0.830, 0.908]	10/37	0.85	25.13	0.099	0.084
0.001	[0.876, 0.935]	11/39	0.88	29.24	0.073	0.092
0.001	[0.857, 0.923]	11/40	0.86	30.23	0.086	0.075
0.003	[0.837, 0.910]	11/41	0.85	30.27	0.100	0.062
0.043	[0.816, 0.895]	11/42	0.86	23.56	0.099	0.083
0.001	[0.880, 0.935]	12/43	0.88	32.13	0.072	0.074
0.001	[0.862, 0.924]	12/44	0.87	33.71	0.085	0.059
0.001	[0.844, 0.912]	12/45	0.85	34.69	0.098	0.048
0.032	[0.824, 0.898]	12/46	0.86	26.22	0.098	0.068
0.001	[0.884, 0.936]	13/47	0.89	35.25	0.071	0.058
0.001	[0.868, 0.925]	13/48	0.87	36.43	0.083	0.047
0.001	[0.850, 0.914]	13/49	0.86	37.86	0.095	0.038
0.020	[0.832, 0.901]	13/50	0.86	30.60	0.100	0.046

\*The numbers within the bracket indicate a closed interval with both endpoints included. This applies to all intervals shown in the table.

Simon's optimal two-stage design yields  $n_1 = 11$ ,  $r_1 = 7$ ,  $N_{\max} = 43$ ,  $r = 30$ ,  $\text{PET}(p_0) = 0.70$ , and  $E(N|p_0) = 20.48$  with  $\alpha = 0.049$ ,  $\beta = 0.198$ . The corresponding minimax design yields  $n_1 = 13$ ,  $r_1 = 8$ ,  $N_{\max} = 35$ ,  $r = 25$ ,  $\text{PET}(p_0) = 0.65$ , and  $E(N|p_0) = 20.77$  with  $\alpha = 0.050$  and  $\beta = 0.192$ .

Taking the PP approach, we search the design parameters with a maximum number of patients ranging between 25 and 44, assuming the prior distribution of the response rate as  $\text{beta}(0.6, 0.4)$ , and using continuous monitoring after the first 10 patients are evaluated. Table 3 lists the resulting designs. We find that the design with the smallest  $N_{\max}$  that has desirable type I and II error rates is the one with  $N_{\max} = 35$  (shown in boldface type in Table 3), where  $\theta_L$  and  $\theta_T$  are in the ranges of  $[0.075, 0.079]$  and  $[0.924, 0.963]$ , respectively. In this design, if the true response rate is 60%, the probability of accepting the treatment is 0.050, the probability of early termination of the trial is 0.94 and the expected sample size is 16.87. On the other hand, if the true response rate is 80%, the probability of accepting the treatment is 0.815. Again, compared to Simon's designs, the trial is monitored more frequently applying the PP approach and has a higher probability of early stopping with a smaller expected sample size, if the

regimen is not efficacious. In this example, the maximum number of patients under the PP approach is also the same as that under Simon's minimax two-stage design.

### More examples

Operating characteristics of more examples using Simon's minimax and optimal two-stage designs, and the PP design are shown in Table 4, with  $p_0 = 0.1$  to 0.7 by 0.1 intervals,  $p_1 - p_0 = 0.2$ , type I and type II error rates of 0.10, and continuous monitoring after the first 10 evaluable patients in the PP design. While the type I and type II error rates are controlled in both PP and Simon's two-stage designs, the probability of stopping the trial early is always larger in the PP design. In addition, we find that the PP design has a smaller expected sample size under the null hypothesis in all cases except when  $p_0 = 0.1$  and  $p_1 = 0.3$ . Compared to multi-stage designs, PP designs are also more flexible to conduct and have more robust design properties when the trial conduct does not follow the plan exactly. This topic is described in greater detail in the next section.

**Table 3** Operating characteristics of Simon's two-stage designs and the PP design with type I error rate  $\leq 0.05$  and type II error rate  $\leq 0.20$ , prior for  $p = \text{beta}(0.6, 0.4)$ ,  $p_0 = 0.6$ ,  $p_1 = 0.8$ 

Simon's minimax/optimal 2-stage						
	$r_1/n_1$	$r/N_{\max}$	PET( $p_0$ )	$E(N p_0)$	$\alpha$	$\beta$
Minimax	8/13	25/35	0.65	20.77	0.050	0.192
Optimal	7/11	30/43	0.70	20.48	0.049	0.198
Predictive probability						
$\theta_L$	$\theta_T$	$r/N_{\max}$	PET( $p_0$ )	$E(N p_0)$	$\alpha$	$\beta$
<b>[0.075, 0.079]*</b>	<b>[0.924, 0.963]</b>	<b>25/35</b>	<b>0.94</b>	<b>16.87</b>	<b>0.050</b>	<b>0.1855</b>
0.001	[0.940, 0.972]	26/36	0.94	23.16	0.045	0.168
0.001	[0.953, 0.978]	27/37	0.96	23.05	0.035	0.191
[0.061, 0.067]	[0.925, 0.963]	27/38	0.94	18.20	0.050	0.158
0.001	[0.941, 0.971]	28/39	0.94	25.12	0.045	0.141
0.001	[0.953, 0.978]	29/40	0.96	24.87	0.035	0.161
0.051	[0.927, 0.962]	29/41	0.94	19.57	0.0500	0.135
0.001	[0.942, 0.971]	30/42	0.94	27.28	0.045	0.119
0.001	[0.954, 0.977]	31/43	0.96	26.88	0.035	0.136
0.051	[0.929, 0.962]	31/44	0.94	21.40	0.050	0.111

\*The numbers within the bracket indicate a closed interval with both endpoints included. This applies to all intervals shown in the table.

## Properties of the predictive probability approach

### Robustness for the predictive probability design

We have discussed the schema of continuous monitoring after evaluating the first cohort. In practice, instead of continuous monitoring, investigators may want to monitor a trial by different cohort sizes. To examine the robustness of the PP design without continuous monitoring, we perform simulation studies. Specifically, once we choose  $\theta_L$ ,  $\theta_T$ , and  $N_{\max}$  based on prespecified type I and type II error rates to yield a desirable design, we evaluate the method's robustness by fixing these design parameters but varying the number of stages and cohort size in each stage.

In Example 1 ('Example 1: A lung cancer trial'), with  $N_{\max} = 36$ ,  $\theta_L$  is set at 0.001 and  $\theta_T$  is in a range of [0.852, 0.922]. The trial is designed to monitor every patient after the first 10 patients until the trial reaches the maximum sample size. We investigate the results of monitoring every five or ten patients. In addition, three scenarios of monitoring schedules for this trial are examined. In scenarios 1 and 2, the numbers of stages are fixed to 3 and 10, respectively, but cohort sizes after the first 10 patients are chosen randomly. In scenario 3, both the number of stages, between 3 and 10, and cohort sizes after the first 10 patients vary randomly. We use uniform distributions to choose the number of stages (scenario 3) and the size of each stage (scenarios 1, 2, and 3). When we monitor the trials

after treating every 5 or 10 patients with the true response rate of 0.2, the type I error rates are 0.088 and 0.088, the powers are 0.907 and 0.907, the probabilities of early termination are 0.86 and 0.45 and the expected numbers of patients treated are 29.74 and 30.87, respectively. Applying the variable width distribution plot [39], summaries of the operating characteristics for scenarios 1, 2, and 3 are shown in Figure 1, based on 1000 simulated trials under each scenario. These results indicate that the PP design remains robust in controlling type I and type II error rates. When the trial is monitored less frequently than planned, type I error rates are still under the nominal level of 0.10 and the power is higher than the nominal level of 0.90. Also, the chance of early termination due to futility is smaller than the continuous monitoring for all the scenarios studied. The expected sample size is slightly larger in scenarios 2 and 3 than those from the original PP design and Simon's minimax two-stage design.

In Example 2 ('Example 2: A tongue cancer trial'), under the same evaluation of robustness, almost all the type I error rates are slightly larger than 0.05 and the power values are all higher than 0.80 (Figure 2). Again, the probability of early termination due to futility is smaller and the expected sample size is larger than those from the original PP design. However, all the probabilities of early termination due to futility in the 10-stage scenario and the majority of the probabilities of early termination in the random-stage scenario are larger than those from Simon's minimax two-stage design. This causes all the expected sample sizes in

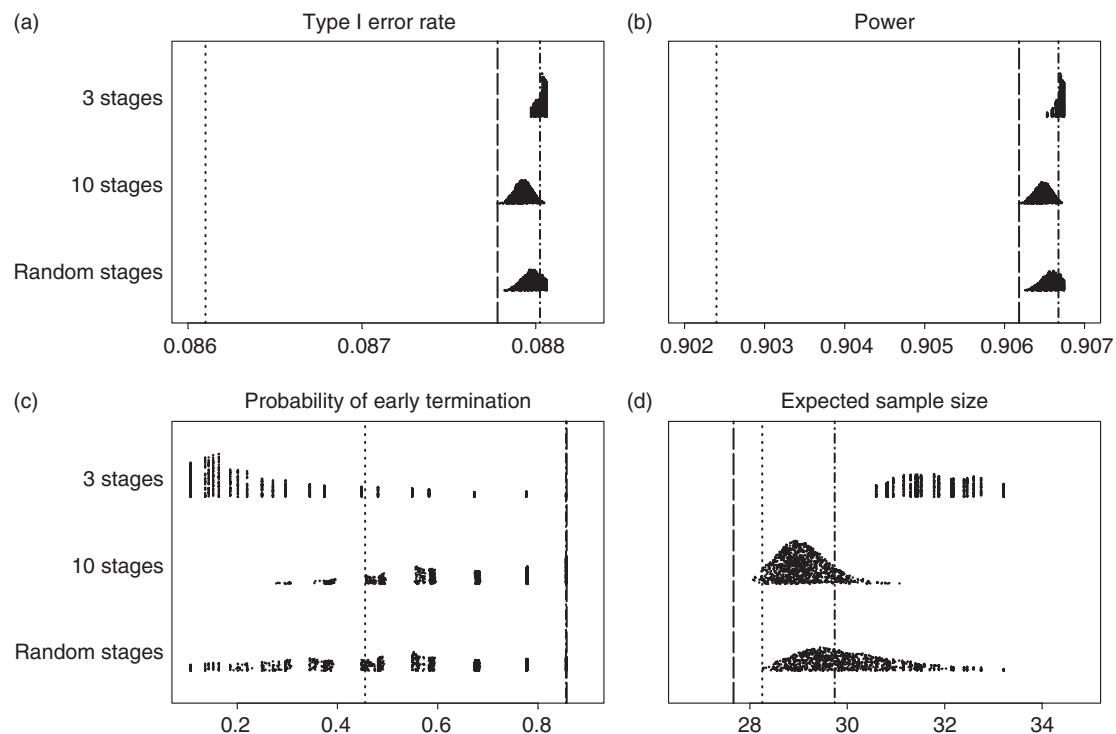


**Table 4** Operating characteristics of additional examples using Simon's two-stage designs and the PP design with type I and type II error rates of 0.10

Simon's minimax/optimal two Stage design <sup>a</sup>														Predictive probability design					
$p_0/p_1$	$r_1/\eta_1$	$r/N_{\max}$	PET( $p_0$ )	$E(N p_0)$	$\alpha$	$\beta$	$\theta_L$	$\theta_T$	$r/N_{\max}$	PET( $p_0$ )	$E(N p_0)$	$\alpha$	$\beta$						
0.1/0.3	1/16	4/25	0.52	20.37	0.095	0.097	0.001	[0.782,0.911]	4/25	0.79	19.99	0.096	0.095						
	1/12	5/35	0.66	19.84	0.098	0.099	0.001	[0.855,0.942]	5/29	0.86	21.98	0.062	0.099						
							0.001	[0.838,0.933]	5/30	0.85	23.25	0.072	0.081						
							0.001	[0.821,0.924]	5/31	0.83	23.94	0.082	0.068						
							0.001	[0.804,0.913]	5/32	0.81	25.42	0.093	0.054						
							0.003	[0.786,0.902]	5/33	0.81	23.50	0.100	0.056						
0.2/0.4							[0.037,0.046]*	[0.767,0.890]	5/34	0.84	19.96	0.099	0.069						
							0.001	[0.879,0.949]	6/35	0.89	26.01	0.054	0.070						
							0.001	[0.866,0.942]	6/36	0.87	26.75	0.061	0.059						
							0.001	[0.852,0.934]	6/37	0.86	28.16	0.070	0.048						
							0.001	[0.838,0.926]	6/38	0.85	29.14	0.078	0.040						
		10/36	0.46	28.26	0.086	0.098	0.001	[0.852,0.922]	10/36	0.86	27.67	0.088	0.094						
0.3/0.5	3/17	10/37	0.55	26.02	0.095	0.097	0.011	[0.830,0.908]	10/37	0.85	25.13	0.100	0.084						
							0.001	[0.876,0.935]	11/39	0.88	29.24	0.073	0.092						
							0.001	[0.857,0.923]	11/40	0.86	30.23	0.086	0.075						
							0.003	[0.837,0.910]	11/41	0.85	30.27	0.100	0.062						
							0.043	[0.816,0.895]	11/42	0.86	23.56	0.099	0.083						
	7/28	15/39	0.37	34.99	0.094	0.100	0.001	[0.859,0.918]	16/42	0.86	32.47	0.096	0.083						
0.4/0.6	7/22	17/46	0.67	29.89	0.097	0.095	0.001	[0.881,0.932]	17/44	0.88	33.50	0.081	0.088						
							0.001	[0.858,0.916]	17/45	0.86	34.84	0.098	0.069						
							0.048	[0.834,0.899]	17/46	0.87	25.11	0.099	0.092						
							0.001	[0.880,0.929]	18/47	0.88	35.70	0.083	0.073						
							0.001	[0.858,0.914]	18/48	0.86	37.33	0.100	0.056						
	11/28	20/41	0.55	33.84	0.095	0.099	0.001	[0.868,0.923]	20/41	0.87	31.07	0.096	0.098						
0.5/0.7	7/18	22/46	0.56	30.22	0.095	0.100	0.001	[0.875,0.927]	21/43	0.88	32.12	0.091	0.093						
							0.001	[0.882,0.930]	22/45	0.89	33.65	0.086	0.087						
							[0.024,0.025]	[0.854,0.911]	22/46	0.87	27.33	0.100	0.084						
							0.001	[0.889,0.934]	23/47	0.89	35.00	0.082	0.082						
							[0.010,0.011]	[0.862,0.915]	23/48	0.87	31.58	0.099	0.068						
	11/23	23/39	0.50	31.00	0.098	0.099	0.001	[0.869,0.925]	23/39	0.87	29.15	0.100	0.095						
0.6/0.8	11/21	26/45	0.67	28.96	0.096	0.098	[0.019,0.020]	[0.863,0.920]	24/41	0.88	25.39	0.100	0.091						
							0.001	[0.892,0.939]	25/42	0.90	30.82	0.082	0.097						
							0.037	[0.858,0.915]	25/43	0.88	24.39	0.100	0.091						
							0.001	[0.887,0.934]	26/44	0.89	32.48	0.087	0.082						
							0.060	[0.852,0.910]	26/45	0.88	24.31	0.099	0.087						
	18/27	24/35	0.82	28.47	0.097	0.100	0.001	[0.885,0.939]	25/36	0.89	25.51	0.090	0.089						
0.7/0.9	6/11	26/38	0.47	25.38	0.097	0.096	[0.042,0.046]	[0.864,0.924]	26/38	0.88	21.65	0.099	0.081						
							0.001	[0.889,0.940]	27/39	0.89	27.73	0.088	0.075						
							0.001	[0.909,0.952]	28/40	0.91	27.43	0.071	0.088						
							0.026	[0.869,0.926]	28/41	0.88	24.65	0.100	0.062						
	11/16	20/25	0.55	20.05	0.091	0.902	[0.001,0.011]	[0.884,0.953]	20/25	0.89	16.42	0.091	0.098						
	6/9	22/28	0.54	17.79	0.099	0.090	[0.103,0.133]	[0.860,0.937]	22/28	0.88	15.73	0.100	0.077						
						0.001	[0.883,0.949]	23/29	0.89	19.55	0.093	0.064							
						0.001	[0.903,0.959]	24/30	0.91	19.64	0.077	0.073							

<sup>a</sup>The first row represents Simon's minimax two-stage design and the second row represents Simon's optimal two-stage design.

\*The numbers within the bracket indicate a closed interval with both endpoints included. This applies to all intervals shown in the table.



**Figure 1** Operating characteristics for 1000 simulated trials under three scenarios for Example 1: 3 stages, 10 stages, and a random number of stages, all with random cohort sizes. Subpanels: (a) Type I error rates, (b) Power for detecting a response rate of 40%, (c) Probability of early termination if the true response rate is 20%, and (d) Expected sample size if the true response rate is 20%. Line types: ..... Simon's minimax two-stage design, - - - - Predictive probability design, monitoring every patient, - · - · Predictive probability design, monitoring every five patients

the 10-stage scenario and most of the expected sample sizes in the random-stage scenario to be smaller than those from Simon's minimax two-stage design.

When trial conduct deviates from the original design, predictive probability can still be calculated at any time during the trial to provide investigators updated information. The robustness study indicates that the PP design remains robust even when the continuous monitoring rule is not implemented after observing the outcome of every patient. We found that the inflation of the type I error rate is small and usually less than 10% of the prespecified level in all of our simulation studies.

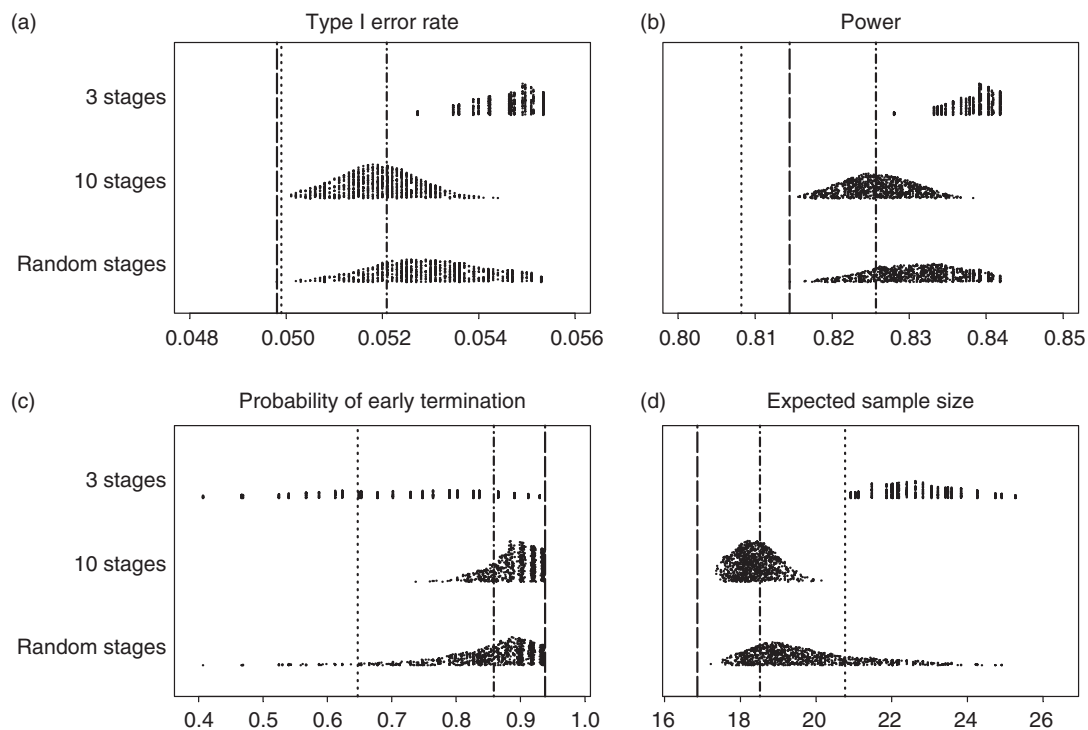
### Unplanned early termination

Clinical trials can be terminated earlier than planned due to slow accrual or some other reasons. For this situation, we examine the influence of early termination on the design properties. Using our first trial example, presented in section 'Example 1: A lung cancer trial', we suppose the trial is stopped after 20 evaluable patients. When  $\theta_T$

is held at the prespecified value of 0.922, we will declare that the new regimen is not promising if six or fewer responses have been observed in 20 patients, and promising otherwise. The corresponding type I error rate and power are 0.087 and 0.750, respectively. When this unplanned early termination occurs, the type I error rate is still controlled at a level under 10%, whereas power suffers a loss (<90%) due to the smaller than planned sample size. Similarly, we assume that the trial is stopped after 20 patients in our second example (section 'Example 2: A tongue cancer trial'). With  $\theta_T = 0.963$ , the type I error rate is controlled at 0.051 (a 2% increase from 0.05) but the power is reduced to 0.630, much less than the targeted 80% level due to the smaller sample size.

### Estimation bias

It is well known that sequential design with outcome-based early stopping rules can result in bias in estimating the parameters corresponding to that outcome. We performed simulation studies to evaluate the bias for Examples 1 and 2 presented



**Figure 2** Operating characteristics for 1000 simulated trials under three scenarios for Example 2: 3 stages, 10 stages, and a random number of stages, all with random cohort sizes. Subpanels: (a) Type I error rates, (b) Power for detecting a response rate of 80%, (c) Probability of early termination if the true response rate is 60%, and (d) Expected sample size if the true response rate is 60%. Line types: ..... Simon's minimax two-stage design, - - - - Predictive probability design, monitoring every patient, - · - · Predictive probability design, monitoring every five patients

in 'Comparison between predictive probability approach and Simon's two-stage design' section. Based on 5000 simulations, the median and mean (standard deviation) of the estimated response rates for Example 1 under  $p_0 = 0.20$  and  $p_1 = 0.40$  are 0.19, 0.17 (0.09) and 0.39, 0.40 (0.09), respectively. For Example 2, the corresponding statistics for the estimated response rates under  $p_0 = 0.60$  and  $p_1 = 0.80$  are 0.55, 0.55 (0.12) and 0.80, 0.78 (0.10), respectively. Due to the higher probability of early stopping under  $H_0$ , the bias is more prominent in  $H_0$  than in  $H_1$ . Under  $H_0$ , the observed median and mean underestimate the true response rate by about 10%. The early stopping rate under  $H_1$  is low. Hence, less bias is observed in estimating the true response rate.

#### Comparison between the designs based on the posterior probability versus designs based on predictive probability

Taking the settings in Examples 1 and 2, we also evaluate the operating characteristics for the designs based on the posterior approach. To the

aforementioned predictive probability approach, we define the early stopping rule for the posterior probability approach: (1) Stop the trial when  $P(p > p_1) < \theta_*$  for futility and (2) declare a positive trial at the end of the study when  $P(P > p_0) > \theta^*$ . In the setting of Example 1, with  $N_{\max} = 36$ , the corresponding design parameters for the posterior probability approach are  $\theta_* = 0.001$ ,  $\theta^* = [0.852, 0.922]$ . The resulting type I error rate, probability of early stopping, and expected sample size under  $H_0$  are 0.088, 0.45, and 28.73, respectively. Under  $H_1$ , the study power is 0.905 and the expected sample size is 35.73. These results are quite similar to the predictive probability approach reported in Section 3, except that the probability of early stopping is much lower (0.45 vs 0.86) under  $H_0$ .

Another notable difference is the construct of rejection regions. For the posterior probability approach, the rejection region is 0/10, 1/15, 2/20, 3/24, 4/28, 5/32, and 10/36. There is a big jump toward the end of the study (5/32 to 10/36) for the posterior probability approach while the transition for the predictive probability approach is smoother. Similar results are found in Example 2 (data not shown).

## Discussion

In the frequentist multi-stage design, the study design is rigid in the sense that decisions can only be made at predetermined cohort sizes of the trial. However, the design with the predictive probability approach provides an excellent alternative for conducting multi-stage phase II trials. It is efficient and flexible. The design parameters can be found by searching the parameter space and choosing appropriate values of  $\theta_L$  and  $\theta_T$  such that the type I and type II error rates are controlled. The sample size can be determined by choosing the smallest  $N_{\max}$  among all designs that satisfy the design criteria. The PP design yields a higher probability of early stopping and a smaller expected sample size compared to Simon's two-stage designs when the treatment is unlikely to be efficacious. By varying the number of stages and cohort sizes, the PP design also shows robust operating characteristics. When the trial conduct deviates from the original plan, the type I error rate only increases slightly. To ensure that the nominal type I error rate is controlled, we can design the trial with a stricter type I error rate. For example, we can set type I error rates as 0.045 and 0.09 for targeting 0.05 and 0.10 type I error rates, respectively. Furthermore, through the specification of the prior distribution, the PP design can formally incorporate the additional efficacy information obtained before and throughout the trial into the decision making process. The PP design allows for a highly flexible monitoring schedule that is suitable for clinical applications, yet its operating characteristics remain robust. In our trial examples, we monitor the trial continuously after the first 10 patients are treated and are evaluable for response. Although we present the PP design using continuous monitoring, the approach can be applied with any number of stages and cohort sizes. In practice, the first cohort of patients and the number of stages are usually determined after consulting with study investigators to identify a reasonable choice that balances the practical considerations with trial efficiency.

We find that comparable operating characteristics can be obtained by taking both the predictive probability and the posterior probability approaches. However, the predictive probability approach resembles more closely the clinical decision making process, i.e., deciding whether to continue the study based on the interim data, as well as projecting into the future. The predictive probability approach also leads to higher early stopping rates under the null hypothesis (when treatment not working). Furthermore, the rejection region has a smooth transition compared to the posterior probability approach, which is likely to

have a 'jump' between the interim data analysis and the final analysis. Further research on comparing the applications of the two approaches in designing clinical trials is warranted.

Regarding the choice of  $\theta_L$  and  $\theta_T$ , in general, the lower  $\theta_T$  is, the easier it is to reject  $H_0$ , hence, there is increased power and type I error rate. On the other hand, the higher  $\theta_T$  is, the harder it is to reject  $H_0$ , hence, there is decreased power and type I error rate. Likewise, a larger  $\theta_L$  corresponds to easier stopping due to futility and decreased power and type I error rate, and a smaller  $\theta_L$  corresponds to the opposites. However, due to the discrete nature of the binomial distribution, for a fixed parameter (e.g., response rate = 20%) with a given prior distribution, there may be a range of  $\theta_L$  and  $\theta_T$  which gives the same rejection boundaries. In this case, from the trial conduct point of view, it does not matter which values of  $\theta_L$  and  $\theta_T$  are used. If a range of  $\theta_L$  and  $\theta_T$  exists which satisfies the prespecified constraints, one may choose the midpoint of the range for defining the decision rule using the predictive probability. The effect of varying parameters or the prior distributions can be evaluated accordingly.

Although frequentist approaches have historically dominated the field of clinical trial design and analysis, Bayesian methods provide many appealing properties. These include the ability to incorporate the information obtained before the trial into the study design, to use the information obtained during the trial for monitoring the study, flexibility in trial conduct, and a consistent way for making inference [36,40–42]. Instead of taking an ideological stand of choosing either the Bayesian or frequentist method, we take a pragmatic approach in searching for a better method for evaluating treatment efficacy in the phase II setting. We use the Bayesian framework as a tool to design clinical trials with desirable frequentist properties.[19] Taking the Bayesian approach, we derive an efficient and flexible design. In the meantime, we choose the design parameters (in our case,  $N_{\max}$ ,  $\theta_L$  and  $\theta_T$ ) to control the type I and type II error rates under a variety of settings. Several similar approaches of taking the Bayesian framework to achieve good frequentist properties have been proposed in the literature [43,44]. We advocate the use of extensive computation and/or simulation studies to search for the optimal design parameters and to evaluate the design's operating characteristics. Sensitivity analysis should be conducted to examine how the design parameters influence the design properties. Robustness analysis should also be carried out to study the impact on design properties when the study conduct deviates from the original design. Based on our extensive studies, we conclude that the predictive probability approach offers practical and desirable designs for

phase II cancer clinical trials. S-PLUS/R programs can be downloaded from <http://biostatistics.mdanderson.org/SoftwareDownload/> to assist in developing a study design using the described predictive probability method.

One reviewer pointed out the limitation of the traditional hypothesis testing framework when designs are constructed with the primary goal for controlling type I and type II error rates. For example, as shown in Example 2 and Table 3, both Simon's minimax design and our predictive probability design will reject the null hypothesis if we observe 25 responses in 35 patients when  $p_0 = 0.6$ ,  $p_1 = 0.8$ ,  $\alpha = 0.05$ , and  $\beta = 0.2$ . It seems unreasonable that we fail to reject  $p_0 = 0.6$  when the observed response rate  $\hat{p} = 0.71$  is considerably larger than 0.6. This is a result of choosing a small type I error rate. To achieve a valid scientific inference, we emphasize the importance of estimation even when the trial is designed under the hypothesis testing framework. In this example, the posterior distribution for the response rate is  $\text{beta}(25.6, 10.4)$  if we take the prior as  $\text{beta}(0.6, 0.4)$ . The probabilities that the response rate is greater than 0.6 and 0.8 are 0.92 and 0.11, respectively. The 95% highest probability density interval for the response rate is (0.56, 0.85). The posterior probability provides a more thorough assessment of the response rate under the Bayesian framework.

Lastly, we would like to emphasize that reaching an efficacy threshold is not the only purpose of phase II trials. Information collected from phase II studies will enable the investigators to provide further safety analysis, to find out appropriate dosing schedules, to identify appropriate populations for a new treatment, and to assess the possibility for combination studies, etc. Depending on the purpose of the study, the investigators may not always want to terminate the study early, even when the early stopping boundary is crossed. However, the predictive probability approach still offers a consistent way to evaluate the strength of the treatment efficacy based on the observed data. Phase II trials can be considered as learning studies. The predictive probability design under the Bayesian framework provides an ideal environment for learning.

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## Abbreviations

$E(N)$	expected sample size
PET	probability of early termination
PP	Predictive probability