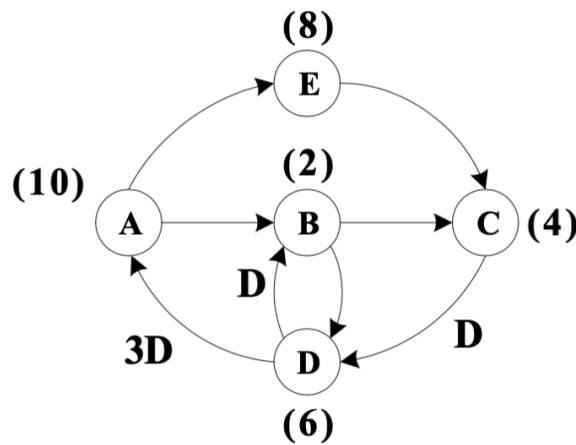


1 Question

Consider the DFG below. The numbers in parentheses are the computation times of the nodes.

- What is the iteration bound of this DFG? What is the actual iteration period?
- Retime this DFG to minimize the iteration period. What is the actual iteration period of the retimed DFG?
- Unfold both the original DFG and the retimed DFG by a factor of 2. what are their actual iteration periods?
- Determine the minimum unfolding factor J such that the J-unfolded DFG (unfold from the original DFG) can be retimed so that the critical path of this unfolded and retimed DFG is , where is the iteration bound of the original DFG below. Unfold the DFG by this minimum unfolding factor and retime the unfolded DFG so that its critical path is .



2 Answer

(a) By inspection, we observe several loops in the DFG:

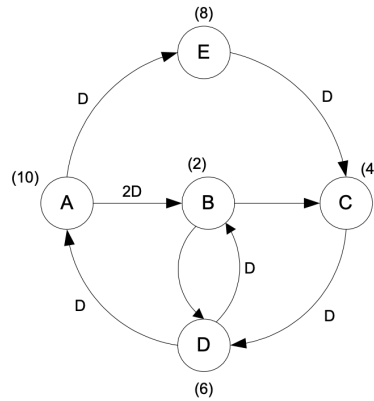
So, the boundary iteration is as below:

$$T^{(\infty)} = \max\left\{\frac{10 + 8 + 4 + 6}{4}, \frac{10 + 2 + 4 + 6}{4}, \frac{10 + 2 + 6}{3}, \frac{6 + 2}{1}, \frac{6 + 4 + 2}{2}\right\} = 8$$

BI is 8 u.t.

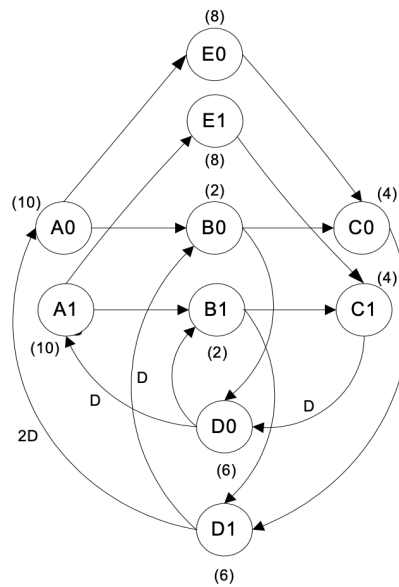
The actual iteration period is A->E->C->D (critical path), the value is 22 u.t

(b) We can retime the item of A. and E. the result DFG is like below:



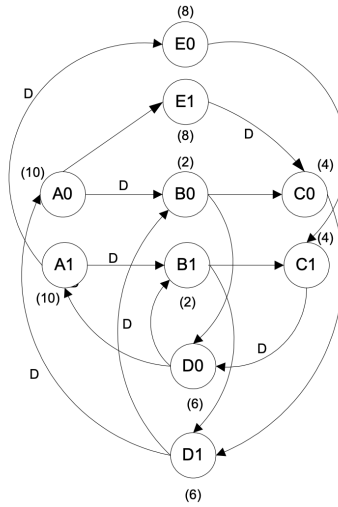
The minimum iteration period is 10 u.t. (because a single **A** is 10 u.t.), so the actual iteration period is A itself.

(c) Unfolding the original DFG by a factor of $J=2$, the new DFG is like follows:



The critical path is 28 u.t (A0->E0->C0->D1)

Unfolding the retimed DFG by $J=2$, the new DFG is like this:

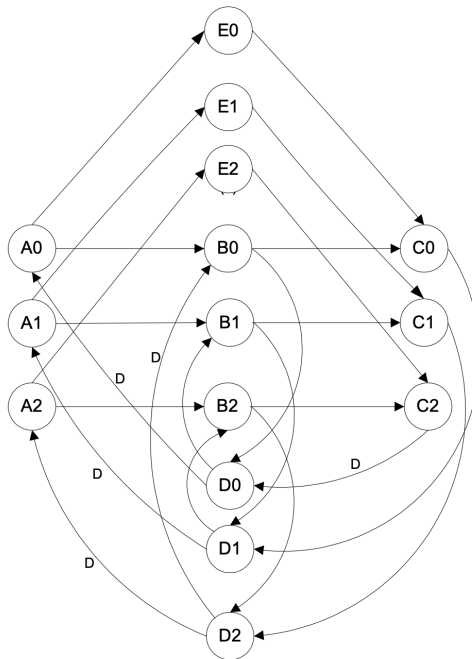


The critical path is 18 u.t (A0->E1)

(d) Solving the following equation retiming problems for the original DFG:

- For all edges $U \rightarrow V$ in the DFG, $r(U) - r(V) \leq w(e)$;
- If $D(U, V) \geq c$, then $r(U) - r(V) \leq W(U, V) - J$

with increasing value of J until a solution is feasible and $c = 8J$. Then this J is the minimum unfolding factor. It turns out that the minimum unfolding factor is equal to 3, and the 3-unfolded DFG is shown below:



Without further retiming, this DFG has an iteration period equal to $J \times T_\infty = 24u.t.$ where T_∞ is the iteration bound of the original graph.