



# 3rd Degree Polynomial Curve Fitting Approach To Improve OpenStreetMap Derived Curved Road Lengths



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*Mohammed Zia  
Omer Ozyıldırım*

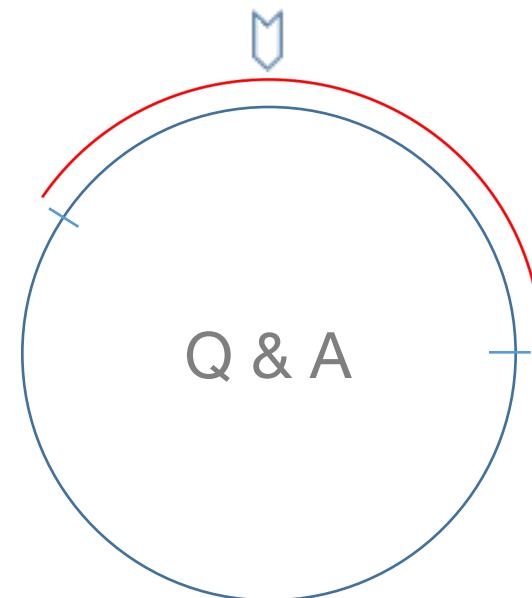
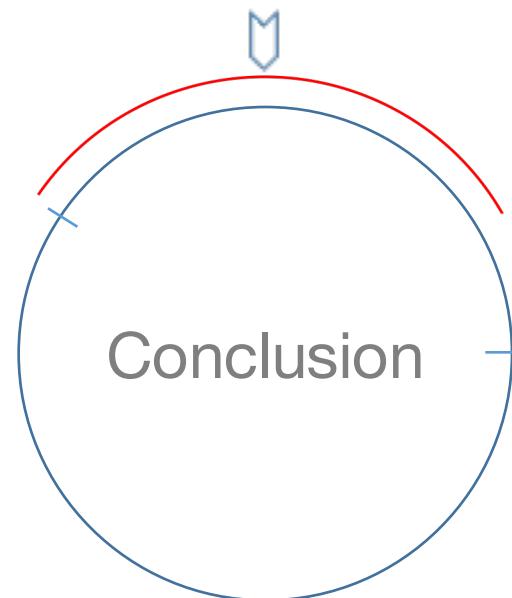
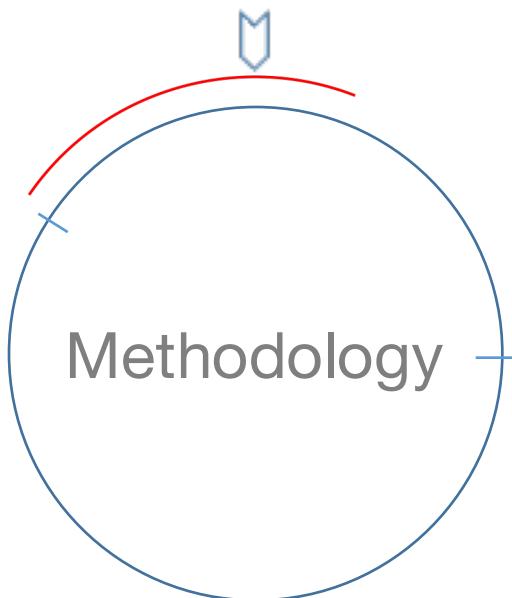
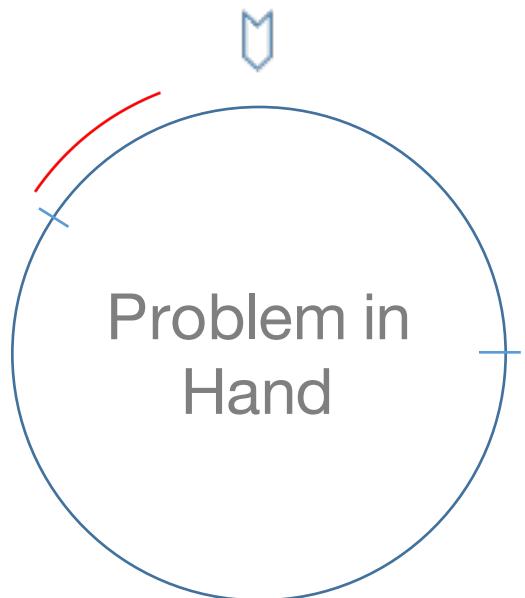
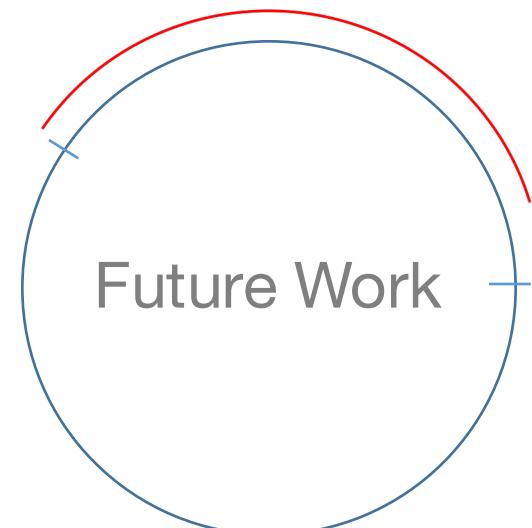
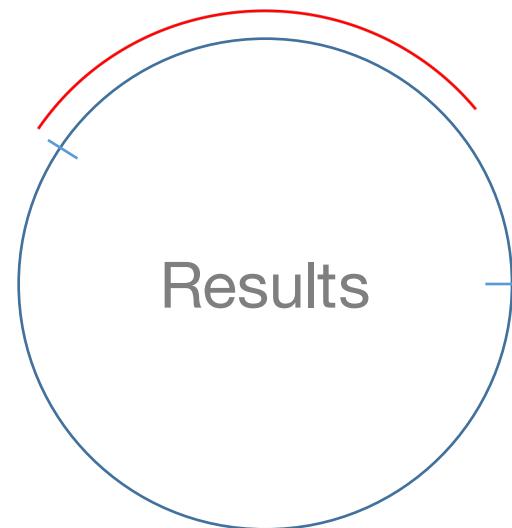
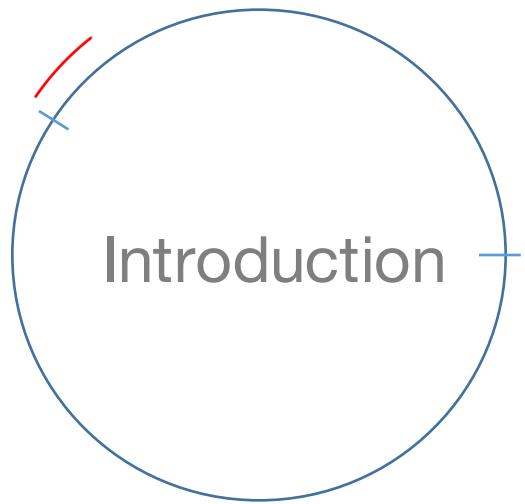


## About Me

- Currently doing *Doctoral of Philosophy* at Istanbul Technical University<sup>1</sup> under the Department of Geomatics Engineering.
- Additionally, working as a *Full Stack GeoSpatial Developer* at National Innovation and Research Center for Geographical Information Technologies<sup>2</sup> (Istanbul Technical University).
- This work is fully funded by The Scientific and Technological Research Council of Turkey<sup>3</sup> (TUBITAK) under 2215 - *Graduate Scholarship Programme for International Students*.

## Funding 💰

# Content



# Introduction



2004 -

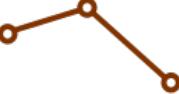
OpenStreetMap (OSM) is currently one of the most popular Volunteered Geographic Information (VGI) project with objective to establish a free and editable street map of the world.

## OSM Statistics September 2015

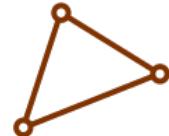
8 billion  
nodes



3 billion  
ways



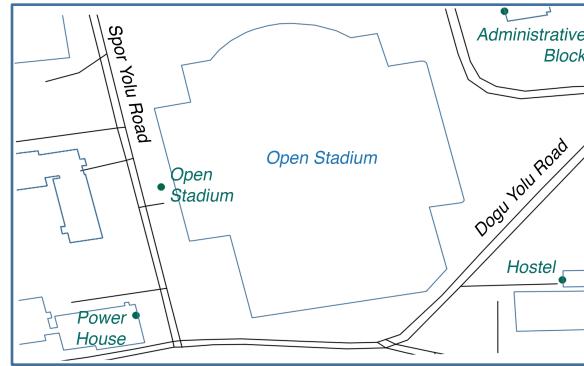
4 million  
relations



2.5 million  
users

## OSM Data Format

Vector

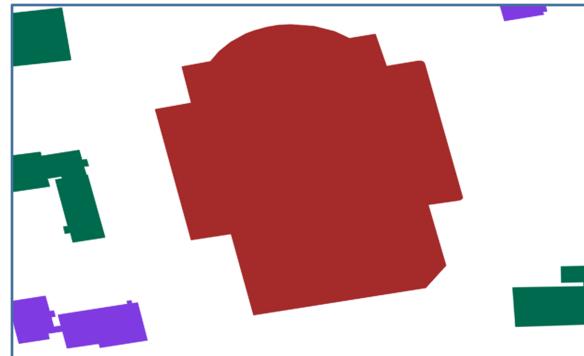


Raster

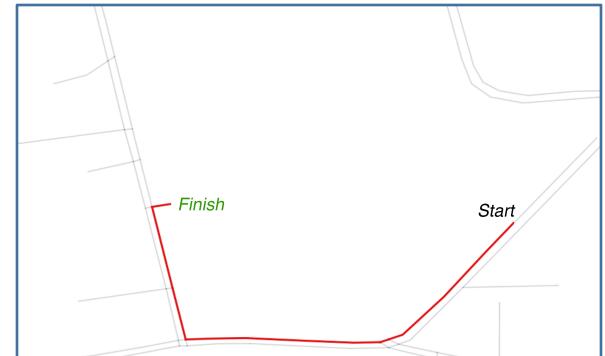


## OSM Applications

Thematic Maps



Routing Services



# Problem in Hand?

## OSM XML Format

```
<?xml version="1.0" encoding="UTF-8"?>
<osm>
  <node/> _____ Point
  <node/> _____
  <node/> _____
  <node/> _____
  <node/> _____
  <node/> _____ Line
  <way></way> _____
  <relation></relation> _____
</osm>
```

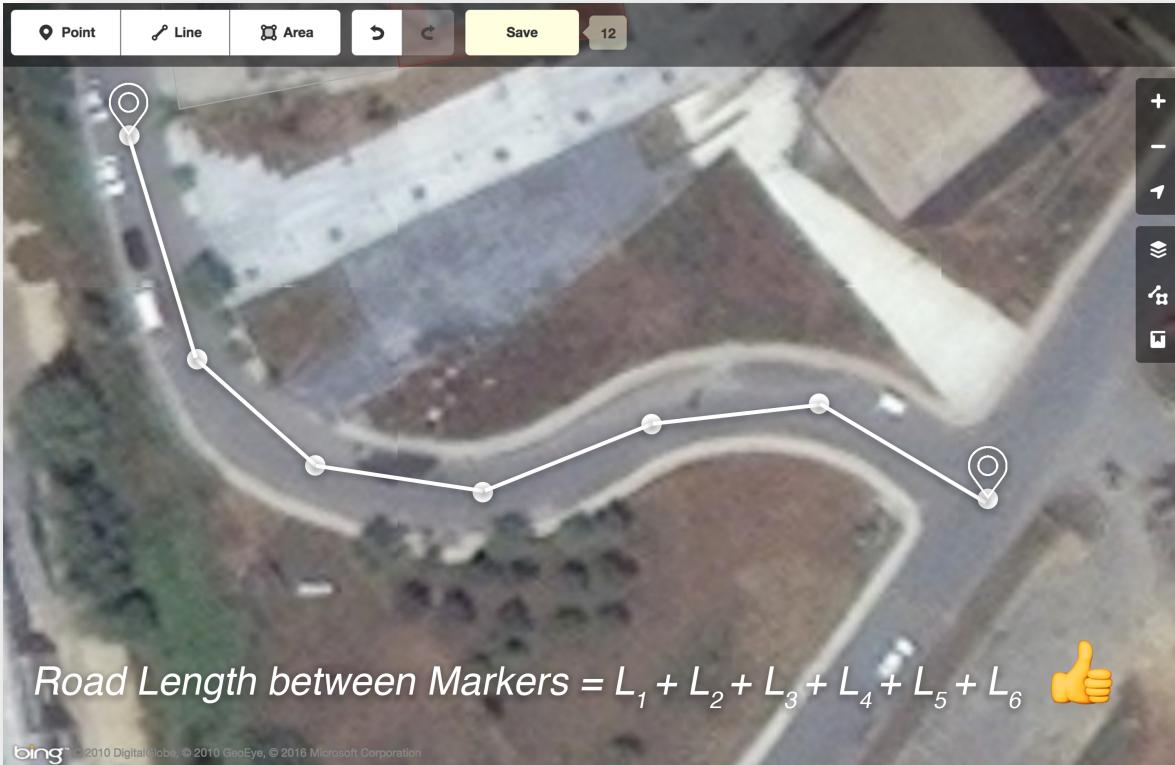
*Point*  
*Polygon*  
*Line*

## A Small Road Section



# Problem in Hand? . . .

OSM Road Euclidean Length



$Road\ Length\ between\ Markers = L_1 + L_2 + L_3 + L_4 + L_5 + L_6$

OSM Road Curve Fitted Length



$Road\ Length\ between\ Markers = C_1 + C_2 + C_3 + C_4 + C_5 + C_6$

Euclidean Length  $\leq$  Curve Fitted Length

# Literature Review

Road Length Amelioration  
**No Similar Work!**

OSM Dataset  
Time-Series  
Evolution

Urban Planning

3D Modelling

Quality  
Check-Up

Vandalism

Road  
Classification

OSM  
Semantics

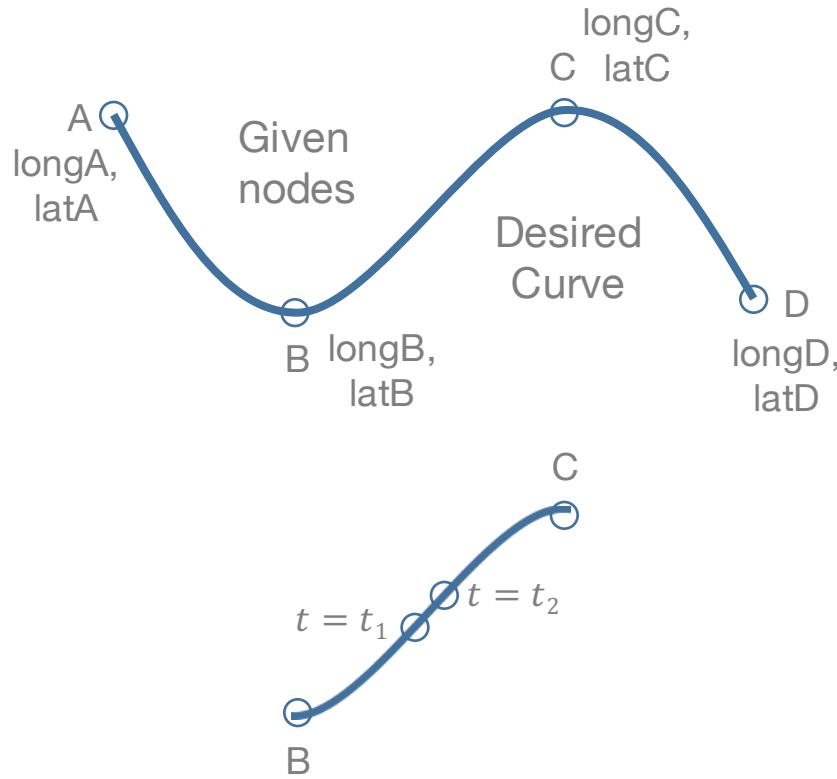
Vehicle Traffic

Case Studies

Different  
Applications

# Methodology

## Cubic Curve Equation Derivation



Parametric curve equation of 3<sup>rd</sup> degree

$$\text{long}(t) = x = f(t) = a_1 t^3 + b_1 t^2 + c_1 t + d_1$$

$$\text{lat}(t) = y = g(t) = e_1 t^3 + f_1 t^2 + g_1 t + h_1$$

Length from  $t_1$  to  $t_2$  (using mean-value theorem)

$$(1) L(\text{in radian}) = \int_{t_1}^{t_2} \left[ \sqrt{\left\{ \frac{df(t)}{dt} \times \frac{[\cos\{g(t_1)\} + \cos\{g(t_2)\}]}{2} \right\}^2 + \left\{ \frac{dg(t)}{dt} \right\}^2} \right] dt$$

(2) Applying Simpson's rule to solve  $L(\text{in radian})$

(3)  $L(\text{in meter}) = \text{RadiusEarth}(\text{lat}_1) \times L(\text{in radian})$

(4) Summing up all segments from B to C

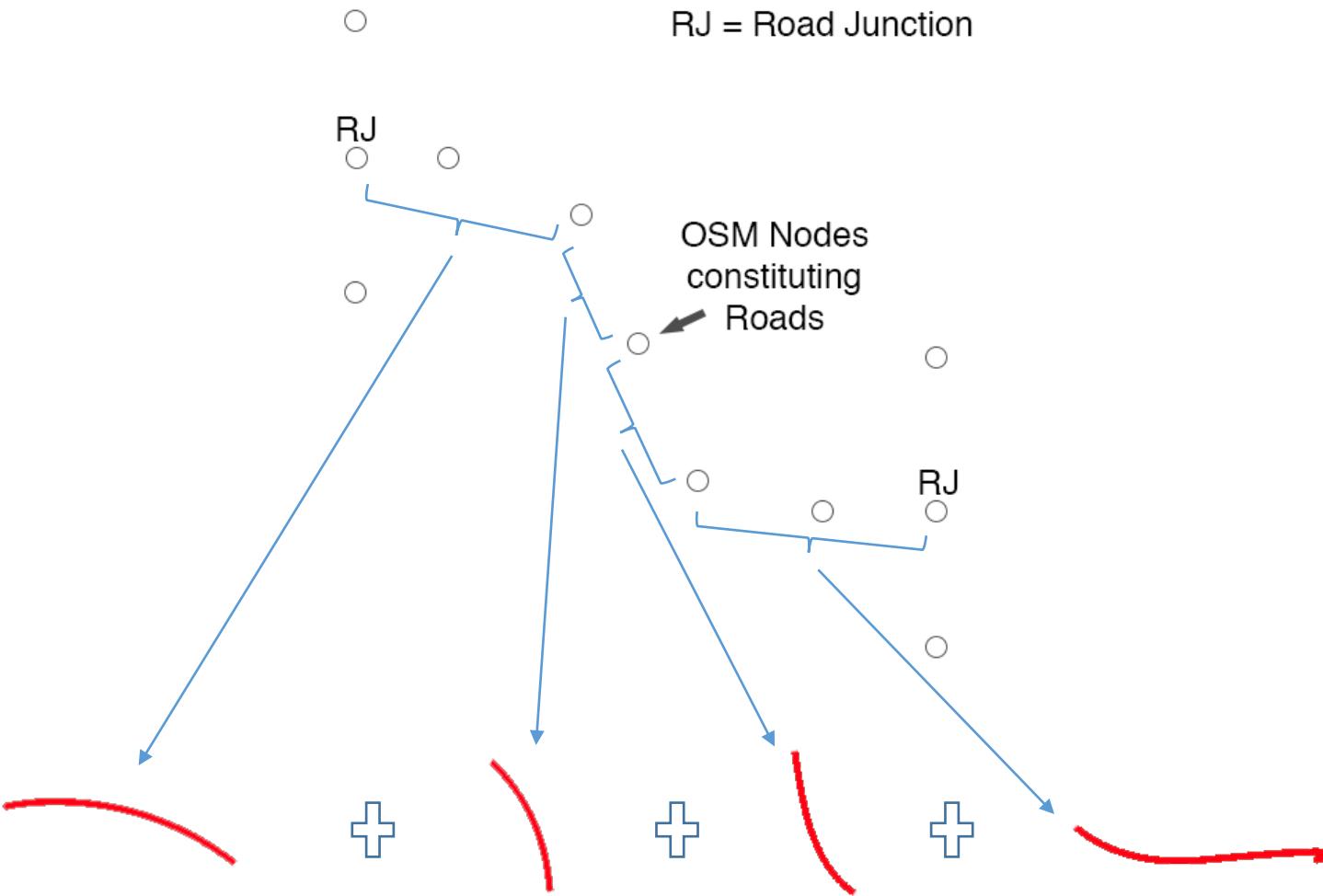
$$\text{RadiusEarth}(\text{lat}_1) = ((\cos \text{lat}_1/a)^2 + (\sin \text{lat}_1/c)^2)^{-0.5}$$

$$\tan \text{lat}_1 = (c/a)^2 \times \tan \{\text{latt mean}\}$$

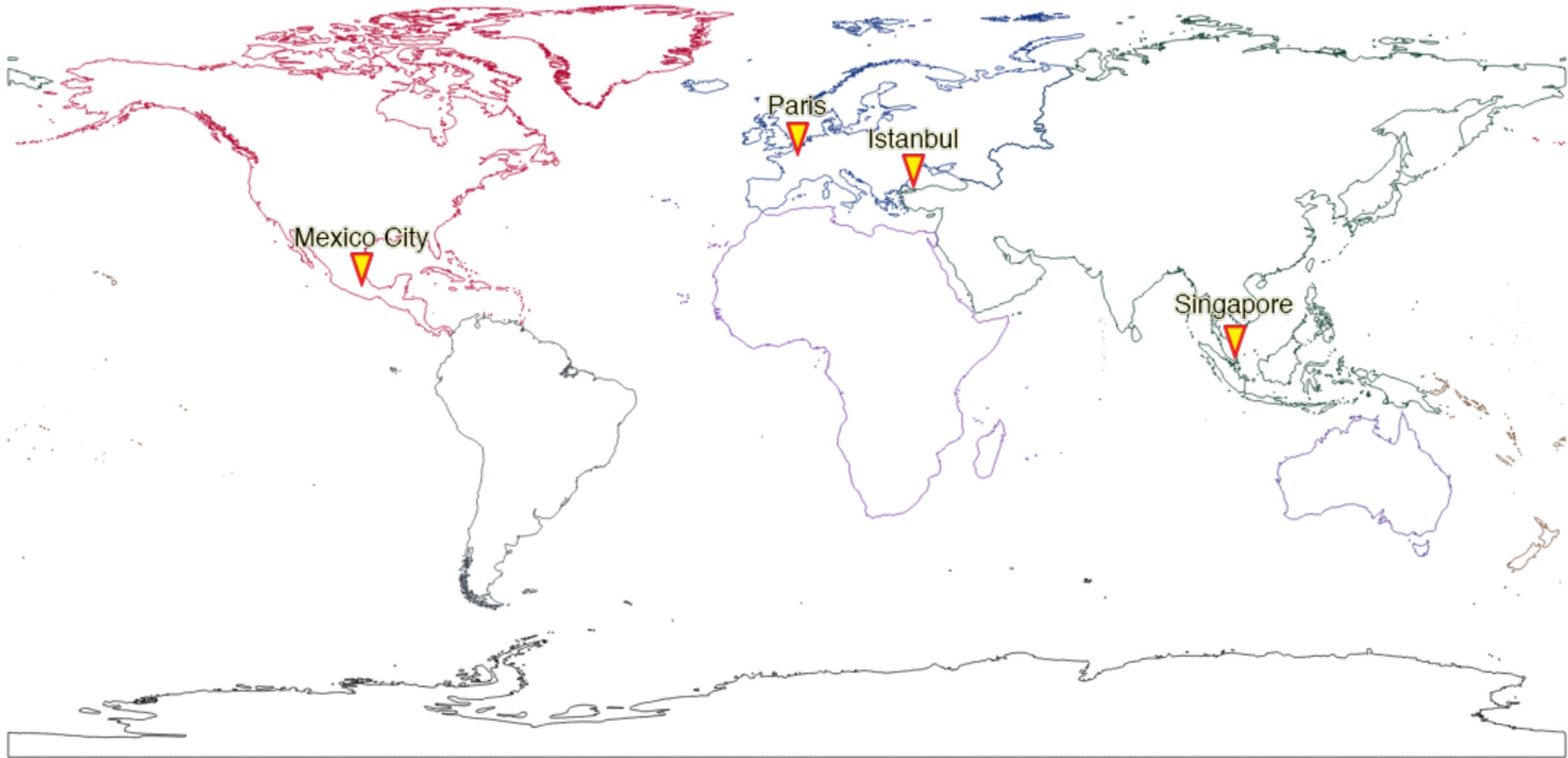
$$\text{latt}_{\text{mean}} = \frac{\{\text{latt}_1 + \text{latt}_2\}}{2}$$

where  $a$  is equatorial and  $c$  polar radius

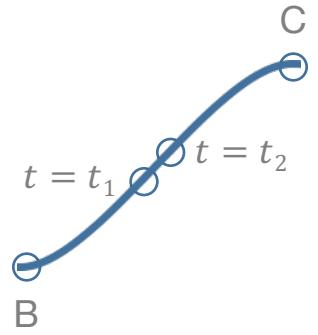
# Methodology



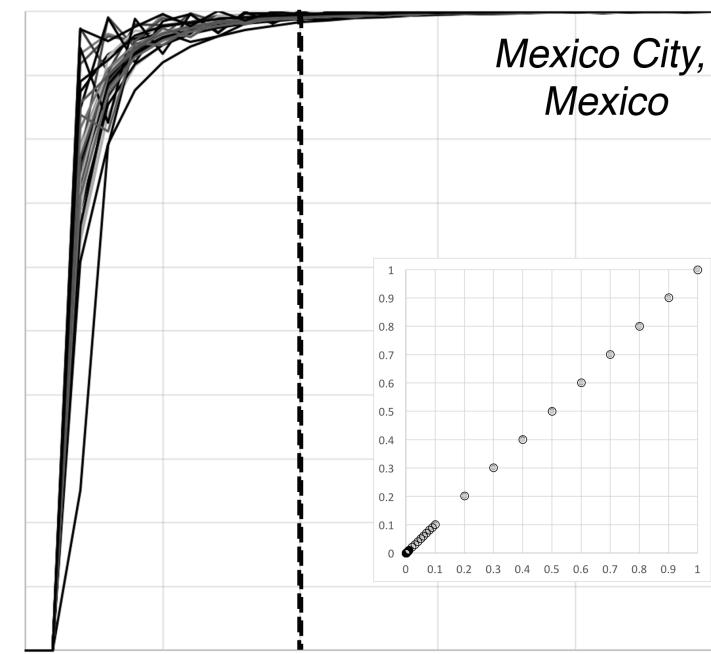
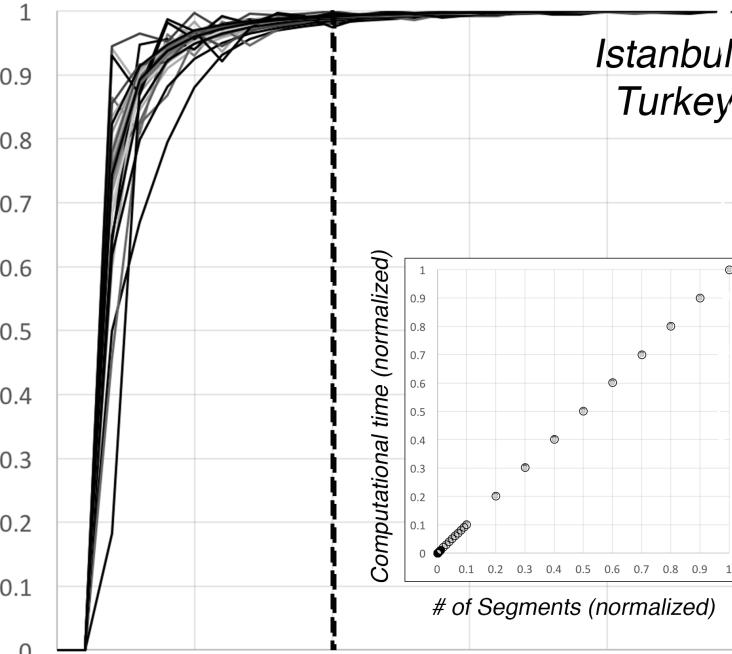
# Results



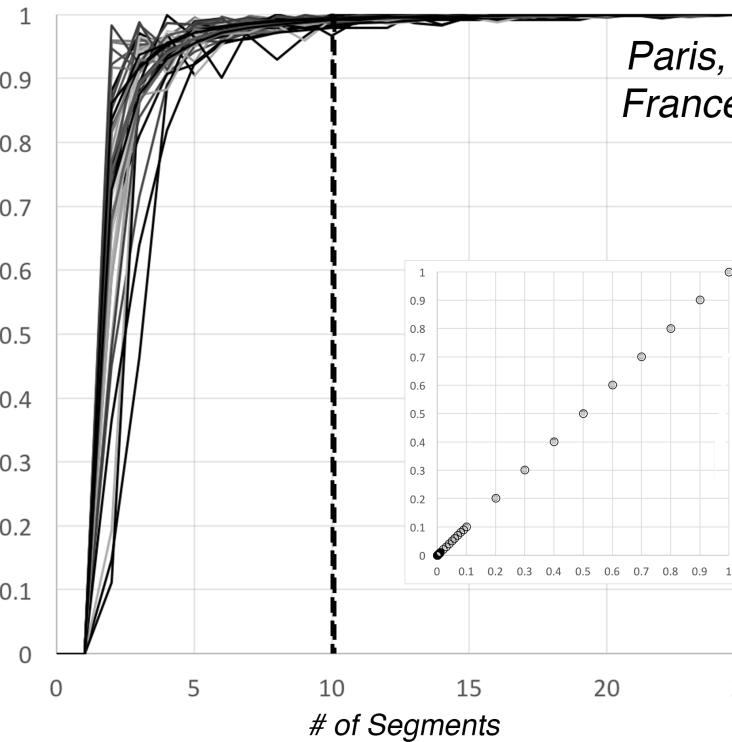
# Results ...



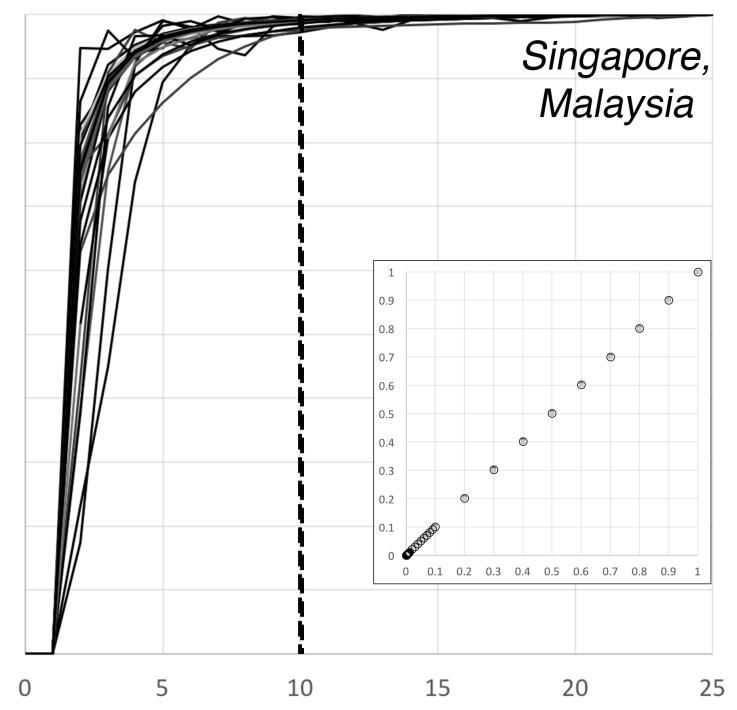
OSM cubic polynomial curve  
fitted length (normalized)



Paris,  
France

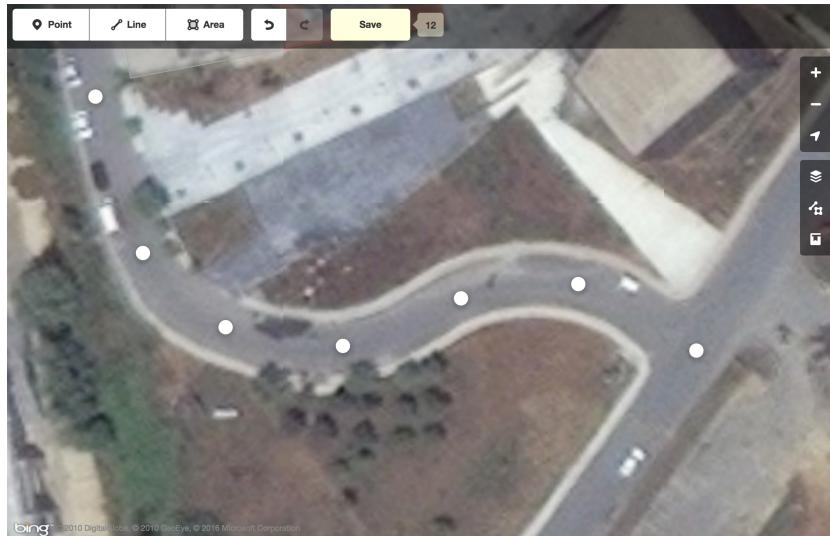


Singapore,  
Malaysia

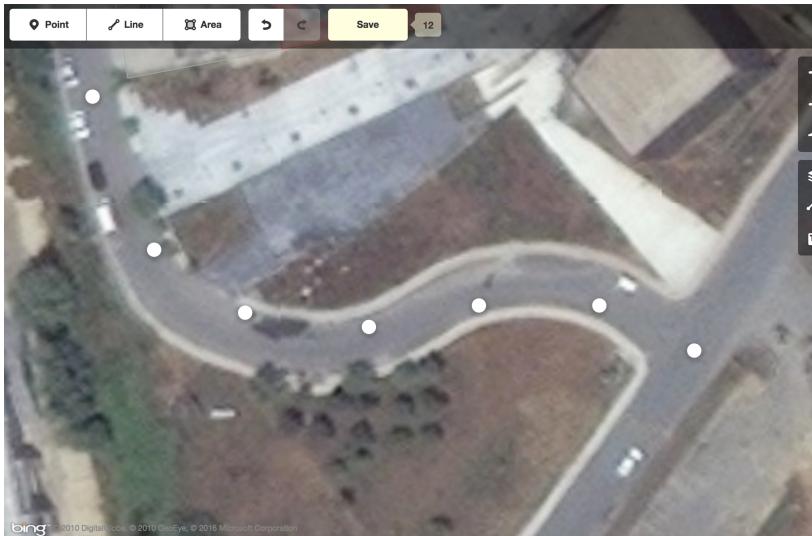


# Results ...

Nodes Precisely Mapped



Road Curvature Underestimated

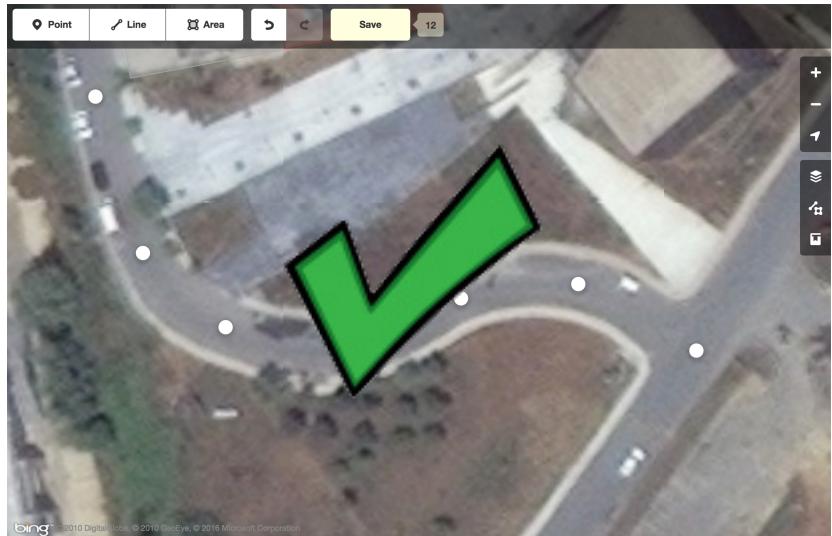


Road Curvature Overestimated

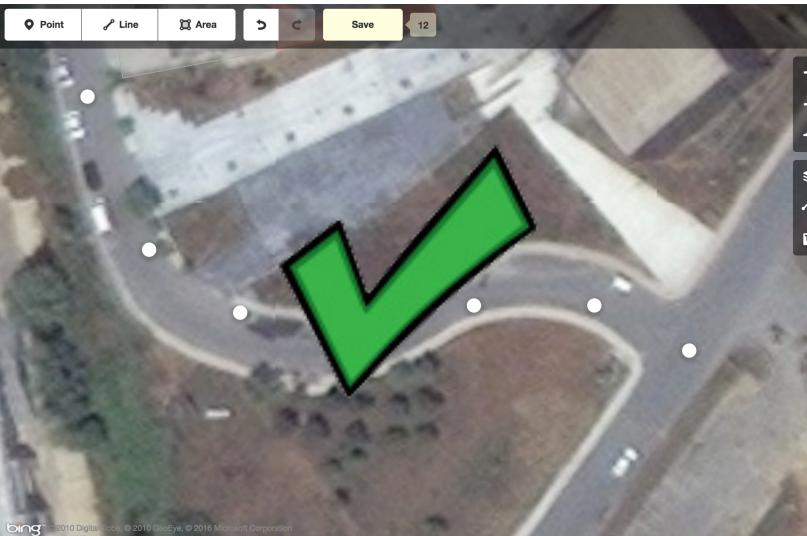


# Results ...

Nodes Precisely Mapped



Road Curvature Underestimated



Road Curvature Overestimated



Euclidean Length  $\leq$  Curve Fitted Length

# Results . . .



Euclidean Length

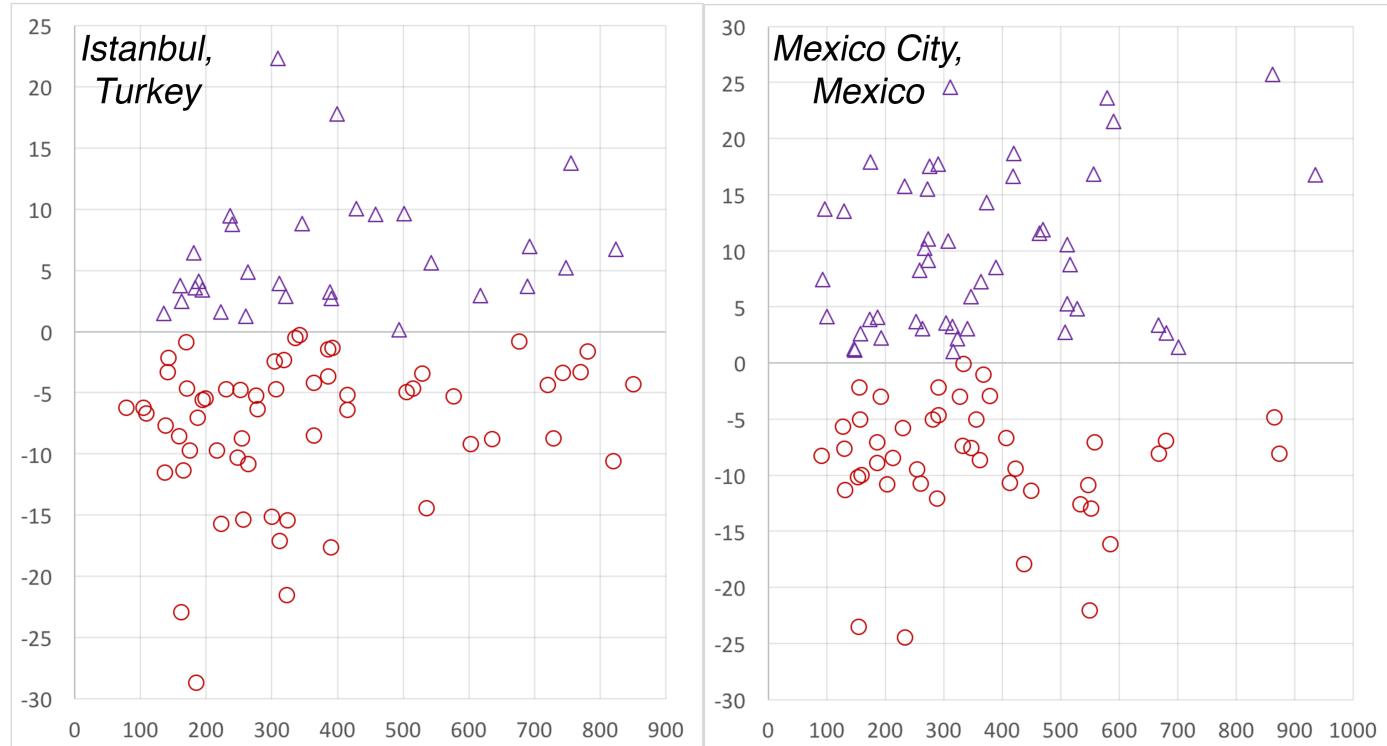


Curve Fitted Length

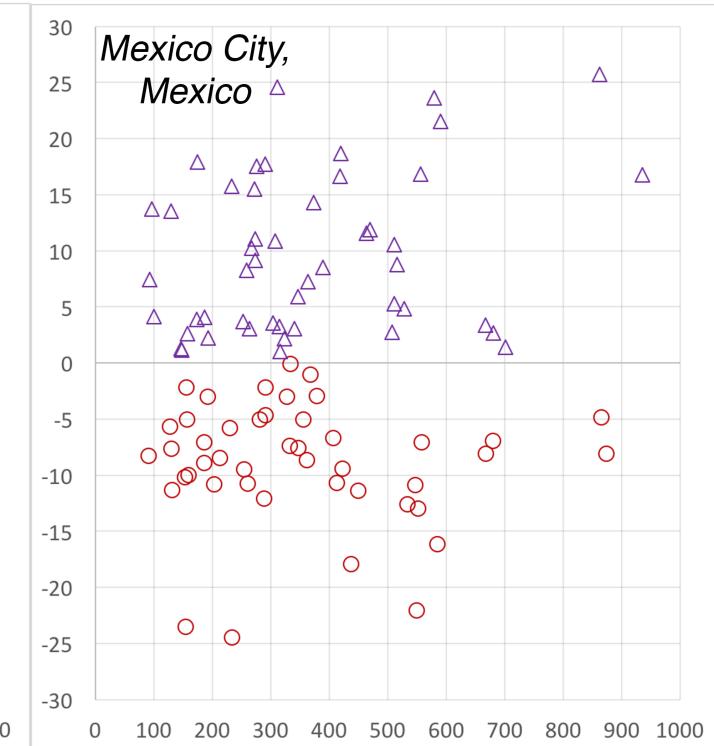


Best Length

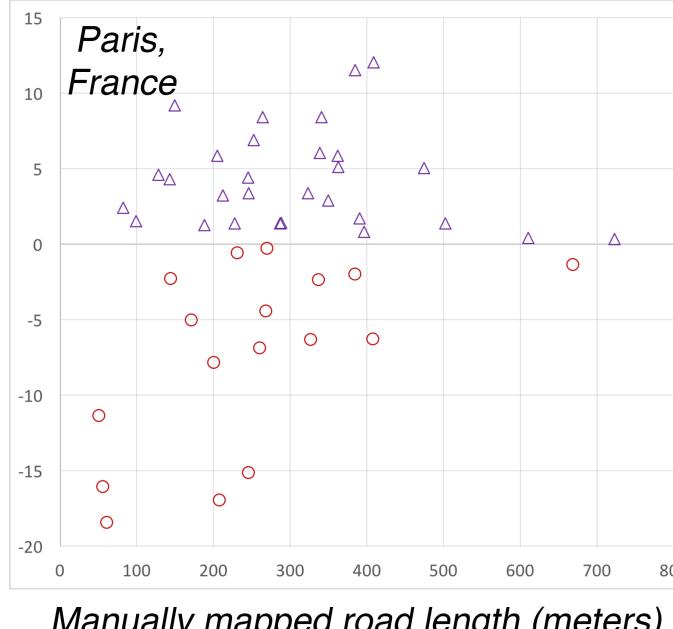
(Manually mapped road length) -  
(OSM derived road length without curve fit)  
(meters)



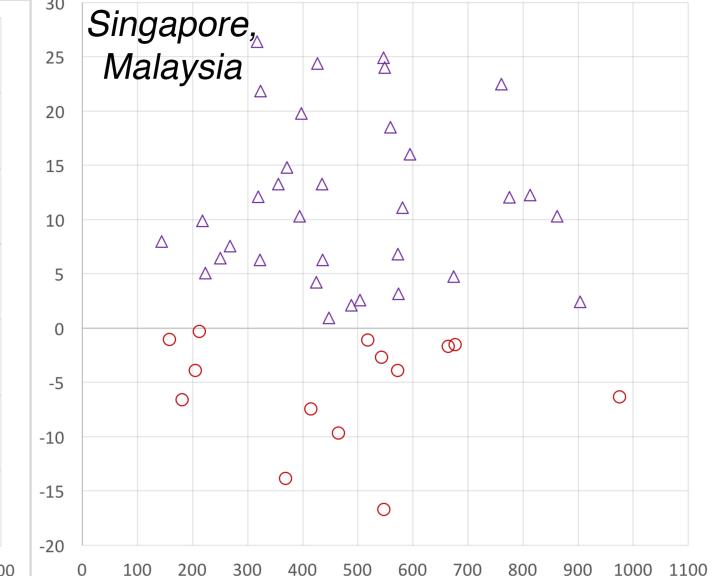
Mexico City,  
Mexico



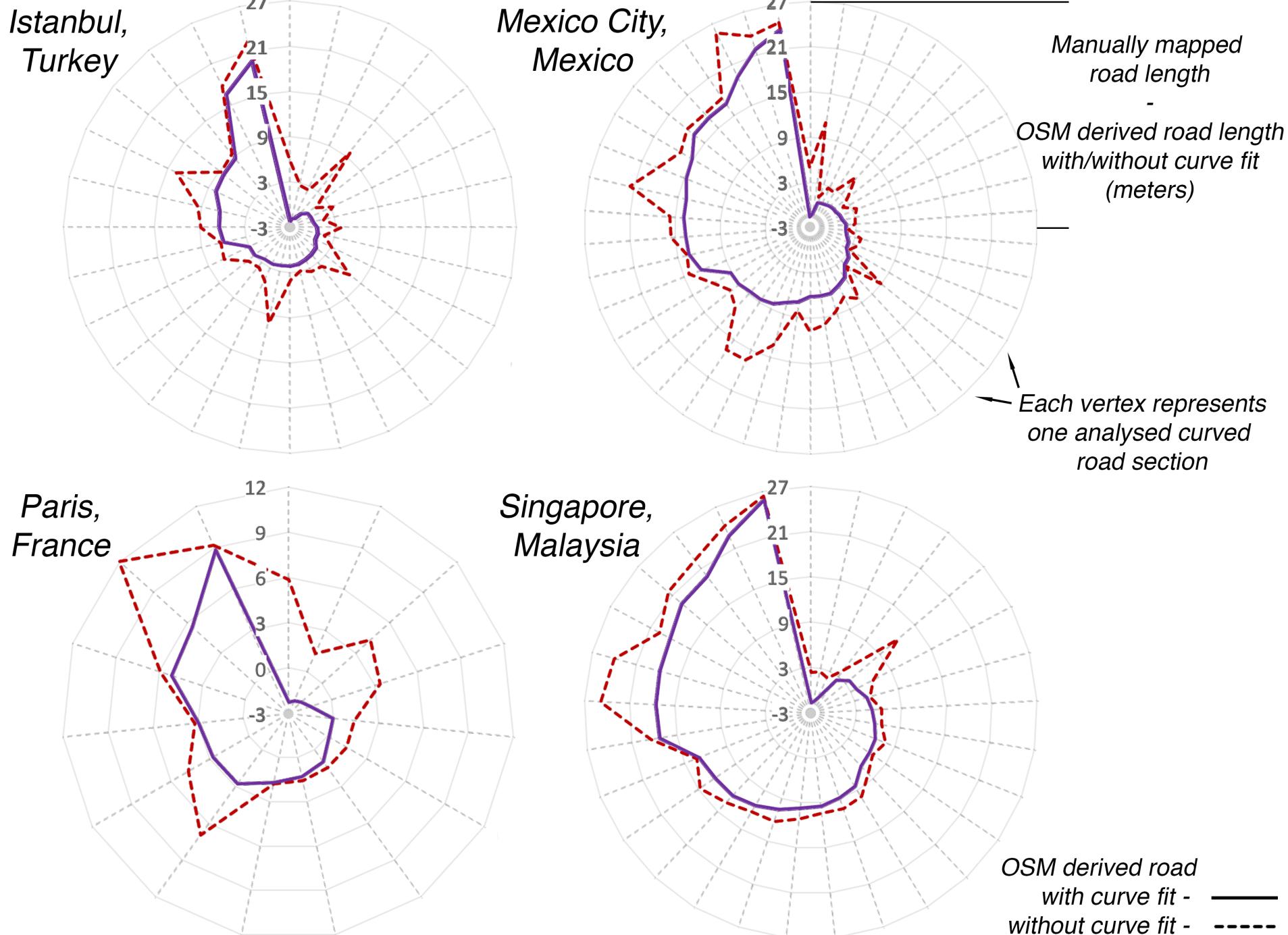
Paris,  
France



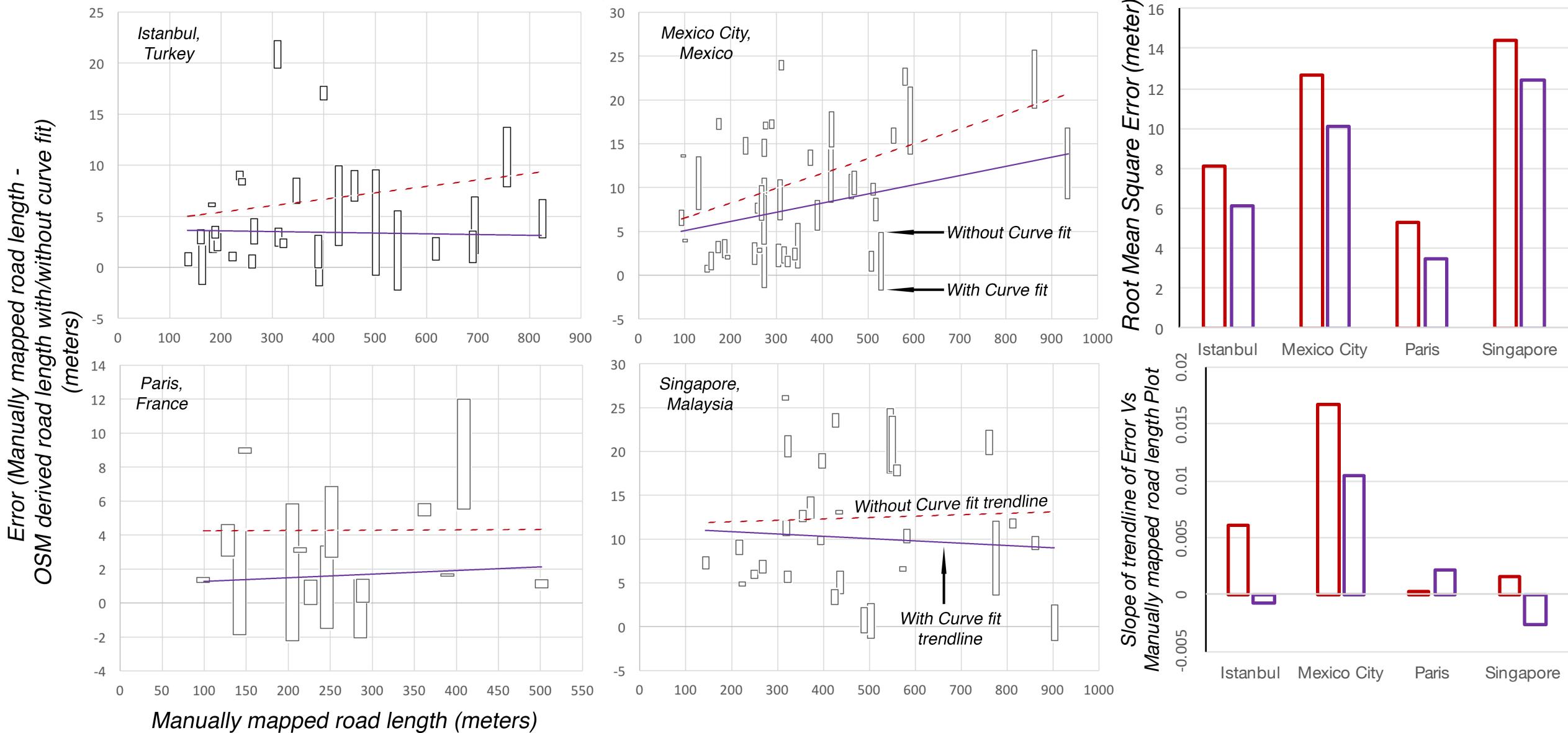
Singapore,  
Malaysia



# Results ...



# Results . . .



# Conclusion

- Curve Fitted Road Length is better than Euclidean Length.
- Proposed algorithm, although, can not be used for a whole city blindly.
- For overly mapped curved road lengths it will bring more error than Euclidean Length.
- 10 number of road segmentation during formulation is apt for OSM data, after preliminary results.

# Future Work

- Developing an automated way to estimate overly estimated road curves.
- A web-GUI to visualize fitted curve.
- A methodology to remove nodes causing curvature over estimation.
- Cross checking results with some proprietary or governmental data.
- Running developed algorithm on other similar cities.

Thanks!

## Any questions?

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 Zia- (This presentation will get online soon at author's GitHub account!)