



First year students

Final exam

Name:

ID Number:

Date:

Time:

Score:

Q (1): Choose the correct answer:

1- If $y = \cos(2x)$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | | | |
|---|---------------|--------------|---------------|
| <input checked="" type="radio"/> a) $-2\sin 2x$ | b) $2\sin 2x$ | c) $2\cos x$ | d) $-2\cos x$ |
|---|---------------|--------------|---------------|

2- If $y = \cot(x)$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | | | |
|--|-----------------------|-----------------|---------------|
| <input checked="" type="radio"/> a) $-\csc^2(x)$ | b) $-\csc(x) \cot(x)$ | c) $-\cot^2(x)$ | d) $-\cot(x)$ |
|--|-----------------------|-----------------|---------------|

3- If $y = \sin^2(2x)$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | | | |
|-------------------------|---------------|---|-----------------------|
| a) $2\sin 2x(\cos 2x)2$ | b) $4\sin 2x$ | <input checked="" type="radio"/> c) $2\sin 2x(\cos 2x)$ | d) $2\sin(x) \cos(x)$ |
|-------------------------|---------------|---|-----------------------|

4- If $y = \sin^{-1}(x)$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | | | |
|-----------------------------|------------------------------|----------------------------|-----------------------------|
| a) $\frac{1}{\sqrt{1-x^2}}$ | b) $\frac{-1}{\sqrt{1-x^2}}$ | c) $\frac{1}{\sqrt{1-2x}}$ | d) $\frac{-1}{\sqrt{1-2x}}$ |
|-----------------------------|------------------------------|----------------------------|-----------------------------|

5- If $y = \tan^{-1}(e^{x^3})$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | | | |
|---|------------------------------|------------------------------|---|
| <input checked="" type="radio"/> a) $\frac{1}{1+x^3}$ | b) $\frac{-1}{\sqrt{1-x^3}}$ | c) $\frac{1}{1+(e^{x^3})^2}$ | d) $\frac{1}{1+(e^{x^3})^2} \cdot e^{x^3} \cdot 3x^2$ |
|---|------------------------------|------------------------------|---|

6- If $y = x^3 \sin^{-1}(x)$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | |
|--|---|
| a) $x^3 \cdot \frac{1}{1+x^2}$ | b) $x^3 \cdot \frac{1}{\sqrt{1-x^2}}$ |
| c) $3x^2 \sin^{-1}(x) - 3x^2 \frac{1}{\sqrt{1-x^2}}$ | d) $3x^2 \sin^{-1}(x) + x^3 \frac{1}{\sqrt{1-x^2}}$ |

7- If $y = 6x^3 - 9x + 4$, then $\frac{dy}{dx} = \dots\dots\dots$

- | | | | |
|--------------|----------------|----------------|---|
| a) $18x - 9$ | b) $20x^2 + 9$ | c) $18x^2 + 9$ | <input checked="" type="radio"/> d) $18x^2 - 9$ |
|--------------|----------------|----------------|---|

8- If $y = 2t^4 - 10t^2 + 13$, then $\frac{dy}{dx} = \dots\dots\dots$

$8t^3 - 20t$



Mathematics

a) $8t^2 - 20t + 13$

b) $8t^3 - 2t + 13$

c) $8t^3 + 20t$

d) $8t^3 - 20t$

9- If $y = x(3x^2 - 9)$, then $\frac{dy}{dx} = \dots\dots\dots$

a) $9x - 9$

b) $9x^3 - 9$

c) $6x^2 - 6$

d) $9x^2 - 9$

10- If $y = x^3 \tan x$, then $\frac{dy}{dx} = \dots\dots\dots$

a) $X^3 \sec^2 x$

b) $3x^2 \tan x$

c) $X^3 \sec^2 x + 3x^2 \tan x$

d) $X^3 \sec x + 3x^2 \tan x$

11- If $y = (\sin x)^{-1}$, then $\frac{dy}{dx} = \dots\dots\dots$

a) $\cos x$

b) $-\cos x$

c) $-(\sin x)^{-2} \cdot (\cos x)$

d) $-(\sin x)^{-1} \cdot (\cos x)$

* 12- The domain of the function $y = x^2 - 4$ is $\dots\dots\dots$

a) $R - \{-4\}$

b) $R - \{4\}$

c) R

d) ∞

13- The range of the function $y = \frac{1}{x+2}$ is $\dots\dots\dots$

a) R

b) $R - \{2\}$

c) $R - \{0\}$

d) ∞

14- The domain of the function $y = (x-2)^3 + 1$ is $\dots\dots\dots$

a) R

b) $R - \{2\}$

c) $R - \{-2\}$

d) ∞

15- The range of the function $y = 1 - 2^x$ is $\dots\dots\dots$

a) $]-\infty, 1[$

b) R

c) $R - \{2\}$

d) ∞

16- The domain of the function $y = \ln x$ is $\dots\dots\dots$

a) $]0, \infty[$

b) $]-\infty, 0[$

c) R

d) ∞

17- $\ln\left(\frac{x}{y}\right) = \dots\dots\dots$

a) $\ln x - \ln y$

b) $\ln x + \ln y$

c) $\ln(xy)$

d) 1

* 18- The function $f(x) = \begin{cases} \frac{x^2-4}{x-2} & x \neq 2 \\ 5 & x = 2 \end{cases}$ is continuous at $x = 2$.

a) True

b) False

19- $\lim_{x \rightarrow 0} \frac{\sin 2\sqrt{x}}{\sqrt{x}} = \dots\dots\dots$

a) 1

b) 2

c) 3

d) 4

* 20- The function $f(x) = \sqrt[3]{x} + |x|$ is continuous at $x = -8$.

a) True

b) False

21- The amplitude of the function $f(x) = -4 \tan 3x$ is $\dots\dots\dots$



Mathematics

- 22- The period of the function $f(x) = 3 \sin x$ is
a) 4 b) $\frac{\pi}{3}$ c) $\frac{2\pi}{3}$ d) ∞
- 23- $\lim_{x \rightarrow \infty} (1 + \frac{1}{x})^x$ is
a) 3 b) $\frac{\pi}{2}$ c) π ~~d) 2π~~
- 24- $\lim_{x \rightarrow -3} \frac{x^2+x-6}{x+3}$ is
a) 0 b) ∞ c) 1 ~~d) e~~
- 25- $\lim_{x \rightarrow 1} \frac{x^3-1}{x-1}$ is
a) 0 e) ∞ f) $-\infty$ ~~g) -5~~
- 26- $\lim_{x \rightarrow 3} \frac{x^2+x-12}{x-3}$ is
a) 1 b) 2 c) 3 d) 0
- 27- $\sinh 2x = \dots\dots\dots$
a) $\cosh 2x - 1$ b) 1 c) $2 \sinh x \cosh x$ d) $\cos^2 x$
- 28- $2 \cos^2 x - 1 = \dots\dots\dots$
a) $\cos 2x$ b) $\sin 2x$ c) $2 \sin^2 x$ ~~d) $2 \cos^2 x$~~
- 29- $\sin^2 x + \cos^2 x = \dots\dots\dots$
a) 1 b) $\cos 2x$ c) $2 \sin^2 x$ d) $\cos 2x$
- 30- The amplitude of the function $f(x) = -2 \cos 3x$ is ...
a) -2 b) $\frac{2\pi}{3}$ ~~c) 2~~ d) $\frac{\pi}{3}$