



Evolutionary Computation
Assignment 1 report

By:

| | |
|----------|--------------|
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Exercise 1:

We allocated the six exercises to six teammates and we chose Hao Zhang as our team leader to manage the task completing progress.

Hao zhang(Exercise 2):

- Followed the instructions in exercise 2 we wrote a class called TSPProblem in the file :TspProblem.py
- Structure design and implete
- Bugs fixing
- Integrating codes together

Zibo Lin (Exercise 3):

- Implement a possible solution to the TSP as a permutation of given cities under the class “Individual”
- Implement a class “Population” for representing a population which is a set of individuals.
- Implement functions to evaluate the quality of a solution

Xiaoman Li (Exercise 4):

- Do the research of different approaches to mutation and crossover.
- Implement functions of mutation operators (insert, swap, inversion, scramble) for permutations.
- Implement functions of crossover operators include Order Crossover, PMX Crossover, Cycle Crossover, and Edge Recombination for permutations.
- Edit the parameter and return of the functions to satisfy the requirements of the teammate who did the integration.

Yiyuan Tang (Exercise 5):

- Implement functions of selection methods including fitness-proportional, tournament selection, and elitism.
- Implement functions to calculate the fitness of the individual, which is part of the Class Population.

Hanyue Zhang(Exercise 6):

- Design three evolutionary algorithms.
- Prepare and report the results in exercise 6 (Experiment 1 and 2) and exercise 7.

Xiaocen Guo(Exercise 7):

Do research about GuoTao algorithm in the report

Cooperate with Hao Zhang to implement the algorithm

Learn how to draw the route graph and trend chart in python

Prepare for assignment 1 report

Exercise 6 (Design three evolutionary algorithms and justify the design choices)

From the perspective of time complexity, we get rid of insert and scramble mutation operators. Then we test all the combinations of mutation and crossover operators with the same population size and generations three times. The average result shows that inversion with edge recombination ranked first, inversion with order crossover ranked second, inversion with cycle crossover ranked third. These three algorithms perform best, the best algorithm nearly reaches the optimum result in experiment 1. We choose elitism as the selection method because it performs best.

| | Algorithm 1 | Algorithm 2 | Algorithm 3 |
|------------------|-----------------|-----------------|--------------------|
| Mutation method | Inversion | inversion | Inversion |
| Mutation rate | 0.5 | 0.6 | 0.7 |
| Crossover method | Order crossover | Cycle crossover | edge recombination |

| | | | |
|------------------|---------|---------|---------|
| Crossover rate | 0.5 | 0.7 | 0.6 |
| Selection method | Elitism | Elitism | Elitism |

Exercise 6 (experiment 1)

| | | | Algorithm 1(inversion, order crossover) | | | Algorithm 2(inversion, cycle crossover) | | | Algorithm 3(inversion, edge recombination) | | |
|--------|-----------------|----------------|---|----------|----------|---|----------|----------|--|----------|----------|
| files | Population size | Optimum result | 5000 generation | 10000 | 20000 | 50000 | 100000 | 200000 | 500000 | 1000000 | 2000000 |
| eil51 | 10 | 429.982 | 455.674 | 455.1750 | 443.2426 | 448.9347 | 449.8734 | 445.2531 | 451.3946 | 450.1342 | 450.2942 |
| | 20 | | 461.320 | 456.0051 | 453.2167 | 470.3583 | 470.6584 | 469.4213 | 461.4598 | 461.0335 | 460.1365 |
| | 50 | | 441.7001 | 441.9751 | 443.4701 | 468.0832 | 471.9083 | 468.2319 | 452.3259 | 450.2475 | 450.7421 |
| | 100 | | 455.7176 | 457.7134 | 449.4963 | 471.2364 | 468.3291 | 469.2312 | 452.7684 | 454.2301 | 449.2497 |
| eil76 | 10 | 545.387 | 591.8350 | 595.5649 | 582.0766 | 599.8177 | 603.6354 | 600.9862 | 591.6302 | 599.5349 | 593.7202 |
| | 20 | | 593.3220 | 598.5491 | 605.1218 | 605.6842 | 607.3567 | 601.2410 | 574.2370 | 588.9832 | 600.3587 |
| | 50 | | 593.2882 | 590.6419 | 589.3679 | 607.6929 | 605.2342 | 600.3198 | 576.6843 | 574.9553 | 573.9753 |
| | 100 | | 592.8128 | 590.2388 | 589.0371 | 607.0211 | 601.4392 | 600.2851 | 582.8589 | 580.3132 | 579.0932 |
| eil101 | 10 | 642.315 | 761.5288 | 733.9799 | 722.7949 | 763.1825 | 767.2343 | 766.9887 | 737.4648 | 730.8723 | 694.5713 |

| | | | | | | | | | | | |
|-------------|-----|---------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|---------------------|--------------------|
| | 20 | | 723.2 923 | 722.7 128 | 722.9 789 | 759.8 865 | 762.0 124 | 760.9 786 | 703.6 841 | 700.3 129 | 685.8 391 |
| | 50 | | 707.5 955 | 710.7 127 | 709.9 789 | 755.0 217 | 759.9 886 | 760.2 304 | 709.8 358 | 703.8 719 | 684.3 12 |
| | 100 | | 706.2 211 | 709.2 876 | 707.0 981 | 765.0 134 | 766.3 460 | 768.3 142 | 695.2 191 | 691.2 123 | 686.7 131 |
| st70 | 10 | 678.5 97 | 729.2 717 | 710.0 803 | 706.1 23 | 724.7 722 | 727.1 832 | 722.9 153 | 700.6 313 | 702.2 543 | 700.2 126 |
| | 20 | | 700.5 051 | 702.6 326 | 704.0 150 | 720.2 291 | 722.9 871 | 721.0 863 | 699.2 542 | 700.0 868 | 706.0 585 |
| | 50 | | 786.0 234 | 714.0 274 | 705.8 712 | 743.9 916 | 729.8 549 | 722.9 227 | 752.0 078 | 698.2 57 | 689.0 624 |
| | 100 | | 714.9 009 | 709.9 102 | 705.7 153 | 719.3 315 | 722.6 122 | 720.9 689 | 687.0 928 | 691.4 753 | 688.9 212 |
| kroa1 00 | 10 | 2128 5.443 | 2691 5.909 4 | 24119 .8808 | 2380 2.886 3 | 2754 4.512 3 | 2743 1.721 5 | 2489 4.263 8 | 2457 3.741 3 | 2486 9.339 6 | 2212 0.610 3 |
| | 20 | | 2367 3.678 6 | 2364 7.690 1 | 2362 3.941 0 | 2521 0.519 2 | 2610 0.418 2 | 2538 3.729 0 | 2394 5.035 4 | 2353 3.601 2 | 2299 3.817 1 |
| | 50 | | 2384 1.442 3 | 2393 2.497 5 | 2382 1.998 5 | 25112 .9152 | 2539 8.309 7 | 2512 0.329 9 | 2374 1.442 3 | 2358 86.21 95 | 2232 1.860 3 |
| | 100 | | 2378 8.252 7 | 2383 1.965 1 | 2365 2.749 2 | 2487 2.091 2 | 2485 6.239 5 | 2466 7.389 2 | 2210 1.886 2 | 2238 8.285 4 | 2218 4.064 2 |
| kroc1 00 | 10 | 2075 0.762 | 2761 4.938 8 | 2609 3.112 5 | 2470 6.883 4 | 2964 6.468 | 2975 4.347 | 2788 1.091 | 2470 6.999 7 | 2364 8.926 8 | 2236 2.843 3 |
| | 20 | | 2477 9.570 1 | 24116 .7072 | 2406 5.112 | 2798 2.101 7 | 2756 4.076 9 | 2690 3.739 2 | 2372 3.848 7 | 2245 1.398 9 | 2216 1.931 3 |
| | 50 | | 2334 3.520 | 2339 7.762 | 23116 .7072 | 2557 0.062 | 2598 1.986 | 2523 7.821 | 2356 1.901 | 2387 5.213 | 2269 0.981 |

| | | | | | | | | | | | |
|--------------|----|--------------------|----------------------|----------------------|----------------------|-----------------------|-----------------------|----------------------|----------------------|----------------------|----------------------|
| | | | 9 | 5 | | 3 | 2 | 9 | 7 | 6 | 3 |
| lin105 | 10 | 1438 2.99 | 1848 3.964 3 | 1655 2.281 7 | 1573 6.165 2 | 2130 2.081 7 | 2122 9.701 9 | 2098 7.632 9 | 1640 4.133 9 | 1625 6.452 3 | 1564 6.152 5 |
| | 20 | | 1674 0.862 3 | 1635 2.327 | 1669 8.712 | 1889 2.072 5 | 1902 3.786 5 | 1865 4.986 0 | 1643 3.760 8 | 1596 6.239 7 | 1573 2.140 3 |
| pcb44 2 | 10 | 5078 3.547 5 | 2070 76.23 42 | 1799 13.83 2 | 11040 7.669 0 | 2435 82.10 94 | 2438 76.70 57 | 2395 61.56 36 | 1819 28.56 62 | 1328 84.97 34 | 9257 6.750 21 |
| pr239 2 | 10 | 3780 62.82 6 | 8014 876.2 355 | 8934 352.9 842 | 8023 741.2 468 | 1009 8234. 2482 | 1042 5256. 3569 | 9910 463.3 985 | 7341 582.1 245 | 7598 342.3 414 | 7324 751.4 535 |
| usa13 509 | 10 | - | - | - | - | - | - | - | - | - | - |

Exercise 6 (experiment 2)

Best algorithm: algorithm 3

Mutation method: Inversion

Mutation rate: 0.7

Crossover method: Edge recombination

Crossover rate: 0.6

Selection method: Elitism

50 population size 20000 generation

| files | 1st result | 2nd result | 3rd result | 4th result | Average cost | Standard deviation |
|--------|------------|------------|------------|------------|--------------|--------------------|
| eil51 | 450.7421 | 453.1220 | 449.8761 | 458.2390 | 452.9948 | 3.2526 |
| eil76 | 573.9753 | 586.2384 | 579.3183 | 585.6321 | 581.2910 | 5.0182 |
| eil101 | 684.312 | 698.0735 | 695.3288 | 685.3981 | 690.7781 | 6.0142 |

| | | | | | | |
|----------|------------------|------------------|------------------|------------------|-----------------|-----------------|
| st70 | 689.0624 | 710.2681 | 698.6179 | 688.2096 | 696.5395 | 8.9175 |
| kroa100 | 23813.346 2 | 22661.359 7 | 22321.860 3 | 22893.312 5 | 22922.469 6 | 553.0418 |
| kroc100 | 22942.616 2 | 22690.981 3 | 23252.241 9 | 22809.540 7 | 22923.845 0 | 209.4563 |
| lin105 | 15609.103 2 | 16043.987 3 | 15462.724 5 | 15689.540 7 | 15701.338 9 | 213.8874 |
| pcb442 | 92134.873 0 | 95598.669 0 | 93126.124 5 | 93985.390 0 | 93711.264 1 | 1271.4609 |
| pr2392 | 7324751.4 535 | 7529834.0 988 | 7387452.3 582 | 7609284.2 418 | 7462830.5 38 | 112567.61 09 |
| usa13509 | - | - | - | - | - | - |

Exercise 7 Inver-over

Population size 50, generation size 20000

| | eil51 | eil76 | eil10 1 | st70 | kroa 100 | kroc 100 | lin10 5 | pcb4 42 | pr23 92 _(1 hour limit) | usa1 3509 |
|---|--------------|--------------|---------------|---------------|----------------|----------------|----------------|-----------------|--|--------------|
| 1 | 446.87 16 | 667.93 20 | 1076.6 803 | 701.24 350 | 43071. 4110 | 42871. 9391 | 31920. 7474 | 48062 5.3978 | 14600 043.13 57 | |
| 2 | 448.14 03 | 670.86 75 | 1079.4 812 | 875.09 12 | 44210. 2471 | 43494. 8901 | 31303. 6728 | 48152 3.6374 | 14607 469.3 | |
| 3 | 447.14 98 | 687.74 02 | 1085.6 390 | 854.50 33 | 42645. 0825 | 42361. 0414 | 30939. 3151 | 47557 1.0353 | 14559 996.1 | |
| 4 | 435.12 44 | 677.29 85 | 1082.6 043 | 863.39 10 | 41290. 2570 | 42981. 333 | 31207. 8322 | 47172 1.8069 | 14654 229.3 | |
| 5 | 436.64 30 | 689.16 97 | 1075.2 534 | 817.19 24 | 42183. 2592 | 43644. 2326 | 31312. 5914 | 47272 2.9834 | 14585 883.4 | |
| 6 | 445.43 55 | 691.17 03 | 1096.1 760 | 850.53 64 | 41975. 2089 | 42887. 3998 | 32505. 3384 | 47345 3.4325 | 14607 469.26 6 | |
| 7 | 447.69 12 | 642.19 49 | 1060.3 765 | 844.34 22 | 42389. 8408 | 42675. 3845 | 31427. 4958 | 48029 1.5887 | 14559 996.14 | |

| | | | | | | | | | | |
|----|--------------|--------------|---------------|--------------|----------------|----------------|----------------|-----------------|-----------------------|--|
| | | | | | | | | | 92 | |
| 8 | 445.75 82 | 703.97 80 | 1058.3 488 | 798.90 63 | 42123. 8530 | 43103. 9874 | 30989. 4788 | 47199 5.3492 | 14578 507.80 54 | |
| 9 | 452.08 05 | 665.22 39 | 1060.7 568 | 863.23 79 | 43001. 4832 | 42357. 0564 | 31406. 3875 | 47386 2.4925 | 14688 736.34 24 | |
| 10 | 442.20 41 | 707.69 06 | 1076.3 461 | 871.72 36 | 42586. 0842 | 42769. 4573 | 31748. 3259 | 47954 2.5685 | 14548 834.59 23 | |
| 11 | 448.25 75 | 688.63 28 | 1080.3 477 | 832.89 43 | 42886. 8391 | 42324. 2263 | 30639. 5939 | | | |
| 12 | 444.87 08 | 711.63 57 | 1078.2 389 | 842.57 11 | 42761. 7545 | 43550. 3348 | 31571. 7785 | | | |
| 13 | 445.96 35 | 686.35 72 | 1075.9 826 | 800.12 02 | 42355. 3487 | 42579. 3667 | 30758. 0864 | | | |
| 14 | 447.23 41 | 690.23 41 | 1083.4 588 | 821.45 94 | 42618. 5381 | 43520. 6751 | 31592. 4691 | | | |
| 15 | 448.90 43 | 687.33 10 | 1088.6 081 | 886.27 41 | 42819. 4278 | 42311. 6781 | 31348. 2574 | | | |
| 16 | 448.27 94 | 701.32 48 | 1079.2 456 | 846.56 44 | 41706. 4521 | 42578. 3459 | 31698. 4064 | | | |
| 17 | 446.95 27 | 702.34 58 | 1084.8 943 | 833.99 03 | 41261. 4788 | 43499. 2681 | 31712. 6709 | | | |
| 18 | 445.35 77 | 689.61 94 | 1073.2 954 | 810.28 17 | 42854. 4676 | 42497. 0251 | 30825. 6508 | | | |
| 19 | 445.16 08 | 707.12 36 | 1077.2 418 | 883.19 52 | 41588. 3567 | 43417. 3297 | 30910. 6254 | | | |
| 20 | 449.04 25 | 688.70 17 | 1089.4 345 | 799.08 87 | 43011. 0187 | 42312. 4561 | 31943. 5253 | | | |
| 21 | 450.25 39 | 682.59 31 | 1065.3 783 | 845.36 28 | 42299. 5673 | 42886. 3401 | 31873. 2459 | | | |
| 22 | 447.24 45 | 691.27 63 | 1078.2 349 | 867.34 21 | 42801. 2958 | 42655. 2976 | 31873. 2547 | | | |
| 23 | 448.54 42 | 711.63 77 | 1083.2 636 | 812.64 24 | 43350. 4496 | 42318. 6723 | 31567. 0732 | | | |
| 24 | 446.24 75 | 703.67 32 | 1087.2 367 | 843.15 73 | 43152. 6044 | 43012. 4595 | 31662. 3361 | | | |
| 25 | 447.35 29 | 700.70 42 | 1069.3 426 | 850.88 44 | 42957. 5494 | 43224. 9835 | 30883. 4561 | | | |

| | | | | | | | | | | |
|-----------------------|--------------|--------------|---------------|--------------|----------------|----------------|----------------|-----------------|-----------------|--|
| 26 | 450.92 01 | 692.47 59 | 1060.4 577 | 842.49 61 | 42866. 3578 | 42719. 8410 | 30882. 4982 | | | |
| 27 | 445.78 91 | 687.45 26 | 1080.3 457 | 827.43 29 | 42356. 9876 | 43397. 5378 | 31093. 2884 | | | |
| 28 | 448.23 07 | 688.09 21 | 1076.3 453 | 844.98 87 | 42147. 2357 | 42831. 7369 | 32015. 4321 | | | |
| 29 | 447.79 08 | 702.02 23 | 1072.4 250 | 810.24 72 | 42811. 8762 | 43512. 4589 | 31849. 3327 | | | |
| 30 | 453.61 06 | 679.75 39 | 1059.2 385 | 848.09 87 | 41226. 2389 | 42597. 3488 | 31639. 3591 | | | |
| Average cost | 446.77 02 | 689.87 51 | 1076.4 892 | 836.30 86 | 42510. 3524 | 42896. 4701 | 31436. 7175 | 47613 1.0292 | 14599 116.54 | |
| Standard deviation | 3.7161 | 15.070 7 | 9.7391 | 35.304 6 | 662.96 16 | 443.47 34 | 452.26 04 | 3930.1 918 | 43967. 7211 | |

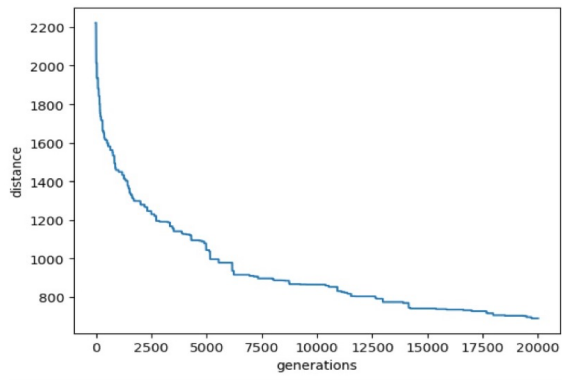
Reflection:

During the group assignment process, our final goal was to design and implement the algorithm completely to get the optimal solution. However, in the testing period, we noticed that the running time for a 20000 generations' result will take 60000 minutes. We considered it as a normal situation and we decided to minimise the generation to get results as soon as possible. Two days before the deadline, we found that it is reasonable to improve the algorithm performance to reduce the running time, but it is a bit late to calculate all the required results. The remaining time is only enough for us to run once for each file. Learned from this experience, the assignment is supposed to start early to leave more time for the testing period.

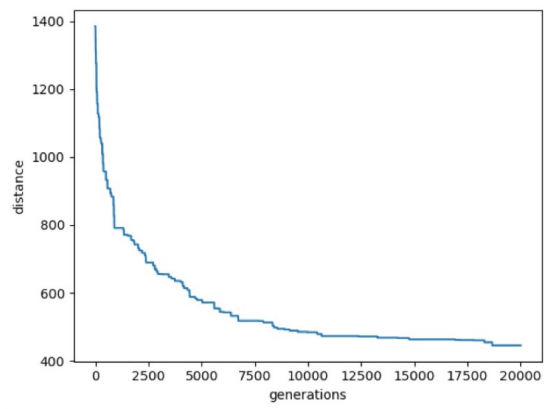
PLOTS

Exercise 7 plots:

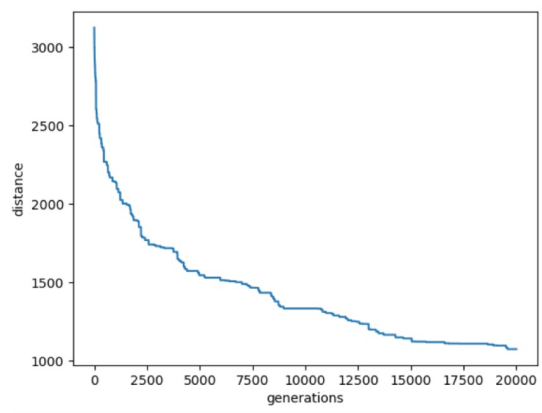
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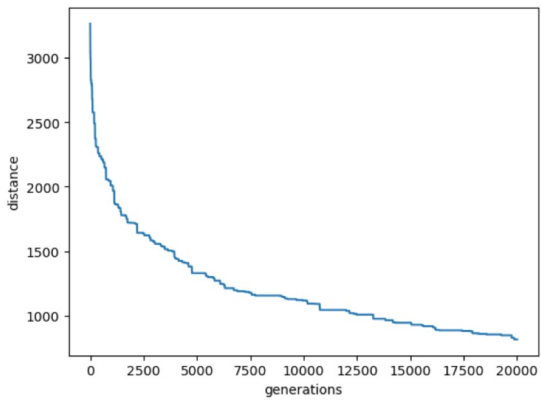
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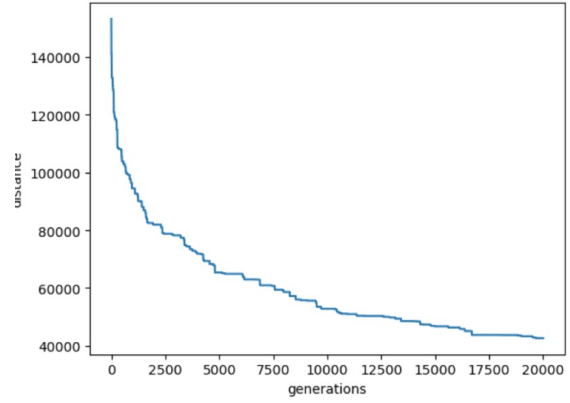
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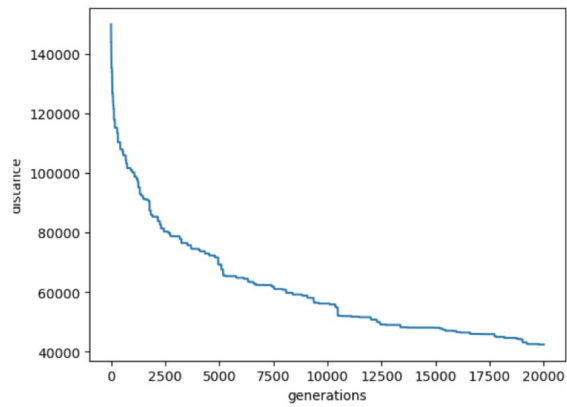
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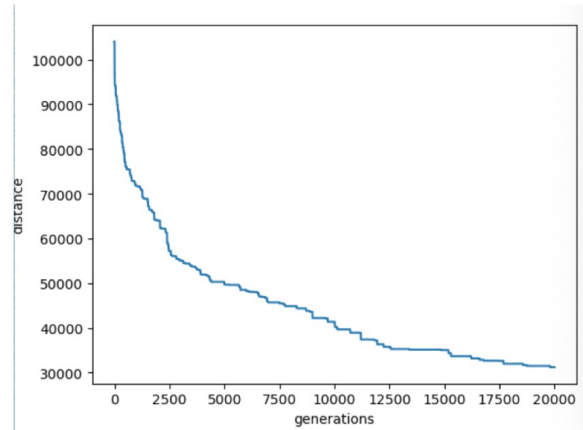
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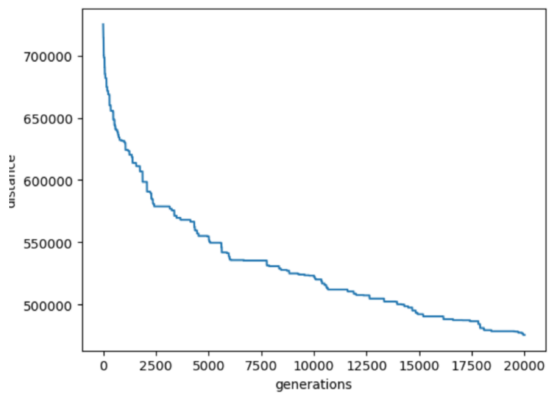
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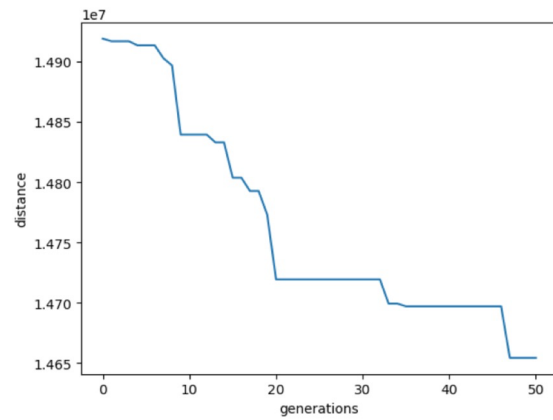
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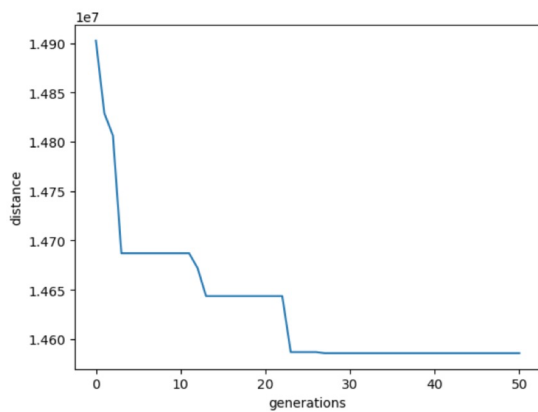
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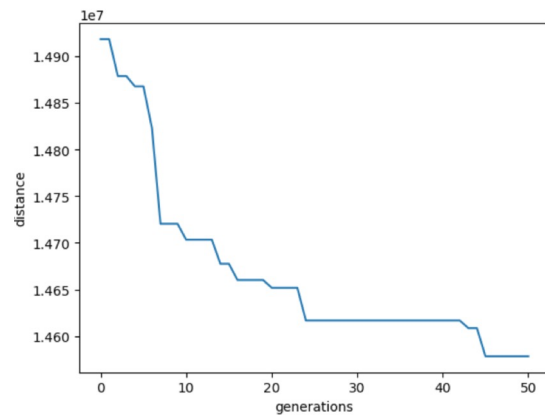
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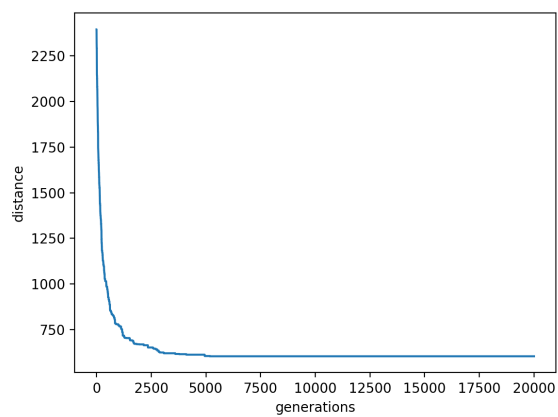
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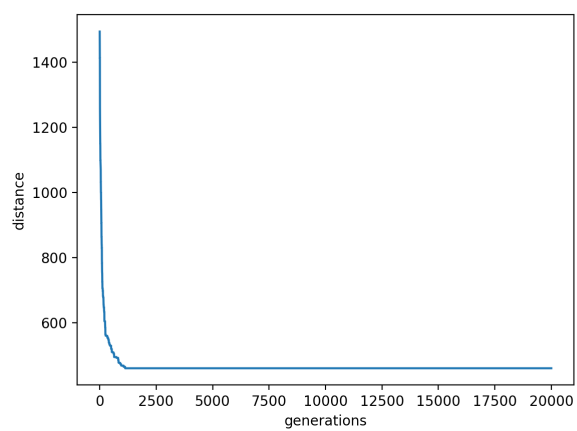
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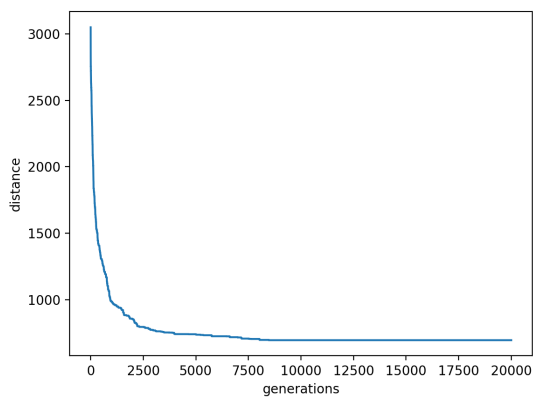
Exercise 6 Best algorithm plots



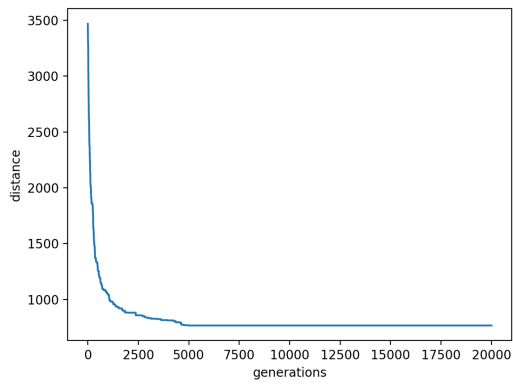
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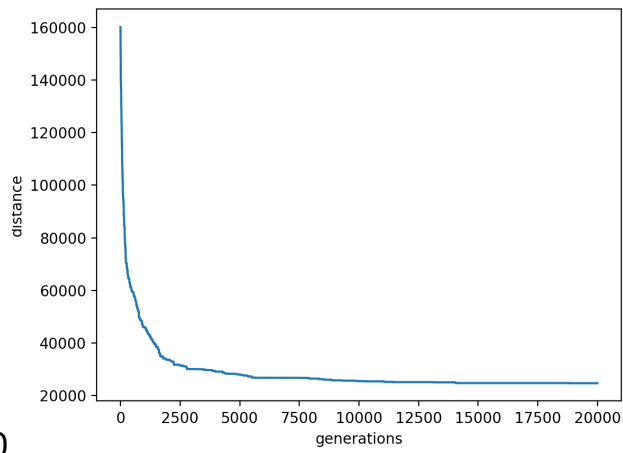
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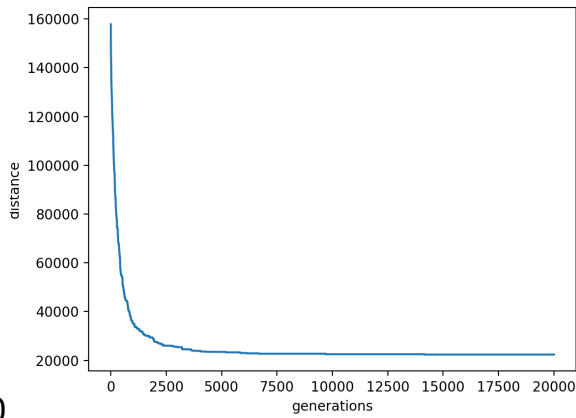
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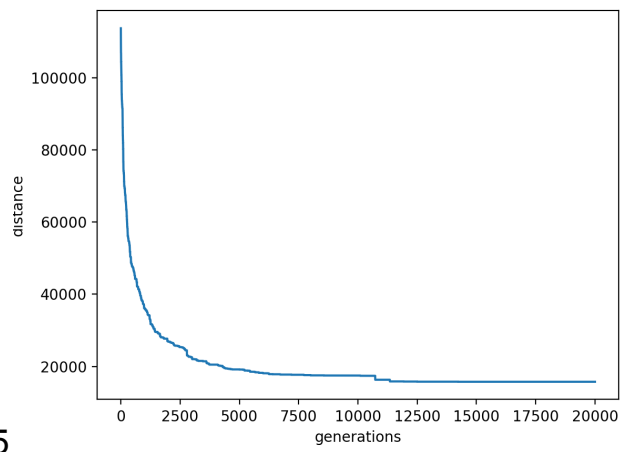
st70



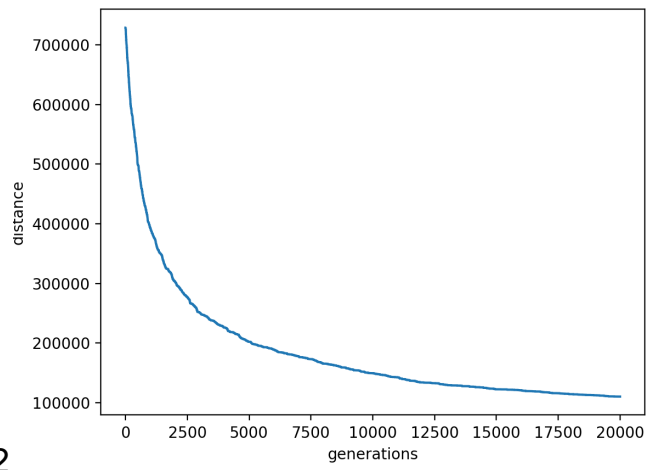
kroa100



kroc100



lin105



pcb442