The Weighted Mean and the Median: Takeaways

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Syntax

• Computing the weighted mean for a distribution distribution_X with weights weights_X :

```
### Using numpy ###
from numpy import average
weighted_mean_numpy = average(distribution_X, weights = weights_X)

### By coding a function from scratch ###
def weighted_mean(distribution, weights):
    weighted_sum = []
    for mean, weight in zip(distribution, weights):
        weighted_sum.append(mean * weight)

    return sum(weighted_sum) / sum(weights)

weighted_mean_function = weighted_mean(distribution_X, weights_X)

    • Finding the median for a Series :

median = Series.median()

    • Finding the median for any numerical array:

from numpy import median
median_numpy = median(array)
```

Concepts

• When data points bear different weights, we need to compute **the weighted mean**. The formulas for the weighted mean are the same for both samples and populations, with slight differences in notation:

$$ar{x} = rac{\displaystyle\sum_{i=1}^{n} x_i w_i}{\displaystyle\sum_{i=1}^{n} w_i} = rac{x_1 w_1 + x_2 w_2 + ... + x_n w_n}{w_1 + w_2 + ... + w_n}$$

$$\mu = rac{\displaystyle \sum_{i=1}^{N} x_i w_i}{\displaystyle \sum_{i=1}^{N} w_i} = rac{x_1 w_1 + x_2 w_2 + ... + x_n w_N}{w_1 + w_2 + ... + w_N}$$

- It's difficult to define the median algebraically. To compute the median of an array, we need to:
 - Sort the values in an ascending order.
 - Select the middle value as the median. If the distribution is even-numbered, we select the middle two values, and then compute their mean the result is the median.
- The median is ideal for:
 - Summarizing numerical distributions that have **outliers**.
 - Open-ended distributions.
 - Ordinal data.

Resources

- An intuitive introduction to the weighted mean.
- <u>The Wikipedia entry</u> on the weighted mean.
- The Wikipedia entry on the median.
- Useful documentation:
 - numpy.average()
 - Series.median()
 - numpy.median()

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