LORA: LOW-RANK ADAPTATION OF LARGE LANGUAGE MODELS

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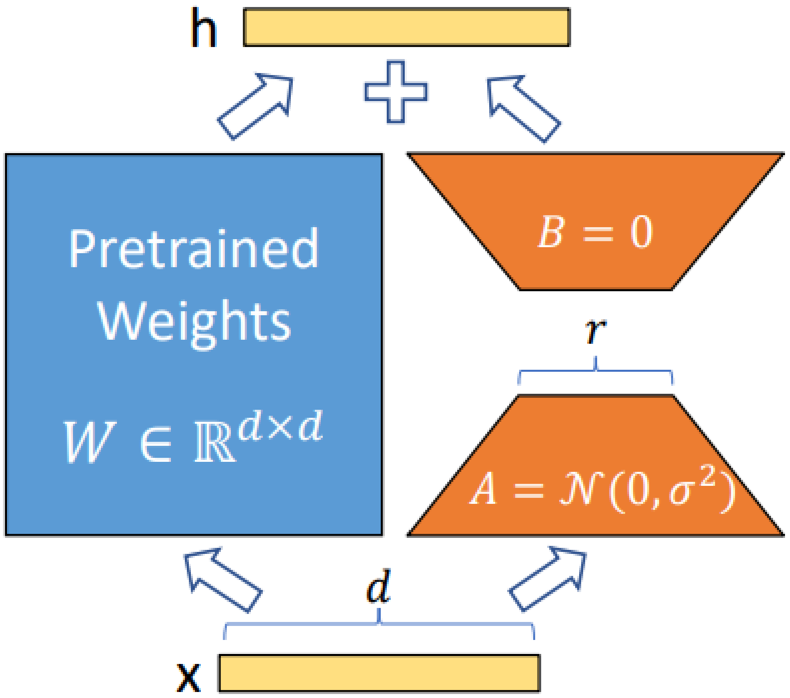
Background

- Personalized model: heterogenous distribution/ multiple downstream tasks
- Full Finetuning: updating all parameters of pre-trained model
  - Pretrained model $P_{\Phi_0}(y|x)$ with parameter Φ_0, update Φ_0 to $\Phi_0 + \Delta\Phi$
  - Dimension of $\Delta\Phi$ = Dimension of Φ , too many parameters to update
  - Learn a different $\Delta\Phi$ for each downstream task
- Existing solutions
  - Adding adapter layers: introduce inference latency
  - Prompt tuning: hard to directly optimize the prompt

LORA

- Inspiration: The change in weights ΔW has a low intrinsic rank. We can train some dense layers by optimizing rank decomposition matrices of the dense layers' change.
- Update parameters:
  - $\mathrm{W_0 + \Delta W = W_0 + BA}$
  - $\mathrm{B} \in R^{d\times r}, A \in R^{r\times k}, r \ll \min(d, k)$
  - $O\big(r(d+k)\big) \ll O(dk)$
- Training A and B
  - Initialization: A= random Gaussian, B=zeros
  - Forward pass: $\mathrm{h = W_0x + \Delta Wx = W_0}x + \mathrm{B}A\mathrm{x}$
  - Use Adam Adapter to train A and B



Applying LORA to Transformer

- Only adapting the attentions weights (W_q, W_k, W_v, W_o) for downstream tasks, freeze MLP layers.
- Benefits:
  - Reduce memory and storage usage (VRAM, checkpoint size, GPUs)
  - Easy to switch between tasks by only changing LORA parameters instead of full parameters
- Limitations:
  - If we choose to absorb A and B into W to eliminate inference latency, it is not straight forward to batch inputs to different tasks with different A and B

Experiments

- Evaluate downstream task performance of Lora and other adaptation method on different models
- Lora trains fewer parameters without sacrificing too much accuracy

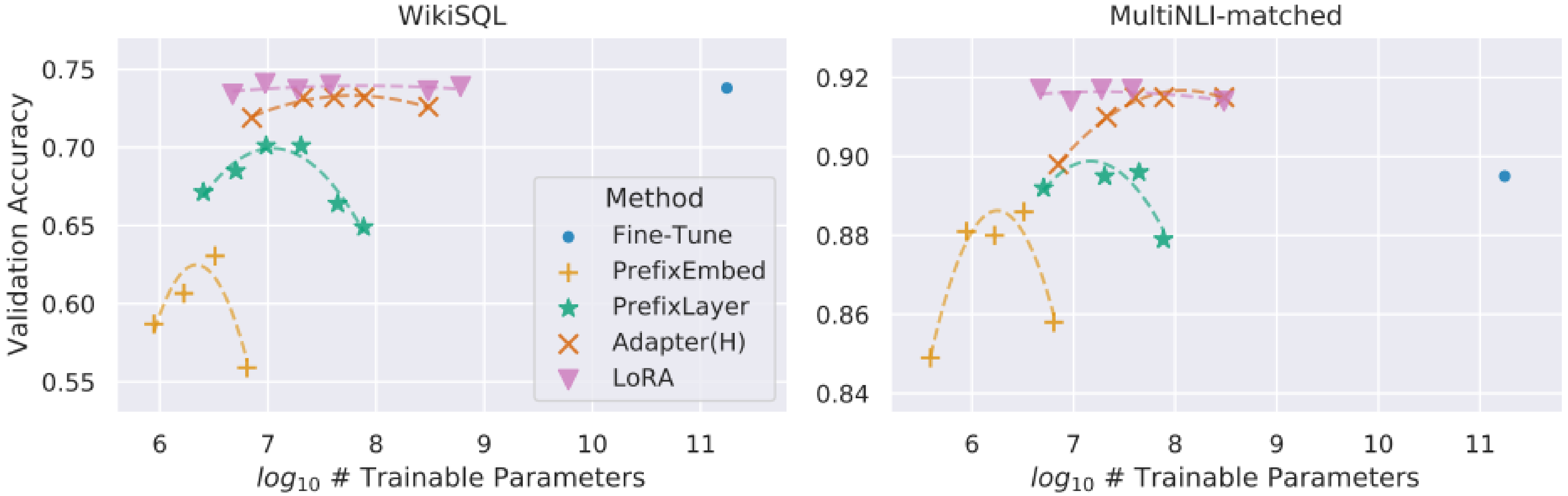
Model & Method	# Trainable Parameters	MNLI	SST-2	MRPC	CoLA	QNLI	QQP	RTE	STS-B	Avg.
RoB_{base} (FT)*	125.0M	**87.6**	94.8	90.2	**63.6**	92.8	**91.9**	78.7	91.2	86.4
RoB_{base} (BitFit)*	0.1M	84.7	93.7	**92.7**	62.0	91.8	84.0	81.5	90.8	85.2
RoB_{base} (Adpt^{D})*	0.3M	$87.1_{\pm.0}$	$94.2_{\pm.1}$	$88.5_{\pm1.1}$	$60.8_{\pm.4}$	$93.1_{\pm.1}$	$90.2_{\pm.0}$	$71.5_{\pm2.7}$	$89.7_{\pm.3}$	84.4
RoB_{base} (Adpt^{D})*	0.9M	$87.3_{\pm.1}$	$94.7_{\pm.3}$	$88.4_{\pm.1}$	$62.6_{\pm.9}$	$93.0_{\pm.2}$	$90.6_{\pm.0}$	$75.9_{\pm2.2}$	$90.3_{\pm.1}$	85.4
RoB_{base} (LoRA)	0.3M	$87.5_{\pm.3}$	$\mathbf{95.1}_{\pm.2}$	$89.7_{\pm.7}$	$63.4_{\pm1.2}$	$\mathbf{93.3}_{\pm.3}$	$90.8_{\pm.1}$	$\mathbf{86.6}_{\pm.7}$	$\mathbf{91.5}_{\pm.2}$	**87.2**
$\text{RoB}_{\text{large}}$ (FT)*	355.0M	90.2	**96.4**	**90.9**	68.0	94.7	**92.2**	86.6	92.4	88.9
$\text{RoB}_{\text{large}}$ (LoRA)	0.8M	$\mathbf{90.6}_{\pm.2}$	$96.2_{\pm.5}$	$\mathbf{90.9}_{\pm1.2}$	$\mathbf{68.2}_{\pm1.9}$	$\mathbf{94.9}_{\pm.3}$	$91.6_{\pm.1}$	$\mathbf{87.4}_{\pm2.5}$	$\mathbf{92.6}_{\pm.2}$	**89.0**
$\text{RoB}_{\text{large}}$ (Adpt^{P})†	3.0M	$90.2_{\pm.3}$	$96.1_{\pm.3}$	$90.2_{\pm.7}$	$\mathbf{68.3}_{\pm1.0}$	$\mathbf{94.8}_{\pm.2}$	$\mathbf{91.9}_{\pm.1}$	$83.8_{\pm2.9}$	$92.1_{\pm.7}$	88.4
$\text{RoB}_{\text{large}}$ (Adpt^{P})†	0.8M	$\mathbf{90.5}_{\pm.3}$	$\mathbf{96.6}_{\pm.2}$	$89.7_{\pm1.2}$	$67.8_{\pm2.5}$	$\mathbf{94.8}_{\pm.3}$	$91.7_{\pm.2}$	$80.1_{\pm2.9}$	$91.9_{\pm.4}$	87.9
$\text{RoB}_{\text{large}}$ (Adpt^{H})†	6.0M	$89.9_{\pm.5}$	$96.2_{\pm.3}$	$88.7_{\pm2.9}$	$66.5_{\pm4.4}$	$94.7_{\pm.2}$	$92.1_{\pm.1}$	$83.4_{\pm1.1}$	$91.0_{\pm1.7}$	87.8
$\text{RoB}_{\text{large}}$ (Adpt^{H})†	0.8M	$90.3_{\pm.3}$	$96.3_{\pm.5}$	$87.7_{\pm1.7}$	$66.3_{\pm2.0}$	$94.7_{\pm.2}$	$91.5_{\pm.1}$	$72.9_{\pm2.9}$	$91.5_{\pm.5}$	86.4
$\text{RoB}_{\text{large}}$ (LoRA)†	0.8M	$\mathbf{90.6}_{\pm.2}$	$96.2_{\pm.5}$	$\mathbf{90.2}_{\pm1.0}$	$68.2_{\pm1.9}$	$\mathbf{94.8}_{\pm.3}$	$91.6_{\pm.2}$	$\mathbf{85.2}_{\pm1.1}$	$\mathbf{92.3}_{\pm.5}$	**88.6**
DeB_{XXL} (FT)*	1500.0M	91.8	**97.2**	92.0	72.0	**96.0**	92.7	93.9	92.9	91.1
DeB_{XXL} (LoRA)	4.7M	$\mathbf{91.9}_{\pm.2}$	$96.9_{\pm.2}$	$\mathbf{92.6}_{\pm.6}$	$\mathbf{72.4}_{\pm1.1}$	$\mathbf{96.0}_{\pm.1}$	$\mathbf{92.9}_{\pm.1}$	$\mathbf{94.9}_{\pm.4}$	$\mathbf{93.0}_{\pm.2}$	**91.3**

Experiments

Model & Method	# Trainable Parameters	E2E NLG Challenge				
		BLEU	NIST	MET	ROUGE-L	CIDEr
GPT-2 M (FT)*	354.92M	68.2	8.62	46.2	71.0	2.47
GPT-2 M (Adapter^{L})*	0.37M	66.3	8.41	45.0	69.8	2.40
GPT-2 M (Adapter^{L})*	11.09M	68.9	8.71	46.1	71.3	2.47
GPT-2 M (Adapter^{H})	11.09M	67.3$_{\pm.6}$	8.50$_{\pm.07}$	46.0$_{\pm.2}$	70.7$_{\pm.2}$	2.44$_{\pm.01}$
GPT-2 M (FT^{Top2})*	25.19M	68.1	8.59	46.0	70.8	2.41
GPT-2 M (PreLayer)*	0.35M	69.7	8.81	46.1	71.4	2.49
GPT-2 M (LoRA)	0.35M	**70.4**$_{\pm.1}$	**8.85**$_{\pm.02}$	**46.8**$_{\pm.2}$	**71.8**$_{\pm.1}$	**2.53**$_{\pm.02}$
GPT-2 L (FT)*	774.03M	68.5	8.78	46.0	69.9	2.45
GPT-2 L (Adapter^{L})	0.88M	69.1$_{\pm.1}$	8.68$_{\pm.03}$	46.3$_{\pm.0}$	71.4$_{\pm.2}$	**2.49**$_{\pm.0}$
GPT-2 L (Adapter^{L})	23.00M	68.9$_{\pm.3}$	8.70$_{\pm.04}$	46.1$_{\pm.1}$	71.3$_{\pm.2}$	2.45$_{\pm.02}$
GPT-2 L (PreLayer)*	0.77M	70.3	8.85	46.2	71.7	2.47
GPT-2 L (LoRA)	0.77M	**70.4**$_{\pm.1}$	**8.89**$_{\pm.02}$	**46.8**$_{\pm.2}$	**72.0**$_{\pm.2}$	2.47$_{\pm.02}$

Experiments

- Scaling up to GPT-3
- LoRA matches or exceeds the fine-tuning baseline on all three datasets
- Not all methods benefit monotonically from having more trainable parameters



Which weight matrices in Transformer should we apply LORA to?

- Even we only adapt Lora to attention heads, there are still 4 kinds of weights to be finetuned. Which one is more appropriate?

	# of Trainable Parameters = 18M						
Weight Type	W_q	W_k	W_v	W_o	W_q, W_k	W_q, W_v	W_q, W_k, W_v, W_o
Rank r	8	8	8	8	4	4	2
WikiSQL ($\pm 0.5\%$)	70.4	70.0	73.0	73.2	71.4	**73.7**	**73.7**
MultiNLI ($\pm 0.1\%$)	91.0	90.8	91.0	91.3	91.3	91.3	**91.7**

What is the optimal rank r for LORA?

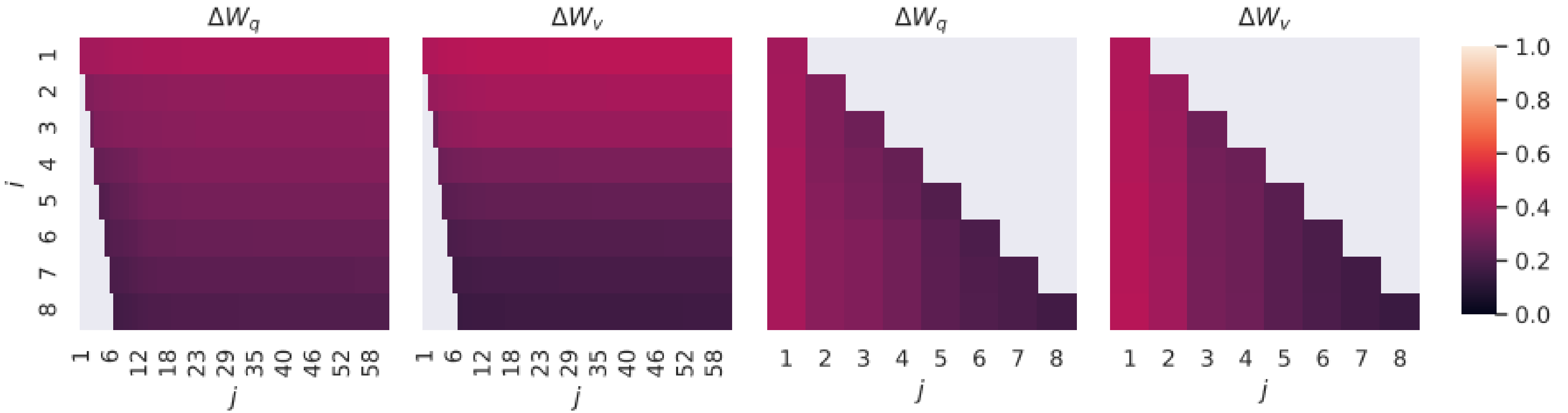
- Adapting W_q *and* W_v can achieve very high accuracy with rank r=1, but training W_q alone needs much larger r.
- In creasing r does not cover a more meaningful subspace

  -> Updating matrix ΔW could have a very small "intrinsic rank"

	Weight Type	$r = 1$	$r = 2$	$r = 4$	$r = 8$	$r = 64$
WikiSQL($\pm 0.5\%$)	W_q	68.8	69.6	70.5	70.4	70.0
	W_q, W_v	$\boxed{73.4}$	73.3	73.7	73.8	73.5
	W_q, W_k, W_v, W_o	74.1	73.7	74.0	74.0	73.9
MultiNLI ($\pm 0.1\%$)	W_q	90.7	90.9	91.1	90.7	90.7
	W_q, W_v	91.3	91.4	91.3	91.6	91.4
	W_q, W_k, W_v, W_o	91.2	91.7	91.7	91.5	91.4

Subspace similarity between different r

- We do singular value decomposition to $A_{r=8}$ and $A_{r=64}$, and get $U_{r=8}$, $U_{r=64}$. Then we measure the normalized subspace similarity based on Grassmann distance.
- The top singular-vector directions of $A_{r=8}$ and $A_{r=64}$ are the most useful



How does the adaptation matrix ΔW compare to W?

- We project W onto the r-dimensional subspace of ΔW by computing $U^T W V^T$
- ΔW has a stronger correlation with W compared to a random matrix
  - -> ΔW enhance some features of W
- ΔW only amplifies directions that are not emphasized in W instead of repeating the top singular directions
- The amplification factor is huge

	$r=4$			$r=64$		
	ΔW_q	W_q	Random	ΔW_q	W_q	Random
$\|\|U^\top W_q V^\top\|\|_F =$	0.32	21.67	0.02	1.90	37.71	0.33
$\|\|W_q\|\|_F = 61.95$	$\|\|\Delta W_q\|\|_F = 6.91$			$\|\|\Delta W_q\|\|_F = 3.57$		

Discussion

- Are LoRA adapters more robust to malicious client updates compared to full-model FL?
- If we apply Lora to federated learning, will the heterogeneity of data among clients undermine the "low-rank assumption" of LoRA?
- Does LoRA, by only transmitting low-rank parameters, provide better privacy protection?