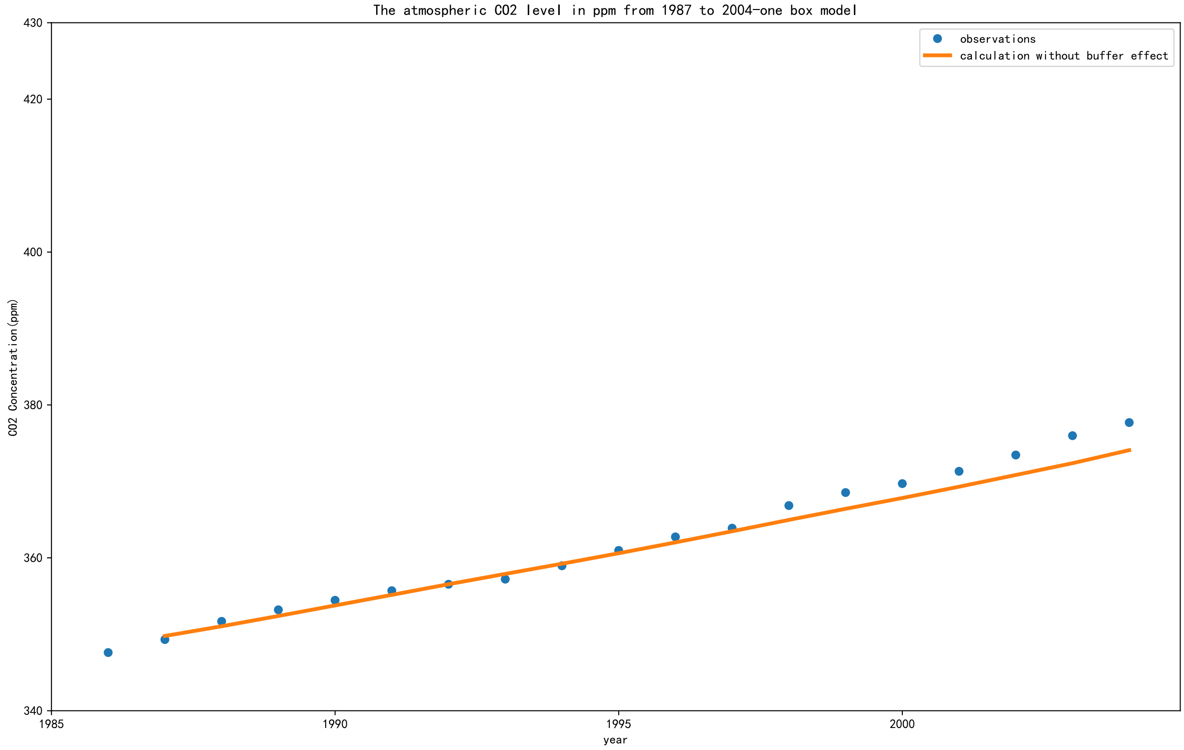
In [2]:
```
#import module
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from scipy import integrate
from scipy.integrate import solve_ivp
from scipy.optimize import curve_fit
from numpy import exp
import glob

#modify the font
#plt.rcParams['配置参数']=[修改值]进行修改
#运行配置参数中的字体（font）为黑体（SimHei）
plt.rcParams['font.sans-serif'] = ['SimHei']
%matplotlib inline
%config InlineBackend.figure_format = 'svg'

#ignore the warnings
import warnings
warnings.filterwarnings('ignore')
```

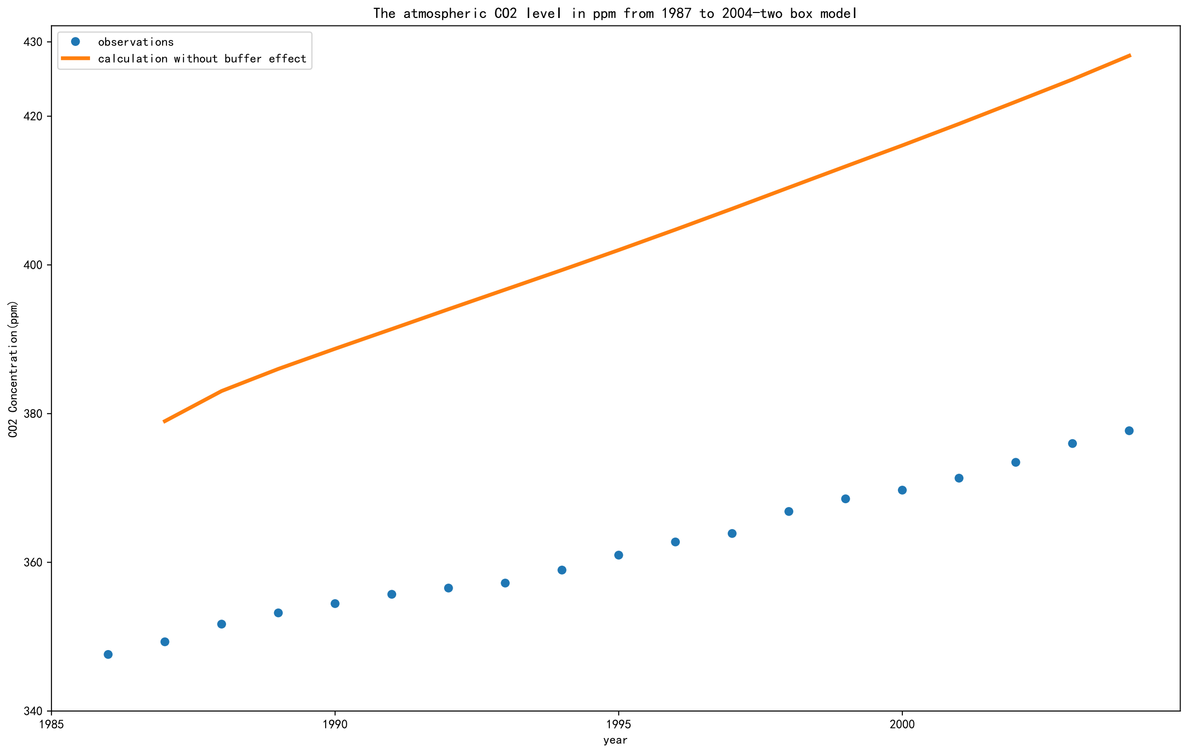
In [3]:
```
#1.1
#read the file
data = pd.read_csv("co2_annmean_mlo.csv",
                   skiprows = 55)
CO2=data.loc[ (data['year'] >1985)&(data['year'] <2005)][['year','mean']]

#define γ  (This step is taught by Yin Yuling)
def γ(t):
    #get the fossil fuel data
    data2 = pd.read_csv("global.1751_2008 (3).csv")
    γ=float(data2.loc[ (data2['Year"'] ==int(t))]['Total carbon emissions from foss
    return γ

#define a function to resovel the equation
def fuc(f, t, k12, k21):
    N1,N2=f
    dfdt = [-k12*N1+k21*N2+γ(t),k12*N1-k21*N2]
    return dfdt

k12 = 105/740
k21 = 102/900
f0 = [740/2.13,900/2.13]
t = np.linspace(1985,2004,20)

#solve ODE
f = integrate.odeint(fuc, f0, t, args=(k12,k21))
ans1 = f[2:,0]

#plot (Yin Yuling told me that the results need to plot)
plt.figure(figsize=(16,10),dpi=120)
plt.plot(CO2['year'], CO2['mean'],'o',label='observations', markersize=6)
plt.plot(t[2:], ans1,label='calculation without buffer effect', linewidth=3)
plt.xlabel('year')
plt.ylabel('CO2 Concentration(ppm)')
plt.xticks([1985,1990,1995,2000])
plt.yticks([340,360,380,400,420,430])
plt.legend(loc='best')
plt.title('The atmospheric CO2 level in ppm from 1987 to 2004-one box model')
plt.show()
```



In [4]:

```
#1.2
#read the file
data = pd.read_csv("co2_annmean_mlo.csv",
                   skiprows = 55)
CO2=data.loc[ (data['year'] >1985)&(data['year'] <2005)][['year','mean']]

#define γ (the same as 1.1)
def γ(t):
    #get the fossil fuel data
    data2 = pd.read_csv("global.1751_2008 (3).csv")
    γ=float(data2.loc[ (data2['Year"'] ==int(t))]['Total carbon emissions from foss
    return γ

#define x to caculate the parameter
def x(N1):
    x=3.69+1.86*(1e-2)*N1-1.8*(1e-6)*N1*N1
    return x

#define a function to resovel the equation
def fuc(f, t, k12, k21, N20):
    N1,N2=f
    dfdt = [-k12*N1+k21*(N20+x(N1)*(N2-N20))+γ(t),k12*N1-k21*(N20+x(N1)*(N2-N20))
    return dfdt

k12 = 105/740
k21 = 102/900
N20 = 821/2.13
f0 = [740/2.13,900/2.13]
t = np.linspace(1985,2004,20)

# caculate the ode
f = integrate.odeint(fuc, f0, t, args=(k12,k21,N20))
ans2 = f[2:,0]

#plot
plt.figure(figsize=(16,10),dpi=120)
plt.plot(CO2['year'], CO2['mean'],'o',label='observations', markersize=6)
plt.plot(t[2:], ans2,label='calculation without buffer effect', linewidth=3)
plt.xlabel('year')
```

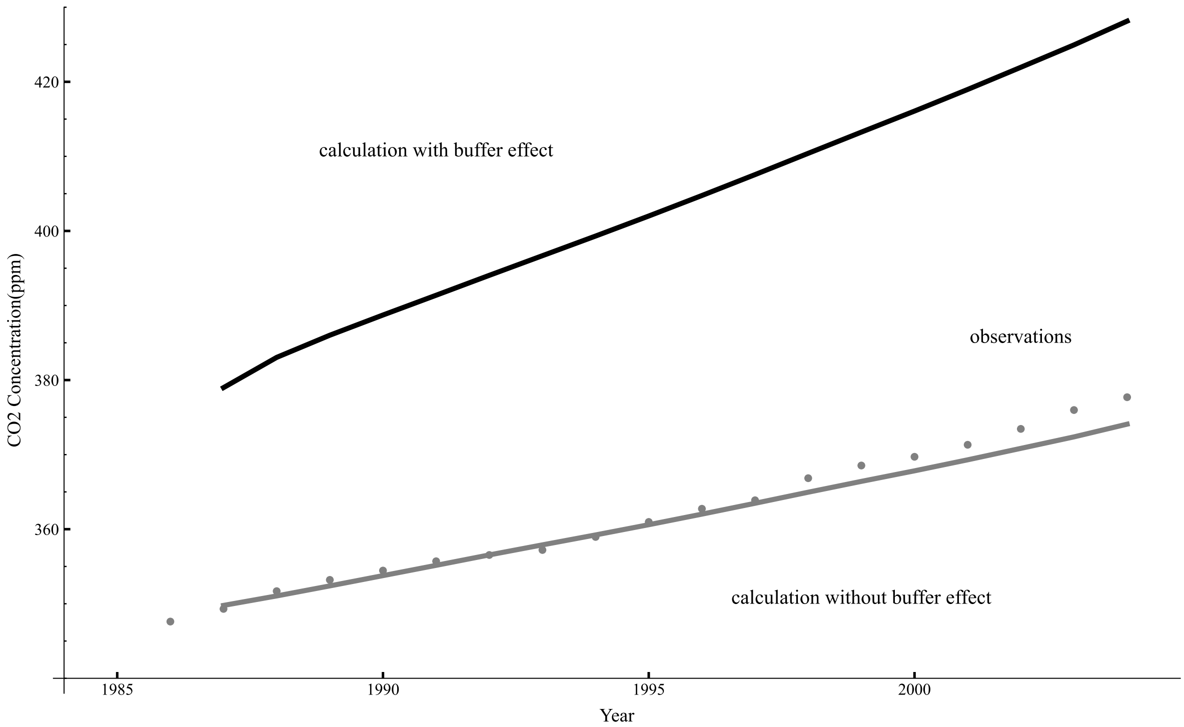
```
plt.ylabel('CO2 Concentration(ppm)')
plt.xticks([1985,1990,1995,2000])
plt.yticks([340,360,380,400,420,430])
plt.legend(loc='best')
plt.title('The atmospheric CO2 level in ppm from 1987 to 2004-two box model')
plt.show()
```



In [5]:

```
#1.3
#Set the Font
plt.rcParams['font.family'] = 'serif'
plt.rcParams['font.serif'] = ['Times New Roman'] + plt.rcParams['font.serif']
plt.rcParams['mathtext.default'] = 'regular'

#Set the figure size
fig = plt.figure(figsize=(16, 10))
ax = fig.add_subplot(1, 1, 1)

#Remove the right border and top border
ax.spines['right'].set_visible(False)
ax.spines['top'].set_visible(False)

#Set the scale and ticks of the coordinate axis
plt.xlim(1983.8,2005)
ax.tick_params(axis='x',which='major',direction='in',width=2,length=5, pad=4,labels
ax.set_xticks(np.arange(1985, 2000 + 5, 5))
ax.set_xticks(np.arange(180, 180 + 2.5, 2.5), minor=True)
ax.set_xlabel('Year',labelpad=8,fontsize=15)
plt.ylim(338,430)
ax.tick_params(axis='y',which='major',direction='in',width=2,length=5, pad=4,labels
ax.tick_params(axis='y',which='minor',direction='in',width=1,length=2)
ax.set_yticks(np.arange(360, 420 + 20, 20))
ax.set_yticks(np.arange(340, 430 + 5, 5), minor=True)
ax.set_ylabel('CO2 Concentration(ppm)',labelpad=8,fontsize=15)

#Set the origin of axes and plot it(ask for Yin Yuling)
ax.spines['bottom'].set_position(('data',340))
ax.spines['left'].set_position(('data',1984))
ax.plot(t[2:], ans1[:],linewidth=4,color='grey',label='calculation without buffer ef
ax.plot(t[2:], ans2[:],linewidth=4,color='k',label='calculation with buffer effect')
ax.scatter(CO2['year'], CO2['mean'],s=32,c='grey',marker='o',lw=0.5,label='observat
```

```
#add the text
ax.text(1999,350,
        "calculation without buffer effect",
        horizontalalignment ='center',
        fontsize = 16,zorder=2)
ax.text(1991,410,
        "calculation with buffer effect",
        horizontalalignment ='center',
        fontsize = 16,zorder=2)
ax.text(2002,385,
        "observations",
        horizontalalignment ='center',
        fontsize = 16,zorder=2)
plt.show()
```

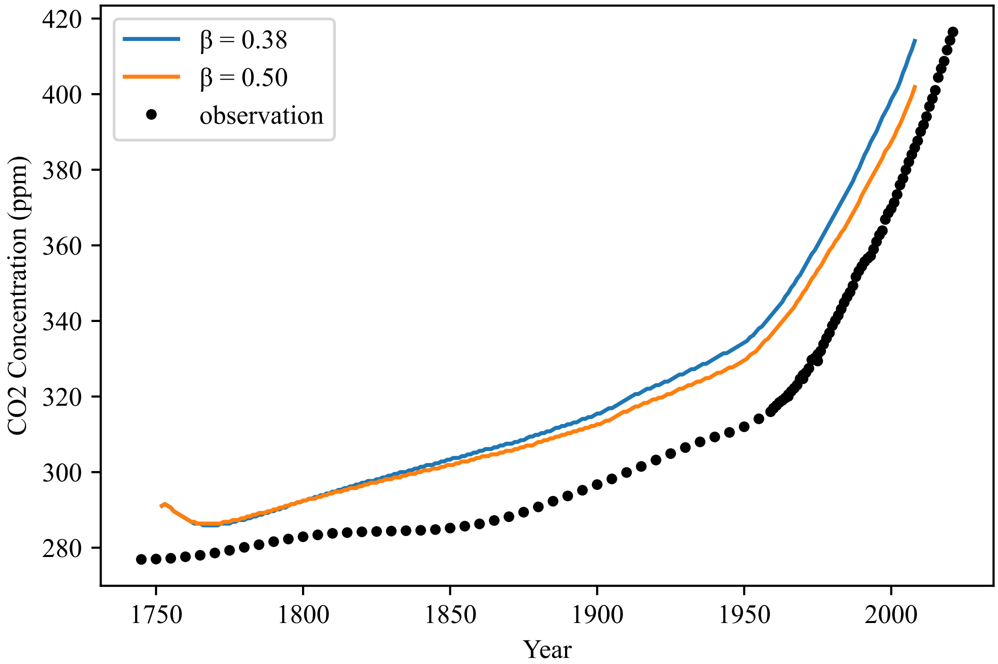


In [22]:

```
# Bonus
#This code comes from Shi Shao, he taught us about how to understand the question. L
import math
import numpy as np
from scipy.integrate import odeint
import matplotlib.pyplot as plt
from math import e


# read the data of gama
gama = np.loadtxt("global.1751_2008 (3).csv", delimiter=",", skiprows = 2, usecols =
# create year vector
yearCount = 2008 - 1751 + 1
t = np.linspace(1751,1751+yearCount-1,yearCount,dtype='int')
# read CO2 observation data 1
co2_1010 = np.loadtxt("co2.csv", delimiter=",", skiprows = 149)
# read CO2 observation data 2
annual_CO2_Obs = np.loadtxt("co2_annmean_mlo.csv", delimiter=",", skiprows = 56 )[:,
annual_CO2_Obs_t = np.loadtxt("co2_annmean_mlo.csv", delimiter=",", skiprows = 56 )[
# read the data of delta
delta = np.empty_like(gama)
delta[0:100] = np.linspace(0.2,0.5,100)
delta[99:-2]= np.loadtxt("Global_land-use_flux-1850_2005.csv", delimiter=",", skipro
delta[-3:] = delta[-4]
```

```
def compute_xi(CO2_ppm):
    xi = 3.69 + 1.86 * 10**-2 * CO2_ppm - 1.80 * 10**-6 * CO2_ppm**2
    return xi

def compute_f(P,beta):
    f0 = 62
    P0=290.21
    f = f0 * (1 + beta * math.log(P/P0))
    return f

# ODE creation of eq.6 to eq.12
def eq_6_12(N,t,gama,xi,f,delta):
    N02 = 821
    k12 = 60/615
    k21 = 60/842
    k23 = 9/842
    k24 = 43/842
    k32 = 52/9744
    k34 = 162/9744
    k43 = 205/26280
    k45 = 0.2/26280
    k51 = 0.2/90000000
    k67 = 62/731
    k71 = 62/1328
    N1,N2,N3,N4,N5,N6,N7 = N
    dN1dt = -k12 * N1 + k21 * (N02 + xi*(N2 - N02)) + gama - f + delta + k51 * N5
    dN2dt = k12 * N1 - k21 * (N02 + xi*(N2 - N02)) - k23 * N2 + k32 * N3 - k24 * N
    dN3dt = k23*N2 - k32*N3 - k34*N3 +k43*N4
    dN4dt = k34*N3 - k43*N4 + k24*N2 -k45*N4
    dN5dt = k45*N4 - k51*N5
    dN6dt = f - k67*N6 - 2*delta
    dN7dt = k67*N6 - k71*N7 + delta
    return [dN1dt, dN2dt, dN3dt, dN4dt, dN5dt, dN6dt, dN7dt]

N1_eq_6_12_beta1 = np.empty_like(t)
N1_eq_6_12_beta2 = np.empty_like(t)

# beta = 0.38
beta = 0.38
N0 = [615, 842, 9744, 26280, 90000000, 731, 1238]
N1_eq_6_12_beta1[0] = N0[0]
CO2_ppm = N1_eq_6_12_beta1[0]/2.13
xi = compute_xi(CO2_ppm)
f = compute_f(CO2_ppm,beta)
# slove the ODE year by year
for i in range(1,yearCount):
    #set the setp size
    dt = [0,1]
    # numericly solve the eq.s
    N = odeint(eq_6_12,N0,dt,args=(gama[i-1],xi,f,delta[i-1]))
    # store the result
    N1_eq_6_12_beta1[i] = N[1][0]
    # initiation of the next step
    CO2_ppm = N1_eq_6_12_beta1[i]/2.13
    N0 = N[1]
    xi = compute_xi(CO2_ppm)
    f = compute_f(CO2_ppm,beta)

# beta = 0.50
beta = 0.5
N0 = [615, 842, 9744, 26280, 90000000, 731, 1238]
N1_eq_6_12_beta2[0] = N0[0]
CO2_ppm = N1_eq_6_12_beta2[0]/2.13
```

```python
xi = compute_xi(CO2_ppm)
f = compute_f(CO2_ppm,beta)
# slove the ODE year by year
for i in range(1,yearCount):
    #set the setp size
    dt = [0,1]
    # numericly solve the eq.s
    N = odeint(eq_6_12,N0,dt,args=(gama[i-1],xi,f,delta[i-1]))
    # store the result
    N1_eq_6_12_beta2[i] = N[1][0]
    # initiation of the next step
    CO2_ppm = N1_eq_6_12_beta2[i]/2.13
    N0 = N[1]

    xi = compute_xi(CO2_ppm)
    f = compute_f(CO2_ppm,beta)

plt.plot(t[1:],N1_eq_6_12_beta1[1:]/2.13,label='β = 0.38')
plt.plot(t[1:],N1_eq_6_12_beta2[1:]/2.13,label='β = 0.50')
plt.plot(co2_1010[:,0], co2_1010[:,1],'k.')
plt.plot(annual_CO2_Obs_t,annual_CO2_Obs,'k.',label='observation')
plt.ylabel('CO2 Concentration (ppm)')
plt.xlabel('Year')
plt.legend(loc='best')
my_x_ticks = np.arange(1985,2004,3)
plt.show()
```



In [ ]: