# **Lesson 13 Cluster Analysis for Time Series**

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Quiz

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- Quiz
- DTW

#### DTW vs Euclidean distance

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#### DTW vs Euclidean distance

- Euclidean distance has become one of the most commonly used distance measures when working with time series
- Due to **linear aligning** of related points of time series, it is very sensitive to distortions along the time axis
- DTW finds optimal non-linear alignment

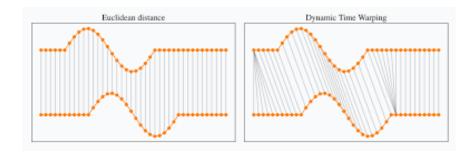
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- The main purpose of Dynamic Time Warping (DTW) in time series clustering is to measure the **similarity** between two time series, even if they have different lengths or exhibit time distortions.
- DTW helps to find the best alignment between the two time series by warping, stretching, or compressing them along the time axis.

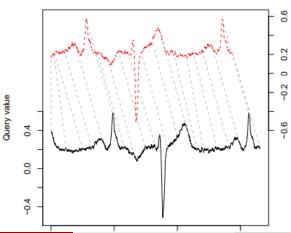
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- The main purpose of Dynamic Time Warping (DTW) in time series clustering is to measure the **similarity** between two time series, even if they have different lengths or exhibit time distortions.
- DTW helps to find the best alignment between the two time series by warping, stretching, or compressing them along the time axis.
- It finds the alignment that minimizes the total distance between corresponding points in the time series.

## **Idea of DTW**



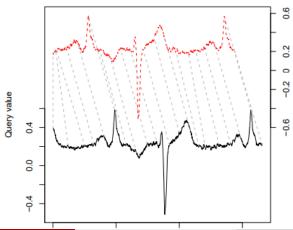
### Idea of CA

• Make one time series resembles the other as much as possible.



## Idea of CA

- Make one time series resembles the other as much as possible.
- We can stretch or compress them.



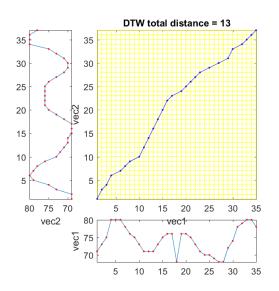
Continuity

- Continuity
- Endpoints

- Continuity
- Endpoints
- Local distance definitions

- Continuity
- Endpoints
- Local distance definitions
- Global constraints

## Matrix of correlations and path



## Type of step functions

```
dtw(a1, a2)$stepPattern
```

```
## Step pattern recursion:
## g[i,j] = min(
## g[i-1,j-1] + 2 * d[i ,j ] ,
## g[i ,j-1] + d[i ,j ] ,
## g[i-1,j ] + d[i ,j ] ,
## )
## "
## Normalization hint: N+M
```

## Type of step functions

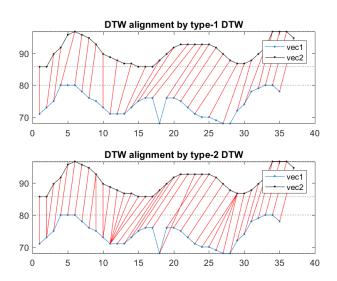
```
dtw(a1, a2, step.pattern = symmetric1)$stepPattern
```

```
## g[i-1,j-1] + d[i ,j ] ,
## g[i ,j-1] + d[i ,j ] ,
## g[i-1,j ] + d[i ,j ] ,
## )
## )
## 
## Normalization hint: NA
```

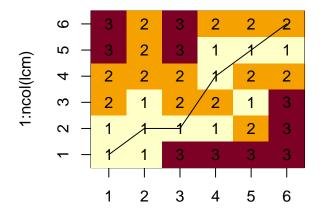
## Step pattern recursion:

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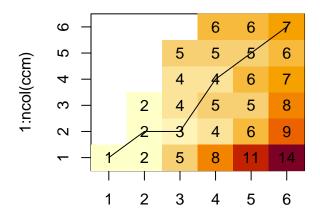
## Type of step functions



### Local distance matrix



### **Cumulative distance matrix**



### **Problems**

 $\bullet$  Finding the optimal alignment can be quite slow

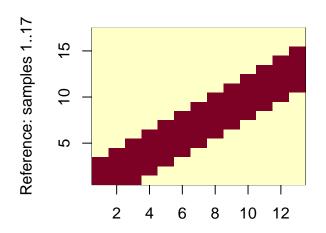
### **Problems**

- Finding the optimal alignment can be quite slow
- It can lead to bad alignments where a relatively small part of one time series maps onto a large section of the other one.

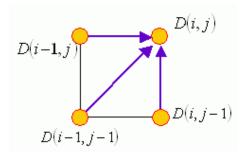
### **Problems**

- Finding the optimal alignment can be quite slow
- It can lead to bad alignments where a relatively small part of one time series maps onto a large section of the other one.
- This can be avoided by narrowing the searching window around the diagonal of the warping matrix using global constraints.

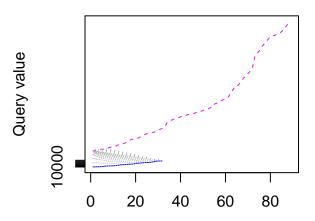
### Global Path Constraint: Sakoe Chiba Window



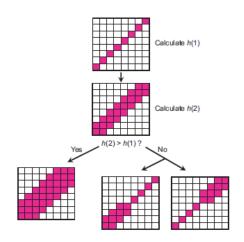
### **Local Path contraint**



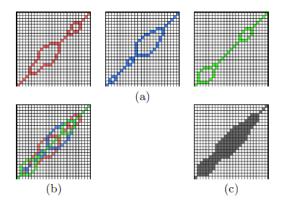
# **Unconstrained endpoints**



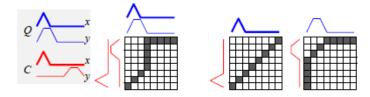
# R-K band forward searching algorithm



# R-K band forward searching algorithm



## Dealing with multivariate time series



## And

The end.