

1. 10%

Write an equivalent Lisp expression for

$$\frac{\exp(x) - \cos(y)}{\sin(x - y * \log(y))}$$

where x , y , \sin , \cos , \log and \exp have been defined somewhere.

2. 10% + 5%

```
(let ((x (+ z 5))
      (y (+ x 2))
      (z (+ x y)))
    (* (+ x y) z))
```

a) For the above 'let expression', write its equivalent 'lambda form'.

b) With $x=1$, $y=2$, and $z=4$, evaluate the above 'let expression'.

3. 15%

Write a procedure, (make-mod-m-k m k), which accepts two parameters, m , k and will return a one-argument function. The returned function is a predicate which will determine if remainder of the argument by m equals to k . That is, if the parameter is named by n , it will return true if $n \% m == k$, or return false.

```
> (define mod-3-1? (make-mod-m-k 3 1))
; no values returned
> (mod-3-1? 10)
#t
> (mod-3-1? 12)
#f
>
```

4. 15% + 15%

A function f defined for non-negative integers is defined as:
$$f(n) = \begin{cases} 3, & \text{if } n=0 \\ 1, & \text{if } n=1 \\ f(n-1) + f(n-2), & \text{if } n>1 \text{ and } n \bmod 3 == 1 \\ f(n-1) - f(n-2), & \text{if } n>1 \text{ and } n \bmod 3 \neq 1 \end{cases}$$
a) Write a procedure, (rec n), that computes f in linear recursive way.b) Write a procedure, (iter n), that computes f in linear iterative way.

Note: You may assume (mod-3-1? n) defined in previous problem is available.

5. 15%

The previous process can be generalized as follows:

$$f(n) = \begin{cases} f_0, & \text{if } n=0 \\ f_1, & \text{if } n=1 \\ \alpha(n, f(n-1), f(n-2)) & \text{if } n>1 \end{cases}$$
where α is a function.

Write a function, (make-fun f_0 f_1 α), which will return a designed function as specified and the returned function is run iteratively.

6. 10% + 5%

a) Use previous (make-fun f_0 f_1 α) to redefine (iter n) (the function defined in problem 4).b) Use previous (make-fun f_0 f_1 α) to redefine (fib n).

```
> (iter 1035)
-3
> (redefine-iter 1035)
-3
> (fib 102)
927372692193078999176
> (redefine-fib 102)
927372692193078999176
> ,exit
```

$0! = 1$
 $1! = 1$

$-a + 5b -$

$4b^2$