```
There are two different versions of the insert member
function. The first version inserts the entry into the set and
                                                                    else return iterator(p,this);
returns a pair. The first component of the returned pair refers
to the location in the set containing the entry. The second
component is true if the entry wasn't already in the set and
                                                                   TreeNode<T>*& p.
therefore was inserted. It is false otherwise. The second
                                                                   TreeNode<T>* the parent) {
version also inserts the key if it is not already there. The
                                                                    if (!p) {
iterator pos is a "hint" as to where to put it. This makes the
insert faster if the hint is good.
                                                                      p->parent = the_parent;
pair<iterator,bool> set<Key>::insert(const Key& entry);
                                                                      this->size_++;
iterator set<Key>::insert(iterator pos, const Key& entry);
There are three versions of erase. The first erase returns the
number of entries removed (either 0 or 1). The second and
third erase functions are just like the corresponding erase
functions for maps. Note that the erase functions do not
return iterators. This is different from the vector and list
erase functions.
size_type set<Key>::erase(const Key& x);
                                                                    if (!p) return 0;
                                                                    // look left & right
void set<Key>::erase(iterator p);
void set<Key>::erase(iterator first, iterator last);
// increment & decrement operators
tree iterator<T> & operator++() {
 if (ptr_->right != NULL) { // find the leftmost child of the right
                                                                    if (!p->left && !p->right) { // leaf
node
                                                                      delete p;
                                                                     p=NULL;
  ptr_ = ptr_->right;
  while (ptr_->left != NULL) ptr_ = ptr_->left;
                                                                      this->size --:
 else { // go upwards along right branches.stop after the first
left
                                                                     TreeNode<T>* a = p:
  while (ptr_->parent != NULL && ptr_->parent->right == ptr_)
                                                                      p=p->right;
   ptr = ptr ->parent;
                                                                      assert (p->parent == q);
                                                                     p->parent = q->parent;
  ptr_ = ptr_->parent;
                                                                      delete q:
 return *this;
                                                                      this->size_--;
tree iterator<T> operator++(int) {
 tree_iterator<T> temp(*this);
                                                                      TreeNode<T>* q = p;
 ++(*this);
                                                                      p=p->left;
 return temp;
                                                                     assert (p->parent == q);
                                                                     p->parent = q->parent;
tree iterator<T> & operator--() {
                                                                      delete a:
 if (ptr == NULL) {
                                                                      this->size --;
  assert(set != NULL);
  ptr_ = set_->root_;
  while (ptr_->right != NULL) ptr_ = ptr_->right;
                                                                      TreeNode<T>* q = p->left;
                                                                      while (q->right) q = q->right;
 else if (ptr_->left != NULL) {
                                                                      p->value = q->value:
  ptr = ptr ->left;
  while (ptr_->right != NULL) ptr_ = ptr_->right;
                                                                     assert (check == 1):
  while (ptr ->parent != NULL && ptr ->parent->left == ptr )
                                                                    return 1;
   ptr_ = ptr_->parent;
  ptr = ptr ->parent;
 return *this;
                                                                   end called the top
tree_iterator<T> operator--(int) {
 tree_iterator<T> temp(*this);
 --(*this):
                                                                   All stack operations are O(1)
 return temp;
TreeNode<T>* copy_tree(TreeNode<T>* old_root,
TreeNode<T>* the parent) {
 if (old_root == NULL) return NULL;
 TreeNode<T> *answer = new TreeNode<T>();
                                                                   riaht.
                                                                   All queue operations are O(1)
 answer->value = old_root->value;
 answer->left = copy_tree(old_root->left,answer);
 answer->right = copy_tree(old_root->right,answer);
 answer->parent = the parent;
 return answer:
void destroy_tree(TreeNode<T>* p) {
                                                                     if (itr != locations.end()) {
 if (!p) return:
 destroy tree(p->right);
                                                                    element << std::endl;
 destroy_tree(p->left);
 delete p:
                                                                    assert (itr == locations.end());
iterator find(const T& key_value, TreeNode<T>* p) {
 if (!p) return end():
```

```
if (p->value > key value) return find(key value, p->left);
                                                                     m heap.push back(element);
else if (p->value < key_value) return find(key_value, p->right);
                                                                     locations[element] = m heap.size()-1:
                                                                     this->percolate up(int(m heap.size()-1));
std::pair<iterator,bool> insert(const T& key_value,
                                                                    // remove the top element (minimum value) from the heap
                                                                    template <class T> void PriorityQueue<T>::pop() {
                                                                    assert(!m heap.empty());
                                                                     int success = locations.erase(m_heap[0]);
 p = new TreeNode<T>(key value);
                                                                     assert (success == 1);
                                                                    // place the last element temporarily at the top of the heap,
  return std::pair<iterator,bool>(iterator(p,this), true);
                                                                    // push it down to a proper position using percolate down
                                                                     m_heap[0] = m_heap.back();
else if (key_value < p->value) return insert(key_value, p->left, p);
                                                                     m heap.pop back():
else if (key_value > p->value) return insert(key_value, p->right,
                                                                     this->percolate_down(0);
else return std::pair<iterator,bool>(iterator(p,this), false);
                                                                    // remove a specific element that could be anywhere in the
                                                                    heap
                                                                    template <class T> void PriorityQueue<T>::remove(T element) {
int erase(T const& key_value, TreeNode<T>* &p) {
                                                                    // Put the last element to the location where the element is to
                                                                    be RemoveEdge Pop back the last element and percolate
if (p->value < key_value) return erase(key_value, p->right);
                                                                    down the heap
else if (p->value > key_value) return erase(key_value, p->left);
                                                                    if (exist(element)) {
// Found the node. Let's delete it
                                                                      int loc = locations[element];
assert (p->value == key value);
                                                                      locations.erase(element);
                                                                      m_heap[loc] = m_heap.back();
                                                                      locations[m heap.back()] = loc;
                                                                      m_heap.pop_back();
                                                                      update_position(m_heap[loc]);
 else if (!p->left) { // no left child
                                                                   // this element may have had its value change, so we should
                                                                    adjust the position of the element within the heap (it might
                                                                    need to move up or down)
                                                                    template <class T> void PriorityQueue<T>::update_position(T
                                                                     typename std::map<T,int>::iterator itr = locations.find(element);
                                                                     assert (itr != locations.end());
 else if (!p->right) { // no right child
                                                                     this->percolate up(itr->second);
                                                                     this->percolate_down(itr->second);
                                                                   // for debugging, print all of the data in the heap
                                                                    template <class T>
                                                                    void PriorityQueue<T>::print_heap(std::ostream & ostr) const {
                                                                     for (int i=0; i<(int)m_heap.size(); ++i)
                                                                      ostr << "[" << std::setw(4) << i << "] :
 else { // Find rightmost node in left subtree
                                                                         << std::setw(6) << m_heap[i]->getPriorityValue()
                                                                         << " " << *m heap[i] << std::endl;
                                                                    // allow the element at this location to move up
  // recursively remove the value from the left subtree
                                                                    template <class T> void PriorityQueue<T>::percolate_up(int i) {
  int check = erase(q->value, p->left);
                                                                     while(i > 0) {
                                                                     if (m_heap[i]->getPriorityValue() < m_heap[get_parent(i)]-
                                                                    >getPriorityValue()) {
                                                                        locations[m_heap[i]] = get_parent(i);
                                                                       locations[m_heap[get_parent(i)]] = i;
std::swap(m heap[i], m heap[get parent(i)]);
Stacks allow access, insertion and deletion from only one
                                                                       i = get_parent(i);
There is no access to values in the middle of a stack.
                                                                      else break;
Stacks may be implemented efficiently in terms of vectors and
lists, although vectors are preferable.
                                                                    // allow the element at this location to move down
Queues allow insertion at one end, called the back and
                                                                    template <class T> void PriorityQueue<T>::percolate_down(int i) {
                                                                     while (has left child(i)) {
removal from the other end, called the front
There is no access to values in the middle of a queue
                                                                      int child = 0;
Queues may be implemented efficiently in terms of a list. Using
                                                                      // Choose the child to compare against
vectors for queues is also possible, but requires more work to get
                                                                      if (has_right_child(i) && m_heap[get_right_child(i)]-
                                                                    >getPriorityValue() <
                                                                       m_heap[get_left_child(i)]->getPriorityValue())
Priority Queue<<<<<<<<
                                                                       child = get_right_child(i);
// add a new element to the heap
                                                                      else child = get_left_child(i);
template <class T> void PriorityQueue<T>::push(T element) {
                                                                      if (m_heap[child]->getPriorityValue() < m_heap[i]-
                                                                   >getPriorityValue()) {
// first, verify that the element isn't already in the heap
typename std::map<T,int>::iterator itr = locations.find(element);
                                                                       locations[m_heap[child]] = i;
                                                                       locations[m heap[i]] = child;
  std::cout << "ERROR! priority queue aleady contains " <<
                                                                       std::swap(m_heap[child], m_heap[i]);
                                                                       i = child;
  assert (element == itr->first);
                                                                      else break;
// add the element at the edge of heap vector and percolate
```

```
else break;
percolate_up(TreeNode<T> * p) {
 while (p->parent) {
  if (p->value < p->parent->value) {
   swap(p, parent);
   p = p->parent;
  else break;
int my_func(int a, int b) throw(double,bool) {
 if (a > b) throw 20.3;
 else throw false;
int main() {
try my_func(1,2);
 catch (double x) std::cout << " caught a double " << x <<
 catch (...) std::cout << " caught some other type " << std::endl;
for (std::list<Polygon*>::iterator i = polygons.begin(); i!
=polygons.end(); ++i) {
 Quadrilateral *q = dynamic cast<Quadrilateral*> (*i);
 if (q) std::cout << "diagonal: " << q->LongerDiagonal() <<
std::endl:
Map<<<<<<<<<<
1. Map search, insert and erase are O(log n).
2. Maps are ordered by increasing value of the key. Therefore,
there must be an operator< defined for the key.
3. The function std::make pair creates a pair object from the
given values.
4. The result of using [] is that the key is always in the map
afterwards.
5. m.find(key) where m is the map object and key is the search
key. It returns a map iterator: If the key is in one of the pairs
stored in the map, find returns an iterator referring to this pair.
If the key is not in one of the pairs stored in the map, find
returns m.end().
6. Insert: m.insert(std::make_pair(key, value)); returns a pair of a
map iterator and a bool: std::pair<map<key_type,
value type>::iterator, bool> The insert function checks to see if
the key being inserted is already in the map. If so, it does not
change the value, and returns a (new) pair containing an
iterator referring to the existing pair in the map and the bool
value false. If not, it enters the pair in the map, and returns a
(new) pair containing an iterator referring to the newly added
pair in the map and the bool value true.
7. void erase(iterator p) erase the pair referred to by iterator p.
void erase(iterator first, iterator last) erase all pairs from the map
starting at first and going up to, but not including, last.
size_type erase(const key_type& k) erase the pair containing key
k, returning either 0 or 1, depending on whether or not the key
was in a pair in the map
Erase and Insert<<<<<<<<
1. The erase member function (for STL vector and STL list)
takes in a single argument, an iterator pointing at an element
in the container. It removes that item, and the function returns
an iterator pointing at the element after the removed item.
2. Similarly, there is an insert function for STL vector and STL
list that takes in 2 arguments, an iterator and a new element.
and adds that element immediately before the item pointed to
by the iterator. The function returns an iterator pointing at the
newly added element.
3. Even though the erase and insert functions have the same
syntax for vector and for list, the vector versions are O(n),
whereas the list versions are O(1).
4. Iterators positioned on an STL vector, at or after the point of
an erase operation, are invalidated. Iterators positioned
anywhere on an STL vector may be invalid after an insert (or
```

percolate\_down(TreeNode<T> \* p) {

if (child->value < p->value) {
 swap(child, p);

if (p->right && p->right->value < p->left->value) child = p->right;

while (p->left) {

p = child;

TreeNode<T>\* child;

else child = p->left;

```
push back or resize) operation.
5. Iterators attached to an STL list are not invalidated after an
insert or erase (except iterators attached to the erased
element!) or push back/push front.
>>>>>>>Counting Occupied & Unoccupied Nodes
template <class T>
std::pair<int,int> count(Node<T>* p) {
 if (p == NULL) return std::make pair(0,0);
 // recurse down both branches
 std::pair<int,int> I = count(p->left);
 std::pair<int,int> r = count(p->right);
 // calculate the two totals
 int occupied = int(p->occupied==true) + l.first + r.first:
 int unoccupied = int(p->occupied==false) + l.second + r.second;
 // prepare the return value
 return std::make_pair(occupied,unoccupied);
>>>>>Implement erase for Trees with Unoccupied Nodes
template <class T>
bool erase(Node<T>* &p, const T& v) {
 if (p == NULL) return false;// value not found
 if (n->occupied) {
  if (p->value == v) { // found the value!
   if (p->left == NÚLL && p->right == NULL) {
    // leaf node is simply deleted
    delete p;
    p = NULL:
   } // otherwise mark this node as unoccupied
   else p->occupied = false;
  return true:
  else if (p->value > v) return erase(p->left,v); // recurse left
  else return erase(p->right,v); // recurse right
 else {
 // this node is unoccupied, and the value to erase might be
down either path! recurse in both directions
 bool success = erase(p->left,v) | erase(p->right,v)
 // if after erasing, this node is now a leaf... delete it!
 if (p->left == NULL && p->right == NULL) {
  assert (success);
  delete n.
  p = NULL;
 return success;
>>>>>>Implement insert for Trees with Unoccupied Nodes
template <class T>
bool insert(Node<T>* &p, const T& v) {
 if (p == NULL) {
  // empty tree, must add a new node!
  p = \text{new Node} < T > (v);
  return true;
 if (p->occupied) {
  if (p->value == v) return false:
  else if (p->value > v) return insert(p->left,v);
  else return insert(p->right,v);
 else {
// duplicate element: recurse left & recurse right
// this node is unoccupied, but the value doesn't necessarily
fit here
// if there are elements to the left, and at least one is larger,
recurse left
  if (p->left != NULL && v <= largest_value(p->left))
   return insert(p->left,v);
// if there are elements to the right, and at least one is smaller,
  else if (p->right != NULL && v >= smallest value(p->right))
   return insert(p->right,v);
  // otherwise this value does fit here!
  p->occupied = true;
  p->value = v;
  return true:
Classroom Scheduler Maps<
bool make reservation(room reservations &rr, const std::string
&building, int room, const std::string &day, int start_time, int
duration, const std::string &event) {
```

```
// locate the room
room reservations::iterator room itr =
rr.find(std::make pair(building,room));
if (room itr == rr.end()) {
  std::cerr << "ERROR! room " << building << " " << room << "
does not exist" << std::endl;
  return false:
// grab the specific day
 week_schedule::iterator day_itr = room_itr->second.find(day);
 if (day_itr == room_itr->second.end()) {
  std::cerr << "ERROR! invalid day: " << day << std::endl;
// check that the time range is valid
 if (start time + duration > 24) {
  std::cerr << "ERROR! invalid time range: " << start_time << "-"
<< start time+duration << std::endl;
  return false;
// loop over the requested hours looking for a conflict
 assert (day itr->second.size() == 24);
for (int i = 0; i < duration; i++) {
std::string prior = day_itr->second[start_time+i];
if (prior != "") {
std::cerr << "ERROR! conflicts with prior event: " << prior <<
std::endl:
   return false;
// if everything is ok, make the reservation
for (int i = 0: i < duration: i++) {
  day_itr->second[start_time+i] = event;
return true:
Fashionable Sets<<<<<<<
// intentionally copying the items & colors lists (will edit them
std::vector<std::string> outfits(std::list<std::string> items,
std::list<std::set<std::string> > colors) {
assert (items.size() == colors.size());
// base case, no items!
std:/vector<std:/string> answer:
if (items.size() == 0) {
  // one answer, the empty outfit
  answer.push_back("");
  return answer;
// pop off the last item & set of colors
std::string item = items.back();
items.pop back();
std::set<std::string> c = colors.back():
colors.pop back();
// recurse with the shortened item list & colors list
std::vector<std::string> recurse_answer = outfits(items,colors);
// combine each color with the current item
for (std::set<std::string>::iterator itr = c.begin(); itr != c.end(); itr+
+) {
  // add that to the front of the list
  for (int i = 0; i < recurse_answer.size(); i++) {
   if (recurse_answer[i].size() > 0)
    answer.push_back(recurse_answer[i]+" & "+*itr+" "+item);
   // special case for first item of clothing
   else answer.push back(*itr+" "+item):
 return answer;
Factor Tree<<<<<<<<<
Node* factor_tree(int num) {
Node* answer = new Node;
answer->value = num:
for (int i = 2; i \le num/2; i++) {
  if (num % i == 0) {
   answer->factors.push back(factor tree(i));
return answer:
Driving in Circles<<<<<<<<
void driving(std::vector<std::string> &path, const Car &car, int
max steps.
```

```
std::vector<Car> previous = std::vector<Car>()) {
 // base case, solution!
 if (path.size() > 0 && car == Car(0,0,"north")) {
  std::cout << "closed loop: ":
  for (int i = 0; i < path.size(); i++) {
   std::cout << " " << path[i];
  std::cout << std::endl;
  return:
 // base case, maximum recursion depth
 if (path.size() == max_steps) { return; }
 // make sure we aren't overlapping previous car positions
 // note: we are allowing the path to cross though!
 for (int i = 0; i < previous.size(); i++) {
  if (car == previous[i]) return;
 previous.push_back(car);
 // try to go straight
 path.push back("straight");
 driving(path,go_straight(car),max_steps,previous);
 path.pop_back();
 // try to go left
 path.push back("left");
 driving(path,turn_left(car),max_steps,previous);
 path.pop back();
 // try to go right
 path.push_back("right");
 driving(path,turn_right(car),max_steps,previous);
 path.pop_back();
 previous.pop back():
Maps of Sets of Factors
void add factors(factor type &factors, int x) {
 // prepare the set of factors
 std::set<int> tmn
 // O(x) loop over the range of all possible factors
 for (int i = 2; i \le x/2; i++) {
  if (x \% i == 0) {
   // insert the factors into the set O(log j)
   tmp.insert(i);
 // O (log n)
 factors.insert(make_pair(x,tmp));
If we are storing the factors of n different numbers in the
factors structure, f different factors will eventually be stored in
the is factor of structure, each number has on average (or at
most) i factors, and each factor is a factor of on average (or at
most) k numbers, what is the order notation for the running
time of your add factors function to add the number x and the
factors of x?
O(x * log j + log n) or O(x + j * log j + log n)
factor type reverse(const factor type &factors) {
 factor_type answer;
 // O(n) loop over the numbers/rows in the map table
 for (factor_type::const_iterator itr = factors.begin(); itr !=
factors.end(); itr++) {
  // O(i) loop over the factors
  for (std::set<int>::iterator tmp = itr->second.begin(); tmp != itr-
>second.end(); tmp++) {
   // O(log f + log k) add an association to the output table
   answer[*tmp].insert(itr->first);
 return answer;
O(n * j * (log f + log k))
void remove(int n, factor_type &factors, factor_type &is_factor_of) {
 // locate the item in the factors table, O(log n)
 factor type::iterator itr = factors.find(n);
 if (itr == factors.end()) return;
 // loop over the j factors of that number, O(j)
 for (std::set<int>::iterator tmp = itr->second.begin(); tmp != itr-
>second.end(): tmp++) {
  // locate the factor in the is_factor_of table, O(log f)
  factor_type::iterator itr3 = is_factor_of.find(*tmp);
  assert (itr3 != is factor of.end()):
```

The average number of child or parent links that must be traversed when moving from one node to the next node in an in-order traversal is O(1) = CONSTANT. The WORST CASE number of links that must be traversed when moving from one node to the next node in an in-order traversal is O(log n), where n is the number of elements in the tree AND THE TREE IS RAI ANCED.

Executing a breadth-first search for the shortest path from root to leaf on a balanced binary search tree is most likely going to be faster BUT ALSO REQUIRE MORE ADDITIONAL MEMORY than a depth-first search on the same tree.

A hash function should run in O(1) time, to ensure that the hash table will be able to achieve O(1) = CONSTANT EXPECTED query time, where n is the number of elements in the hash table.

Maintaining the Red-Black property for a BINARY SEARCH TREE, ensures that the data remains balanced and elements can be accessed in O(log n) time.

We need to handle bad input, the input strings are equal to each other or one or more input strings does not match a person object in the graph. We need to handle the case where the two person objects are directly linked to each other with a pointer in one or both directions. We'll want to handle cases where the two accounts have no nodes in common, or where both accounts point to or are pointed at by the same account (and prevent duplicates in the merged structure). We should also test cases where one or both accounts is not connected to the other nodes in the graph or where one node has only outgoing links and the other node has only ingoing links.

When the same member function is implemented in more than one class within the inher- itance hierarchy, the virtual keyword on the parent class function indicates that the derived class function should be used if it is available. Without the virtual keyword, the search for a matching function begins at the pointer type and searches "up" the inheritance hierarchy as necessary.

A class constructor may "fail" only in two manners: it may throw an exception or it may return NULL (useful when the system is out of memory).

Solution: False, the only way for a constructor to fail is to throw an exception. If the system is out of memory, the constructor should throw an out-of-memory exception.

When the inheritance diagram includes a set of classes that form a diamond, two instances of the base class will be created unless the keyword "trapezoid" is used in the .cpp file to explicitly specify the construction of only one instance of the base class.

Solution: False. The keyword "virtual" should be used in the .h file to specify virtual inheritance from the base class.

Good programming style for class design encourages the use of operator overloading even when the operator meaning is not intuitively clear because a shorter program will always be easier to understand and maintain.

Solution: False. Operator overloading should be used sparingly, and only when intuitively clear, because otherwise it will be easy to use incorrectly, and it may be confusing to track down the problem.

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