CSCI-1200 Data Structures Test 3 — Practice Problems

Note: This packet contains practice problems from three previous exams. Your exam will contain approximately one third as many problems.

1 Un-Occupied Erase [/ 39]

Ben Bitdiddle was overwhelmed during the Data Structures lecture that covered the implementation details of erase for binary search trees. Separately handling the cases where the node to be erased had zero, one, or two non-NULL child pointers and then moving data around within the tree and/or disconnecting and reconnecting pointers seemed pointlessly complex (pun intended). Ben's plan is to instead leave the overall tree structure unchanged, but mark a node as unoccupied when the node containing the value to be erased has one or more children.

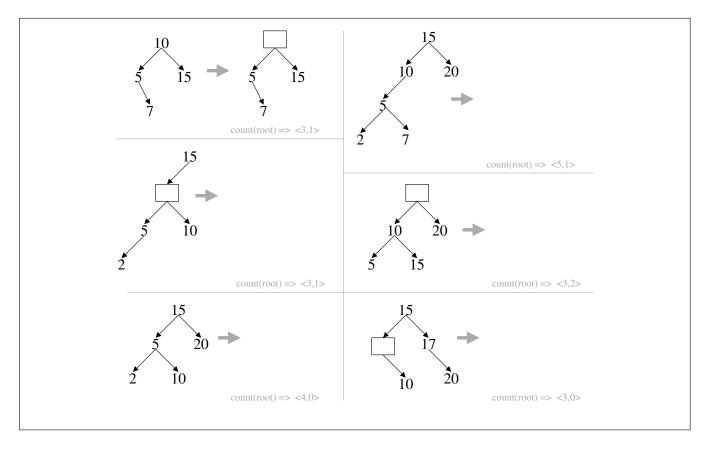
Ben's modified Node class is provided on the right.

```
template <class T>
class Node {
public:
   Node(const T& v) :
    occupied(true), value(v),
   left(NULL), right(NULL) {}
   bool occupied;
   T value;
   Node* left;
   Node* right;
};
```

1.1 Diagramming the Expected Output of erase [/ 6]

First, help Ben work through different test cases for the erase function. For each of the sample trees below, draw the tree after the call erase(root, 10). The first one has been done for you.

If a node is unoccupied, we draw it as an empty box. Below each result diagram we note the counts of occupied nodes and the number of unoccupied nodes within the tree. (We'll write the count function on the next page!) Note that an unoccupied node should always have at least one non-NULL child.



1.2 Counting Occupied & Unoccupied Nodes [/ 8]

Now let's write a recursive **count** function that takes a single argument, a pointer to the root of the tree, and returns an STL pair of integers. The first integer is the total number of *occupied* nodes in the tree and the second integer is the total number of *unoccupied* nodes in the tree. Refer to the diagrams on the previous page as examples.

```
sample solution: 10 line(s) of code
```

Alyssa P. Hacker stops by to see if Ben needs any help with his programming. She notes that when we insert a value into a tree, sometimes we will be able to re-use an unoccupied node, and other times we will have to create a new node and add it to the structure. She suggests a few helper functions that will be helpful in implementing the insert function for his binary search tree with unoccupied nodes:

```
template <class T>
                                                  template <class T>
const T& largest_value(Node<T>* p) {
                                                  const T& smallest_value(Node<T>* p) {
 assert (p != NULL);
                                                    assert (p != NULL);
  if (p->right == NULL) {
                                                    if (p->left == NULL) {
    if (p->occupied)
                                                       if (p->occupied)
     return p->value;
                                                        return p->value;
      return largest_value(p->left);
                                                         return smallest_value(p->right);
 return largest_value(p->right);
                                                    return smallest_value(p->left);
                                                  }
```

	in the tree.	

Implement erase for Trees with Unoccupied Nodes [

1.3

/ 13]

Now implement the insert function for Ben's binary search tree with unoccupied nodes. This function takes in two arguments, a pointer to the root node and the value to insert, and returns true if the value was successfully inserted or false if the value was not inserted because it was a duplicate of a value already in the tree. Use the provided smallest_value and largest_value functions in your implementation.
sample solution: 25 line(s) of code

Implement insert for Trees with Unoccupied Nodes [

1.4

/ 12]

2 Classroom Scheduler Maps [/ 37]

Louis B. Reasoner has been hired to automate RPI's weekly classroom scheduling system. A big fan of the C++ STL map data structure, he decided that maps would be a great fit for this application. Here's a portion of the main function with an example of how his program works:

```
room_reservations rr;
add_room(rr, "DCC", 308);
add_room(rr, "DCC", 318);
add_room(rr, "Lally", 102);
add_room(rr, "Lally", 104);
                                                                                "DS Exam")
bool success = make_reservation(rr, "DCC", 308, "Monday",
                                                                       18, 2,
                                                                                                &&
                make_reservation(rr, "DCC", 318, "Monday",
                                                                      18, 2,
                                                                                "DS Exam")
                make_reservation(rr, "DCC", 308, "Tuesday", 10, 2, "DS Lectus
make_reservation(rr, "Lally", 102, "Wednesday", 10, 10, "DS Lab")
                                                                                "DS Lecture") &&
                make_reservation(rr, "Lally", 104, "Wednesday", 10, 10, "DS Lab")
                make_reservation(rr, "DCC", 308, "Friday",
                                                                                "DS Lecture");
                                                                       10, 2,
assert (success == true);
```

In the small example above, only 4 classrooms are schedulable. To make a reservation we specify the building and room number, the day of the week (the initial design only handles Monday-Friday), the start time (using military 24-hour time, where 18 = 6 pm), the duration (in # of hours), and an STL string description of the event.

Here are a few key functions Louis wrote:

```
bool operator< (const std::pair<std::string,int> &a, const std::pair<std::string,int> &b) {
    return (a.first < b.first || (a.first == b.first && a.second < b.second));
}

void add_room(room_reservations &rr, const std::string &building, int room) {
    week_schedule ws;
    std::vector<std::string> empty_day(24,"");
    ws[std::string("Monday")] = empty_day;
    ws[std::string("Tuesday")] = empty_day;
    ws[std::string("Wednesday")] = empty_day;
    ws[std::string("Thursday")] = empty_day;
    ws[std::string("Friday")] = empty_day;
    rr[std::make_pair(building,room)] = ws;
}
```

Unfortunately, due to hard disk crash, Louis has lost the details of the two typedefs and his implementation of the make_reservation function. Your task is to help him recreate the implementation.

He does have a few more test cases for you to examine. Given the current state of the reservation system, these attempted reservations will all fail:

With these explanatory messages printed to std::cerr:

```
ERROR! conflicts with prior event: DS Exam ERROR! room DCC 307 does not exist ERROR! invalid time range: 22-25 ERROR! invalid day: Saturday
```

2.2 Diagram of the data stored in room_reservations rr [/8] Now, following the conventions from lecture for diagramming map data structures, draw the s stored in the rr variable after executing the instructions on the previous page. Yes, this is ac a big diagram, so don't attempt to draw everything, but be neat and draw enough detail to detai	
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that you understand now each component of the data structure is organized and his together.	tually quit demonstrat

2.3	Implementing make_reserva	cion [/ 16]		
	, implement the make_reservation problem to match the arguments, re			amples shown on the	e first page o
				sample solution: 28	line(s) of $code$

2.4	Performance and Memory Analysis [/ 8]
build days the sa times	let's analyze the running time of the make_reservation function you just wrote. If RPI has t ings, and each building has on average c classrooms, and we are storing schedule information for t (in the sample code t =5 days of the week), and the resolution of the schedule contains t time slots (in ample code t =24 1-hour time blocks), with a total of t 0 different events, each lasting an average of t 1 slots (data structures lecture lasts 2 1-hour time blocks), what is the order notation for the running of this function? Write 2-3 concise and complete sentences explaining your answer.
to sto bytes not s	g the same variables, write a simple formula for the approximate upper bound on the memory required ore this data structure. Assume each int is 4 bytes and each string has at most 32 characters = 32 per string. Omit the overhead for storing the underlying tree structure of nodes & pointers. Desimplify the answer as we normally would for order notation analysis. Write 1-2 concise and complete notes explaining your answer.
didn'	ly, using the same variables, what would be the order notation for the running time of a function (we task you to write this function!) to find all currently available rooms for a specific day and time of the task your answer.

3 Fashionable Sets [/ 14]

In this problem you will write a recursive function named outfits that takes as input two arguments: items and colors. items is an STL list of STL strings representing different types of clothing. colors is an STL list of STL sets of STL strings representing the different colors of each item of clothing. Your function should return an STL vector of STL strings describing each unique outfit (in any order) that can be created from these items of clothing.

Here is a small example:

red hat & red shirt & blue pants red hat & green shirt & blue pants red hat & white shirt & blue pants red hat & red shirt & black pants red hat & green shirt & black pants red hat & white shirt & black pants

sample solution: 22 line(s) of code

4 Spicy Chronological Sets using Maps [/ 33]

Ben Bitdiddle is organizing his spice collection using an STL set but runs into a problem. He needs the fast find, insert, and erase of an STL set, but in addition to organizing his spices alphabetically, he also needs to print them out in chronological order (so he can replace the oldest spices).

Ben is sure he'll have to make a complicated custom data structure, until Alyssa P. Hacker shows up and says it can be done using an STL map. She quickly sketches the diagram below for Ben, but then has to dash off to an interview for a Google summer internship.

Alyssa's diagram consists of 3 variables. The first variable, containing most of the data, is defined by a typedef. Even though he's somewhat confused by Alyssa's diagram, Ben has pushed ahead and decided on the following interface for building his spice collection:

```
chrono_set cs;
std::string oldest = "";
std::string newest = "";
insert(cs,oldest,newest,"garlic");
insert(cs,oldest,newest,"oregano");
insert(cs,oldest,newest,"nutmeg");
insert(cs,oldest,newest,"cinnamon");
insert(cs,oldest,newest,"basil");
insert(cs,oldest,newest,"sage");
insert(cs,oldest,newest,"dill");
```

chrono_set cs:

"basil"	<"cinnamon", "sage">
"cinnamon"	<"nutmeg", "basil">
"dill"	<"sage", "">
"garlic"	<"","oregano">
"nutmeg"	<"oregano","cinnamon">
"oregano"	<"garlic", "nutmeg">
"sage"	<"basil", "dill">

std::string oldest: "garlic"
std::string newest: "dill"

Ben would like to output the spices in 3 ways:

ALPHA ORDER:	basil	cinnamon	dill	garlic	nutmeg	oregano	sage
OLDEST FIRST:	garlic	oregano	nutmeg	cinnamon	basil	sage	dill
NEWEST FIRST:	dill	sage	basil	cinnamon	nutmeg	oregano	garlic

If he buys more of a spice already in the collection, the old spice jar should be discarded and replaced. For example, after calling:

```
insert(cs,oldest,newest,"cinnamon");
```

The spice collection output should now be:

sage	oregano	nutmeg	garlic	dill	cinnamon	basil	ALPHA ORDER:
cinnamon	dill	sage	basil	nutmeg	oregano	garlic	OLDEST FIRST:
garlic	oregano	nutmeg	basil	sage	dill	cinnamon	NEWEST FIRST:

4.1 The typedef [/ 3]

First, help Ben by completing the definition of the typedef below:

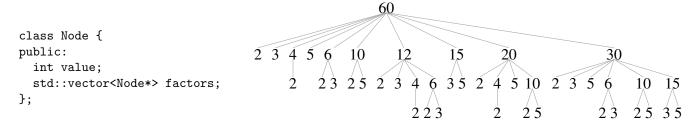
```
typedef chrono_set;
```

4.2 Printing out the spice collection [Next, write the code to output (to std::cout) Ben's	/ 8] spices in alphabetical and chronological order:
std::cout << "ALPHA ORDER: ";	
	sample solution: $4 line(s)$ of $code$
std::cout << std::endl;	
std::cout << "OLDEST FIRST: ";	
	sample solution: $5 line(s)$ of $code$
std::cout << std::endl;	
4.3 Performance Analysis [/ 5]	
Assuming Ben has n spices in his collection, what is	the order notation for each operation? <i>Note:</i> You
may want to first complete the implementation of the	
printing in alphabetical order:	
printing in chronological order:	
insert-ing a spice to the collection:	

4.4	Implementing insert for the chrono_set [/ 17]
Finally	y, implement the insert function for Ben's spice collection.	Make sure to handle all corner cases.
		sample solution: $26 \text{ line}(s)$ of code

5 Factor Tree [/ 13]

Write a recursive function named factor_tree that takes in a single argument of integer type and constructs the tree of the factors (and factors of each factor) of the input number. The function returns a pointer to the root of this tree. The example below illustrates the tree returned from the call factor_tree(60).

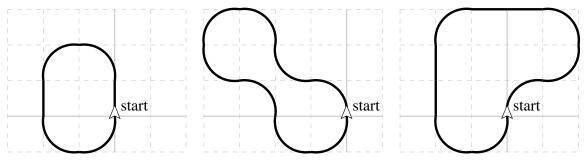


sample solution: 10 line(s) of code

6 Driving in Circles [/ 18]

In this problem you will write a recursive function named driving that outputs to std::cout all *closed* loop paths of driving instructions on a rectangular grid less than or equal to a specified maximum path length. The car begins at (0,0) pointing north and at each step can go *straight*, *left*, or *right*. A path is said to "close the loop" if it is finishes where it started, pointing in the same direction. For example, here are three sample closed loop paths (also illustrated below):

```
closed loop: straight left left straight left left
closed loop: left right left left right left left
closed loop: right left left straight straight left straight left left
```



We provide the Car class and several helper functions:

```
class Car {
public:
  Car(int x_{,int} y_{,std}::string dir_) : x(x_{,y}(y_{,dir}(dir_{,dir}))  {}
  int x;
  int y;
  std::string dir;
bool operator == (const Car &a, const Car &b) {
  return (a.x == b.x && a.y == b.y && a.dir == b.dir);
Car go_straight(const Car &c) {
         (c.dir == "north") { return Car(c.x ,c.y+1,c.dir); }
  else if (c.dir == "east") { return Car(c.x+1,c.y ,c.dir); }
  else if (c.dir == "south") { return Car(c.x ,c.y-1,c.dir); }
  else
                             { return Car(c.x-1,c.y ,c.dir); }
}
Car turn_left(const Car &c) {
          (c.dir == "north") { return Car(c.x-1,c.y+1,"west"); }
  else if (c.dir == "east") { return Car(c.x+1,c.y+1,"north"); }
  else if (c.dir == "south") { return Car(c.x+1,c.y-1,"east"); }
                             { return Car(c.x-1,c.y-1, "south"); }
}
Car turn_right(const Car &c) {
          (c.dir == "north") { return Car(c.x+1,c.y+1,"east"); }
  else if (c.dir == "east") { return Car(c.x+1,c.y-1,"south"); }
  else if (c.dir == "south") { return Car(c.x-1,c.y-1,"west"); }
                             { return Car(c.x-1,c.y+1,"north"); }
  else
}
```

Your function should take in 3 arguments: the path constructed so far, the current car position & direction, and the maximum number of steps/instructions allowed. For example:

```
std::vector<std::string> path;
Car car(0,0,"north");
int max_steps = 10;
driving (path,car,max_steps);
```

ow implement the re	cursive driving full	nction.		
			sample solution.	$25 \ line(s) \ of \ code$
			Sample boundedle.	~ 00000 01 01 0000

7	Maps	of Sets	of Factors		/ 32
---	------	---------	------------	--	------

In this problem we will use STL map and STL set to store and access a collection of integers and their factors. Below are the commands we use to initialize the two data structures diagrammed on the right.

factors			
5			
6	2 3		
8	2 4		
9	3		
10	2 5		
12	2346		
13			
14	2 7		
15	3 5		
21	3 7		

is_factor_of				
2	6 8 10 12 14			
3	6 9 12 15 21			
4	8 12			
5	10 15			
6	12			
7	14 21			

7.1 The typedef [/ 2]

First, complete the definition of the typedef below:

typedef factor_type;

7.2 Implementing add_factors [/ 8]

Now, implement the add_factors function. Note that this function only initializes the factors table.

 $sample\ solution:\ 8\ line(s)\ of\ code$

If we are storing the factors of n different numbers in the factors structure, f different factors will eventually be stored in the <code>is_factor_of</code> structure, each number has on average (or at most) j factors, and each factor is a factor of on average (or at most) k numbers, what is the order notation for the running time of your add_factors function to add the number x and the factors of x ?
7.3 Implementing reverse [/ 10]
Next, implement the reverse function to build the is_factor_of table from the completed factors table.
sample solution: $9 line(s)$ of code
Using the variables n, f, j , and k as defined above, what is the order notation for the running time of your reverse function?

7.4 Implementing remove [/ 12]

Finally, we would like to remove data from the tables. The remove function will remove a given number's row from the factors table and remove the number from each of its factors in the is_factor_of table. For example, the call below results in the tables to the right.

remove(12,factors,is_factor_of);

Your task is to efficiently implement the **remove** function. Using the variables defined above, you should assume that $n \ge f \ge k \ge j$.

factor	'S
5	
6	2 3
8	2 4
9	3
10	2 5
13	
14	2 7
15	3 5

s_factor_of				
2	6 8 10 14			
3	6 9 15 21			
4	8			
5	10 15			
7	14 21			

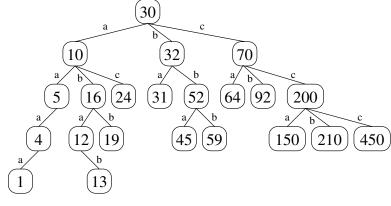
iables defined above, you sl	hould assume that $n \geq f \geq$	$k \ge j$.	21 37	
			1 1 1 4	, 1: () C
			sample solution: 14	$\frac{line(s) \text{ of } c}{c}$
	d k as defined above, what i	is the order not	ation for the running	ng time of y
ove function?				

8 Double Tries [/ 30]

class Node {
public:
 int value;
 Node *a;
 Node *b;
 Node *c;
 Node *parent;

Ben Bitdiddle thinks he's come up with a fantastic enhancement for binary search trees of integers he calls the Double Trie. Each Node will have up to 3 children. The a branch will store all elements less than the current node. The b branch will store all elements greater than the current node, but less than or equal to twice the current node. And the c branch will store all elements greater than twice the current node.

Ben suggests we start the implementation by writing a recursive insert function that takes in a pointer to node (initially the root of the Double Trie), the value to insert, and a pointer to the parent node (initially NULL). The function returns true if the value was successfully inserted and false if the value is already in the structure.



8.1 Implementing insert [

/ 10]

sample solution: 19 line(s) of code

Ben's project partner Alyssa P. Hacker isn't thrilled with the design. (She's not sure it will significantly reduce the tree height because this structure is difficult to keep balanced.) However, they have a deadline, so this is a make-it-work moment and she tackles the challenge of reverse iteration over this structure. Specifically if the root variable points to the top of the diagram on the previous page, she would like this fragment of code:

```
Node *tmp = find_largest(root);
while (tmp != NULL) {
   std::cout << tmp->value << " ";
   tmp = find_previous(tmp);
}
std::cout << std::endl;

to print all of the data in the tree in reverse order:
   450 210 200 150 92 70 64 59 52 45 32 31 30 24 19 16 13 12 10 5 4 1</pre>
```

8.2 Implementing find_largest [/ 6]

Next, Alyssa implements the find_largest function:

```
sample solution: 8 line(s) of code
```

Given a reasonably balanced Double Trie with n elements, what is the order notation of the running time of the find_largest function? Write one or two sentences explaining your answer.

8.3 Implementing find_previous [/ 14]				
Finally, Alyssa implements the find_previous function:				
San	$nple\ solution:\ 17\ line(s)\ of\ code$			
	1			

9 Re-Truthization [$/$ 14]
The statements below are false. Make a small change to correct each statement, ensuring that it remains interesting and informative.
Binary Search Tree Iterators [/2] The average number of child or parent links that must be traversed when moving from one node to the next node in an in-order traversal is $O(\log n)$, where n is the number of elements in the tree.
Incomplete type [/2] In HW8 Friendly Recursion, many students encountered the compiler message "error: invalid use of incomplete type 'class Message'", which should be solved by implementing all custom class member functions in the class declaration .h file.
Breadth-First Search [/3] Executing a breadth-first search for the shortest path from root to leaf on a binary search tree will often be faster and require less additional memory than a depth-first search on the same tree.
Been Here Before? [/2] To optimize the HW6 Ricochet Robots solver, the search tree for a board with three robots can be pruned (and the forward search from that point terminated) if any one of the robots reaches a board location that it has previously occupied.
Hash Function Performance [$/2$] A hash function should run in $O(1)$ time, to ensure that the hash table will achieve $O(\log n)$ query time, where n is the number of elements in the hash table.
Red-Black Property [/3] Maintaining the Red-Black property for a hash table ensures that the data remains balanced and elements can be accessed in $O(\log n)$ time.

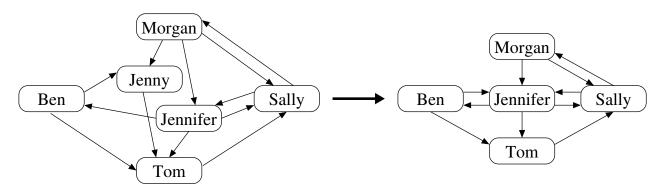
10 Friend Graphs [/ 21]

In this problem you will work with a simplified version of the Twitter or Google+ friendship/follower directed graph from HW8. Your task is to write a merge_account function that takes in a Graph object and the STL string names of two accounts and then modifies the graph to merge the two corresponding Person objects into a single object. Other people in the graph who were connected to either of the original accounts by a connection of either direction will be updated to link to the merged account. For example, let's start with the graph connectivity on the left below. We want to merge the accounts for "Jennifer" and "Jenny", preserving the name "Jennifer" on the merged account. We execute the following statement, resulting in the picture on the right.

```
class Person {
public:
    std::string name;
    std::set<Person*> friends;
};

class Graph {
public:
    std::vector<Person*> people;
};
```

merge_accounts(graph, "Jennifer", "Jenny");



10.1 Corner Cases for merge_accounts [/ 6]

Think carefully about a typical use case for merging accounts, and also about corner cases for the merge_accounts function. What different test cases will you need to write to ensure that your implementation is fully debugged and will work when attempting to join two arbitrary Person objects in a large graph? Write three or four concise and well written sentences describing sample input and the expected output.

10.2	Implementation of merge_accou	nts [/ 15 $]$		
Now, errors	implement the merge_accounts function or memory leaks.	n. Make sure	e that your	function does no	ot lead to memory
				cample solution	a. 22 line(e) of code

11 Lamp Class Inheritance [/26]

In this problem you will complete the implementation for a group of three interrelated classes. The first class is used to represent a light bulb and simply stores the wattage of that bulb:

```
class Bulb {
public:
   int getWatts() const { return watts; }
   void setWatts(int w) { watts = w; }
private:
   int watts;
};
```

The second class represents an electric lamp with a fixed number of sockets to hold Bulb objects. The constructor takes the number of bulbs and initial wattage and dynamically allocates an array of bulbs of the specified wattage. The switch_lights_on member function turns on the bulbs in the lamp and returns the total number of watts consumed by the lights in the lamp (the sum of the individual bulb wattages).

```
class Lamp {
public:
  Lamp(int n, int watts);
  virtual ~Lamp();
  // MODIFIERS
  void replace_bulb(int i, int watts) {
    assert (i >= 0 && i < num_bulbs);</pre>
    sockets[i].setWatts(watts); }
  int switch_lights_on();
  virtual void switch_off() { lights_on = false; }
private:
  // REPRESENTATION
  int num_bulbs;
  Bulb *sockets; // a dynamically allocated array
  bool lights_on;
};
```

The third class is derived from the Lamp object to represent ceiling lamps that also have a fan. The lights and fan can be separately switched on for FanLamp objects, but the switch_off member function should turn switch off both components.

Here's an example of how to construct a polymorphic vector of these objects, switch on the light bulbs in the third lamp, and replace one of the bulbs in the second lamp (a FanLamp).
<pre>vector<lamp*> lamps; lamps.push_back(new Lamp(1,100)); lamps.push_back(new FanLamp(3,40)); lamps.push_back(new Lamp(2,60));</lamp*></pre>
<pre>lamps[2]->switch_lights_on(); lamps[1]->replace_bulb(2,60);</pre>
11.1 Constructors & Destructors [/9]
Implement the constructor and destructor for the Lamp class, as they would appear in the implementation $(.cpp)$ file.
11.2 The virtual keyword [/3]
What is the purpose of the virtual keyword? Write 1-2 concise and well-written sentences.

11.3	3 Turning the Lamps On & Off [/9]				
	lement the the Lamp::switch_lights_on() and FanLamp::swear in the implementation file.	ritch_off()	functions as	s they	would
11.4	Manipulating a Polymorphic Vector of Lamps [/5]			
	write a fragment of code that manipulates lamps, a polymorph		pointers to 1	Lamp o	bjects,
	irn the lights on for only the FanLamp objects in that vector.				

12 Advanced Topics Potpourri [/9]
Most (but not all) of the statements below are false. Identify each statement as false or true, and correct each false statement so that it is true (but still informative). 12.1 Exceptions [/3]
True or False A class constructor may "fail" only in two manners: it may throw an exception or it may return NULL (useful when the system is out of memory).
12.2 Multiple Inheritance [/3]
True or False When the inheritance diagram includes a set of classes that form a diamond, two instance of the base class will be created unless the keyword "trapezoid" is used in the .cpp file to explicitly specific the construction of only one instance of the base class.
12.3 Operator Overloading [/3]
True or False Good programming style for class design encourages the use of operator overloading ever when the operator meaning is not intuitively clear because a shorter program will always be easier tunderstand and maintain.