Leetcode 题解 - 树

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 - Trie
 - 1. 实现一个 Trie
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递归

一棵树要么是空树,要么有两个指针,每个指针指向一棵树。树是一种递归结构,很多树的问题可以使用递归 来处理。

1. 树的高度

104. Maximum Depth of Binary Tree (Easy)

Leetcode / 力扣

```
public int maxDepth(TreeNode root) {
   if (root == null) return 0;
   return Math.max(maxDepth(root.left), maxDepth(root.right)) + 1;
}
```

2. 平衡树

110. Balanced Binary Tree (Easy)

Leetcode / 力扣

```
3
/\
9 20
/\
15 7
```

平衡树左右子树高度差都小于等于 1

```
private boolean result = true;

public boolean isBalanced(TreeNode root) {
    maxDepth(root);
    return result;
}

public int maxDepth(TreeNode root) {
    if (root == null) return 0;
    int 1 = maxDepth(root.left);
    int r = maxDepth(root.right);
    if (Math.abs(1 - r) > 1) result = false;
    return 1 + Math.max(1, r);
}
```

3. 两节点的最长路径

543. Diameter of Binary Tree (Easy)

```
Input:

1
/ \
2 3
/ \
4 5

Return 3, which is the length of the path [4,2,1,3] or [5,2,1,3].
```

```
private int max = 0;

public int diameterOfBinaryTree(TreeNode root) {
    depth(root);
    return max;
}

private int depth(TreeNode root) {
    if (root == null) return 0;
    int leftDepth = depth(root.left);
    int rightDepth = depth(root.right);
    max = Math.max(max, leftDepth + rightDepth);
    return Math.max(leftDepth, rightDepth) + 1;
}
```

4. 翻转树

226. Invert Binary Tree (Easy)

Leetcode / 力扣

```
public TreeNode invertTree(TreeNode root) {
   if (root == null) return null;
   TreeNode left = root.left; // 后面的操作会改变 left 指针, 因此先保存下来
   root.left = invertTree(root.right);
   root.right = invertTree(left);
   return root;
}
```

5. 归并两棵树

617. Merge Two Binary Trees (Easy)

```
Input:
                           Tree 2
     Tree 1
       1
                            2
      /\
                           /\
                           1 3
      3 2
     /
    5
Output:
      3
     / \
     4 5
    / \ \
    5 4 7
```

```
public TreeNode mergeTrees(TreeNode t1, TreeNode t2) {
   if (t1 == null && t2 == null) return null;
   if (t1 == null) return t2;
   if (t2 == null) return t1;
   TreeNode root = new TreeNode(t1.val + t2.val);
   root.left = mergeTrees(t1.left, t2.left);
   root.right = mergeTrees(t1.right, t2.right);
   return root;
}
```

6. 判断路径和是否等于一个数

Leetcdoe: 112. Path Sum (Easy)

Leetcode / 力扣

```
Given the below binary tree and sum = 22,

5
/\
4 8
//\
11 13 4
/\\
7 2 1

return true, as there exist a root-to-leaf path 5->4->11->2 which sum is 22.
```

路径和定义为从 root 到 leaf 的所有节点的和。

```
public boolean hasPathSum(TreeNode root, int sum) {
   if (root == null) return false;
   if (root.left == null && root.right == null && root.val == sum) return true;
   return hasPathSum(root.left, sum - root.val) || hasPathSum(root.right, sum -
   root.val);
}
```

7. 统计路径和等于一个数的路径数量

437. Path Sum III (Easy)

Leetcode / 力扣

路径不一定以 root 开头,也不一定以 leaf 结尾,但是必须连续。

```
public int pathSum(TreeNode root, int sum) {
    if (root == null) return 0;
    int ret = pathSumStartWithRoot(root, sum) + pathSum(root.left, sum) +
    pathSum(root.right, sum);
    return ret;
}

private int pathSumStartWithRoot(TreeNode root, int sum) {
    if (root == null) return 0;
    int ret = 0;
    if (root.val == sum) ret++;
    ret += pathSumStartWithRoot(root.left, sum - root.val) +
    pathSumStartWithRoot(root.right, sum - root.val);
    return ret;
}
```

8. 子树

572. Subtree of Another Tree (Easy)

```
Given tree s:
    3
   / \
  4 5
 / \
 1 2
Given tree t:
  4
 / \
1 2
Return true, because t has the same structure and node values with a subtree of s.
Given tree s:
   3
   /\
  4 5
 / \
 1 2
   /
  0
Given tree t:
  4
 / \
Return false.
```

```
public boolean isSubtree(TreeNode s, TreeNode t) {
   if (s == null) return false;
   return isSubtreeWithRoot(s, t) || isSubtree(s.left, t) || isSubtree(s.right, t);
}

private boolean isSubtreeWithRoot(TreeNode s, TreeNode t) {
   if (t == null && s == null) return true;
   if (t == null || s == null) return false;
   if (t.val != s.val) return false;
   return isSubtreeWithRoot(s.left, t.left) && isSubtreeWithRoot(s.right, t.right);
}
```

9. 树的对称

101. Symmetric Tree (Easy)

Leetcode / 力扣

```
1
/\
2 2
/\\/
3 4 4 3
```

```
public boolean isSymmetric(TreeNode root) {
   if (root == null) return true;
   return isSymmetric(root.left, root.right);
}

private boolean isSymmetric(TreeNode t1, TreeNode t2) {
   if (t1 == null && t2 == null) return true;
   if (t1 == null || t2 == null) return false;
   if (t1.val != t2.val) return false;
   return isSymmetric(t1.left, t2.right) && isSymmetric(t1.right, t2.left);
}
```

10. 最小路径

111. Minimum Depth of Binary Tree (Easy)

Leetcode / 力扣

树的根节点到叶子节点的最小路径长度

```
public int minDepth(TreeNode root) {
   if (root == null) return 0;
   int left = minDepth(root.left);
   int right = minDepth(root.right);
   if (left == 0 || right == 0) return left + right + 1;
   return Math.min(left, right) + 1;
}
```

11. 统计左叶子节点的和

404. Sum of Left Leaves (Easy)

```
3
/\
9 20
/\
15 7

There are two left leaves in the binary tree, with values 9 and 15 respectively.
Return 24.
```

```
public int sumOfLeftLeaves(TreeNode root) {
    if (root == null) return 0;
    if (isLeaf(root.left)) return root.left.val + sumOfLeftLeaves(root.right);
    return sumOfLeftLeaves(root.left) + sumOfLeftLeaves(root.right);
}

private boolean isLeaf(TreeNode node){
    if (node == null) return false;
    return node.left == null && node.right == null;
}
```

12. 相同节点值的最大路径长度

687. Longest Univalue Path (Easy)

```
1
/\
4 5
/\\
4 4 5
Output: 2
```

```
private int path = 0;

public int longestUnivaluePath(TreeNode root) {
    dfs(root);
    return path;
}

private int dfs(TreeNode root) {
    if (root == null) return 0;
    int left = dfs(root.left);
    int right = dfs(root.right);
    int leftPath = root.left != null && root.left.val == root.val ? left + 1 : 0;
```

```
int rightPath = root.right != null && root.right.val == root.val ? right + 1 :
0;
  path = Math.max(path, leftPath + rightPath);
  return Math.max(leftPath, rightPath);
}
```

13. 间隔遍历

337. House Robber III (Medium)

Leetcode / 力扣

```
3 /\ 2 3 \\ 3 1 Maximum amount of money the thief can rob = 3 + 3 + 1 = 7.
```

```
public int rob(TreeNode root) {
   if (root == null) return 0;
   int val1 = root.val;
   if (root.left != null) val1 += rob(root.left.left) + rob(root.left.right);
   if (root.right != null) val1 += rob(root.right.left) + rob(root.right.right);
   int val2 = rob(root.left) + rob(root.right);
   return Math.max(val1, val2);
}
```

14. 找出二叉树中第二小的节点

671. Second Minimum Node In a Binary Tree (Easy)

Leetcode / 力扣

```
Input:

2
/\
2 5
/\
5 7

Output: 5
```

一个节点要么具有 0 个或 2 个子节点,如果有子节点,那么根节点是最小的节点。

```
public int findSecondMinimumValue(TreeNode root) {
    if (root == null) return -1;
    if (root.left == null && root.right == null) return -1;
    int leftVal = root.left.val;
    int rightVal = root.right.val;
    if (leftVal == root.val) leftVal = findSecondMinimumValue(root.left);
    if (rightVal == root.val) rightVal = findSecondMinimumValue(root.right);
    if (leftVal != -1 && rightVal != -1) return Math.min(leftVal, rightVal);
    if (leftVal != -1) return leftVal;
    return rightVal;
}
```

层次遍历

使用 BFS 进行层次遍历。不需要使用两个队列来分别存储当前层的节点和下一层的节点,因为在开始遍历一层的节点时,当前队列中的节点数就是当前层的节点数,只要控制遍历这么多节点数,就能保证这次遍历的都是当前层的节点。

1. 一棵树每层节点的平均数

637. Average of Levels in Binary Tree (Easy)

Leetcode / 力扣

```
public List<Double> averageOfLevels(TreeNode root) {
   List<Double> ret = new ArrayList<>();
   if (root == null) return ret;
   Queue<TreeNode> queue = new LinkedList<>();
   queue.add(root);
   while (!queue.isEmpty()) {
        int cnt = queue.size();
        double sum = 0;
        for (int i = 0; i < cnt; i++) {
            TreeNode node = queue.poll();
            sum += node.val;
            if (node.left != null) queue.add(node.left);
            if (node.right != null) queue.add(node.right);
        ret.add(sum / cnt);
   return ret;
}
```

2. 得到左下角的节点

513. Find Bottom Left Tree Value (Easy)

```
Input:

1
/\
2 3
//\
4 5 6
/
7

Output:
7
```

```
public int findBottomLeftValue(TreeNode root) {
    Queue<TreeNode> queue = new LinkedList<>();
    queue.add(root);
    while (!queue.isEmpty()) {
        root = queue.poll();
        if (root.right != null) queue.add(root.right);
        if (root.left != null) queue.add(root.left);
    }
    return root.val;
}
```

前中后序遍历

```
1
/\
2 3
/\ \
4 5 6
```

层次遍历顺序: [123456]
前序遍历顺序: [124536]
中序遍历顺序: [425136]
后序遍历顺序: [452631]

层次遍历使用 BFS 实现,利用的就是 BFS 一层一层遍历的特性;而前序、中序、后序遍历利用了 DFS 实现。 前序、中序、后序遍只是在对节点访问的顺序有一点不同,其它都相同。

① 前序

```
void dfs(TreeNode root) {
   visit(root);
   dfs(root.left);
```

```
dfs(root.right);
}
```

2 中序

```
void dfs(TreeNode root) {
    dfs(root.left);
    visit(root);
    dfs(root.right);
}
```

③ 后序

```
void dfs(TreeNode root) {
    dfs(root.left);
    dfs(root.right);
    visit(root);
}
```

1. 非递归实现二叉树的前序遍历

144. Binary Tree Preorder Traversal (Medium)

Leetcode / 力扣

```
public List<Integer> preorderTraversal(TreeNode root) {
   List<Integer> ret = new ArrayList<>();
   Stack<TreeNode> stack = new Stack<>();
   stack.push(root);
   while (!stack.isEmpty()) {
      TreeNode node = stack.pop();
      if (node == null) continue;
      ret.add(node.val);
      stack.push(node.right); // 先右后左, 保证左子树先遍历
      stack.push(node.left);
   }
   return ret;
}
```

2. 非递归实现二叉树的后序遍历

145. Binary Tree Postorder Traversal (Medium)

前序遍历为 root -> left -> right, 后序遍历为 left -> right -> root。可以修改前序遍历成为 root -> right -> left, 那么这个顺序就和后序遍历正好相反。

```
public List<Integer> postorderTraversal(TreeNode root) {
   List<Integer> ret = new ArrayList<>();
   Stack<TreeNode> stack = new Stack<>();
   stack.push(root);
   while (!stack.isEmpty()) {
        TreeNode node = stack.pop();
        if (node == null) continue;
        ret.add(node.val);
        stack.push(node.left);
        stack.push(node.right);
   }
   Collections.reverse(ret);
   return ret;
}
```

3. 非递归实现二叉树的中序遍历

94. Binary Tree Inorder Traversal (Medium)

Leetcode / 力扣

BST

- 二叉查找树 (BST) : 根节点大于等于左子树所有节点,小于等于右子树所有节点。
- 二叉查找树中序遍历有序。
- 1. 修剪二叉查找树

669. Trim a Binary Search Tree (Easy)

Leetcode / 力扣

```
Input:

3
/\
0     4
\
2
//
1

L = 1
R = 3

Output:

3
//
2
//
1
```

题目描述: 只保留值在 L~R之间的节点

```
public TreeNode trimBST(TreeNode root, int L, int R) {
   if (root == null) return null;
   if (root.val > R) return trimBST(root.left, L, R);
   if (root.val < L) return trimBST(root.right, L, R);
   root.left = trimBST(root.left, L, R);
   root.right = trimBST(root.right, L, R);
   return root;
}</pre>
```

2. 寻找二叉查找树的第 k 个元素

230. Kth Smallest Element in a BST (Medium)

Leetcode / 力扣

中序遍历解法:

```
private int cnt = 0;
private int val;

public int kthSmallest(TreeNode root, int k) {
```

```
inOrder(root, k);
  return val;
}

private void inOrder(TreeNode node, int k) {
  if (node == null) return;
  inOrder(node.left, k);
  cnt++;
  if (cnt == k) {
    val = node.val;
    return;
  }
  inOrder(node.right, k);
}
```

递归解法:

```
public int kthSmallest(TreeNode root, int k) {
   int leftCnt = count(root.left);
   if (leftCnt == k - 1) return root.val;
   if (leftCnt > k - 1) return kthSmallest(root.left, k);
   return kthSmallest(root.right, k - leftCnt - 1);
}

private int count(TreeNode node) {
   if (node == null) return 0;
   return 1 + count(node.left) + count(node.right);
}
```

3. 把二叉查找树每个节点的值都加上比它大的节点的值

Convert BST to Greater Tree (Easy)

Leetcode / 力扣

先遍历右子树。

```
private int sum = 0;

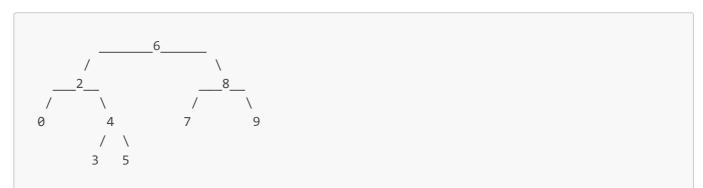
public TreeNode convertBST(TreeNode root) {
    traver(root);
    return root;
}

private void traver(TreeNode node) {
    if (node == null) return;
    traver(node.right);
    sum += node.val;
    node.val = sum;
    traver(node.left);
}
```

4. 二叉查找树的最近公共祖先

235. Lowest Common Ancestor of a Binary Search Tree (Easy)

Leetcode / 力扣

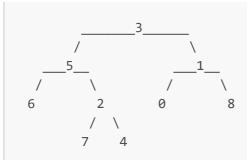


For example, the lowest common ancestor (LCA) of nodes 2 and 8 is 6. Another example is LCA of nodes 2 and 4 is 2, since a node can be a descendant of itself according to the LCA definition.

```
public TreeNode lowestCommonAncestor(TreeNode root, TreeNode p, TreeNode q) {
   if (root.val > p.val && root.val > q.val) return
lowestCommonAncestor(root.left, p, q);
   if (root.val < p.val && root.val < q.val) return
lowestCommonAncestor(root.right, p, q);
   return root;
}</pre>
```

5. 二叉树的最近公共祖先

236. Lowest Common Ancestor of a Binary Tree (Medium)



For example, the lowest common ancestor (LCA) of nodes 5 and 1 is 3. Another example is LCA of nodes 5 and 4 is 5, since a node can be a descendant of itself according to the LCA definition.

```
public TreeNode lowestCommonAncestor(TreeNode root, TreeNode p, TreeNode q) {
   if (root == null || root == p || root == q) return root;
   TreeNode left = lowestCommonAncestor(root.left, p, q);
   TreeNode right = lowestCommonAncestor(root.right, p, q);
   return left == null ? right : right == null ? left : root;
}
```

6. 从有序数组中构造二叉查找树

108. Convert Sorted Array to Binary Search Tree (Easy)

Leetcode / 力扣

```
public TreeNode sortedArrayToBST(int[] nums) {
    return toBST(nums, 0, nums.length - 1);
}

private TreeNode toBST(int[] nums, int sIdx, int eIdx){
    if (sIdx > eIdx) return null;
    int mIdx = (sIdx + eIdx) / 2;
    TreeNode root = new TreeNode(nums[mIdx]);
    root.left = toBST(nums, sIdx, mIdx - 1);
    root.right = toBST(nums, mIdx + 1, eIdx);
    return root;
}
```

7. 根据有序链表构造平衡的二叉查找树

109. Convert Sorted List to Binary Search Tree (Medium)

```
Given the sorted linked list: [-10,-3,0,5,9],
```

```
One possible answer is: [0,-3,9,-10,null,5], which represents the following height balanced BST:

0
/\
-3 9
/ /
-10 5
```

```
public TreeNode sortedListToBST(ListNode head) {
    if (head == null) return null;
    if (head.next == null) return new TreeNode(head.val);
    ListNode preMid = preMid(head);
    ListNode mid = preMid.next;
    preMid.next = null; // 断开链表
   TreeNode t = new TreeNode(mid.val);
   t.left = sortedListToBST(head);
   t.right = sortedListToBST(mid.next);
   return t;
}
private ListNode preMid(ListNode head) {
   ListNode slow = head, fast = head.next;
   ListNode pre = head;
   while (fast != null && fast.next != null) {
        pre = slow;
        slow = slow.next;
        fast = fast.next.next;
   return pre;
}
```

8. 在二叉查找树中寻找两个节点, 使它们的和为一个给定值

653. Two Sum IV - Input is a BST (Easy)

```
Input:
    5
    / \
    3    6
    / \    \
    2    4    7

Target = 9

Output: True
```

使用中序遍历得到有序数组之后, 再利用双指针对数组进行查找。

应该注意到,这一题不能用分别在左右子树两部分来处理这种思想,因为两个待求的节点可能分别在左右子树中。

```
public boolean findTarget(TreeNode root, int k) {
    List<Integer> nums = new ArrayList<>();
    inOrder(root, nums);
    int i = 0, j = nums.size() - 1;
    while (i < j) {
        int sum = nums.get(i) + nums.get(j);
       if (sum == k) return true;
       if (sum < k) i++;
        else j--;
    return false;
}
private void inOrder(TreeNode root, List<Integer> nums) {
    if (root == null) return;
    inOrder(root.left, nums);
    nums.add(root.val);
    inOrder(root.right, nums);
}
```

9. 在二叉查找树中查找两个节点之差的最小绝对值

530. Minimum Absolute Difference in BST (Easy)

Leetcode / 力扣

利用二叉查找树的中序遍历为有序的性质,计算中序遍历中临近的两个节点之差的绝对值,取最小值。

```
private int minDiff = Integer.MAX_VALUE;
private TreeNode preNode = null;
```

```
public int getMinimumDifference(TreeNode root) {
    inOrder(root);
    return minDiff;
}

private void inOrder(TreeNode node) {
    if (node == null) return;
    inOrder(node.left);
    if (preNode != null) minDiff = Math.min(minDiff, node.val - preNode.val);
    preNode = node;
    inOrder(node.right);
}
```

10. 寻找二叉查找树中出现次数最多的值

501. Find Mode in Binary Search Tree (Easy)

Leetcode / 力扣

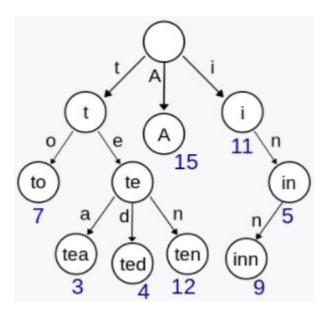
```
1
\
2
/
2
return [2].
```

答案可能不止一个,也就是有多个值出现的次数一样多。

```
private int curCnt = 1;
private int maxCnt = 1;
private TreeNode preNode = null;
public int[] findMode(TreeNode root) {
   List<Integer> maxCntNums = new ArrayList<>();
    inOrder(root, maxCntNums);
    int[] ret = new int[maxCntNums.size()];
    int idx = 0;
    for (int num : maxCntNums) {
        ret[idx++] = num;
   return ret;
}
private void inOrder(TreeNode node, List<Integer> nums) {
   if (node == null) return;
    inOrder(node.left, nums);
    if (preNode != null) {
```

```
if (preNode.val == node.val) curCnt++;
    else curCnt = 1;
}
if (curCnt > maxCnt) {
    maxCnt = curCnt;
    nums.clear();
    nums.add(node.val);
} else if (curCnt == maxCnt) {
    nums.add(node.val);
}
preNode = node;
inOrder(node.right, nums);
}
```

Trie



Trie,又称前缀树或字典树,用于判断字符串是否存在或者是否具有某种字符串前缀。

1. 实现一个 Trie

208. Implement Trie (Prefix Tree) (Medium)

```
class Trie {
    private class Node {
        Node[] childs = new Node[26];
        boolean isLeaf;
}

private Node root = new Node();

public Trie() {
```

```
public void insert(String word) {
        insert(word, root);
   private void insert(String word, Node node) {
        if (node == null) return;
       if (word.length() == 0) {
            node.isLeaf = true;
            return;
        }
        int index = indexForChar(word.charAt(∅));
        if (node.childs[index] == null) {
            node.childs[index] = new Node();
        insert(word.substring(1), node.childs[index]);
   }
    public boolean search(String word) {
        return search(word, root);
   private boolean search(String word, Node node) {
        if (node == null) return false;
        if (word.length() == 0) return node.isLeaf;
        int index = indexForChar(word.charAt(∅));
        return search(word.substring(1), node.childs[index]);
   }
    public boolean startsWith(String prefix) {
        return startWith(prefix, root);
   private boolean startWith(String prefix, Node node) {
        if (node == null) return false;
       if (prefix.length() == 0) return true;
        int index = indexForChar(prefix.charAt(0));
        return startWith(prefix.substring(1), node.childs[index]);
   }
   private int indexForChar(char c) {
        return c - 'a';
   }
}
```

2. 实现一个 Trie, 用来求前缀和

677. Map Sum Pairs (Medium)

```
Input: insert("apple", 3), Output: Null
Input: sum("ap"), Output: 3
Input: insert("app", 2), Output: Null
Input: sum("ap"), Output: 5
```

```
class MapSum {
   private class Node {
        Node[] child = new Node[26];
       int value;
   }
   private Node root = new Node();
   public MapSum() {
   }
   public void insert(String key, int val) {
        insert(key, root, val);
   }
   private void insert(String key, Node node, int val) {
        if (node == null) return;
       if (key.length() == 0) {
            node.value = val;
            return;
       }
       int index = indexForChar(key.charAt(∅));
       if (node.child[index] == null) {
            node.child[index] = new Node();
        insert(key.substring(1), node.child[index], val);
   }
   public int sum(String prefix) {
        return sum(prefix, root);
   }
   private int sum(String prefix, Node node) {
       if (node == null) return 0;
       if (prefix.length() != 0) {
            int index = indexForChar(prefix.charAt(∅));
            return sum(prefix.substring(1), node.child[index]);
        int sum = node.value;
       for (Node child : node.child) {
            sum += sum(prefix, child);
        return sum;
```

```
private int indexForChar(char c) {
    return c - 'a';
}
```