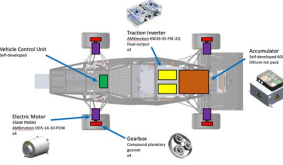


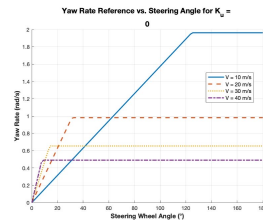
## Project Background

Zips Racing designs and builds an electric formula-style race car to compete against other universities in the Formula SAE challenge every year. This project's objective is to design a vehicle control unit to control a new four-wheel drive electric powertrain and improve vehicle performance by implementing torque-vectoring and regenerative braking algorithms, while ensuring safe and reliable operation of the vehicle.



## Yaw Controller Design

### Yaw Reference Calculation



### Goal

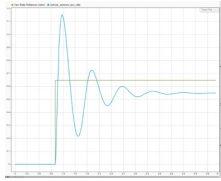
Control the yaw-rate to achieve a desired understeer behavior for the vehicle, by actuating the yaw moment. By increasing the steady-state yaw rate, the vehicle can achieve a higher cornering speed.

### Method

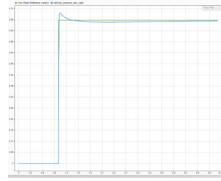
PID controller with gain scheduling. Non-linear model is tuned using a gradient-descent method by analyzing the step response at different operating points.

### Target Response

10% overshoot, zero steady-state error, with the fastest rise time.

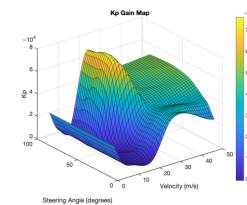


Natural Response Sample

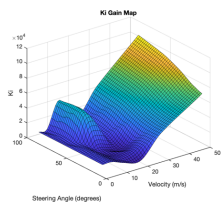


Tuned Response Sample

### Results:



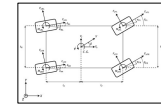
Kf Gain Map



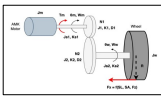
Kf Gain Map

## Model Development

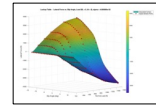
### Vehicle Body Dynamics



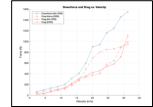
### Wheel Dynamics



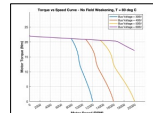
### Tire Data



### Aerodynamics



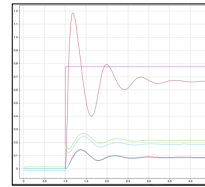
### Electric Motor Model



### Full Vehicle Model



A non-linear vehicle model was made in MATLAB Simulink to analyze the transient cornering response of the vehicle, before it is built. The model is based on the double-track vehicle dynamics model



The model takes in (accelerator, brake, and steering inputs, allowing simulation of different driving maneuvers. Steady-state cornering, step-steer, and sine-steer maneuvers were prioritized.

## Torque Optimization

### Goal

Calculate all four motor torques in real-time to meet objectives.

$$\text{minimize } w_1 \frac{f_1}{a_1} + w_2 \frac{f_2}{a_2} + w_3 \frac{f_3}{a_3}$$

### Method

Multi-objective constrained optimization was chosen. Lookup tables for vehicle data are linearized around the vehicle's operating point in real-time. An embedded quadratic programming solver, CVXGEN, is used to solve a matrix form of the problem to find the best solutions for each motor's torque command.

$$\text{subject to } l_i \leq A_i \leq u_i$$

$$\text{Decision Variables: } T = \begin{bmatrix} T_{FL} \\ T_{FR} \\ T_{RL} \\ T_{RR} \end{bmatrix}$$

### Objective functions

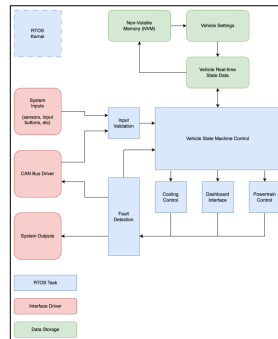
Functions of the motor torques

Achieve yaw controller output	$f_1 = (M_{x,lv} - M_x)^2$
Achieve driver longitudinal acceleration target	$f_2 = (a_{x,ref} - a_x)^2$
Minimize slip ratios to prevent wheel spin	$f_3 = SL_{FL}^2 + SL_{FR}^2 + SL_{RL}^2 + SL_{RR}^2$

### Constraints

Individual Motor Torque Limit	for $\tau_{min,i} \leq \tau_i \leq \tau_{max,i}$ $i \in \{FL, FR, RL, RR\}$
Battery Power Limit	$P_{min} \leq \frac{1}{\eta_{batt} + \eta_{inverter}} \sum_{j=0}^4 \tau_j \omega_j \leq P_{max}$
Total Torque Limit	$\tau_{min} \leq \sum_{j=0}^4 \tau_j \leq \tau_{max}$
Slip Ratio Magnitude Limit	for $SL_{min,i} \leq SL_i \leq SL_{max,i}$ $i \in \{FL, FR, RL, RR\}$

## Firmware Development



### Vehicle State Machine Control

The vehicle control unit runs through a central finite state machine (FSM) that determines the running mode of the vehicle. All RTOS tasks communicate with the FSM so that it can determine the state and allowable functionality of the vehicle.

### Real-time Operating System

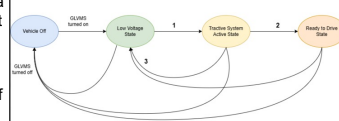
The firmware uses freeRTOS to schedule multiple tasks, ensuring the requirements of the control system are met. Some major tasks are:

**CAN Communication Task** – Handles communication between auxiliary vehicle devices.

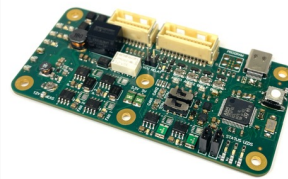
**Fault Task** – Checks for all vehicle faults and determines appropriate response.

**Torque Control Task** – Determines vehicle control mode and utilizes torque optimization algorithms to output individual motor torques.

**Vehicle Data Task** – All tasks send data to this task, storing the current vehicle state. Tasks interpret this state to determine proper functionality.



## Implementation

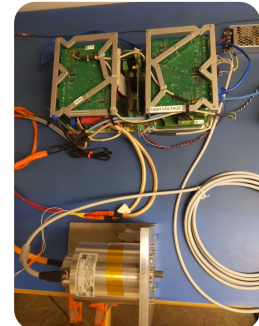


### Vehicle Control Unit Hardware

- STM32F405 Microcontroller
- CAN bus for vehicle communication
- Analog / Digital sensor inputs
- Powertrain safety interlock control

### Hardware-in-the-Loop Testing (HIL)

To validate the embedded implementation of the control system, a HIL test was setup. The Simulink simulation sends driver inputs and sensor data to the hardware via a python CAN interface. The device under test calculates the control system output using the simulation time and updates the vehicle model.



### Powertrain Bench Testing

The VCU was bench tested with the high voltage powertrain to develop the firmware and validate safety fault logic in a controlled environment. Driver inputs and dash controls were also mocked up to validate proper functionality.