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**13-1 Atomic Theory of Matter**

- **Atomic Theory of Matter:** Matter is made up of atoms
  - Brownian motion: pollen grains in water moved randomly as liquid molecules collided into them (kinetic theory)
- Atomic mass unit (u):  $1u = 1/12$  mass of C-12 =  $1.6605 \times 10^{-27}$  kg
- Diameter of an atom  $\approx 10^{-10}$  m (calculated by Albert Einstein)
- Intermolecular force
- Three phases of matter
  - Crystalline solid: strong attractive force, atoms oscillate about a fixed position
  - Liquid: weaker force, moving more rapidly
  - Gas: weak force, high speeds, molecules do not stay close together

## 13-2 Temperature and Thermometers

- Definitions
  - (1) Temperature (T) is a measure of how hot or cold something is.
  - (2) Temperature measures the **average kinetic energy** of the particles in the object.
- Property changes based on temperature:
  - Volume (most materials expand when heated)
  - Color radiated by objects (e.g., fire turns red -> blue -> white)
  - Electrical resistance (usually increases with increasing temperature))
- Two fixed points: **freezing point and boiling point of water** (at atmospheric pressure)
- Temperature Scales:
  - Celsius (°C) scale = centigrade scale
    - Freezing point of water: 0°C
    - Boiling point of water: 100°C
  - Kelvin (K) scale = absolute scale (SI unit)
    - Absolute zero = 0K = -273.15°C, the temperature at which all thermal motion is the minimum in the classical description of thermodynamics
    - Change in 1K = change in 1°C
    - $T(K) = T(^{\circ}C) + 273$
  - Fahrenheit (°F) scale
    - Freezing point of water: 32°F
    - Boiling point of water: 212°F
    - $T_F = 9/5T_C + 32$
    - $T_C = 5/9(T_F - 32)$
    - Change in 1°C = change in 1.8°F
- Types of Thermometers
  - Liquid in glass thermometer (principle: thermal expansion)
    - Liquid expands more than the glass, the liquid level rises in the tube
    - Liquid: mercury (better for high T), colored alcohol (better for low T)
  - **Bimetallic strip**
    - Binding together 2 dissimilar metals whose rate of expansion are different.
    - When T increases, the bimetallic strip bends toward the metal with a lower expansion rate.
    - **Thermostat**: a device for keeping a steady T.
  - **Thermistor thermometer** (very precise)

- The probe consists of a thermistor, which is a semiconductor device with a resistance that is very sensitive to the change of T.
- $T \uparrow$ ,  $R \downarrow$  (resistance),  $I \uparrow$  (current), larger reading on the meter.

### 13-3 Thermal Equilibrium and the Zeroth Law of Thermodynamics

- **Thermal equilibrium:** If two bodies of different temperature are placed close together, thermal energy will be transferred from one to the other, and the two objects will eventually reach the same temperature (high T to low T).
- **Zeroth law of thermodynamics:** If two systems are in thermal equilibrium with a third system, they are also in thermal equilibrium with each other.

### 13-4 Thermal Expansion

- **Thermal expansion:** as the temperature of an object (solid, liquid, gas) increases, volume increases.
- The particles in a substance increase their spacing, but do not expand themselves
- Linear Expansion (change of T not too large) —> **only for solids**
  - $\Delta L = \alpha L_0 \Delta T$
  - $L = L_0 (1 + \alpha \Delta T)$
- Volume thermal expansion
  - $\Delta V = \beta V_0 \Delta T$
  - $V = V_0 (1 + \beta \Delta T)$
  - For solids that are isotropic (having the same properties in all direction):  $\beta \approx 3\alpha$ 
    - Pure metals
- **Anomalous Behavior of Water Below 4°C**
  - If water at 0°C is heated, it decreases in volume until it reaches 4°C.
  - Above 4 °C, water expands in volume as temperature increases.
  - Water has its greatest density at 4°C.
  - When temperature is between 0°C and 4°C, the number of hydrogen bonds increases if temperature decreases. The hydrogen bonds will increase the volume of the water.

### 13-5 The Gas Law and the Absolute Temperature

- Atmospheric pressure ( $P_A$ ): At sea level, the pressure of the atmosphere on average is **1.013  $\times 10^5$  N/m<sup>2</sup>**
  - Pascal (Pa): 1Pa = 1N/m<sup>2</sup>

- Atmosphere (atm):  $1 \text{ atm} = 1.013 \times 10^5 \text{ N/m}^2 = 101.3 \text{ kPa}$
- Bar:  $1 \text{ bar} = 1.00 \times 10^5 \text{ N/m}^2$
- Gauge pressure ( $P_G$ )
  - Most pressure gauges only register pressure above atmospheric pressure.
- Absolute pressure ( $P$ )
  - Sum of the atmospheric pressure and the gauge pressure.
  - $P = P_A + P_G$
- Gas Laws
  - **Equation of state:** The relation between the volume ( $V$ ), the pressure ( $P$ ), the temperature ( $T$ ) and the mass ( $m$ ) of a gas.
  - **Equilibrium state of a system:** when the variables that describe the system (such as  $T$  and  $P$ ) are the same throughout the system and are not changing in time.
  - Conditions for gas laws to be accurate: the gas is close to an ideal gas.
    - **Gas is not too dense,  $P$  is not too high**
    - **Gas is not close to the liquefaction/boiling point ( $T$  not too low).**
- Boyle's Law: P-V law
  - Mass and temperature are constant:  $P$  and  $V$  change
  - When adding pressure onto a gas, it's compressed and gets smaller  $\rightarrow P$  increases,  $V$  decreases (inverse proportion)
  - **$PV = \text{constant}$  or  $P_1V_1 = P_2V_2$  ( $P$  is absolute pressure, atm or Pa;  $P$  and  $V$  have the same units for both sides)**
- Charles's Law: V-T Law
  - Mass and pressure is constant:  $V$  and  $T$  change
  - When gas is heated  $\rightarrow$  particles move more randomly and faster  $\rightarrow$  takes up more space  $\rightarrow$  volume is larger
  - **$V/T = \text{constant}$  or  $V_1/T_1 = V_2/T_2$  ( $T$ : Kelvin;  $V$  has the same units for both sides)**
- Gay-Lussac's Law: P-T Law
  - Mass and volume is constant:  $P$  and  $T$  change
  - When gas is heated  $\rightarrow$  particles move more randomly and faster  $\rightarrow$  exert more  $F$  on the walls  $\rightarrow$  pressure is larger
  - **$P/T$  is constant or  $P_1/T_1 = P_2/T_2$  ( $P$  has the same units for both sides;  $T$ : Kelvin)**
- General Gas Law

$$\frac{PV}{T} = c \Rightarrow \frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

### 13-6 & 7 The Ideal Gas Law

- Molar mass and mole
  - One mole (mol): The amount of substance that contains as many atoms or molecules as there are in precisely 12 grams of carbon-12

$$n(\text{mol}) = \frac{\text{mass (grams)}}{\text{molar mass (g/mol)}}$$

- The number of moles (n)
- Ideal Gas Law Equation
  - $PV = nRT$  (P: Pa; V: m<sup>3</sup>; T: K; n: mol)
  - R: universal gas constant
  - $R = 8.314 \text{ J/mol}\cdot\text{K} = 8.314 \text{ Pa}\cdot\text{m}^3/\text{mol}\cdot\text{K}$  (SI unit)

- Ideal Gas
  - A gas in which the molecules do not exert forces on each other except when colliding.

- STP
  - Standard conditions or standard temperature and pressure.
  - T = 273 K (0°C)
  - $P = 1.00 \text{ atm} = 1.013 \times 10^5 \text{ Pa} = 101.3 \text{ kPa}$ 
    - Volume of one mol at STP = 22.4 L

- Molar Volume ( $V_m$ )
  - The volume occupied by one mole of a substance at a given T and P.
  - Molar volume (m<sup>3</sup>/mol) = molar mass (g/mol) / molar density (g/m<sup>3</sup>)

$$V_m = \frac{M}{\rho}$$

### 13-8 Ideal Gas Law in Terms of Molecules: Avogadro's Number

- Avogadro's Hypothesis: Equal volumes of gas at the same pressure and temperature contain equal numbers of molecules.
- Avogadro's number ( $N_A$ ) =  $6.02 \times 10^{23}$  molecules/mol
- N (number of molecules) =  $nN_A$
- Ideal gas law in terms of molecules:
  - $PV = nRT = NkT$
  - k: Boltzmann's constant =  $1.38 \times 10^{-23} \text{ J/K}$