

HW10

Zirui Zhang

2023-05-02

```
library(dplyr)
library(survival)
library(MASS)
library(KMsurv)
library(survminer)
```

Question 1

```
# build data frame
time = c(4, 12, 15, 21, 23,
         2, 6, 8, 10, 19)
cens = c(0, 1, 0, 1, 0,
         0, 1, 1, 0, 0)
group = c(rep("group1", 5),
          rep("group2", 5))
df = data.frame(time, cens, group)
# log-rank test
survdif(Surv(time, cens)~group, data = df)
```

```
## Call:
## survdiff(formula = Surv(time, cens) ~ group, data = df)
##
##           N Observed Expected (O-E)^2/E (O-E)^2/V
## group=group1 5         2     2.87     0.264     1.16
## group=group2 5         2     1.13     0.673     1.16
##
##  Chisq= 1.2  on 1 degrees of freedom, p= 0.3
```

The p-value of the chi-sq test is $0.3 > 0.05$, thus we fail to reject the null and conclude that there's no significant difference between the hazard function of the two groups.

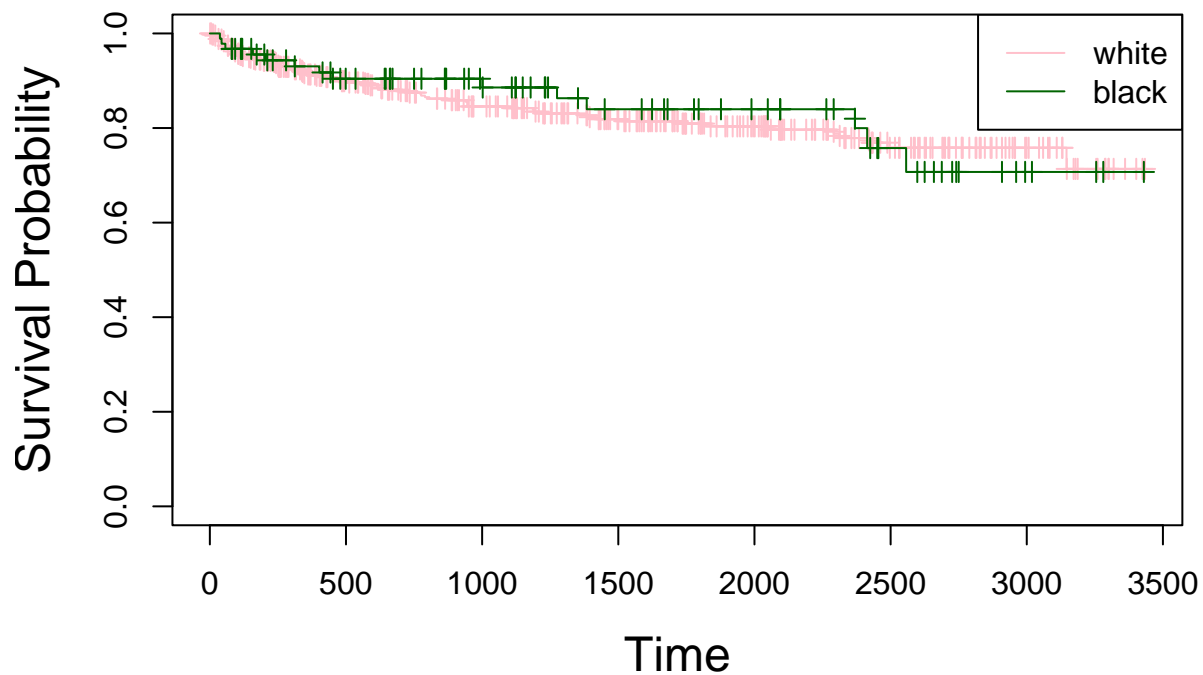
Question 2

```
data(kidtran)
kidtran %>% head(10)
```

```
##      obs time delta gender race age
## 1      1      1      0      1      1 46
## 2      2      5      0      1      1 51
## 3      3      7      1      1      1 55
## 4      4      9      0      1      1 57
## 5      5     13      0      1      1 45
## 6      6     13      0      1      1 43
## 7      7     17      1      1      1 47
## 8      8     20      0      1      1 65
## 9      9     26      1      1      1 55
## 10    10     26      1      1      1 44
```

```
# for male group
KM1 = survfit(Surv(time, delta)~race, data = subset(kidtran, gender == 1), conf.type = "log")
plot(KM1, conf.int = F, mark.time = T,
     xlab = "Time", ylab = "Survival Probability", main = "Male K-M curve",
     col = c("pink", "dark green"),
     cex.lab = 1.5, cex.main = 1.5)
legend('topright', c("white", "black"), lty=1, col = c("pink", "dark green"))
```

Male K-M curve



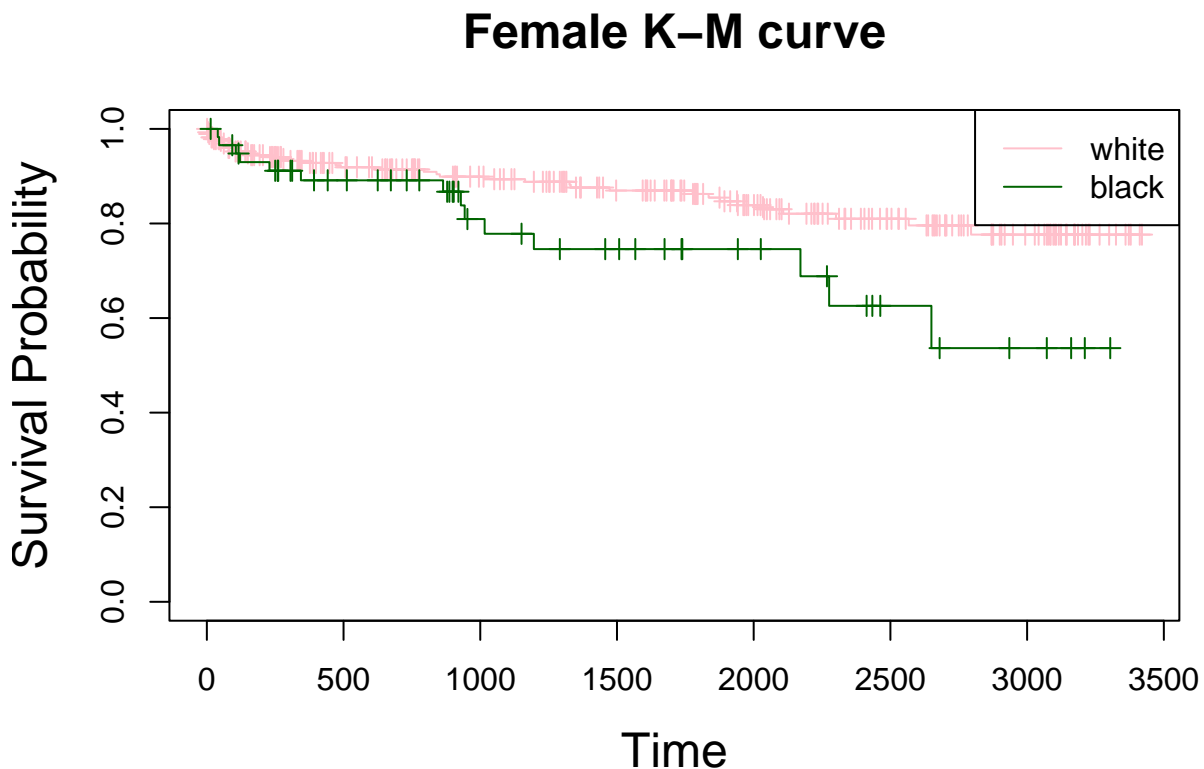
```
# log rank test
survdif(Surv(time, delta)~race, data = subset(kidtran, gender == 1))
```

```
## Call:
## survdiff(formula = Surv(time, delta) ~ race, data = subset(kidtran,
##      gender == 1))
##
##      N Observed Expected (O-E)^2/E (O-E)^2/V
```

```
## race=1 432      73      71.9    0.0168    0.097
## race=2  92      14      15.1    0.0801    0.097
##
## Chisq= 0.1  on 1 degrees of freedom, p= 0.8
```

Among males, White people showed higher survival rates than Black people on the first half of time and lower after. The p-value from log-rank test is $0.8 > 0.05$, thus we fail to reject the null and conclude that there's no significant difference between the survival rates of the two races among male patients.

```
# for female group
KM2 = survfit(Surv(time, delta)~race, data = subset(kidtran, gender == 2), conf.type = "log")
plot(KM2, conf.int = F, mark.time = T,
     xlab = "Time", ylab = "Survival Probability", main = "Female K-M curve",
     col = c("pink", "dark green"),
     cex.lab = 1.5, cex.main = 1.5)
legend('topright', c("white", "black"), lty=1, col = c("pink", "dark green"))
```



```
# log rank test
survdif(Surv(time, delta)~race, data = subset(kidtran, gender == 2))
```

```
## Call:
## survdiff(formula = Surv(time, delta) ~ race, data = subset(kidtran,
##   gender == 2))
##
##           N Observed Expected (O-E)^2/E (O-E)^2/V
## race=1 280      39   44.79    0.748    4.85
## race=2  59      14    8.21    4.076    4.85
##
## Chisq= 4.8  on 1 degrees of freedom, p= 0.03
```

From the K-M plot we can see that White people have higher survival rates than Black people among females in most of the time. The p-value from log-rank test is $0.03 < 0.05$, thus we reject the null and conclude that there exists significant difference between the survival rates of the two races among female patients.

Question 3

```
data(larynx)
larynx %>% head(10)
```

```
##      stage time age diagyr delta
## 1         1  0.6  77      76      1
## 2         1  1.3  53      71      1
## 3         1  2.4  45      71      1
## 4         1  2.5  57      78      0
## 5         1  3.2  58      74      1
## 6         1  3.2  51      77      0
## 7         1  3.3  76      74      1
## 8         1  3.3  63      77      0
## 9         1  3.5  43      71      1
## 10        1  3.5  60      73      1
```

```
attach(larynx)
```

```
## The following object is masked _by_ .GlobalEnv:
##
##      time
```

```
Z1 = as.numeric(stage == 2)
Z2 = as.numeric(stage == 3)
Z3 = as.numeric(stage == 4)
Z4 = age
fit2 = coxph(Surv(time, delta)~Z1+Z2+Z3+Z4+Z1*Z4, data=larynx, method = 'breslow')
summary(fit2)
```

```
## Call:
## coxph(formula = Surv(time, delta) ~ Z1 + Z2 + Z3 + Z4 + Z1 *
##      Z4, data = larynx, method = "breslow")
##
##      n= 90, number of events= 50
##
##              coef exp(coef)    se(coef)      z Pr(>|z|)
## Z1      -7.3820143  0.0006223  3.4027542 -2.169   0.0301 *
## Z2       0.6218044  1.8622853  0.3558078  1.748   0.0805 .
## Z3       1.7534270  5.7743576  0.4239595  4.136 3.54e-05 ***
## Z4       0.0059729  1.0059908  0.0148792  0.401   0.6881
## Z1:Z4    0.1116674  1.1181409  0.0476728  2.342   0.0192 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##      exp(coef) exp(-coef) lower .95 upper .95
```

```

## Z1      0.0006223 1606.8231 7.900e-07    0.4903
## Z2      1.8622853    0.5370 9.272e-01    3.7403
## Z3      5.7743576    0.1732 2.516e+00   13.2550
## Z4      1.0059908    0.9940 9.771e-01    1.0358
## Z1:Z4   1.1181409    0.8943 1.018e+00    1.2277
##
## Concordance= 0.682 (se = 0.04 )
## Likelihood ratio test= 24.11 on 5 df,    p=2e-04
## Wald test              = 23.77 on 5 df,    p=2e-04
## Score (logrank) test = 27.98 on 5 df,    p=4e-05

```

- Explanation:

Z1, Z3 and Z1*Z4 are significant variables. Holding the age, the HR between patients in stage II and patients in stage I is 0, HR between patients in stage III and patients in stage I is 1.86, HR between patients in stage IV and patients in stage I is 5.77. When a patient is in stage I, one unit increase in age would increase the probability of death by 1%. When a patient is in stage II, one unit increase in age would increase the probability of death by 12%.

- HR:

For a stage II patient of age 50, Z1=1, Z4=50; for a stage I patient of age 50, Z1=0, Z4=50. The probability of death at given time t of the former is 0.17 times the probability of death of the latter.