

1.

(1)

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{u}{\cos \theta}$$

(2)

$$\begin{aligned} a &= \frac{u \sin \theta}{\cos^2 \theta} \frac{u \tan \theta}{h / \sin \theta} \\ &= \frac{u^2}{h} \tan^3 \theta \end{aligned}$$

2.

$$\begin{aligned} F_T &= \rho_l l g - \frac{\rho_l l g}{2} + \frac{3}{2} \rho_l g x \\ &= \frac{l+x}{2} \rho_l g + \rho_l x g \end{aligned}$$

3.

$$(1) v_1 = m_1 \sqrt{\frac{2gl}{m_2(m_2 + m_1)}} \quad (2) v_2 = m_1 \sqrt{\frac{gl}{3m_1^2 + 7m_1 m_2 + 4m_2^2}}$$

$$(3) \text{ 作功, } W = \frac{-m_1^2}{m_1 + m_2} gl$$

4.

(1)

$$v_0 = \sqrt{gh}$$

(2)

$$x = \sqrt{3}h$$

这里舍去了负根. 即小球在  $h$  和  $(1+\sqrt{3})h$  两极限高度间往返运动.

5.

(1)

$$F = m\ddot{x}_c = \frac{3}{4}mg\sin\theta_0\cos\theta_0$$

$$F_N = m\ddot{y}_c + mg = mg\left(1 - \frac{3}{4}\sin^2\theta_0\right)$$

(2)

$$\theta_m = \arccos\left(\frac{2}{3}\cos\theta_0\right)$$

即若杆不受其他约束,则当  $\theta$  增大到  $\arccos\left(\frac{2}{3}\cos\theta_0\right)$  时,杆的上端将脱离墙.