

# KOLMOGOROV SMIRNOV'S ONE SAMPLE TEST

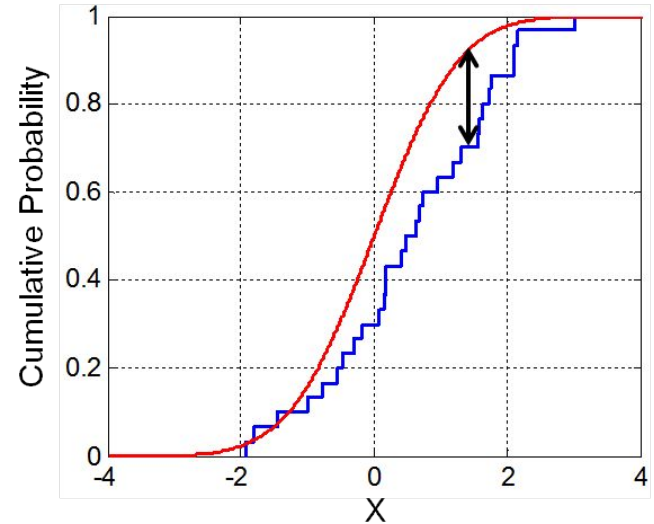
A Brief Guide to KS One Sample Test

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# KOLMOGOROV SMIRNOV TEST

The Kolmogorov–Smirnov test is a **nonparametric goodness-of-fit test**

- It is used to determine whether two distributions differ, or whether an underlying probability distribution differs from a hypothesized distribution.



# WHEN TO USE KOLMOGOROV SMIRNOV TEST??

- It is used when we have two samples coming from two populations that can be different.
- It can also be used as a goodness-of-fit test. In this case, we have only one random sample obtained from a population where the distribution function is specific and known.

# What Is One-Sample Kolmogorov-Smirnov Test?

- The Kolmogorov Smirnov's one sample test is concerned with the degree of agreement between the distribution of the **observed sample values** and some specified **theoretical distribution**.
- It determines whether or not the values in a sample can reasonably be thought to have come from a population having a theoretical distribution.



## Tip

This test is used as a test of **goodness of fit** and is ideal when the size of the sample is small.

## Formula:

$$D = \text{Maximum} | F_o(X) - F_r(X) |$$

Where ,

- $F_o(X)$  = Observed cumulative frequency distribution of a random sample of  $n$  observations.

$$F_o(X) = k/n$$

= ( Number of observations  $\leq X$  ) / ( Total number of observations )

- $F_r(X)$  = The theoretical frequency distribution.

The critical value of  $D$  is found from the K-S table values for one sample test.



# Decision Criteria

## → Acceptance Criteria

If calculated value is less than critical value accept null hypothesis

## → Rejection Criteria

If calculated value is greater than table value reject null hypothesis

## Example 1:

In a study done from various streams of a college 60 students, with equal number of students drawn from each stream, are we interviewed and their intention to join the Drama Club of college was noted.

	B.Sc	B.A.	B.Com	M.A	M . Com
No in Each Class	5	9	11	16	19

- It was expected that 12 students from each class would join the Drama Club. Using the K-S test to find if there is any difference among student classes with regard to their intention of joining the Drama Club

# Solution:

- **Ho: There is no difference among students of different streams with respect to their intention of joining the drama club.**

Test statistic  $|D|$  is calculated as:

$$D = \text{Maximum}|F_0(X) - F_T(X)| \\ = 11/60 = 0.183$$

The table value of  $D$  at 5% significance level is given by :

$$D_{0.05} = 1.36/\sqrt{n} = 1.36/\sqrt{60} \\ = 0.175$$

- Since the calculated value is greater than the critical value, hence we reject the null hypothesis and conclude that there is a difference among students of different streams in their intention of joining the Club.

Streams	No. of students interested in joining		FO(X)	FT(X)	FO(X) - FT(X)
	Observed (O)	Theoretical (T)			
B.Sc.	5	12	5/60	12/60	7/60
B.A.	9	12	14/60	24/60	10/60
B.COM.	11	12	25/60	36/60	11/60
M.A.	16	12	41/60	48/60	7/60
M.COM.	19	12	60/60	60/60	0
Total	n=60				



## Solution Using R Software(Codes):

The screenshot displays the RStudio environment with the following components:

- Menu Bar:** File, Edit, Code, View, Plots, Session, Build, Debug, Profile, Tools, Help.
- Toolbar:** Includes icons for saving, running, and navigating, along with a "Go to file/function" search bar.
- File Explorer:** Shows two open files: "R codes.R" and "Ks one sample test 1.R".
- Source Editor:** Contains the R script for the Kolmogorov-Smirnov test.
 

```

1
2 ##### KOLMOGROV SMIRNOV'S ONE SAMPLE TEST #####
3
4 #Example 1:
5
6 #Ho: There is no difference among students of different streams
7 #with respect to their intention of joining the drama club
8 #H1: Not HO
9 n=5
10 N=60
11 obs=c(5,9,11,16,19)
12 Theo=60/n
13 Theo
14 FO_xi=cumsum(obs/N)
15 FT_xi=cumsum(Theo/N)
16 Theo=rep(60/n,5)
17
18 Theo
19 FO_xi=cumsum(obs/N)
20 FT_xi=cumsum(Theo/N)
21 dc1=abs(FO_xi-FT_xi)
22 Table1=data.frame(obs,Theo,FO_xi,FT_xi,dc1)
23 Table1
24 D=max(dc1)
25 D
26 #D0.05=1.36/sqrt(n)=1.36/sqrt(60)=0.175
27 #Since the calculated value is greater than the critical value, hence we reject the null hypothesis
28 #ie 0.1833> 0.175
29 #conclude that there is a difference among students of different streams in their intention of joining the clu
30 |
31
32 #

```
- Run/Source Buttons:** Located at the bottom right of the editor window.

# Output:

```
Console Terminal x Jobs x
~/
> #Example 1:
>
> #Ho: There is no difference among students of different streams
> #with respect to their intention of joining the drama club
> #H1: Not Ho
> n=5
> N=60
> obs=c(5,9,11,16,19)
> Theo=60/n
> Theo
[1] 12
> FO_xi=cumsum(obs/N)
> FT_xi=cumsum(Theo/N)
> Theo=rep(60/n,5)
>
> Theo
[1] 12 12 12 12 12
> FO_xi=cumsum(obs/N)
> FT_xi=cumsum(Theo/N)
> dc1=abs(FO_xi-FT_xi)
> Table1=data.frame(obs,Theo,FO_xi,FT_xi,dc1)
> Table1
  obs Theo    FO_xi FT_xi    dc1
1    5   12 0.08333333 0.2 0.1166667
2    9   12 0.23333333 0.4 0.1666667
3   11   12 0.41666667 0.6 0.1833333
4   16   12 0.68333333 0.8 0.1166667
5   19   12 1.00000000 1.0 0.0000000
> D=max(dc1)
> D
[1] 0.1833333
> #D0.05=1.36/vn=1.36/v60=0.175
> #Since the calculated value is greater than the critical value, hence we reject the null hypothesis
> #ie 0.1833> 0.175
> #conclude that there is a difference among students of different streams in their intention of joining the club
> |
```

## Example 2:

Using K-S Test, check for the property of uniformity for the input set of random numbers. 0.54, 0.73, 0.98, 0.11, 0.68. Assume level of significance to be 0.05

- **Solution:**

Ho: Random no. are not uniform    V/S    H1: Not Ho            N=5

i	1	2	3	4	5
Ri	0.11	0.54	0.68	0.73	0.98

## Example 2:

$$D^+ = \max_{1 \leq i \leq N} \{i/N - R_i\} = 0.09$$

$$D^- = \max_{1 \leq i \leq N} \{R_i - (i-1/n)\} = 0.34$$

$$D = \max \{D^+, D^-\}$$

$$D = \max \{0.09, 0.34\}$$

$$D = 0.34$$

## Example 2:

$$D^+ = \max \{i/N - R_i\} = 0.09 \quad 1 \leq i \leq N$$

$$D^- = \max \{R_i - (i-1/n)\} = 0.34 \quad 1 \leq i \leq N$$

$$D = \max \{D^+, D^-\}$$

$$D = \max \{0.09, 0.34\}$$

$$D = 0.34$$

$$\alpha = 0.05$$

$$\therefore D_\alpha = 0.565 \text{ (using KS Table)}$$

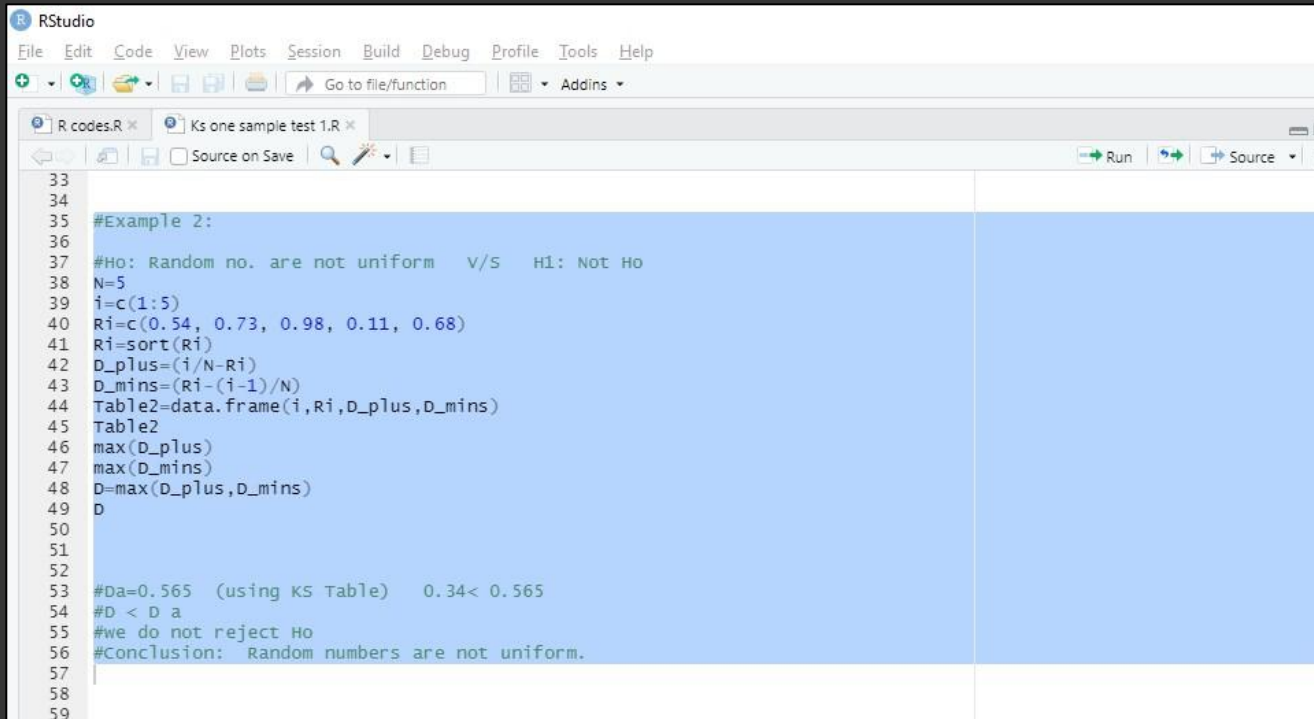
$$\therefore 0.34 < 0.565$$

$$\therefore D < D_\alpha$$

$\therefore$  we do not reject  $H_0$

**Conclusion: Random numbers are not uniform**

# Solution Using R Software(Codes):



The image shows a screenshot of the RStudio interface. The title bar indicates the application is 'RStudio'. The menu bar includes 'File', 'Edit', 'Code', 'View', 'Plots', 'Session', 'Build', 'Debug', 'Profile', 'Tools', and 'Help'. The toolbar contains icons for file operations and a search bar. The source editor shows two tabs: 'R codes.R' and 'Ks one sample test 1.R'. The 'Ks one sample test 1.R' tab is active, displaying the following R code:

```
33
34
35 #Example 2:
36
37 #Ho: Random no. are not uniform   v/s   H1: Not Ho
38 N=5
39 i=c(1:5)
40 Ri=c(0.54, 0.73, 0.98, 0.11, 0.68)
41 Ri=sort(Ri)
42 D_plus=(i/N-Ri)
43 D_mins=(Ri-(i-1)/N)
44 Table2=data.frame(i,Ri,D_plus,D_mins)
45 Table2
46 max(D_plus)
47 max(D_mins)
48 D=max(D_plus,D_mins)
49 D
50
51
52
53 #Da=0.565   (using KS Table)   0.34< 0.565
54 #D < D a
55 #we do not reject Ho
56 #Conclusion: Random numbers are not uniform.
57
58
59
```

# OutPut:

```
Project: (Not...
Console Terminal x Jobs x
~/
> #Example 2:
>
> #Ho: Random no. are not uniform V/S H1: Not Ho
> N=5
> i=c(1:5)
> Ri=c(0.54, 0.73, 0.98, 0.11, 0.68)
> Ri=sort(Ri)
> D_plus=(i/N-Ri)
> D_mins=(Ri-(i-1)/N)
> Table2=data.frame(i,Ri,D_plus,D_mins)
> Table2
  i  Ri D_plus D_mins
1 1 0.11  0.09  0.11
2 2 0.54 -0.14  0.34
3 3 0.68 -0.08  0.28
4 4 0.73  0.07  0.13
5 5 0.98  0.02  0.18
> max(D_plus)
[1] 0.09
> max(D_mins)
[1] 0.34
> D=max(D_plus,D_mins)
> D
[1] 0.34
>
>
>
> #Da=0.565 (using KS Table) 0.34< 0.565
> #D < D a
> #we do not reject Ho
> #Conclusion: Random numbers are not uniform.
> |
```

## Example 3:

Each person in random sample say  $n = 10$  employees was asked about  $X$ , the daily time wasted at work doing non work activities, such as surfing the internet and emailing to friends. The resulting data, in minutes, are as follows:

110, 102, 98, 95, 108, 105, 103, 90, 92, 100

Is it okay assume that these data come from a normal distribution with mean 100 and standard deviation 10?



## Solution:

- $H_0$  : given sample comes from normal distribution with  $\mu=100$  and  $\sigma=10$  i.e  $X \sim N(\mu=100, \sigma=10)$
- $H_1$ : given sample does not come from normal distribution with  $\mu=100$  and  $\sigma=10$  i.e  $X \sim$  does not follow normal with  $\mu=100$  and  $\sigma=10$

### Test statistic:

Under  $H_0$ ,

$$D = \text{Max } |F_n(X_i) - F_0(X_i)|$$

Where

$F_n$  C.D.F of empirical distribution and  $F_0$  is C.D.F ,  $N(\mu=100, \sigma=10)$

# Solution:

$$F_n(x_i) = i/n = i/10; \quad i=1,2,3,\dots, 10$$

Where observation  $X_i$  are written in ascending order

$$F_o(Z_i) = P(X \leq X_i)$$

$$= P(x - \mu/\sigma \leq X_i - \mu/\sigma)$$

$$= P(Z \leq X_i - 100/10)$$

where ,

$$Z \text{ is } X - \mu/\sigma \sim N(0,1)$$

$$= F(X_i - 100/10)$$

S.r no (i)	$X_i$	$F_n(X_i)$	$X_i - 100/10$	$F_o(X_i) = F(X_i - 100/10)$	$ F_n(X_i) - F_o(X_i) $
1	90	$1/10 = 0.1$	-1	0.15866	0.05866
2	92	$2/10 = 0.2$	-0.8	0.21186	0.01186
3	95	$3/10 = 0.3$	-0.5	0.30854	0.00854
4	98	$4/10 = 0.4$	-0.2	0.42074	0.02074
5	100	$5/10 = 0.5$	0	0.5	0
6	102	$6/10 = 0.6$	0.2	0.57926	0.02074
7	103	$7/10 = 0.7$	0.3	0.61791	0.08209
8	105	$8/10 = 0.8$	0.5	0.69146	0.10854
9	108	$9/10 = 0.9$	0.8	0.78814	0.11186
10	110	$10/10 = 1$	1	0.84134	0.15866 » $D_n$

### Example 3:

$$D = \text{Max} | F_n(X_i) - F_o(X_i) |$$
$$= \mathbf{0.15866}$$

*Critical region*

$$= \{ D | D > D_n ; \alpha = D_{10, 0.05} = 0.410 \} \text{ at } \alpha\% \text{ I.o.s}$$

***Decision: As  $D_n = 0.15866 < 0.410$ ,  
accept  $H_o$  at 5 % level of  
significance***

**Conclusion: Given sample may have come from normal distribution with parameter( $\mu=100$  ,  $\sigma=10$ )**

# Solution Using R Software(Codes):

```
62
63
64 #-----#
65 #Example 3
66
67
68 #H??? : given sample comes from normal distribution with  $\mu=100$  and  $s=10$  i.e  $X \sim N(\mu=100, s=10)$ 
69 v/s
70 #H1: given sample does not come from normal distribution with  $\mu=100$  and  $s=10$ 
71
72 xi=c(110,102,98,95,108,105,103,90,92,100)
73 x_bar=100
74 sd=10
75 N=10
76
77 xi_new=sort(xi)
78 i=c(1,2,3,4,5,6,7,8,9,10)
79 Fn_xi=i/N
80 z=(xi_new-x_bar)/sd
81 F0_xi=pnorm(z)
82 dc=abs(Fn_xi-F0_xi)
83 dc
84 Table3=data.frame(xi_new,Fn_xi,z,F0_xi,dc)
85 table
86 max(dc)
87 #Decision: As  $D_n = 0.15866 < 0.410$ ,  $D_n$  is calculated form Table  $a=D_{10} \cdot 0.05 = 0.410$ 
88 #accept H??? at 5 % level of significance.
89 #Conclusion: given sample may have come from normal distribution with parameter( $\mu=100, s=10$ )
90
91 #-----#
```

# OutPut:

```
> xi_new=sort(xi)
> i=c(1,2,3,4,5,6,7,8,9,10)
> Fn_xi=1/N
> z=(xi_new-x_bar)/sd
> F0_xi=pnorm(z)
> dc=abs(Fn_xi-F0_xi)
> dc
[1] 0.058655254 0.011855399 0.008537539 0.020740291 0.000000000 0.020740291 0.082088578 0.108537539
[9] 0.111855399 0.158655254
> Table3=data.frame(xi_new,Fn_xi,z,F0_xi,dc)
> table
  xi_new Fn_xi    z    F0_xi      dc
1     90  0.1 -1.0 0.1586553 0.058655254
2     92  0.2 -0.8 0.2118554 0.011855399
3     95  0.3 -0.5 0.3085375 0.008537539
4     98  0.4 -0.2 0.4207403 0.020740291
5    100  0.5  0.0 0.5000000 0.000000000
6    102  0.6  0.2 0.5792597 0.020740291
7    103  0.7  0.3 0.6179114 0.082088578
8    105  0.8  0.5 0.6914625 0.108537539
9    108  0.9  0.8 0.7881446 0.111855399
10   110  1.0  1.0 0.8413447 0.158655254
> max(dc)
[1] 0.1586553
> #Decision: As  $D_n = 0.15866 < 0.410$ ,  $D_n$  is calculated form Table a= $D_{10} \square 0.05 = 0.410$ 
> #accept  $H_{000}$  at 5 % level of significance.
> #Conclusion: given sample may have come from normal distribution with parameter( $\mu=100$  ,  $s=10$ )
> |
```



# Mann–Whitney U test

A Brief Guide to Mann-Whitney U Test

---

# MANN-WHITNEY U TEST

- In **statistics**, the Mann–Whitney  $U$  test is a **nonparametric test** of the **null hypothesis** that, for randomly selected values  $X$  and  $Y$  from two populations, the probability of  $X$  being greater than  $Y$  is equal to the probability of  $Y$  being greater than  $X$ .
- A similar nonparametric test used on *dependent* samples is the **Wilcoxon signed-rank test**.

# WHEN TO USE MANN-WHITNEY U TEST??

- The Mann-Whitney U test is used to compare whether there is a difference in the dependent variable for two independent groups.
- It compares whether the distribution of the dependent variable is the same for the two groups and therefore from the same population.



# What Is Mann-Whitney U Test?

- The Mann-Whitney U test is a non-parametric test that can be used in place of an unpaired t-test. It is used to test the null hypothesis that two samples come from the same population (i.e. have the same median) or, alternatively, whether observations in one sample tend to be larger than observations in the other.
- The Mann-Whitney U Test is a statistical test used to determine if 2 groups are significantly different from each other on your variable of interest.



Tip:

Test use to compare the difference in the dependent variable for two independent groups.

## Formula:

$$U_1 = R_1 - \frac{n_1(n_1 + 1)}{2}$$

or

$$U_2 = R_2 - \frac{n_2(n_2 + 1)}{2}$$

Either of the two formulas are valid for the Mann Whitney U Test.

Where,

R : sum of ranks in the sample

n : number of items in the sample.



# Decision Criteria

## → Acceptance Criteria

if the observed value of  $U$  exceeds the critical value we do not reject  $H_0$ .

## → Rejection Criteria

if the observed value of  $U$  is less than or equal to the critical value, we reject  $H_0$  in favor of  $H_1$

## Example 1:

We want to measure the reaction time of male and female and check whether there is difference in both the group.

Gender	F	F	F	F	F	F	M	M	M	M	M
Reaction time	34	36	41	43	44	37	45	33	35	39	42

### Hypothesis:

H0: there is no significant difference between reaction time of male and female.

H1: not H0.

## Solution:

Gender	F	F	F	F	F	F	M	M	M	M	M
Reaction time	34	36	41	43	44	37	45	33	35	39	42
Rank	2	7	4	9	10	5	11	1	3	6	8

### Test statistic:

$n_1 = 6$ ;  $n_2 = 5$

R1: It is the sum of rank of female

$$2+4+7+9+10+5=37$$

R2: It is the sum of rank of male

$$11+1+3+6+8=29$$

## Example 1:

$$U1 = n1n2 + [n1(n1+1)]/2 - \sum R1$$
$$= 6*5 + [6(6+1)]/2 - 37$$

$$U1 = 14$$

$$U2 = n1n2 + [n2(n2+1)]/2 - \sum R2$$
$$= 6*5 + [5(5+1)]/2 - 29$$

$$U2 = 16$$

$$U = \min(U1, U2)$$
$$= 14$$

**Conclusion:** Therefore we accept null hypothesis and conclude that rank of both male and female are same

**Decision:**

$$U_{tab} = U_{n1, n2, \alpha}$$

$$= U_{6, 5, 0.05}$$

$$= 3$$

**Since  $U_{cal} > U_{tab}$**

# Solution Using R Software(Codes):

```
1 -----#Mann-whitney test-----
2
3 #Ex 1
4
5 #H0: there is no significant difference between reaction time of male and female.
6 #H1: Not H0
7
8
9 Gender=c('Female','Female','Female','Female','Female','Female','Male','Male','Male','Male','Male')
10 Reaction_time=c(34,36,41,43,44,37,45,33,35,39,42)
11 Data=data.frame(Gender,Reaction_time)
12 view(Data)
13 str(Data)
14 wilcox.test(Reaction_time~Gender,data = Data,mu=0,alt="two.sided",conf.int=T,conf.level=0.95,exact=F)
15
16 #DC:Null Hypothesis is not rejected
17 #There is no significant difference between reaction time of Male and Female
18
19 |
```

# OutPut:

```
> #H0: there is no significant difference between reaction time of male and female.
> #H1: Not H0
>
>
> Gender=c('Female','Female','Female','Female','Female','Female','Female','Male','Male','Male','Male','Male')
> Reaction_time=c(34,36,41,43,44,37,45,33,35,39,42)
> Data=data.frame(Gender,Reaction_time)
> View(Data)
> str(Data)
'data.frame':  11 obs. of  2 variables:
 $ Gender      : chr  "Female" "Female" "Female" "Female" ...
 $ Reaction_time: num  34 36 41 43 44 37 45 33 35 39 ...
> wilcox.test(Reaction_time~Gender,data = Data,mu=0,alt="two.sided",conf.int=T,conf.level=0.95,exact=F)

      Wilcoxon rank sum test with continuity correction

data:  Reaction_time by Gender
W = 16, p-value = 0.9273
alternative hypothesis: true location shift is not equal to 0
95 percent confidence interval:
 -7.999979  8.000019
sample estimates:
difference in location
      0.9999627

>
> #DC:Null Hypothesis is not rejected
> #There is no significant difference between reaction time of Male and Female
> |
```



## —Example 2:

The effectiveness of advertising for two rival products (Brand X and Brand Y) was compared. Market research at a local shopping centre was carried out, with the participants being shown adverts for two rival brands of coffee, which they then rated on the overall likelihood of them buying the product (out of 10, with 10 being "definitely going to buy the product"). Half of the participants gave ratings for one of the products, the other half gave ratings for the other product.

Brand X Rating	3	4	2	6	2	5
Brand Y Rating	9	7	5	10	6	8

## Solution:

Brand	X	X	X	X	X	X	Y	Y	Y	Y	Y	Y
Rating	3	4	2	6	2	5	9	7	5	10	6	8
Rank	3	4	1.5	7.5	1.5	5.5	11	9	5.5	12	7.5	10

### Test statistic:

- Add up the ranks for Brand X, to get T1

Therefore  $T1 = 3 + 4 + 1.5 + 7.5 + 1.5 + 5.5 = 23$

- Add up the ranks for Brand Y, to get T2

Therefore,  $T2 = 11 + 9 + 5.5 + 12 + 7.5 + 10 = 55$

## Example 2:

Find  $U$

(Note:  $T_x$  is the larger rank total)

In our case it's  $T_2$

$$U = n_1 \times n_2 + n_x \times \frac{(n_x + 1)}{2} - T_x$$

$$U = 6 \times 6 + 6 \times \frac{(6 + 1)}{2} - 55$$

$$U = 2$$

**Decision:**

$$U_{tab} = U_{n_1, n_2, \alpha}$$

$$= U_{6, 6, 0.05}$$

$$= 5$$

Since  $U_{cal} < U_{tab}$

**Conclusion:** We can say that there is a highly significant difference between the ratings given to each brand in terms of the likelihood of buying the product.

# Solution Using R Software(Codes):

```
1 #R CODE
2
3 #H0:- Brand X and Brand Y are not significant (equal)
4 #H1: Brand X and Brand Y are significant (not equal)
5
6
7 Brand=c(rep("X",6),rep("Y",6))
8 Brand
9 Rating=c(3,4,2,6,2,5,9,7,5,10,6,8)
10 BData=data.frame(Brand,Rating)
11 head(BData)
12 wilcox.test(Rating~Brand,data =BData,mu=0,alt="two.sided",conf.int=T,conf.level=0.95,exact=F)
13 #DC: we can say that there is a highly significant difference between the ratings
14 # given to each brand in terms of the likelihood of buying the product.
15
```

# OutPut:

```
> #EX2:
>
> #H0:- Brand X and Brand Y are not significant (equal)
> #H1: Brand X and Brand Y are significant (not equal)
>
>
> Brand=c(rep("X",6),rep("Y",6))
> Brand
[1] "X" "X" "X" "X" "X" "X" "Y" "Y" "Y" "Y" "Y" "Y"
> Rating=c(3,4,2,6,2,5,9,7,5,10,6,8)
> BData=data.frame(Brand,Rating)
> head(BData)
  Brand Rating
1     X      3
2     X      4
3     X      2
4     X      6
5     X      2
6     X      5
> wilcox.test(Rating~Brand,data =BData,mu=0,alt="two.sided",conf.int=T,conf.level=0.95,exact=F)

    wilcoxon rank sum test with continuity correction

data:  Rating by Brand
W = 2, p-value = 0.01259
alternative hypothesis: true location shift is not equal to 0
95 percent confidence interval:
 -6.000001 -1.000006
sample estimates:
difference in location
 -3.999954

> #DC: We can say that there is a highly significant difference between the ratings
> # given to each brand in terms of the likelihood of buying the product.
> |
```

## Example 3:

With the Help of Mann Whitney U test find if significant difference exist between the score obtained on organizational commitment scale obtain by public and private bank employees ( $\alpha=0.05$ )

Public Bank employee	Rank R1	Private Bank employee	Rank R2
10	1	34	16
12	2	54	22
21	3	56	23
23	5.5	43	19
34	16	32	10
45	21	23	5.5
32	10	34	16
23	5.5	32	10
34	16	33	13
23	5.5	44	20
		32	10
		34	16
		32	10

# Solution:

## Hypothesis:

H0: There is no significant difference between public bank and private bank employee

H1: Not H0.

## Test statistic:

$$n_1=10 \quad n_2=13$$

$$u_1 = n_1 n_2 + (n_1)(n_1 + 1)/2 - \sum R_1 = 99.5$$

$$u_2 = n_1 n_2 + (n_2)(n_2 + 1)/2 - \sum R_2 = 30.5$$

## Example 2:

$$U = \min(U_1, U_2) = 30.5$$

$$U = 30.5$$

*Decision:*  
*U From U table*  
*U-critical = 33*  
 *$U_{cal} < U_{tab}$*

**Conclusion: Null Hypothesis is rejected**  
**There is Significant difference between the**  
**public bank and Private bank employee**



# Solution Using R Software(Codes):

```
#Ex3
#H0: There is no significant difference between public bank and private bank employee
#H1: Not H0.

Bank=c(rep("PublicBank",10),rep("PrivateBank",13))
score=c(10,12,21,23,34,45,32,23,34,23,34,54,56,43,32,23,34,32,33,44,32,34,32)
SData=data.frame(Bank,score)
head(SData)
wilcox.test(score~Bank,data =SData,mu=0,alt="two.sided",conf.int=T,conf.level=0.95,exact=F)

#DC:Null Hypothesis is rejected
#There is Significant difference between the public bank and Private bank employee
```

# OutPut:

```
> #Ex3
> #H0: There is no significant difference between public bank and private bank employee
> #H1: Not H0.
>
>
> Bank=c(rep("PublicBank",10),rep("PrivateBank",13))
> score=c(10,12,21,23,34,45,32,23,34,23,34,54,56,43,32,23,34,32,33,44,32,34,32)
> SData=data.frame(Bank,score)
> head(SData)
  Bank score
1 PublicBank 10
2 PublicBank 12
3 PublicBank 21
4 PublicBank 23
5 PublicBank 34
6 PublicBank 45
> wilcox.test(score~Bank,data =SData,mu=0,alt="two.sided",conf.int=T,conf.level=0.95,exact=F)

    wilcoxon rank sum test with continuity correction

data:  score by Bank
W = 99.5, p-value = 0.03275
alternative hypothesis: true location shift is not equal to 0
95 percent confidence interval:
 5.808113e-05 2.100002e+01
sample estimates:
difference in location
                11

>
> #DC:Null Hypothesis is rejected
> #There is Significant difference between the public bank and Private bank employee
> |
```

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# Presented By:

- Zeenat(ppt & explanation)
- Hunain(example 1,2)
- Jasmin(example 2,3)
- Sidharth(example 3,1)
- Zishan( R codes)

Get All R Codes At:

<https://github.com/ZishanSayyed/KS-ONE-SAMPLE-TEST-MANN-WHITNEY-U-TEST>

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