# **Agglomerative Clustering Algorithm**

**Agglomerative clustering** is a type of hierarchical clustering that uses a *bottom-up* approach of constructing a dendrogram while repeatedly merging separate clusters into one.

- 1. Start with every point in its own cluster
- 2. Compute the distance between all pairs of clusters
- 3. Merge the two nearest clusters
- 4. Repeat steps 2 and 3 until every point belongs to the same cluster

The *bottom-up* approach refers to the fact that the dendrogram is **built up** by successively combining data points from individual singleton<sup>1</sup> clusters into one maximal cluster.<sup>2</sup>

# **Distance Functions for Agglomerative Clustering**

## **Single-Link Distance**

The **min** of all pairwise distances between a point from one cluster and a point from the other cluster.

- Can handle clusters of varying sizes
- · Sensitive to noise points
- Tends to create elongated clusters

$$D_{SL}(C_1, C_2) = \min\{d(p_1, p_2) | p_1 \in C_1, p_2 \in C_2\}$$

### **Complete-Link Distance**

The **max** of all pairwise distances between a point from one cluster and a point from the other cluster.

- Less susceptible to noise than single-link
- Creates more balanced clusters (equal diameter)
- Tends to split up large clusters

$$D_{CL}(C_1, C_2) = \max\{d(p_1, p_2) | p_1 \in C_1, p_2 \in C_2\}$$

pierce77@bu.edu 1

<sup>&</sup>lt;sup>1</sup>informally, a cluster that contains a single data point.

<sup>&</sup>lt;sup>2</sup>summarized from An Introduction to Statistical Learning with Applications in Python, 525-526

## **Average-Link Distance**

The **average** of all pairwise distances between a point from one cluster and a point from the other cluster.

- · Less susceptible to noise and outliers
- Biased towards globular clusters

$$D_{AL}(C_1, C_2) = \left(\frac{1}{|C_1| \cdot |C_2|}\right) \quad \cdot \sum_{p_1 \in C_1, p_2 \in C_2} d(p_1, p_2)$$

### **Centroid Distance**

The distance between the centers of separate clusters.

$$D_C(C_1, C_2) = d(\mu_1, \mu_2)$$

### **Ward's Distance**

The difference between the spread of points in the merged cluster and the unmerged clusters.

$$D_{WD}(C_1, C_2) = \sum_{p \in C_{12}} d(p, \mu_{12}) - \sum_{p_1 \in C_1} d(p_1, \mu_2) - \sum_{p_2 \in C_2} d(p_2, \mu_2)$$

pierce77@bu.edu 2